Difference-in-Differences in Stata 17

StataCorp LLC

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- One of the most popular causal effects estimators (1855)
- Understand the effect of a treatment on an outcome for the treated group
 - Subsidy on productivity
 - A drug on cholesterol levels
 - An after-school program on GPA

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 - Identification hinges on control for group and time unobservable characteristics

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 - Identification does not depend on controlling for covariates
 - Identification hinges on control for group and time unobservable characteristics
- Estimate of causal effect of a treatment controlling for unobservables

Stata implementation

- Two-way fixed effects also known as generalized DID (default)
- Allows 2x2 design
- Verifies assumptions
- Provides a wide range of standard errors
- Provides diagnostics and tests
- Binary or continuous treatment
- Difference-in-differences (DDD) with group and time interactions

Stata implementation

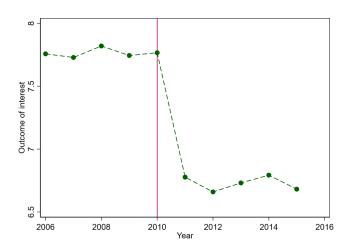
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- Binary or continuous treatment
- Difference-in-differences (DDD) with group and time interactions
- Caveats
 - Treatment effects are homogeneous
 - Standard error literature is large and growing
 - Diagnostics and tests
 - https://sites.google.com/site/matthewdwebb/
 - https://friosavila.github.io/playingwithstata/index.html

Outline

- Basic concepts
- Stata examples

Basic Concepts

Treated group



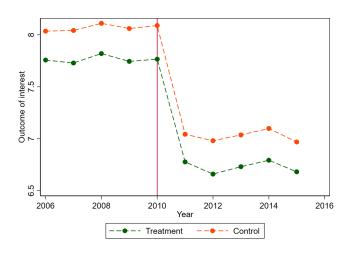
What have we learned

- Clearly there is a change in the outcome after treatment for the treated
- Is it causal?
 - Time specific effects. Another policy. Covid-19.
 - Group unobservable characteristics correlated to treatment. Jargon.

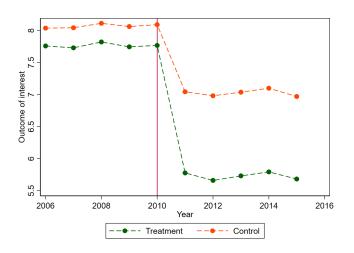
What have we learned

- Clearly there is a change in the outcome after treatment for the treated
- Is it causal?
 - Time specific effects. Another policy. Covid-19.
 - Group unobservable characteristics correlated to treatment. Jargon.
- What can we do?
 - Control for time-specific effects
 - Control for group-specific unobservables (fixed-effects)
 - Use a causal-inference framework

Graphical representation I



Graphical representation II



Card and Krueger (1994)

• Intervention: Increase in the minimum wage

Group: New Jersey and Pennsylvania

Outcome: Employment

Linear Framework: Card and Krueger (1994)

- Individuals (i) in a state (s) at two time period $t \in \{0,1\}$
- Potential outcomes (for now no covariates):

$$E(y_{ist0}|s,t) = \lambda_t + \gamma_s$$

$$E(y_{ist1}|s,t) = \lambda_t + \gamma_s + \beta$$

- λ_t is a time effect
- γ_s is a state effect

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- λ_t is a time effect
- γ_s is a state effect
- y_{ist1} is only observed if state s at time t receives the treatment, an increase in minimum wage, $D_{st}=1$
- y_{ist0} is only observed if state s at time t does not receive the treatment, $D_{st} = 0$

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- New Jersey increased minimum wage in April (treatment)
- Neighboring Pennsylvania did not (control)
- Before wage change in February:

$$\begin{array}{rcl} E\left(y_{ist}|PA,Feb\right) & = & \lambda_{Feb} + \gamma_{PA} \\ E\left(y_{ist}|NJ,Feb\right) & = & \lambda_{Feb} + \gamma_{NJ} \\ E\left(y_{ist}|NJ,Feb\right) - E\left(y_{ist}|PA,Feb\right) & = & \gamma_{NJ} - \gamma_{PA} \end{array}$$

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- The model assumes a common time trend and differing state effects
- Differencing eliminates unobserved time effects

• After the minimum wage change, in November:

$$E(y_{ist}|NJ,Nov) - E(y_{ist}|PA,Nov) = \gamma_{NJ} - \gamma_{PA} + \beta$$

 Difference-in-differences looks at differences before and after the policy:

$$[E(y_{ist}|., Nov) - E(y_{ist}|., Nov)] - [E(y_{ist}|., Feb) - E(y_{ist}|., Feb)]$$

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 Difference-in-differences looks at differences before and after the policy:

$$[E(y_{ist}|., Nov) - E(y_{ist}|., Nov)] - [E(y_{ist}|., Feb) - E(y_{ist}|., Feb)]$$

- The difference in these two differences is β
- It is also the average treatment effect on the treated (ATT)

Parallel trends

- y_{ist0} potential outcome of not being treated
- $D_{st} \equiv D$ if group s was treated at time t, $D \in \{0,1\}$
- s and t are $\in \{0,1\}$
- At t = 0 no one is treated
- Parallel trends:

$$E(y_{ist0}|s=1, D=1, t=1)$$

potential outcome of treated in group s=1 had they remained untreated at t=1

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$$E(y_{ist0}|s=1, D=1, t=1)$$

potential outcome of treated in group s=1 had they remained untreated at t=1

$$E(y_{ist0}|s=1, D=1, t=1) - E(y_{ist0}|s=1, D=1, t=0) = E(y_{ist0}|s=0, D=1, t=1) - E(y_{ist0}|s=0, D=1, t=0)$$

Could be conditional on covariates

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Observed Outcome and Estimating equation

$$E(y_{ist}|s,t) = D_{st}E(y_{ist1}|s,t) + (1 - D_{st})E(y_{ist0}|s,t)$$

$$E(y_{ist}|s,t) = D_{st}(\lambda_t + \gamma_s + \beta) + (1 - D_{st})(\lambda_t + \gamma_s)$$

$$E(y_{ist}|s,t) = \lambda_t + \gamma_s + D_{st}\beta$$

- ullet This suggests fitting a regression model with a dummy variable D_{st}
- The specification could have regressors

Generalized DID or two-way fixed effects

$$y_{ist} = \gamma_s + \gamma_t + D_{st}\beta + \varepsilon_{ist}$$

- ullet D_{st} is an observation level indicator of treatment $D_{st} \in \{0,1\}$
- In panel data if individuals are nested in s individual effect absorb state effects
- You may include covariates in the specification above

2 x 2 specification DID

$$y_{its} = \gamma_{1treated} + \gamma_{1post} + 1treated \times 1post\beta + \varepsilon_{its}$$

- Works when all units are treated at the same time (balanced)
- This model is nested in the generalized DID
 - 1 treated is a linear combination of the group dummies
 - 1 post is a linear combination of the time dummies
- This model assumes all post periods and all treatment groups are equivalent.

Alternative specifications

- D_{st} is not binary but continuous (intensity of treatment)
- Differences occur between two groups (differencing two group unobservables)
- DDD or triple differences. It incorporates unobservables from two control groups.
 - Number of parameters is large
 - Identification is more challenging

Standard error computation

Treatment occurs at the group level, state, county, country, etc. and time

- Cluster at the group level Bertrand, Dufflo, Mullainathan (2004)
- Few number of elements in the group:
 - Donald and Lang (2007) aggregation and other aggregation methods
 - Wild-cluster bootstrap
 - Bias-corrected standard errors with Bell and McCaffrey (2002) degrees of freedom adjustment
 - Other suggestions

Stata Examples

Artificial data

. webuse hospdd, clear (Artificial hospital admission procedure data)

. describe

Contains data from https://www.stata-press.com/data/r17/hospdd.dta

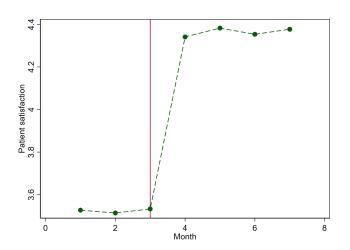
Observations: 7,368 Artificial hospital admission

Variables: 5 7 Mar 2021 19:52

Variable	Storage	Display	Value	Variable label
name	type	format	label	
hospital frequency month procedure satis	byte byte byte byte float	%9.0g %9.0g %8.0g %9.0g %9.0g	size mnth pol	Hospital ID Hospital visit frequency Month Admission procedure Patient satisfaction score

Sorted by: hospital

Graphical representation III



Estimation

```
. didregress (satis) (procedure), group(hospital) time(month)
Number of groups and treatment time
Time variable: month
Control:
               procedure = 0
Treatment:
               procedure = 1
                 Control Treatment
Group
    hospital
                      28
                                 18
Time
     Minimum
     Maximum
                                  4
Difference-in-differences regression
                                                         Number of obs = 7.368
Data type: Repeated cross-sectional
                              (Std. err. adjusted for 46 clusters in hospital)
                             Robust
       satis
               Coefficient std. err.
                                           t P>|t|
                                                          [95% conf. interval]
ATET
   procedure
```

Note: ATET estimate adjusted for group effects and time effects.

.8479879 .0321121 26.41 0.000

.912665

(New vs Old)

.7833108

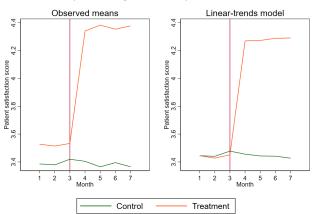
Diagnostic plots

estat trendplot

- First plot: Mean of the outcome for treated and untreated units
- Second plot: Trend of treated and control groups (group interacted with time)

Diagnostic plots

Graphical diagnostics for parallel trends



Tests: estat ptrends

```
. estat ptrends  \begin{array}{lll} \mbox{Parallel-trends test (pretreatment time period)} \\ \mbox{H0: Linear trends are parallel} \\ \mbox{F(1, 45) = } & 0.55 \\ \mbox{Prob > F = } & 0.4615 \\ \end{array}
```

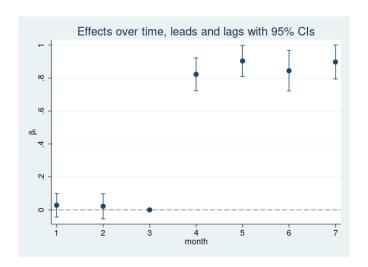
• Augmented model with trends for treated vs. control group before and after treatment. Test if the pretreatment trends are parallel.

Tests: estat granger

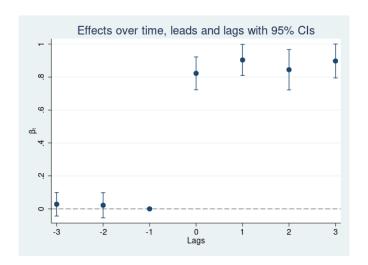
```
. estat granger
Granger causality test
HO: No effect in anticipation of treatment
F(2, 45) = 0.33
Prob > F = 0.7239
```

• Augment the model to include dummies as if treatment had occurred in the past. Test coefficients jointly.

estat grangerplot



estat grangerplot, lagview



estat grangerplot (results)

. estat grangerplot, nodraw verbose Linear regression, absorbing indicators Absorbed variable: hospital

Number of obs = 7,368 No. of categories = 46 F(12, 45) = 94.68 Prob > F = 0.0000 R-squared = 0.5334 Adj R-squared = 0.5298 Root MSE = 0.7240

(Std. err. adjusted for 46 clusters in hospital)

satis	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
month						
February	007044	.0263953	-0.27	0.791	0602068	.0461188
March	.0335696	.0255925	1.31	0.196	0179764	.0851156
April	.0187852	.0250623	0.75	0.457	0316927	.0692632
May	0211152	.0269569	-0.78	0.438	0754092	.0331788
June	.0091208	.0179016	0.51	0.613	026935	.0451766
July	0203444	.0306266	-0.66	0.510	0820296	.0413407
F3_procedure	.027897	.035569	0.78	0.437	0437426	.0995367
F2_procedure	.0217322	.0380076	0.57	0.570	054819	.0982833
L0_procedure	.8228153	.0494933	16.62	0.000	.7231307	.9224999
L1_procedure	.9040498	.0469682	19.25	0.000	.8094511	.9986486
L2_procedure	.844724	.0608006	13.89	0.000	.7222654	.9671826
L3_procedure	.8978885	.0511588	17.55	0.000	.7948494	1.000928
_cons	3.433074	.0198449	173.00	0.000	3.393104	3.473044

A 2×2 specification

- Create dummy variables for treated group and post time period
- Tell didregress not to include group and time effects
- Add dummies to the outcome equation

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```
. bysort hospital: egen treated = mean(procedure)
. replace treated = 1 if treated>0
(3,064 real changes made)
. generate post = 0
. replace post = 1 if month>3
(3,684 real changes made)
```

A 2×2 specification

```
. didregress (satis treated post) (procedure),
         group(hospital) time(month) nogteffects
Number of groups and treatment time
Time variable: month
Control:
             procedure = 0
Treatment:
             procedure = 1
                 Control Treatment
Group
   hospital
                      28
                                 18
Time
    Minimum
    Maximum
```

Difference-in-differences regression

Number of obs = 7,368

Data type: Repeated cross-sectional

(Std. err. adjusted for 46 clusters in hospital)

		(Std. er	r. adjus	ted for 4	o clusters in	nospital)
satis	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET procedure (New vs Old)	.8479879	.0320051	26.50	0.000	.7835263	.9124494

Note: ATET estimate adjusted for covariates.

Difference-in-differences DDD

Augmented DID

Difference-in-differences DDD

- Augmented DID
- Selection on unobservables provides identification
- What if there are unobservables that vary at the group and time level
- Find a new group not exposed to treatment but exposed to the problematic time-varying confounder
- Subtract the effect of that group from the original DID

Difference-in-differences DDD

- Augmented DID
- Selection on unobservables provides identification
- What if there are unobservables that vary at the group and time level
- Find a new group not exposed to treatment but exposed to the problematic time-varying confounder
- Subtract the effect of that group from the original DID
- In our example think about individual's frequency of visit affecting satisfaction

DDD preparing my data

- . generate hightrt = procedure==1 & (frequency==3 | frequency==4)
- . label define trt 0 "Untreated" 1 "Treated" $\,$
- . label values hightrt trt

DDD estimation

```
. didregress (satis) (hightrt), group(hospital frequency) time(month)
  (output omitted)
Number of groups and treatment time
Time variable: month
Control:
              hightrt = 0
              hightrt = 1
Treatment:
                Control Treatment
Group
                                18
   hospital
   frequency
Time
    Minimum
    Maximum
Triple-differences regression
                                                        Number of obs = 7,368
Data type: Repeated cross-sectional
                              (Std. err. adjusted for 46 clusters in hospital)
                            Robust
       satis
              Coefficient std. err.
                                          t P>|t|
                                                         [95% conf. interval]
ATET
    hightrt
   (Treated
 Untreated)
                 .764154 .0402603
                                      18.98 0.000
                                                         6830655
                                                                     8452425
```

Note: ATET estimate adjusted for group effects, time effects, and group- and time-effects interactions.

Other estimation alternatives

- didregress (y x1 ... xk) (c, continuous), ...
- didregress (y ...) (d...), group(g1 g2)
- xtdidregress (y x1 ... xk) (d), group(groupvar) time(timevar)

Standard error considerations

- Default standard errors are cluster robust standard errors at the group level BDM (2004)
- didregress is equivalent to areg considers group fixed effects as regressors in the degrees of freedom adjustment
- xtdidregress is equivalent to xtreg does not consider group fixed effects as regressors
- When the number of elements per groups (states, countries, countries) is small cluster robust standard errors do not work well. Alternatives are:
 - Wild cluster bootstrap
 - Bias corrected standard errors
 - Aggregation methods

Wild-cluster bootstrap

- Covariates remain the same across iteration
- We impose the null hypothesis of ATET = 0
- What changes is the weights given to residuals at each iteration $\tilde{y} = X\tilde{\beta} + \tilde{\varepsilon}$, $\tilde{\beta}$, and $\tilde{\varepsilon} = \hat{\varepsilon} * w$
- No standard errors are computed (rely on normal approximation)
- P-values and confidence intervals are computed
- Algorithm computes p-values and then solves a bisection-algorithm to get CI
- Problem to find CI upper bound and CI lower bound are two separate optimization problems

Error weights

Error weight	Formula
rademacher	-1 with pr 0.5 and 1 with pr 0.5
mammen	$1-\phi$ with pr $\phi/\sqrt(5)$, ϕ otherwise, $\phi=(1+\sqrt{5})/2$
webb	$-\sqrt{3/2}$, $-\sqrt{2/2}$, $-\sqrt{1/2}$, $\sqrt{1/2}$, $\sqrt{2/2}$, $\sqrt{3/2}$ pr $1/6$
normal	standard normal
gamma	shape parameter 4 scale parameter $1/2$

Wildbootstrap I

Wildbootstrap II

```
. didregress (satis) (procedure), ///
         group(hospital) time(month) wildbootstrap(rseed(111))
  (output omitted)
Number of groups and treatment time
Time variable: month
Control:
              procedure = 0
              procedure = 1
Treatment:
                 Control Treatment
Group
   hospital
                      28
                                 18
Time
    Minimum
     Maximum
DID with wild-cluster bootstrap inference
                                                       Number of obs = 7.368
                                                       No. of clusters =
                                                       Replications
                                                                       = 1,000
Data type:
             Repeated cross-sectional
Error weight: rademacher
              Coefficient
                                  P>ItI
                                             [95% conf. interval]
     satis
ATET
  procedure
(New vs Old)
                .8479879
                           26.41
                                  0.000
                                             .7806237
                                                         .9157614
```

Note: ATET estimate adjusted for group effects and time effects.

Bias-corrected standard errors

- Cluster generalization of HC2 (scale residuals inverse of square of diagonals from projection matrix)
- Bell and McCaffrey (2002) suggest a degrees of freedom adjustment (per parameter)

Bias-corrected SEs

```
. didregress (satis) (procedure), group(hospital) time(month) vce(hc2)
Computing degrees-of-freedom:
procedure .....
Number of groups and treatment time
Time variable: month
Control:
              procedure = 0
Treatment:
              procedure = 1
                Control Treatment
Group
    hospital
                                18
Time
     Minimum
     Maximum
Difference-in-differences regression
                                                      Number of obs
                                                      No. of clusters =
Data type: Repeated cross-sectional
                          Robust HC2
              Coefficient std. err.
                                               P>ItI
                                                         [95% conf. interval]
       satis
ATET
   procedure
       (New
         vs
      014)
                 .8479879 .0325552 26.05 0.000 .7819941
                                                                    .9139816
```

Note: ATET estimate adjusted for group effects and time effects.

Degrees of freedom adjustment

```
. mat list r(table)
r(table)[9.9]
               ATET:
                       Controls:
                                    Controls:
                                                 Controls:
                                                              Controls:
                                                                           Controls:
              r1vs0.
                              1h
                                            2.
                                                         3.
                                                                      4.
                                                                                   5
         procedure
                          month
                                        month
                                                    month
                                                                 month
                                                                              month
         .84798786
                                  -.00960766
                                                .02196858
                                                            -.00328387
                                                                         -.00940274
    se
         .03255515
                                   .01836738
                                                .01817606
                                                             .02210113
                                                                          .02325151
         26.047731
                                  -.52308262
                                                1.2086544
                                                            -.14858393
                                                                         -.40439255
pvalue
         3.558e-25
                                   .60348306
                                                .23310851
                                                             .88254581
                                                                          .68783978
         .7819941
                                  -.04660147
                                               -.01463989
                                                            -.04779783
                                                                         -.05623368
    11
         .91398163
                                                .05857705
                                                             .04123009
    111
                                   .02738615
                                                                           .0374282
    đf
         36.496106
                                           45
                                                        45
                                                                     45
                                                                                  45
         2.0271372
                      2.0141034
                                   2.0141034
                                                2.0141034
                                                             2.0141034
                                                                          2.0141034
  crit
 eform
                  0
                               0
                       Controls:
                                    Controls:
          Controls:
                               7.
                  6.
              month
                           month
                                        cons
        -.00383754
                     -.01119415
                                    3.444675
                       .0230133
         .01906173
                                   .01140018
         -.2013216
                     -.48642083
                                   302 15965
         .84135438
                      .62902945
                                   4.517e-76
pvalue
    11
        -.04222984
                      -.0575453
                                   3.4217139
    117
         .03455476
                      .03515701
                                   3.4676362
                              45
                                           45
    df
                 45
  crit
         2.0141034
                      2.0141034
                                   2.0141034
 eform
```

Aggregation methods

$$\begin{array}{lcl} y_{its} & = & \gamma_s + \gamma_t + z_{1ist}\beta_1 + z_{2st}\beta_2 + D_{st}\delta + \varepsilon_{ist} \\ y_{ist} & = & z_{1ist}\beta_2 + C_{st} + \varepsilon_{ist} \\ \widehat{C}_{st} & = & z_{2st}\beta_2 + D_{st}\delta + \nu_{st} \end{array}$$

- Obtain \widehat{C}_{st}
- Aggregate at the s, t level and regress
 - dlang, constant: regress \widehat{C}_{st} on z_{2st} , D_{st} and time and group fixed effects, degrees of freedom are a function of the number of observations in the collapsed sample and the number of regressors in z_{2st} and D_{st} .
 - standard: regress \widehat{C}_{st} on z_{2st} , D_{st}
 - dlang, varying: C_{st} is the constant of a regression of each group defined by st, i.e. β_1 is not constant but varying.

aggregate(dlang)

. didregress (satis) (procedure), group(hospital) time(month) aggregate(dlang) Number of groups and treatment time

Time variable: month

Control: procedure = 0

Treatment: procedure = 1

	Control	Treatment
Group hospital	28	18
Time Minimum Maximum	1 1	4 4

Difference-in-differences regression

Data type: Repeated cross-sectional

Aggregation: Donald-Lang

satis	Coefficient	Std. err.	t	P> t	[95% conf.	interval]
ATET procedure (New vs Old)	.8500467	.0255727	33.24	0.000	.7997311	.9003623

Note: ATET estimate adjusted for group effects and time effects.

Number of obs = 322

aggregate(standard)

```
. didregress `specs´, group(hospital) time(month) aggregate(standard) vce(hc2)
Computing degrees-of-freedom:
procedure .....
Number of groups and treatment time
Time variable: month
              procedure = 0
Control:
             procedure = 1
Treatment:
                Control Treatment
Group
   hospital
                                18
Time
    Minimum
    Maximum
Difference-in-differences regression
                                                        Number of obs = 322
                                                        No. of clusters = 46
Data type:
             Repeated cross-sectional
Aggregation:
             Standard
                          Robust HC2
       satis
              Coefficient std. err.
                                               P>|t|
                                                         [95% conf. interval]
ATET
   procedure
       (New
        WS
       014)
                 8500467
                           0329513
                                       25.80
                                               0.000
                                                         7832444
                                                                      916849
```

Note: ATET estimate adjusted for group effects and time effects.

Conclusions

- DID and DDD estimation for cross-sectional and panel-data
- Graphical diagnostics and tests to validate identification strategy
- Standard errors for situations with the number of groups is small
- Just a first step from which we will build