

# Stata Webinar

## Introduction to lasso using Stata

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# Outline

- Overview of lasso in Stata

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- Lasso for prediction and model selection
  - Motivation and basic theoretical aspects
  - Example for a linear model
    - Basic workflow
    - Some tools and options

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- "Lasso was an acronym for 'least absolute shrinkage and selection operator'. Today, lasso is considered a word"

# Lasso for prediction and model selection

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- For example, a car dealer business needs to predict the market price of used cars, given many potential predictor variables
- If data have lots of covariates, which ones should we include in our prediction model?

## Using penalized regression to avoid overfitting

- Problems if all potential covariates would be included:
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- A way to avoid overfitting is by penalizing the objective function

$$Q = \frac{1}{N} \sum_{i=1}^N w_i f(y_i, \beta_0 + \mathbf{x}_i \beta')$$

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- $f(\cdot)$  is a measure of prediction error
- How does lasso penalize the objective function?

## Using penalized regression to avoid over-fitting

Lasso (Tibshirani, 1996) minimizes the penalized objective function

$$Q_L = \frac{1}{N} \sum_{i=1}^N w_i f(y_i, \beta_0 + \mathbf{x}_i \boldsymbol{\beta}') + \lambda \sum_{j=1}^p k_j |\beta_j|$$

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- Least absolute shrinkage and selection operator (lasso)

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- Penalized objective function for lasso

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$$Q_{en} = \frac{1}{N} \sum_{i=1}^N w_i f(y_i, \beta_0 + \mathbf{x}_i \boldsymbol{\beta}') + \lambda \sum_{j=1}^p k_j \left\{ \frac{1-\alpha}{2} \beta_j^2 + \alpha |\beta_j| \right\}$$

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- Penalized objective function for square-root lasso

$$Q_L = \sqrt{\frac{1}{N} \sum_{i=1}^N w_i (y_i - \beta_0 - \mathbf{x}_i \beta')^2} + \frac{\lambda}{N} \sum_{j=1}^p k_j |\beta_j|$$

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- 5 steps 3 and 4 are repeated for each fold
- 6 the prediction errors are then averaged over all folds
- 7 steps 3, 4, 5 and 6 are repeated for each  $\lambda$  in the grid
- 8 select the  $\lambda^*$  with the smallest average prediction error, and refit lasso using  $\lambda^*$  on the original data

# Example on lasso for prediction with a linear model

- Predicting infant birth weight

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- Basic covariates: 5 binary variables and 6 continuous variables of mothers and fathers
- Covariates: main effects and interactions (117 covariates)



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- Covariates: main effects and interactions (117 covariates)
- Number of observations: 4642
- Among OLS, lasso, elastic-net, and square-root lasso, which method should be used to predict the infant birth weight?

# Workflow

- Step 1: Using **split sample**
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(Excerpt from Cattaneo (2010) Journal of Econometrics 155: 138154)  
. set seed 1907  
. splitsample, generate(sample) split(0.70 0.30)  
. label define lbsample 1 "Training" 2 "Testing"  
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- Step 2: Create macro with factor variable syntax

```
. global covs (c.mage c.fage c.mage c.fage c.monthslb)##(c.mage ///
> c.fage c.mage c.fage c.monthslb) (mmarried mhispl fhispl ///
> foreign alcohol msmove fbaby prenatal1)##(c.mage c.fage ///
> c.medu c.fedu c.monthslb)
```

## • Step 3: Select $\lambda$ parameter value using training sample

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. quietly regress bweight $covs if sample == 1
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- **estimates store** stores estimation results
- In **elasticnet**, option **alpha()** specifies some  $\alpha$  values for the penalty term

# Workflow

- Step 4: Evaluate prediction performance using testing sample

```
. lassogof ols lasso elastnet sqlasso, over(sample)
```

Penalized coefficients

Name	sample	MSE	R-squared	Obs
ols	Training	304368.1	0.0800	3,249
	Testing	328554.5	0.0463	1,393
lasso	Training	310573.1	0.0613	3,249
	Testing	324874.6	0.0570	1,393
elastnet	Training	310358.5	0.0619	3,249
	Testing	324727.4	0.0574	1,393
sqlasso	Training	310176.3	0.0625	3,249
	Testing	324962.4	0.0567	1,393

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lasso	Training	310573.1	0.0613	3,249
	Testing	324874.6	0.0570	1,393
elastnet	Training	310358.5	0.0619	3,249
	Testing	324727.4	0.0574	1,393
sqlasso	Training	310176.3	0.0625	3,249
	Testing	324962.4	0.0567	1,393

- Elastic-net is the best method (lowest MSE in the testing sample)

- Step 5: Compute predictions using the best estimator

```
. quietly elasticnet linear bweight $covs, alpha(0.2 0.5 0.75 0.9)
. estimates store elastnetfull
. use cattaneo2_new, clear
(New data)
. estimates restore elastnetfull
(results elastnetfull are active now)
. predict yhat_pen
(options xb penalized assumed; linear prediction with penalized coefficients)
. predict yhat_postsel, postselection
(option xb assumed; linear prediction with postselection coefficients)
```

- Step 5: Compute predictions using the best estimator

```
. quietly elasticnet linear bweight $covs, alpha(0.2 0.5 0.75 0.9)
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. estimates restore elastnetfull
(results elastnetfull are active now)
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(options xb penalized assumed; linear prediction with penalized coefficients)
. predict yhat_postsel, postselection
(option xb assumed; linear prediction with postselection coefficients)
```

- By default, **predict** uses the penalized coefficients

- Step 5: Compute predictions using the best estimator

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(results elastnetfull are active now)
. predict yhat_pen
(options xb penalized assumed; linear prediction with penalized coefficients)
. predict yhat_postsel, postselection
(option xb assumed; linear prediction with postselection coefficients)
```

- By default, **predict** uses the penalized coefficients
- The **postselection** option uses post-selection coefficients (OLS on variables selected by **elasticnet**). They are expected to perform better in out-of-sample prediction than the penalized coefficients

# Display lasso output

```
. estimates restore lasso  
(results lasso are active now)
```

```
. lasso
```

```
Lasso linear model          No. of obs      =      3,249  
                           No. of covariates =      117  
Selection: Cross-validation No. of CV folds  =       10
```

ID	Description	lambda	No. of nonzero coef.	Out-of- sample R-squared	CV mean prediction error
1	first lambda	115.008	0	0.0003	330748.1
26	lambda before	11.23639	17	0.0514	313825.7
* 27	selected lambda	10.23818	17	0.0515	313799.9
28	lambda after	9.32865	19	0.0515	313823.9
39	last lambda	3.352543	28	0.0501	314281.9

```
* lambda selected by cross-validation.
```



# Display lasso output

```
. estimates restore lasso  
(results lasso are active now)
```

```
. lasso
```

```
Lasso linear model          No. of obs      =      3,249  
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```

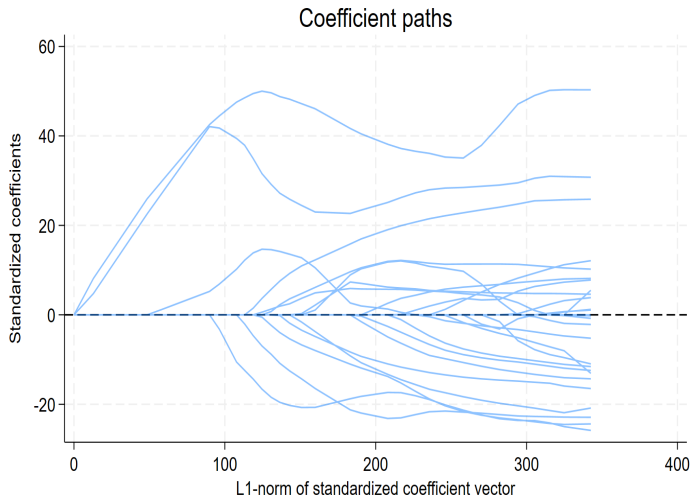
ID	Description	lambda	No. of nonzero coef.	Out-of- sample R-squared	CV mean prediction error
1	first lambda	115.008	0	0.0003	330748.1
26	lambda before	11.23639	17	0.0514	313825.7
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39	last lambda	3.352543	28	0.0501	314281.9

```
* lambda selected by cross-validation.
```

- Notice that the number of nonzero coefficients increases as  $\lambda$  decreases

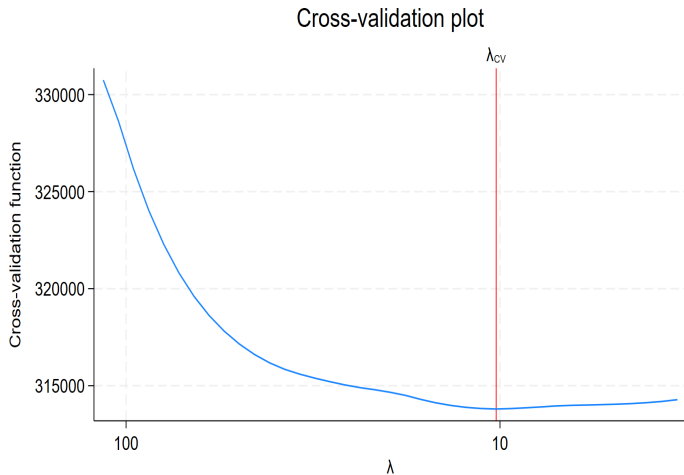
# Plot path of coefficients after lasso

. `coefpath`



# Plot cross-validation function after lasso

. **cvplot**



$\lambda_{cv} = 10$  is the cross-validation minimum  $\lambda$ ; # coefficients = 17.

# Display knot table (`lassoknots`)

```
. lassoknots
```

ID	lambda	No. of nonzero coef.	CV mean pred. error	Variables (A)dded, (R)emoved, or left (U)nchanged
2	104.791	2	328633.1	A 0.msmoke#c.mage 1.mmmarried#c.fedu
6	72.22835	3	320818.5	A 0.msmoke#c.fedu
11	45.36151	4	316613.1	A 0.mmmarried
(output omitted)				
* 27	10.23818	17	313799.9	U
28	9.32865	19	313823.9	A 1.mhisp#c.medu 2.msmoke#c.fage
29	8.499919	18	313863.1	R 0.msmoke#c.fedu
(output omitted)				
39	3.352543	28	314281.9	A c.mage#c.monthslb 0.prenatal1#c.mage

\* lambda selected by cross-validation.

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```
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\* lambda selected by cross-validation.

- **lassoselect** can be used to pick a different  $\lambda$  value (sensitivity analysis)

## Methods for selecting the value of $\lambda$

- Cross-validation (default) computes out-of-sample predictions MSEs using 10 folds and selects the  $\lambda$  with minimum MSE (**`selection(cv)`**)

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- Plugin method uses the structure of the model and advanced theoretical results to find the smallest  $\lambda$  that dominates the noise, given estimates of the penalty weights (**`selection(plugin)`**)



## Methods for selecting the value of $\lambda$

- Cross-validation (default) computes out-of-sample predictions MSEs using 10 folds and selects the  $\lambda$  with minimum MSE (**selection(cv)**)
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## Methods for selecting the value of $\lambda$

- Cross-validation (default) computes out-of-sample predictions MSEs using 10 folds and selects the  $\lambda$  with minimum MSE (**`selection(cv)`**)
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- Bayesian information criteria (BIC) finds  $\lambda$  that minimizes the BIC statistic (**`selection(bic)`**, Stata 17)
- Manual selection (**`lassoselect`**)

## Choosing $\lambda$ using the `selection()` option

```
. quietly lasso linear bweight $covs  
. estimates store cv  
. quietly lasso linear bweight $covs, selection(adaptive)  
. estimates store adaptive  
. quietly lasso linear bweight $covs, selection(plugin)  
. estimates store plugin  
. quietly lasso linear bweight $covs, selection(bic)  
. estimates store bic
```

# Display basic information about lassos (`lassoinfo`)

```
. lassoinfo cv adaptive plugin bic
```

```
Estimate: cv
```

```
Command: lasso
```

Dependent variable	Model	Selection method	Selection criterion	lambda	No. of selected variables
bweight	linear	cv	CV min.	9.867787	19

```
Estimate: adaptive
```

```
Command: lasso
```

Dependent variable	Model	Selection method	Selection criterion	lambda	No. of selected variables
bweight	linear	adaptive	CV min.	3.64e+08	13

```
Estimate: plugin
```

```
Command: lasso
```

Dependent variable	Model	Selection method	lambda	No. of selected variables
bweight	linear	plugin	.0627659	6

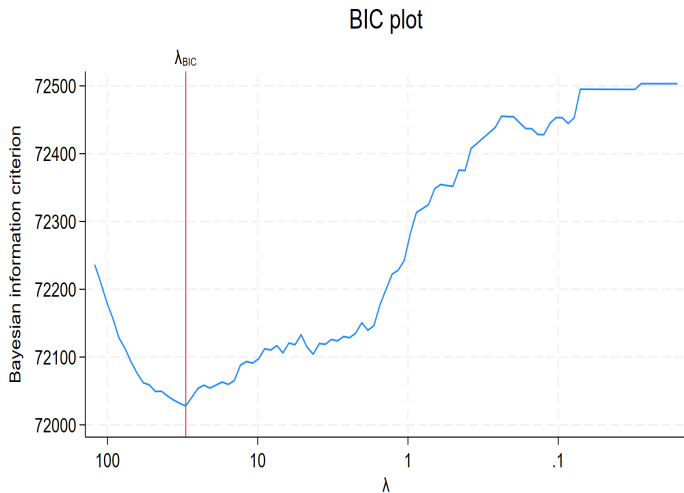
```
Estimate: bic
```

```
Command: lasso
```

Dependent variable	Model	Selection method	Selection criterion	lambda	No. of selected variables
bweight	linear	bic	BIC min.	30.1348	5

# Plot Bayesian information criterion function after lasso

```
. bicplot
```



$\lambda_{BIC} = 30$  is the BIC minimum  $\lambda$ ; # coefficients = 5.

# Display coefficients after lasso (`lassocoeff`)

```
. lassocoef cv adaptive plugin bic, display(coef, standardized)
```

	cv	adaptive	plugin	bic
mmarried				
Not married	-22.11483	-41.92165	-3.921652	-13.51986
Married	8.19e-10		3.38e-10	
msmoke				
0 daily	19.53755			
mmarried#c.fage				
Not married	-7.447833	-5.868928		
mmarried#c.medu				
Not married	-1.549706			
Married	16.17073	15.6786	21.32031	14.89484
mmarried#c.fedu				
Married	13.60921		16.50398	19.33894
foreign#c.fage				
1	-4.972952	-17.05522		
foreign#c.fedu				
0	3.90694			
alcohol#c.mage				
1	-3.167769	-6.859747		
msmoke#c.mage				
0 daily	52.73363	84.46094	57.27693	63.43016

(output omitted)

# Lasso for inference

## Motivation

- Ideally we would have a correct model for both data and theory. If so, we would just need to fit the model (using an appropriate estimator) and we report point estimates, standard errors, p-values, and confidence intervals



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- In practice things are different. Consider the linear model

$$\mathbf{E}[y|\mathbf{d}, \mathbf{x}] = \mathbf{d}\alpha + \beta_0 + \mathbf{x}\beta'$$

- We may fit many models with different subsets of controls

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- We may fit many models with different subsets of controls
  - And, we would choose a model that we believe is the "best" to represent our theory or proposition. We apply an estimator and perform statistical inference
  - But, if we do not account for the model-selection process, inference would be invalid
- Suppose there are many potential controls. Which controls should we include in the model? How to perform valid inference on the variables of interest?

## Invalid approach

- 1 Apply lasso for  $y$  on the variables of interest ( $\mathbf{d}$  vector) and the controls ( $\mathbf{x}$  vector) forcing the variables of interest to be in the model. This selects a subset of controls ( $\mathbf{x}^*$  vector)

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- This approach would produce invalid statistical inference. Why?



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  - 3 Perform inference on the coefficients for the variables of interest (parameter vector  $\alpha$ )
- This approach would produce invalid statistical inference. Why?
    - Model-selection techniques inevitably make mistakes selecting controls
    - The actual sampling distribution of  $\alpha$  is not concentrated (multiple modes). (Leeb and Pötscher, 2005)

# Solutions

- Double selection: Belloni et al. (2014), Belloni et al. (2016) (**dsregress**, **dslogit**, and **dspoisson**)

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- "These solutions all use multiple lassos and moment conditions that are robust to the model-selection mistakes that lasso makes"
- By default, all of the command above fit the lassos using **selection(plugin)**

## Example on lasso for inference with a linear model

$$\mathbf{E}[y|\mathbf{d}, \mathbf{x}] = \mathbf{d}\boldsymbol{\alpha} + \beta_0 + \mathbf{x}\boldsymbol{\beta}'$$

- $y$  = wage (monthly wages)



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- $\mathbf{d}$  = (educ, tenure)
  - educ: Years of education
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- $\mathbf{x}$ : vector of potential control variables
  - 6 continuous variables, 1 categorical variable, 5 binary variables
  - All main effects and all possible interactions generate 230 controls

## Example on lasso for inference with a linear model

$$\mathbf{E}[y|\mathbf{d}, \mathbf{x}] = \mathbf{d}\boldsymbol{\alpha} + \beta_0 + \mathbf{x}\boldsymbol{\beta}'$$

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- Number of observations: 722

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- $\mathbf{d}$  = (educ, tenure)
  - educ: Years of education
  - tenure: Years with current employer
- $\mathbf{x}$ : vector of potential control variables
  - 6 continuous variables, 1 categorical variable, 5 binary variables
  - All main effects and all possible interactions generate 230 controls
- Number of observations: 722
- Which controls should we include in the model to perform valid inference on  $\boldsymbol{\alpha}$ ?

# dsregress – Double-selection lasso linear regression

```
. use nlsy80
. global controls c.(meduc feduc sibs age iq kww)##(exper ///
> pcollege married black south urban)
. dsregress wage educ tenure, controls($controls)
Estimating lasso for wage using plugin
Estimating lasso for educ using plugin
Estimating lasso for tenure using plugin
Double-selection linear model      Number of obs      =      722
                                Number of controls      =      230
                                Number of selected controls =      12
                                Wald chi2(2)              =      17.03
                                Prob > chi2              =      0.0002
```

wage	Robust					
	Coefficient	std. err.	z	P> z	[95% conf. interval]	
educ	29.29732	7.58747	3.86	0.000	14.42615	44.16849
tenure	5.105178	2.950394	1.73	0.084	-.677488	10.88784

Note: Chi-squared test is a Wald test of the coefficients of the variables of interest jointly equal to zero. Lassos select controls for model estimation. Type `lassoinfo` to see number of selected variables in each lasso.

```
. estimates store ds_plugin
```

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```
. use nlsy80
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Estimating lasso for wage using plugin
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Note: Chi-squared test is a Wald test of the coefficients of the variables of interest jointly equal to zero. Lassos select controls for model estimation. Type `lassoinfo` to see number of selected variables in each lasso.

```
. estimates store ds_plugin
```

- Inference on controls would not be valid; and so, they are not reported

# poregress – Partialing-out lasso linear regression

```
. poregress wage educ tenure, controls($controls)
Estimating lasso for wage using plugin
Estimating lasso for educ using plugin
Estimating lasso for tenure using plugin
Partialing-out linear model      Number of obs      =          722
                                Number of controls         =          230
                                Number of selected controls   =           12
                                Wald chi2(2)                  =          17.77
                                Prob > chi2                   =          0.0001
```

	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
wage						
educ	29.61345	7.455942	3.97	0.000	15.00007	44.22683
tenure	4.995759	2.874894	1.74	0.082	-.63893	10.63045

Note: Chi-squared test is a Wald test of the coefficients of the variables of interest jointly equal to zero. Lassos select controls for model estimation. Type `lassoinfo` to see number of selected variables in each lasso.

# xporegress – Cross-fit partialing-out lasso linear regression

```
. xporegress wage educ tenure, controls($controls)
```

(output omitted)

Cross-fit partialing-out	Number of obs	=	722
linear model	Number of controls	=	230
	Number of selected controls	=	25
	Number of folds in cross-fit	=	10
	Number of resamples	=	1
	Wald chi2(2)	=	18.00
	Prob > chi2	=	0.0001

	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
wage						
educ	29.62034	7.430891	3.99	0.000	15.05606	44.18462
tenure	5.082955	2.808093	1.81	0.070	-.420805	10.58672

Note: Chi-squared test is a Wald test of the coefficients of the variables of interest jointly equal to zero. Lassos select controls for model estimation. Type `lassoinfo` to see number of selected variables in each lasso.



# lassoinfo after xpporegress

```
. lassoinfo
```

```
Estimate: active
```

```
Command: xpporegress
```

Variable	Model	Selection method	No. of selected variables		
			min	median	max
educ	linear	plugin	5	7	9
tenure	linear	plugin	1	2	3
wage	linear	plugin	4	6	8

## lassoinfo after xporegress

```
. lassoinfo
```

```
Estimate: active
```

```
Command: xporegress
```

Variable	Model	Selection method	No. of selected variables		
			min	median	max
educ	linear	plugin	5	7	9
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- By default, **lassoinfo** displays summary of lassos by variable

## lassoinfo after xporegress

```
. lassoinfo
```

```
Estimate: active
```

```
Command: xporegress
```

Variable	Model	Selection method	No. of selected variables		
			min	median	max
educ	linear	plugin	5	7	9
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wage	linear	plugin	4	6	8

- By default, **lassoinfo** displays summary of lassos by variable
- The option **each** would display information of each lasso

## General advice

- The cross-fit partialing-out estimators are the best ones (**xporegress**, **xpologit**, **xpopoisson**, **xpoivregress**). But, computations may take extremely long time

## General advice

- The cross-fit partialing-out estimators are the best ones (**xporegress**, **xpologit**, **xpopoisson**, **xpoivregress**). But, computations may take extremely long time
- If you do not have the time, use either the partialing-out estimator (**poregress**, **pologit**, **popoisson**, **poivregress**) or the double-selection estimator (**dsregress**, **dslogit**, **dspoisson**)

# Customize individual lassos

```
. dsregress wage educ tenure, controls($controls) ///  
> lasso(wage, selection(adaptive)) ///  
> lasso(educ, selection(bic)) ///  
> sqrtlasso(tenure, selection(cv))
```

Estimating lasso for wage using adaptive

Estimating lasso for educ using BIC

Estimating square-root lasso for tenure using cv

Double-selection linear model	Number of obs	=	722
	Number of controls	=	230
	Number of selected controls	=	54
	Wald chi2(2)	=	18.28
	Prob > chi2	=	0.0001

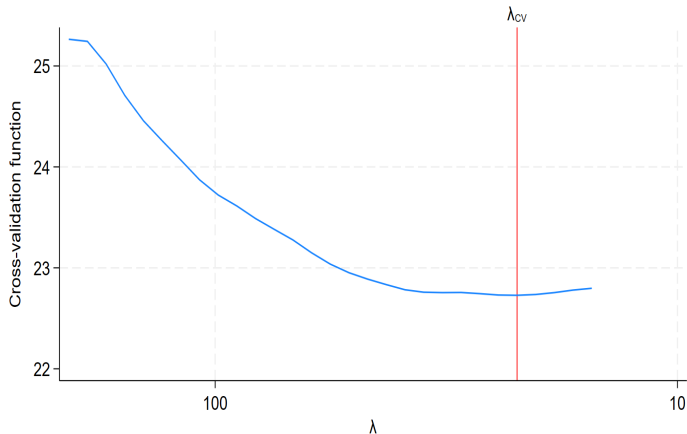
	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
wage						
educ	34.66224	8.708087	3.98	0.000	17.5947	51.72978
tenure	4.881471	3.095039	1.58	0.115	-1.184694	10.94764

Note: Chi-squared test is a Wald test of the coefficients of the variables of interest jointly equal to zero. Lassos select controls for model estimation. Type `lassoinfo` to see number of selected variables in each lasso.

cvplot for a particular lasso

```
. cvplot, for(tenure)
```

### Cross-validation plot for tenure

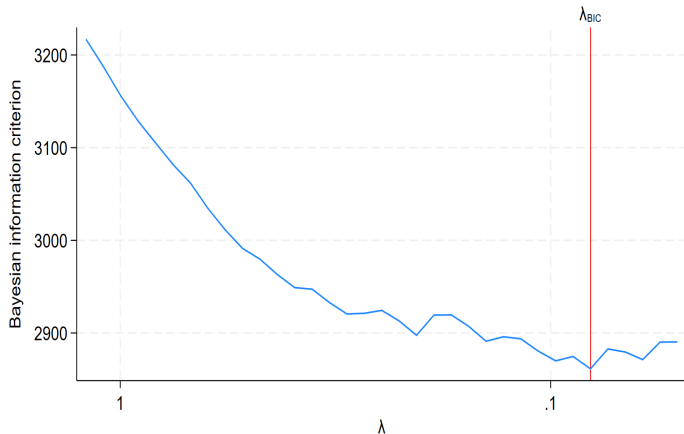


$\lambda_{cv} = 22$  is the cross-validation minimum  $\lambda$ ; # coefficients = 30.

# bicplot for a particular lasso

```
. bicplot, for(educ)
```

BIC plot for educ



$\lambda_{BIC} = .081$  is the BIC minimum  $\lambda$ ; # coefficients = 32.



## Other options for selecting controls

```
. quietly dsregress wage educ tenure, controls($controls) selection(cv)
. estimates store ds_cv
. quietly dsregress wage educ tenure, controls($controls) selection(adaptive)
. estimates store ds_adapt
. quietly dsregress wage educ tenure, controls($controls) selection(bic)
. estimates store ds_bic
. estimates table ds_plugin ds_cv ds_adapt ds_bic, b(%9.4f) se(%9.4f) p(%9.4f)
```

Variable	ds_plugin	ds_cv	ds_adapt	ds_bic
educ	29.2973	32.8323	34.1067	33.3164
	7.5875	8.8374	8.6690	8.6672
	0.0001	0.0002	0.0001	0.0001
tenure	5.1052	5.1631	4.8216	4.6522
	2.9504	3.0597	3.0784	3.0064
	0.0836	0.0915	0.1173	0.1218

Legend: b/se/p

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  - Using lasso for prediction and listing the selected variables in estimation commands will generally lead to invalid statistical inference. Instead, use lasso inferential commands
  - Use cross-fit partialing-out estimators if you have the time; otherwise, use either the partialing-out estimator or the double-selection estimator



## References

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