

# Introduction to Bayesian Analysis in Stata

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Outline

General idea

The method

Fundamental  
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bayes: - bayesmh  
Postestimation

Examples

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## 1 Bayesian analysis: Basic concepts

- The general idea
- The method

## 2 The Stata tools

- The general command `bayesmh`
- The `bayes` prefix
- Postestimation commands

## 3 A few examples

- Probit regression
- Panel data random-effects Poisson model
- Change-point model

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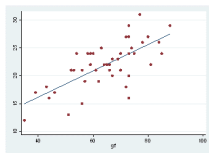
References

# Frequentist

Theoretical Model

. list in\_wage union hours who\_work tenure race grade ctt\_esp in 1/15, noobs

in_wage	union	hours	who_work	tenure	race	grade	ctt_esp
1.451214	-	20	27	.0833333	black	12	1.083333
1.12882	-	44	18	.0833333	black	12	1.271445
1.589977	1	65	51	.1666667	black	12	2.216451
1.198273	-	48	3	.0833333	black	12	2.384182
1.779512	-	10	24	.1666667	black	12	2.771445
1.778481	0	32	52	.1	black	12	2.771445
2.493974	-	32	4	.0833333	black	12	3.861784
2.551715	1	65	75	1.833333	black	12	5.298875
2.422261	1	49	181	.1666667	black	12	5.298875
2.414312	1	42	91	1.916667	black	12	7.183256
2.536374	1	45	95	3.916667	black	12	8.98718
2.662927	1	49	79	5.933333	black	12	10.13331
1.180748	0	40	13	-.75	black	12	-7.715384
1.204598	-	40	22	.5	black	12	1.188815
1.588863	-	40	11	.5833333	black	12	5.488338



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I don't know.

# Bayesian

----- STATA -- bayes option bayes\_which bayes\_which bayes\_which bayes\_which bayes\_which bayes\_which bayes\_which bayes\_which

id	weight	variance	sd	std_err	prob	prob	prob	prob	prob	prob
1	1.45	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
2	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
3	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
4	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
5	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
6	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
7	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
8	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
9	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000
10	1.000000	0.0004	0.02	0.02	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000	0.00000000



# Bayesian Analysis vs Frequentist Analysis

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## Frequentist Analysis

- Estimates unknown fixed parameters.
- The data come from a random sample (hypothetical repeatable).
- Uses data to estimate unknown fixed parameters.
- Data expected to satisfy the assumptions for the specified model.

"Conclusions are based on the distribution of statistics derived from random samples, assuming unknown but fixed parameters."

## Bayesian Analysis

- Probability distributions for unknown random parameters.
- The data are fixed.
- Combines data with prior beliefs to get updated probability distributions for the parameters.
- Posterior distribution is used to make explicit probabilistic statements.

"Bayesian analysis answers questions based on the distribution of parameters conditional on the observed sample."

Stata's convenient syntax: `bayes:`

```
regress y x1 x2 x3
```

```
bayes: regress y x1 x2 x3
```

```
logit y x1 x2 x3
```

```
bayes: logit y x1 x2 x3
```

```
mixed y x1 x2 x3 || region:
```

```
bayes: mixed y x1 x2 x3 || region:
```

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- Inverse law of probability (Bayes' Theorem):

$$p(\theta|y) = \frac{p(y|\theta)p(\theta)}{p(y)} = \frac{f(y; \theta)\pi(\theta)}{f(y)}$$

Where:

$f(y; \theta)$ : probability density function for  $y$  given  $\theta$ .

$\pi(\theta)$ : prior distribution for  $\theta$

- The marginal distribution of  $y$ ,  $f(y)$ , does not depend on  $\theta$ ; then we can write the fundamental equation for Bayesian analysis:

$$p(\theta|y) \propto L(\theta|y)\pi(\theta)$$

Where:

$L(\theta|y)$ : likelihood function of the parameters given the data.

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- Inverse law of probability (Bayes' Theorem):

$$p(\theta|y) = \frac{p(y|\theta)p(\theta)}{p(y)} = \frac{f(y;\theta)\pi(\theta)}{f(y)}$$

Where:

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- The marginal distribution of  $y$ ,  $f(y)$ , does not depend on  $\theta$ ; then we can write the fundamental equation for Bayesian analysis:

$$p(\theta|y) \propto L(\theta|y)\pi(\theta)$$

Where:

$L(\theta|y)$ : likelihood function of the parameters given the data.

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## The method

- Let's assume that both the data and the prior beliefs are normally distributed:
  - **The data:**  $y \sim N(\theta, \sigma_d^2)$
  - **The prior:**  $\theta \sim N(\mu_p, \sigma_p^2)$
- **Homework...:** Doing the algebra with the fundamental equation, we find that the posterior distribution would be normal with (see for example Cameron & Trivedi 2005):
  - **The posterior:**  $\theta|y \sim N(\mu, \sigma^2)$

Where:

$$\begin{aligned}\mu &= \sigma^2 (N\bar{y}/\sigma_d^2 + \mu_p/\sigma_p^2) \\ \sigma^2 &= (N/\sigma_d^2 + 1/\sigma_p^2)^{-1}\end{aligned}$$

# Example (Prior distributions)

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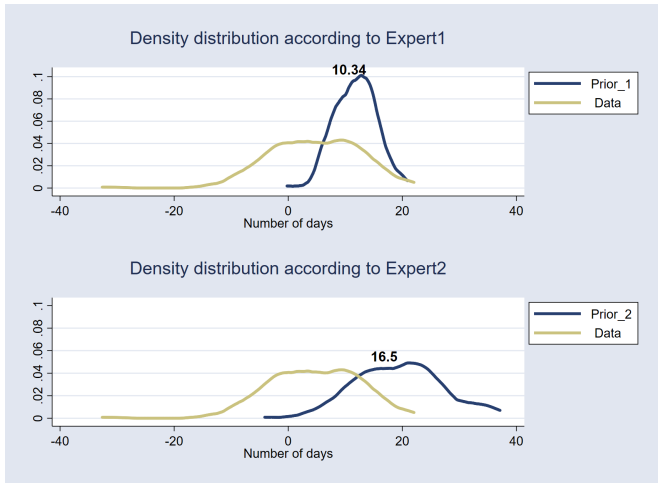
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# Example (Posterior distributions)

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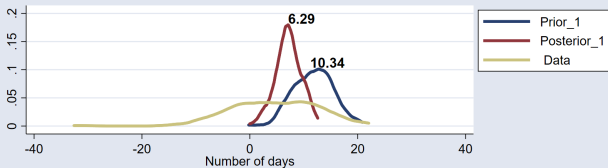
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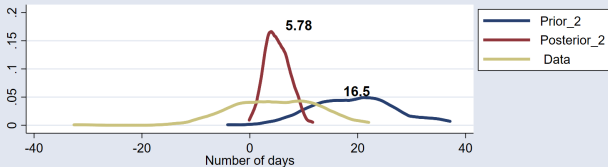
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Posterior density distribution according to Expert1



Posterior density distribution according to Expert2



## The method

- The previous example has a closed form solution.
- What about the cases with non-closed solutions, or more complex distributions?
  - Integration is performed via simulation.
  - We need to use intensive computational simulation tools to find the posterior distribution in most cases.
  - Markov chain Monte Carlo (MCMC) methods are the current standard in most software. Stata implements two alternatives:
    - Metropolis–Hastings (MH) algorithm
    - Gibbs sampling

## The method

- Links for Bayesian analysis and MCMC on our YouTube channel:

- Introduction to Bayesian statistics, part 1: The basic concepts

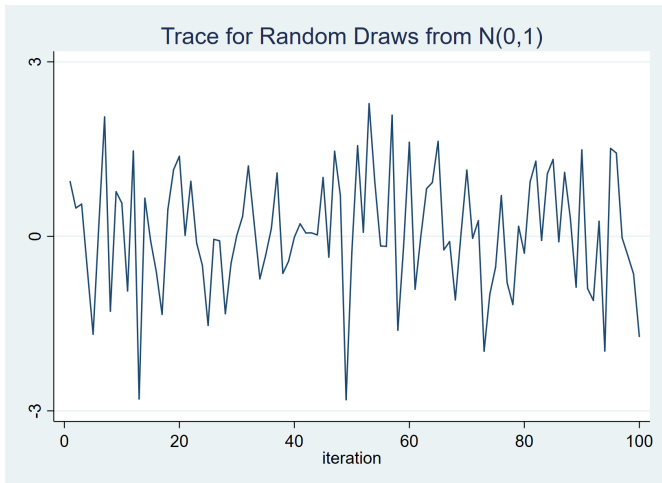
<https://www.youtube.com/watch?v=0F0QoMCSKJ4&feature=youtu.be>

- Introduction to Bayesian statistics, part 2: MCMC and the Metropolis–Hastings algorithm.

<https://www.youtube.com/watch?v=OTO1DygELpY&feature=youtu.be>

# The method

- Monte Carlo Simulation



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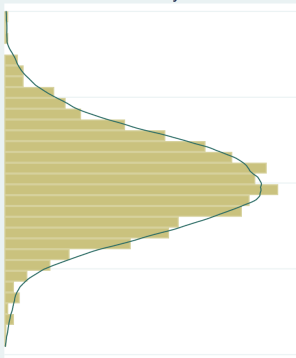
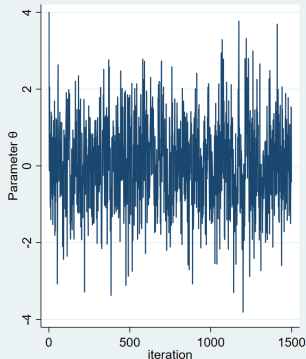
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- Metropolis–Hastings simulation
  - The trace plot illustrates the sequence of accepted proposal states.

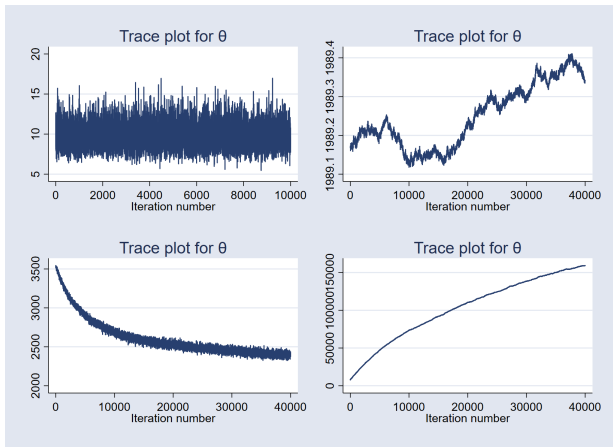
### Adaptive Metropolis-Hastings simulation Graphical illustration

Density

Trace Plot of  $\theta$ 

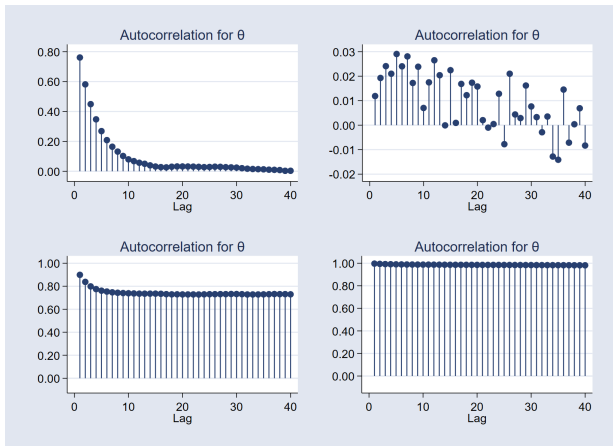
# The method

- We expect to obtain a stationary sequence when convergence is achieved.



# The method

- An efficient MCMC should have small autocorrelation.
- We expect autocorrelation to become negligible after a few lags.



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# The Stata tools for Bayesian regression

## The Stata tools: `bayes:` `bayesmh`

- `bayes:` Convenient syntax for Bayesian regressions
  - Estimation command defines the likelihood for the model.
  - Default priors are assumed to be "weakly informative".
  - Other model specifications are set by default depending on the model defined by the estimation command.
  - Alternative specifications may need to be evaluated.
- `bayesmh` General purpose command for Bayesian analysis
  - You need to specify all the components for the Bayesian regression: likelihood, priors, hyperpriors, blocks, etc.

## The Stata tools: Postestimation commands

- `bayesstats ess`
- `bayesgraph`
- `bayesstats ic`
- `bayestest model`
- `bayestest interval`
- `bayesstats summary`

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## Example 1: Probit regression

- Let's look at our first example:

- We have stats on scores, strength of schedule, and bowl game result (win/loss) for the Texas A&M University football team.
- We fit a probit model for the probability to win the bowl game.
- Let's consider a couple of model specifications for a binary dependent variable, whose values depend on a linear latent variable:

$$win\_bowl^* = \alpha_1 + \beta_{sc\_dif} * score\_dif + \beta_{sos} * sos + \epsilon_1$$

$$win\_bowl^* = \alpha_2 + \beta_{scored} * score\_avg + \beta_{against} * against\_avg + \epsilon_2$$

$$win\_bowl = \begin{cases} 1 & \text{if } win\_bowl^* > 0 \\ 0 & \text{otherwise} \end{cases}$$

Where:

- `win_bowl` : result in the bowl game (winloss).
- `score_dif` : Average score difference during the regular season.
- `sos` : Strength of schedule.
- `score_avg` : Average points scored during the regular season.
- `against_avg` : Average points against during the regular season.

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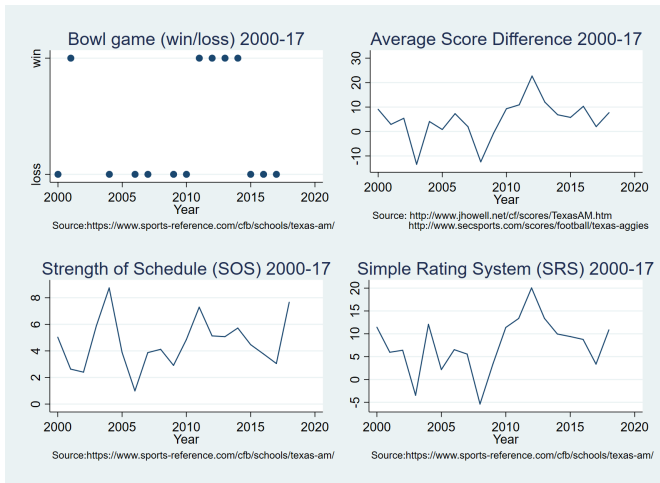
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## Example 1: Probit regression

- Probit regression with the `bayes:` prefix

```
bayes, rseed(123): probit win_bowl score_diff sos
```

- Equivalent model with `bayesmh`

```
bayesmh win_bowl score_diff sos, rseed(123)    ///  
likelihood(probit)                            ///  
prior({win_bowl:score_diff}, normal(0,10000)) ///  
prior({win_bowl:sos}, normal(0,10000))       ///  
prior({win_bowl:_cons}, normal(0,10000))
```

# Example 1: Menu for Bayesian regression

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The screenshot shows the Stata 15.1 interface with the 'Statistics' menu open. The path to 'Binary outcomes' is highlighted: Statistics > User > Bayesian analysis > Regression models > Binary outcomes.

- File
- Edit
- Data
- Graphics
- Statistics
  - Count outcomes
  - Fractional outcomes
  - Generalized linear models
  - Time series
  - Multivariate time series
  - Spatial autoregressive models
  - Longitudinal/panel data
  - Multilevel mixed-effects models
  - Survival analysis
  - Epidemiology and related
  - Endogenous covariates
  - Sample-selection models
  - Treatment effects
  - SEM (structural equation modeling)
  - LCA (latent class analysis)
  - FMM (finite mixture models)
  - IRT (item response theory)
  - Survey data analysis
  - Multiple imputation
  - Nonparametric analysis
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  - Power and sample size
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    - Postestimation
    - Other
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    - Interval hypothesis testing
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  - Categorical outcomes
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  - Multivariate models
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- Help

# Example 1: Menu for Bayesian regression

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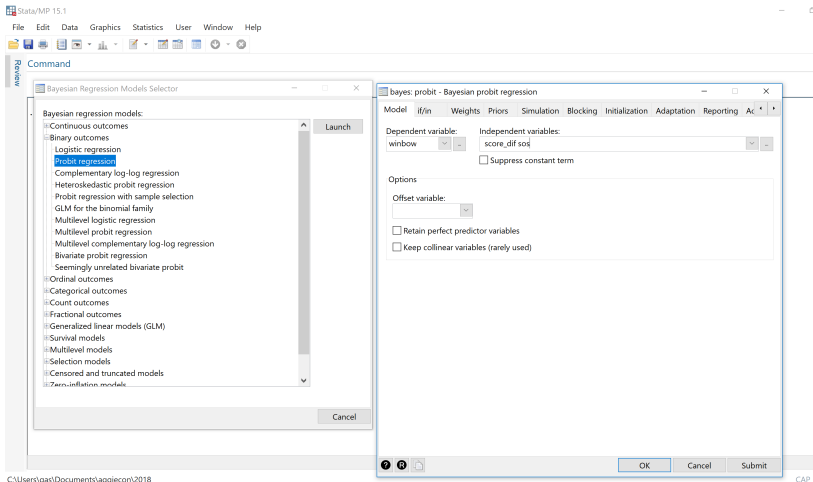
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## Example 1: Menu for Bayesian regression

- 1 Make the following sequence of selection from the main menu:

Statistics > Bayesian analysis > Regression models

- 2 Select "Binary outcomes"
- 3 Select "Probit regression"
- 4 Click on "Launch"
- 5 Specify the dependent variable (`win_bowl`) and the explanatory variables (`score_dif sos`)
- 6 Click on "OK"

# Example 1: bayes : prefix

```
. bayes, rseed(123):probit win_bowl score_dif sos
```

**Burn-in ...**

**Simulation ...**

**Model summary**

---

**Likelihood:**

```
win_bowl ~ probit(xb_win_bowl)
```

**Prior:**

```
{win_bowl:score_dif sos _cons} ~ normal(0,10000)
```

---

(1) Parameters are elements of the linear form `xb_win_bowl`.

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## Example 1: bayes : prefix

```
. bayes, rseed(123):probit win_bowl score_dif sos
```

Bayesian probit regression  
Random-walk Metropolis-Hastings sampling

MCMC iterations = 12,500  
Burn-in = 2,500  
MCMC sample size = 10,000  
Number of obs = 14  
Acceptance rate = .2522  
Efficiency: min = .06504  
              avg = .07364  
              max = .07973

Log marginal likelihood = -25.891444

win_bowl	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
score_dif	.1722847	.1011987	.003668	.1633205	.0064462	.4011969
sos	.0797042	.2138371	.007573	.0882321	-.3346481	.4871838
_cons	-2.08378	1.128949	.044266	-2.033869	-4.501485	.0358983

Note: Default priors are used for model parameters.

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Example 1: `bayesstats ess`

- Let's evaluate the effective sample size.

```
. bayesstats ess
Efficiency summaries      MCMC sample size =      10,000
```

winbowl	ESS	Corr. time	Efficiency
<code>score_dif</code>	761.28	13.14	0.0761
<code>sos</code>	797.34	12.54	0.0797
<code>_cons</code>	650.45	15.37	0.0650

- We expect to have an acceptance rate (see previous slide) that is neither too small nor too large.
- We also expect to have low correlation.
- Efficiencies over 10% are considered good for MH. Efficiencies under 1% would be a source of concern.

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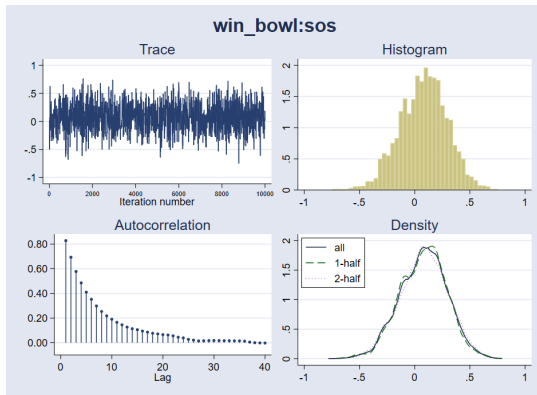
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## Example 1: bayesgraph

- We can use `bayesgraph` to look at the trace, the correlation, and the density. For example:

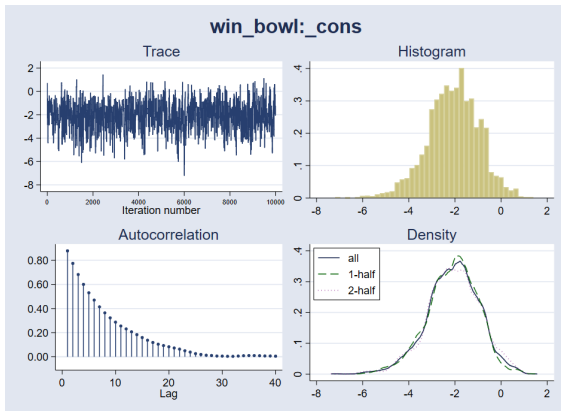
**. bayesgraph diagnostic {sos}**

- The trace indicates that convergence was achieved.
- Correlation dies out after around 10 periods.

## Example 1: bayesgraph

- We can use `bayesgraph` to look at the trace, the correlation, and the density. For example:

### . bayesgraph diagnostic {\_cons}



- Correlation dies out after around 15 periods.

Example 1: `bayestest model`

- `bayestest model` is another postestimation command to compare different models.
- `bayestest model` computes the posterior probabilities for each model.
- The result indicates which model is more likely.
- It requires that the models use the same data and that they have proper posterior.
- It can be used to compare models with:
  - Different priors and/or different posterior distributions.
  - Different regression functions.
  - Different covariates.
- MCMC convergence should be verified before comparing the models.

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Example 1: `bayestest model`

- Let's fit two other models and compare them with the one we already fit.
- We store the results for the three models, and we use the postestimation command `bayestest model` to select one of them.

```
quietly {
    bayes , rseed(123) saving(dif_sos,replace):    ///
        probit winbowl score_dif sos
    estimates store dif_sos

    bayes , rseed(123) saving(score,replace):    ///
        probit winbowl scored_avg against_avg
    estimates store scored_against

    bayes , rseed(123) saving(srs_linear,replace) ///
        prior({winbowl:srs}, normal(10,20)):    ///
        block({winbowl:srs_cons}):             ///
        regress winbowl srs
    estimates store srs_linear
}
bayestest model dif_sos scored_against srs_linear
```

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## Example 1: bayestest model

- Here is the output for bayestest model

```
. quietly {
. bayestest model dif_sos scored_against srs_linear
Bayesian model tests
```

	log(ML)	P (M)	P (M y)
dif_sos	-25.9158	0.3333	0.3679
scored_against	-26.7528	0.3333	0.1593
srs_linear	-25.6652	0.3333	0.4727

**Note:** Marginal likelihood (ML) is computed using Laplace-Metropolis approximation.

- We could also assign different priors for the models:

```
. bayestest model dif_sos scored_against srs_linear, ///
prior(.3 .5 .2)
```

Bayesian model tests

	log(ML)	P (M)	P (M y)
dif_sos	-25.9158	0.3000	0.3879
scored_against	-26.7528	0.5000	0.2799
srs_linear	-25.6652	0.2000	0.3322

**Note:** Marginal likelihood (ML) is computed using Laplace-Metropolis approximation.

## Example 1: bayestest model

- Here is the output for `bayestest model`

```
. quietly {
. bayestest model dif_sos scored_against srs_linear
Bayesian model tests
```

	log(ML)	P (M)	P (M y)
<code>dif_sos</code>	-25.9158	0.3333	<b>0.3679</b>
<code>scored_against</code>	-26.7528	0.3333	<b>0.1593</b>
<code>srs_linear</code>	-25.6652	0.3333	<b>0.4727</b>

Note: Marginal likelihood (ML) is computed using Laplace-Metropolis approximation.

- We could also assign different priors for the models:

```
. bayestest model dif_sos scored_against srs_linear, ///
prior(.3 .5 .2)
```

Bayesian model tests

	log(ML)	P (M)	P (M y)
<code>dif_sos</code>	-25.9158	<b>0.3000</b>	0.3879
<code>scored_against</code>	-26.7528	<b>0.5000</b>	0.2799
<code>srs_linear</code>	-25.6652	<b>0.2000</b>	0.3322

Note: Marginal likelihood (ML) is computed using Laplace-Metropolis approximation.

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## Example 2: Random-effects Poisson model

## Example 2: Random-effects Poisson model

- Let's use `bayes`: to fit a random-effects Poisson model for a count dependent variable.

$$\Pr(y_{it} = y | x_{it}, \alpha_j) = \frac{e^{-\mu_{it}} \mu_{it}^y}{y!}$$

Where:

$$\mu_{i,t} = \exp(x_{i,t}\beta + \alpha_j)$$

$\alpha_j \sim N(0, \sigma_\alpha^2)$  is the individual panel random effect.

- This is also referred to as a two-level random intercept model.
- We can also fit this model with `mepoisson` or `xtpoisson, re normal`.

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## Example 2: Random-effects Poisson model

- This time we are going to work with simulated data.
- Here is the code to simulate the panel dataset:

```
clear
set obs 300
set seed 123

*Panel level*
generate id      = _n
generate alpha  = rnormal(0, .33)

*Observation level*
expand 5
bysort id:generate year = _n
xtset id year
generate x1 = rnormal()
generate x2 = runiform()
generate x3 = rnormal()

*Generate dependent variable*

generate y = rpoisson(exp(.1*x1-.1*x2+.1*x3+.75+alpha))
```

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## Example 2: Random-effects Poisson model

Let's show the results with `mepoisson`:

```
. mepoisson y x1 x2 x3 || id:,nolog
```

```
Mixed-effects Poisson regression
Group variable:          id
```

```
Number of obs      =      1,500
Number of groups   =         300
```

```
Obs per group:
    min =          5
    avg =         5.0
    max =          5
```

```
Integration method: mvaghermite
```

```
Integration pts.   =          7
```

```
Log likelihood = -2646.5534
```

```
Wald chi2(3)       =        68.33
Prob > chi2        =         0.0000
```

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
x1	.0806379	.0192914	4.18	0.000	.0428275	.1184484
x2	-.1134928	.06522	-1.74	0.082	-.2413217	.0143361
x3	.1285766	.0187383	6.86	0.000	.0918502	.1653029
_cons	.7373862	.0416085	17.72	0.000	.655835	.8189375
<b>id</b>						
var(_cons)	.1087738	.0171051			.0799226	.14804

```
LR test vs. Poisson model: chibar2(01) = 116.41
```

```
Prob >= chibar2 = 0.0000
```

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## Example 2: Random-effects Poisson model

- We now fit the model with `bayes` :

```
bayes, nodots rseed(123): ///  
mepoisson y x1 x2 x3 || id:
```

- Equivalent model with `bayesmh`

```
bayesmh y x1 x2 x3, rseed(123)           ///  
likelihood(poisson) reffects(id)        ///  
prior({y:x1 x2 x3 _cons}, normal(0,10000)) ///  
prior({y:i.id}, normal(0,{sigma2}))     ///  
prior({sigma2}, igamma(.01,.01))       ///  
block({sigma2}) nodots
```

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## Example 2: Random-effects Poisson model

```
. bayes, nodots rseed(123) :      ///  
>      mepoisson y x1 x2 x3 || id:
```

**Burn-in ...**

**Simulation ...**

**Multilevel structure**

---

**id**

{U0}: random intercepts

---

**Model summary**

---

**Likelihood:**

y ~ mepoisson(xb\_y)

**Priors:**

{y:x1 x2 x3 \_cons} ~ normal(0,10000) (1)

{U0} ~ normal(0,{U0:sigma2}) (1)

**Hyperprior:**

{U0:sigma2} ~ igamma(.01,.01)

---

(1) Parameters are elements of the linear form **xb\_y**.

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## Example 2: Random-effects Poisson model

```
. bayes, nodots rseed(123) :      ///
>      mepoisson y x1 x2 x3 || id:
```

```
Bayesian multilevel Poisson regression
Random-walk Metropolis-Hastings sampling
```

```
Group variable: id
```

```
Family : Poisson
Link   : log
```

```
Log marginal likelihood
```

```
MCMC iterations = 12,500
Burn-in        = 2,500
MCMC sample size = 10,000
Number of groups = 300
Obs per group:
    min = 5
    avg = 5.0
    max = 5
Number of obs   = 1,500
Acceptance rate = .2715
Efficiency: min = .02614
              avg = .0409
              max = .05729
```

		Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
y	x1	.0810731	.0192223	.000803	.0805926	.0448467	.1195346
	x2	-.1137537	.0648044	.003071	-.1128703	-.2428485	.0164924
	x3	.1296011	.0183267	.00082	.1294387	.0931207	.167355
	_cons	.7368688	.0427745	.002624	.7378466	.6528039	.8186462
id	U0:sigma2	.1099352	.0177164	.001096	.1093387	.0765145	.1469857

Note: Default priors are used for model parameters.

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## Example 2: Random-effects Poisson model

```
. bayesstats ess
```

```
Efficiency summaries      MCMC sample size =      10,000
```

		ESS	Corr. time	Efficiency
<b>y</b>	<b>x1</b>	572.89	17.46	0.0573
	<b>x2</b>	445.22	22.46	0.0445
	<b>x3</b>	499.81	20.01	0.0500
	<b>_cons</b>	265.72	37.63	0.0266
<b>id</b>	<b>U0:sigma2</b>	261.41	38.25	0.0261

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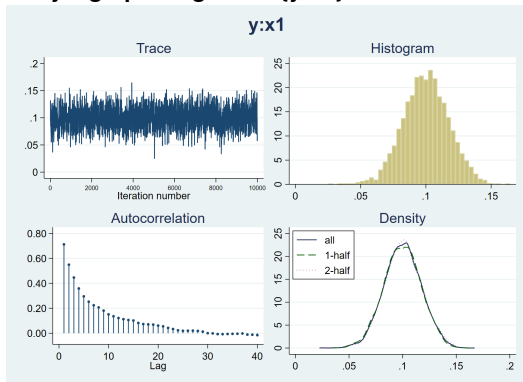
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## Example 2: bayesgraph diagnostic

- We can look at the diagnostic graph for a couple of variables:

```
. bayesgraph diagnostic {y:x1}
```

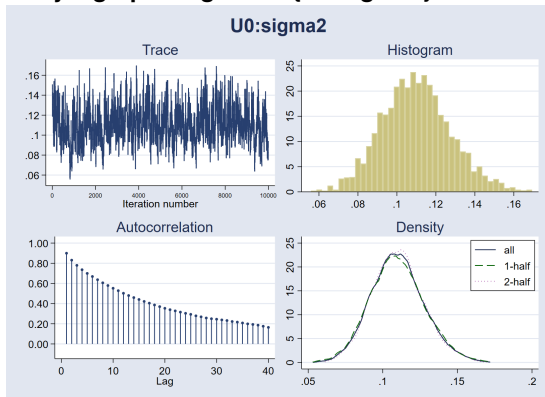


- The trace seems to indicate convergence.
- Autocorrelation becomes negligible after about 15 periods.
- Densities are similar for first and second halves of the MCMC sample.

## Example 2: bayesgraph diagnostic

- We now look at the diagnostic graphs for {U0:sigma2}

### . bayesgraph diagnostic {U0:sigma2}



- The trace seems to indicate convergence.
- Autocorrelation is slightly high, but decays steadily.
- Densities are similar for first and second halves of the MCMC sample.



Example 2: `bayestest interval`

- We can perform interval testing with the postestimation command `bayestest interval`.
- It estimates the probability that a model parameter lies in a particular interval.
- For continuous parameters, the hypothesis is formulated in terms of intervals.
- We can perform point hypothesis testing only for parameters with discrete posterior distributions.
- `bayestest interval` estimates the posterior distribution for a null hypothesis about intervals for one or more parameters .
- `bayestest interval` reports the estimated posterior mean probability for  $H_0$ .

```
bayestest interval ( {y:x1} ,lower(.08) upper(.12)) ///  
                   ( {y:x2} ,lower(-.12) upper(-.09))
```

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## Example 2: bayestest interval

- We can, for example, perform separate tests for different parameters:

```
. bayestest interval (({y:x1},lower(.08) upper(.12)) ///
>                    ({y:x2},lower(-.12) upper(-.09))
Interval tests      MCMC sample size =    10,000
prob1 : .08 < {y:x1} < .12
prob2 : -.12 < {y:x2} < -.09
```

	Mean	Std. Dev.	MCSE
prob1	.4909	0.49994	.0199632
prob2	.1926	0.39436	.0145117

- If we draw  $\theta_1$  from the specified prior and we use the data to update the knowledge about  $\theta_1$ , then there is a 49% chance that  $\theta_1$  belongs to the interval (.08,.12).

- We can also perform a joint test:

```
. bayestest interval ((({y:x1},lower(.08) upper(.12)) ///
>                    ({y:x2},lower(-.12) upper(-.09)),joint)
Interval tests      MCMC sample size =    10,000
prob1 : .08 < {y:x1} < .12, -.12 < {y:x2} < -.09
```

	Mean	Std. Dev.	MCSE
prob1	.0885	0.28403	.0098171

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## Example 2: bayestest interval

- We can, for example, perform separate tests for different parameters:

```
. bayestest interval (({y:x1},lower(.08) upper(.12)) ///
>                    ({y:x2},lower(-.12) upper(-.09))
Interval tests      MCMC sample size =    10,000
prob1 : .08 < {y:x1} < .12
prob2 : -.12 < {y:x2} < -.09
```

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- We can also perform a joint test:

```
. bayestest interval (({y:x1},lower(.08) upper(.12)) ///
>                    ({y:x2},lower(-.12) upper(-.09)), joint)
Interval tests      MCMC sample size =    10,000
prob1 : .08 < {y:x1} < .12, -.12 < {y:x2} < -.09
```

	Mean	Std. Dev.	MCSE
prob1	.0885	0.28403	.0098171

## Example 2: Show random effects

```
. bayes, show({U0[1/6]}) noheader
```

U0[id]	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
1	.1005875	.2248611	.005989	.1137852	-.3503203	.5382369
2	-.1376598	.2372418	.006347	-.1312831	-.6391449	.3238192
3	.1669656	.2171576	.006349	.1645487	-.2620912	.5840191
4	.1415134	.2192747	.006385	.1401843	-.3075952	.5717826
5	-.0802774	.2361239	.007224	-.0747518	-.5665242	.3531596
6	.1128583	.2338012	.006719	.1093227	-.3585934	.5664554

Note: Default priors are used for model parameters.

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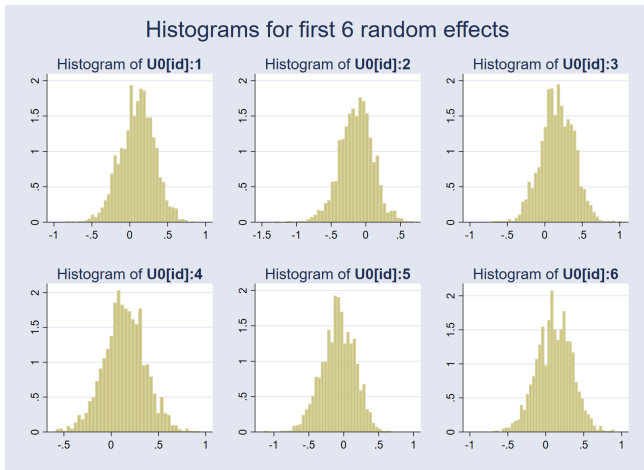
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## Example 2: Histograms for random effects

- `bayesgraph histogram`

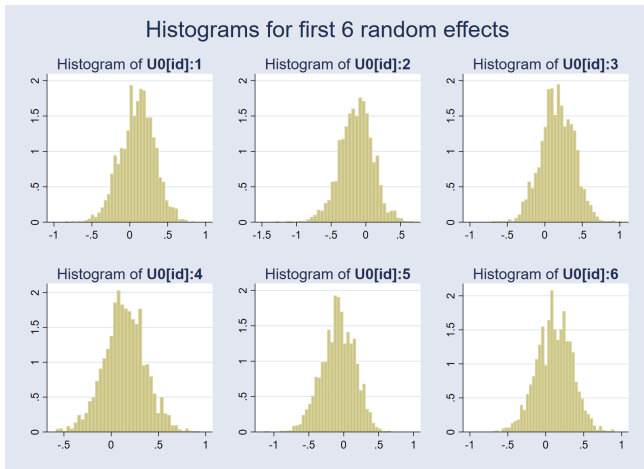
```
. bayesgraph histogram {U0[1/6]},name(g1 g2 g3 g4 g5 g6,replace)
. graph combine g1 g2 g3 g4 g5 g6, ///
> title("Histograms for first 6 random effects")
```



## Example 2: Histograms for random effects

- `bayesgraph histogram`

```
. bayesgraph histogram {U0[1/6]},name(g1 g2 g3 g4 g5 g6,replace)
. graph combine g1 g2 g3 g4 g5 g6, ///
> title("Histograms for first 6 random effects")
```



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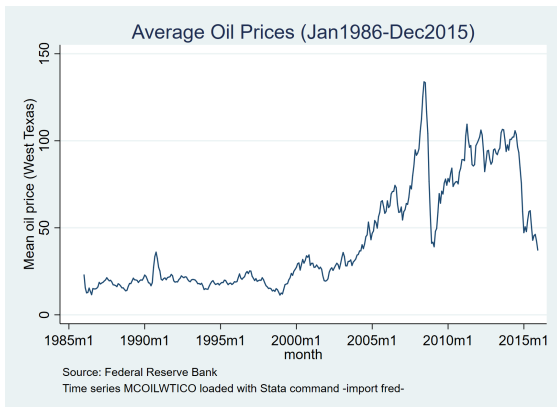
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## Example 3: Change-point model

## Example 3: Change-point model

- Let's work now with an example where we write our model using a substitutable expression.
- We have average oil prices for January 1986 to December 2015:



- The series has a significant increase around 2005.
- We may consider fitting a change-point model.



## Example 3: Gibbs sampling

Change-point model specification with blocking

```

bayesmh oilprice = ({mu1}*sign(year<{cp})           ///
                    + {mu2}*sign(year>={cp})),      ///
    likelihood(normal({var}))                       ///
    prior({mu1}, normal(0,50))                     ///
    prior({mu2}, normal(50,150))                   ///
    prior({cp}, uniform(tm(1986m1),2015m12))       ///
    prior({var}, igamma(.01,.01))                  ///
    initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1)) ///
    block({var}, gibbs) block({cp}) blocksummary  ///
    rseed(123) mcmcsize(40000)                     ///
    dots(500,every(5000))

quietly {
    matrix mean=e(mean)
    noisily display _n _col(10) "Date: " mean[1,1]   ///
                 _n _col(17) "Cut point (Month): " %tm mean[1,1]
}

```

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## Example 3: Gibbs sampling

Change-point model specification with blocking

```

bayesmh oilprice = ({mu1}*sign(year<{cp})
                    + {mu2}*sign(year>={cp})),
likelihood(normal({var}))
prior({mu1}, normal(0,50))
prior({mu2}, normal(50,150))
prior({cp}, uniform(tm(1986m1),2015m12))
prior({var}, igamma(.01,.01))
initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1))
block({var}, gibbs) block({cp}) blocksummary
rseed(123) mcmcsize(40000)
dots(500,every(5000))

quietly {
  matrix mean=e(mean)
  noisily display _n _col(10) "Date: " mean[1,1]
             _n _col(17) "Cut point (Month): " %tm mean[1,1]
}

```

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## Example 3: Gibbs sampling

Change-point model specification with blocking

```

bayesmh oilprice = ({mu1}*sign(year<{cp})           ///
                    + {mu2}*sign(year>={cp})),      ///
likelihood(normal({var}))                          ///
prior({mu1}, normal(0,50))                          ///
prior({mu2}, normal(50,150))                        ///
prior({cp}, uniform(tm(1986m1),2015m12))          ///
prior({var}, igamma(.01,.01))                      ///
initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1))    ///
block({var}, gibbs) block({cp}) blocksummary    ///
rseed(123) mcmcsize(40000)                          ///
dots(500,every(5000))

quietly {
  matrix mean=e(mean)
  noisily display _n _col(10) "Date: " mean[1,1]    ///
    _n _col(17) "Cut point (Month): " %tm mean[1,1]
}

```

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## Example 3: Gibbs sampling

Change-point model specification with blocking

```

bayesmh oilprice = ({mu1}*sign(year<{cp})           ///
                    + {mu2}*sign(year>={cp})),      ///
likelihood(normal({var}))                        ///
prior({mu1}, normal(0,50))                       ///
prior({mu2}, normal(50,150))                    ///
prior({cp}, uniform(tm(1986m1),2015m12))        ///
prior({var}, igamma(.01,.01))                   ///
initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1))  ///
block({var}, gibbs) block({cp}) blocksummary  ///
rseed(123) mcmcsize(40000)                        ///
dots(500,every(5000))

quietly {
  matrix mean=e(mean)
  noisily display _n _col(10) "Date: " mean[1,1]    ///
    _n _col(17) "Cut point (Month): " %tm mean[1,1]
}

```

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## Example 3: Gibbs sampling

Change-point model specification with blocking

```

bayesmh oilprice = ({mu1}*sign(year<{cp})           ///
      + {mu2}*sign(year>={cp})),                 ///
      likelihood(normal({var}))                   ///
      prior({mu1}, normal(0,50))                 ///
      prior({mu2}, normal(50,150))             ///
      prior({cp}, uniform(tm(1986m1),2015m12)) ///
      prior({var}, igamma(.01,.01))             ///
      initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1)) ///
      block({var}, gibbs) block({cp}) blocksummary ///
      rseed(123) mcmcsize(40000)                 ///
      dots(500,every(5000))
quietly {
  matrix mean=e(mean)
  noisily display _n _col(10) "Date: " mean[1,1]      ///
    _n _col(17) "Cut point (Month): " %tm mean[1,1]
}

```

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## Example 3: Gibbs sampling

## Change-point model specification with blocking

```

. bayesmh oilprice=({mu1}*sign(month<{cp}))+{mu2}*sign(month>={cp})), ///
> likelihood(normal({var})) ///
> prior({mu1}, normal(0,50)) ///
> prior({mu2}, normal(50,150)) ///
> prior({cp}, uniform(tm(1986m1),tm(2015m12))) ///
> prior({var}, igamma(.01,.01)) ///
> initial({mu1} =15 {mu2} =100 {cp} =tm(1986m1)) rseed(123) ///
> block({var}, gibbs) block({cp}) blocksummary ///
> mcmcsizes(20000) dots(500, every(5000))

```

Burn-in 2500 aaaaa done

Simulation 20000 .....5000.....10000.....15000.....20000 done

---

**Model summary**
**Likelihood:**

oilprice ~ normal({mu1}\*sign(month<{cp}))+{mu2}\*sign(month>={cp}), {var})

**Priors:**

{var} ~ igamma(.01,.01)

{mu1} ~ normal(0,50)

{mu2} ~ normal(50,150)

{cp} ~ uniform(tm(1986m1),tm(2015m12))

---

**Block summary**

1: {var}

(Gibbs)

2: {cp}

3: {mu1} {mu2}

---

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## Example 3: Gibbs sampling

## Change-point model specification with blocking

```

. bayesmh oilprice={({mul}*sign(month<{cp}))+{mu2}*sign(month>={cp)}), ///
> likelihood(normal({var})) ///
> prior({mul}, normal(0,50)) ///
> prior({mu2}, normal(50,150)) ///
> prior({cp}, uniform(tm(1986m1),tm(2015m12))) ///
> prior({var}, igamma(.01,.01)) ///
> initial({mul} =15 {mu2} =100 {cp} =tm(1986m1)) rseed(123) ///
> block({var}, gibbs) block({cp}) blocksummary ///
> mcmcsize(20000) dots(500, every(5000))

```

```

Bayesian normal regression                MCMC iterations =      22,500
Metropolis-Hastings and Gibbs sampling    Burn-in           =       2,500
                                           MCMC sample size =     20,000
                                           Number of obs     =       360
                                           Acceptance rate   =      .5632
                                           Efficiency: min   =     .09094
                                           avg               =     .3304
                                           max               =       1
Log marginal likelihood = -1481.9487

```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
cp	541.5063	1.806737	.037169	541.4515	536.7238	544.9228
mul	22.07432	.936419	.01974	22.09333	20.23623	23.85525
mu2	78.69139	1.259118	.029524	78.67589	76.2043	81.19035
var	197.286	14.80914	.104716	196.6902	169.991	228.0003

```

. quietly {
                                elapsed date: 541.50629
                                Cut point (Month): 2005m2

```

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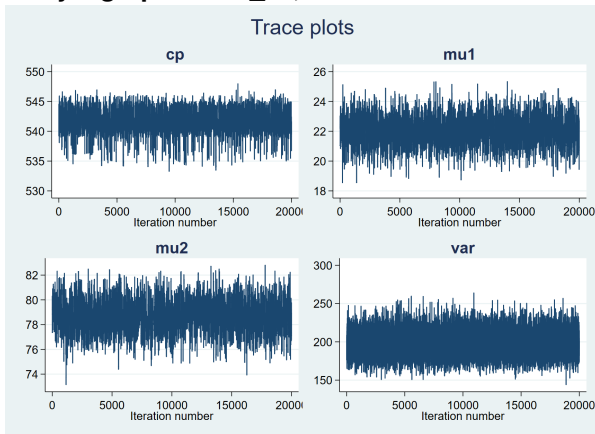
Gibbs sampling

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## Example 3: bayesgraph trace

- Use bayesgraph trace to look at the trace for all the parameters.

**. bayesgraph trace \_all,combine**

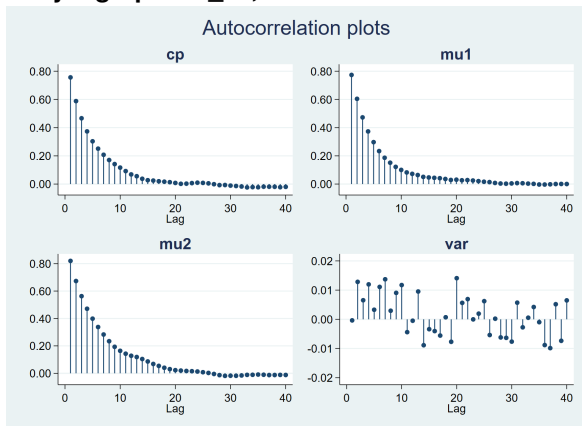
- The plots indicate that convergence seems to be achieved.



## Example 3: bayesgraph ac

- Use bayesgraph ac to look at the autocorrelation for all the parameters.

## . bayesgraph ac \_all,combine

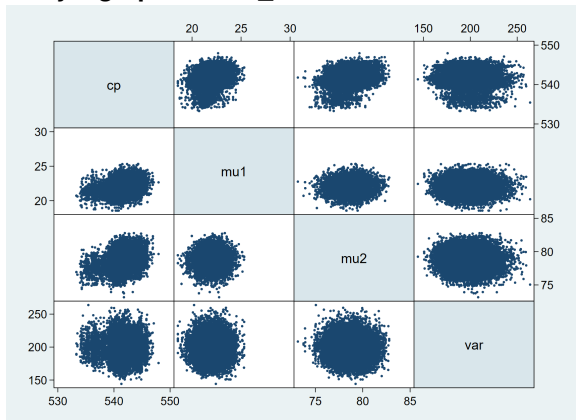


- Autocorrelation quickly becomes negligible for all the parameters.

## Example 3: bayesgraph matrix

- Use `bayesgraph matrix` to look at pairwise correlation for the parameters.

## . bayesgraph matrix\_all



- The plots seem to indicate that there are no significant pairwise correlations among the parameters.

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## Summing up

- **Bayesian analysis:** A statistical approach that can be used to answer questions about unknown parameters in terms of probability statements.
- It can be used when we have prior information on the distribution of the parameters involved in the model.
- Alternative approach or complementary approach to classic/frequentist approach?

## Reference

Cameron, A. and Trivedi, P. 2005. *Microeconometric Methods and Applications*. Cambridge University Press, Section 13.2.2, 422–423.

## Links

[https://www.stata.com/meeting/uk17/slides/uk17\\_Marchenko.pdf](https://www.stata.com/meeting/uk17/slides/uk17_Marchenko.pdf)

<https://www.stata.com/meeting/brazil16/slides/rising-brazil16.pdf>

[https://www.stata.com/meeting/spain18/slides/spain18\\_Sanchez.pdf](https://www.stata.com/meeting/spain18/slides/spain18_Sanchez.pdf)