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# Estimating breast cancer incidence using multiple imputation with chained equations (MICE)

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# Outline

- Brief background: Breast Cancer and its subtypes
- Motivation and aim: Estimating subtype-specific BC incidence using cancer registry data
- Available data – partly missing information on subtype
- Incidence estimation using multiple imputation with chained equations (MICE)
  - Why this is a non-standard multiple imputation
- Conclusions

# This work was recently published

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Methods described in  
Supplemental material.

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**RESEARCH ARTICLE**  
Cancer Epidemiology

**Age-specific breast cancer incidence by subtype, TNM stage and screening status in Sweden 2008–2019 estimated with multiple imputation**

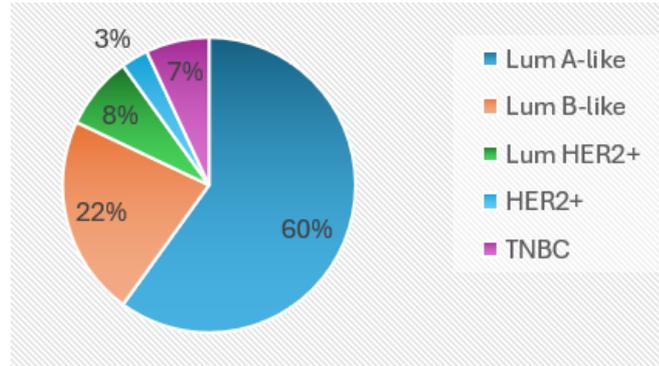
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**Abstract**  
Breast cancer incidence in women increases with age, but less is known about which subtypes contribute the most at different ages. We describe age-specific breast cancer incidence rates in Sweden by subtype, TNM stage and screening status. Population-based data were retrieved from the Swedish National Quality Register for Breast Cancer on 89,322 invasive breast cancer cases diagnosed 2008–2019 in women ≥18 years. Breast cancer subtypes were defined by estrogen and progester-

# Background

- Breast cancer is not one disease but many **subtypes** with different treatment and survival.
  - Underlying **molecular subtypes** are approximated by clinical subtype (“**surrogate subtype**”).
  - **5 “surrogate subtypes”**: ER, PR, HER2 receptors, grade and KI67.



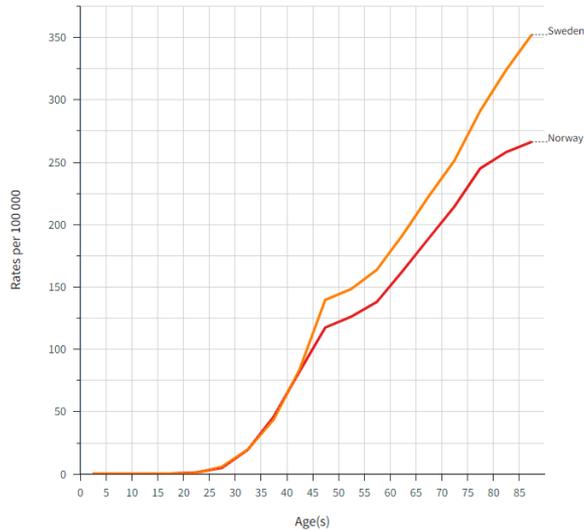
- Breast cancer subtypes have (partly) different underlying **risk factors** and **age-specific risk**.
- Also, **screening** is more likely to detect luminal tumours, while interval cancers are more often TNBC.

# Screening has changed the age-specific incidence pattern of breast cancer

- Data from NORDCAN.

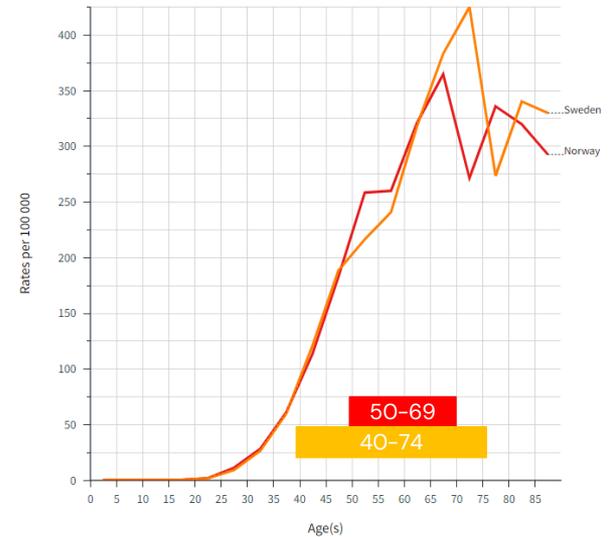
Rates per 100 000, Incidence, Females, [1975-1984]  
Breast  
Norway - Sweden

Before screening



Rates per 100 000, Incidence, Females, [2013-2022]  
Breast  
Norway - Sweden

After screening



## Our aim: Incidence rates of BC subtypes across age

- **Our aim** was to estimate and describe **subtype-specific BC incidence across age**.
- This will be correlated with screening, as well as shifts in underlying risk factors.
  - E.g. reproductive risk factors, obesity, alcohol, MHT (menopausal hormone therapy), genetics, etc.
- These results are important as basis for studies on clinical outcomes, e.g. understanding case-mix over time and ages, and studies on screening, e.g. extended screening ages.

## What data did we have

- Swedish National Quality Register of Breast Cancer (NKBC) was established in 2008.
  - Nationwide (population-based) cancer register.
  - Collects detailed **routine clinical** information on **all new** breast cancer cases diagnosed in women and men.
    - Patient and **tumour characteristics**, diagnostic work-up, planned/given treatment, follow-up.
  - One recorded tumour per side (max 2 per person) for Swedish residents only.
- We had data for women diagnosed with **invasive** BC 2008-2019, aged  $\geq 20$  at diagnosis. **N=89,322**
- Information on
  - **Date and age of diagnosis**
  - **Subtype: ER, PR, HER2, grade**
  - Stage: tumour size (T), lymph node metastasis (N), distant metastasis (M)
  - Screen-detected or symptomatically detected

## What data did we have

- 5 surrogate subtypes were based on: ER, PR, HER2, grade.

Surrogate subtype	ER	PR	HER2	Grade
Luminal A-like	+	+	-	Grade 1,2
	+	-	-	Grade 1
	-	+	-	Grade 1,2
Luminal B-like	+	+	-	Grade 3
	+	-	-	Grade 2,3
	-	+	-	Grade 3
Luminal HER2	+	+/-	+	Grade 1-3
HER2 positive	-	-	+	Grade 1-3
Triple-negative (TNBC)	-	-	-	Grade 1-3
% missing	4.1%	4.2%	7.9%	16.4%

15.5% missing subtype

# Incidence rate estimation

- Incidence rate:  $\lambda(\text{age, year}) = N_{\text{cases}} / N_{\text{poprisk}}$
- $N_{\text{cases}}$  : From NKBC : **case population (individual level)**
- $N_{\text{poprisk}}$  : From Statistics Sweden: **population at risk (counts by 1-year age, 1-year calendar time)**
- Estimated rates separately for each of the 5 subtypes.

- Lum A:  $\lambda_1(\text{age, year}) = N_{\text{cases, subtype 1}} / N_{\text{poprisk}}$
- Lum B:  $\lambda_2(\text{age, year}) = N_{\text{cases, subtype 2}} / N_{\text{poprisk}}$
- Lum HER2:  $\lambda_3(\text{age, year}) = N_{\text{cases, subtype 3}} / N_{\text{poprisk}}$
- HER2 pos:  $\lambda_4(\text{age, year}) = N_{\text{cases, subtype 4}} / N_{\text{poprisk}}$
- TNBC:  $\lambda_5(\text{age, year}) = N_{\text{cases, subtype 5}} / N_{\text{poprisk}}$

Note: Same  $N_{\text{poprisk}}$  for all incidence rates.  
Only the numerator differs.

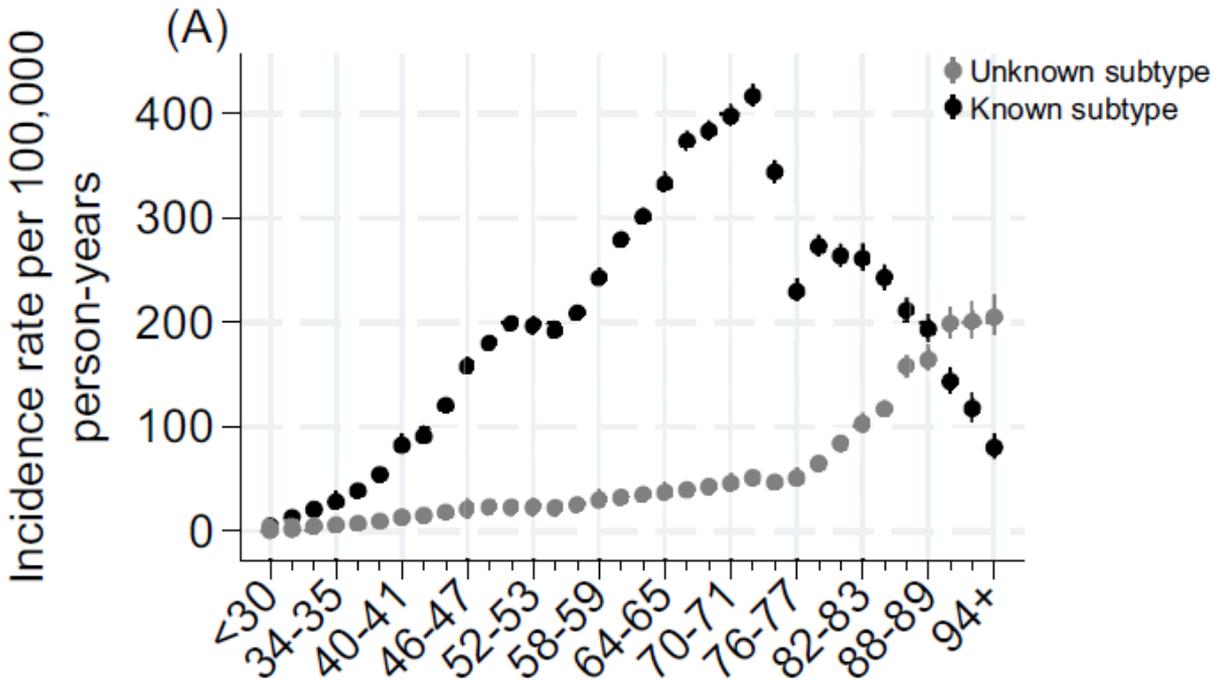
- **Incidence rates** can be estimated with Poisson regression for rates:

- $\ln(\lambda_i(\text{age, year})) = \alpha * X_{\text{age}} + \beta * X_{\text{year}}$
- $\ln(d_i(\text{age, year})) = \alpha * X_{\text{age}} + \beta * X_{\text{year}} + \ln(N_{\text{poprisk}})$
- We ignored the calendar time effect (as only 2008-2019):  $\ln(d_i(\text{age})) = \alpha * X_{\text{age}} + \ln(N_{\text{poprisk}})$
- For stability, we estimated rates per 2-year age groups, i.e. <30, 30-31, 32-33, ..., 90-91, 92-93, 94+.

## Missing data – on subtype

- Missing subtype: 15.5%; components had varying missing %
  - ER 4.1%, PR 4.2%, HER2 7.9%, grade 16.4%
  - **Leads to underestimation of the incidence rates with 15.5% - severe bias!**
- Reasons for missing
  - **Administrative missing** – not recorded in the earlier years, or in some regions/hospitals >> likely MCAR
  - Missing for **known reasons** – frail older women who are not eligible for certain treatments will not be investigated in detail, and thus will not be subtyped >> likely MAR (depending on known factors (age, treatment, comorbidity), which we can adjust for)
  - Missing for **unknown reasons** >> still likely MAR (depending on known factors)? Could also be MCAR/MNAR?
- Solution >> **Multiple Imputation with Chained Equations (MICE)**.
  - Model-based method to impute missing data based on information in known variables (MAR).

# Missing information depends on age



# Multiple Imputation with Chained Equations (MICE)

- We have applied **multiple imputation with chained equations** (MICE).
- This involves a 2-step procedure
  - ✓ Step 1: Imputation model to generate  $m$  imputed (completed) datasets.
  - ✓ Step 2: Analysis (substantive) model (i.e. Poisson) to estimate incidence rates and pooling parameters across imputed datasets using Rubin's rules #1 (mean) and #2 (variance).
- Key points:
  - Imputation model must capture the underlying reasons (patterns) for missing, e.g. age.
  - Imputation model must also reflect the analysis model, e.g. rates vary by age.
  - We added many clinical variables as auxiliary variables, and interactions with age (not trivial!). This will make the MAR assumption more likely.
- Implemented in Stata **mi package**:
  - Step 1: **mi impute**
  - Step 2: **mi estimate**

# Building the imputation model

Nelson-Aalen estimator of cumulative hazard of BC death and Overall death (OS)  
<sup>a</sup>=deterministic prediction before imputation.

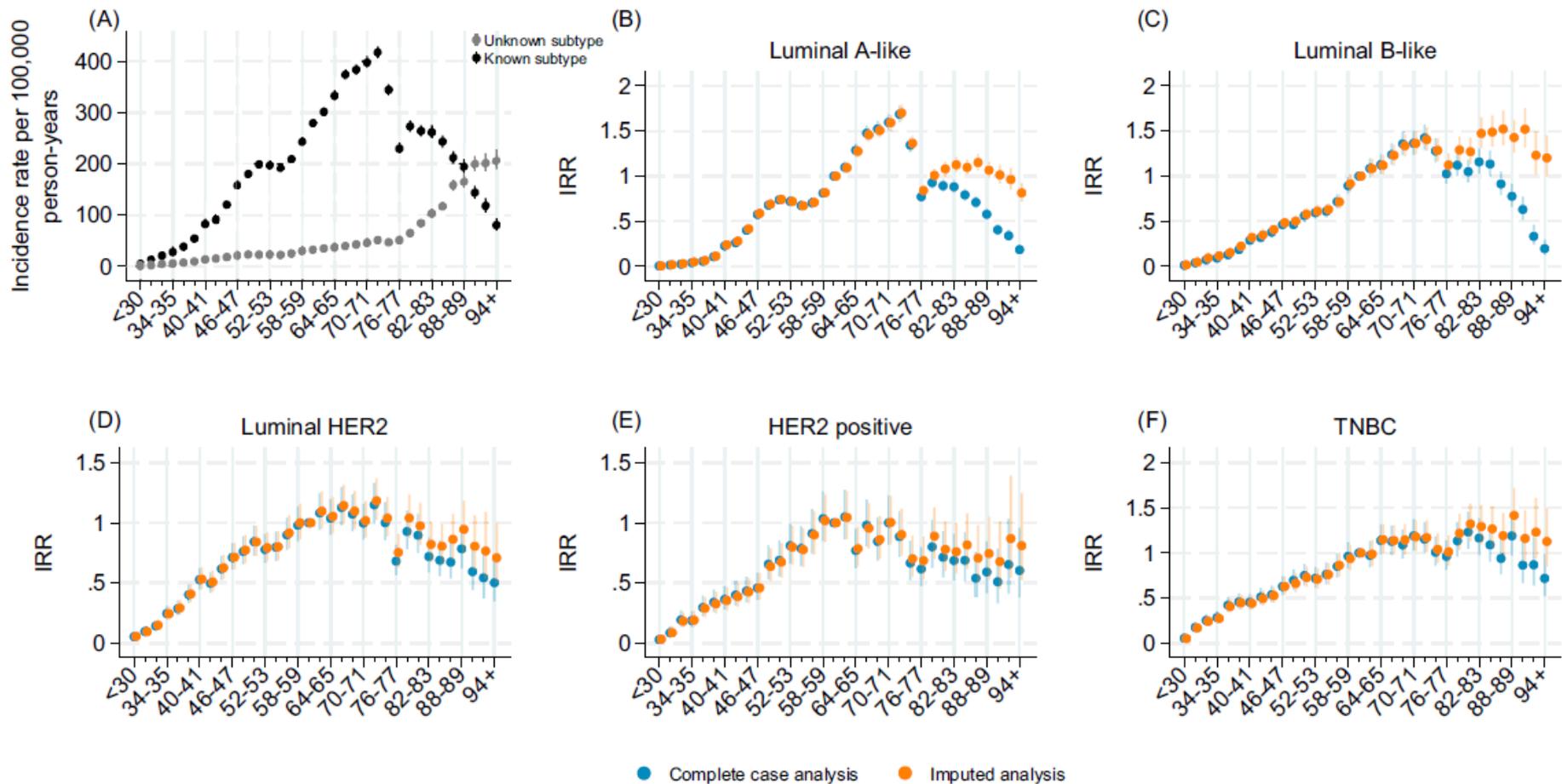
Variable	Missing of N=89,322 N (%)	Type in imputation	Imputation model (logistic, ordinal)	Analytical model (Poisson)
Age of diagnosis	Complete	Complete	X	X
Year of diagnosis	Complete	Auxiliary	X	
Region	Complete	Auxiliary	X	
Country of birth	Complete	Auxiliary	X	
Educational level	1,055 (1.18%)	Auxiliary / imputed	X	
Screening status	386 (0.43%)	Auxiliary / imputed	X	
T	251 (0.28%)	Auxiliary / imputed	X	
N	606 (0.68%)	Auxiliary / imputed	X	
M	Complete <sup>a</sup>	Auxiliary	X	
Stage (TNM)	465 (0.52%)		Not included (composite)	
Grade	14,610 (16.35%)	Imputed	X	
ER	3,657 (4.09%)	Imputed	X	
PR	3,778 (4.23%)	Imputed	X	
HER2	7,049 (7.89%)	Imputed	X	
Subtype	13,857 (15.51%)		Not included (composite)	
Surgery	7,046 (7.89%)	Auxiliary / imputed	X	
Chemotherapy	17,818 (19.95%)	Auxiliary / imputed	X	
Radiotherapy	17,941 (20.08%)	Auxiliary / imputed	X	
Endocrine therapy	17,535 (19.63%)	Auxiliary / imputed	X	
Targeted therapy	17,992 (20.14%)	Auxiliary / imputed	X	
Survival indicators, CumHaz.(BC, OS)	Complete	Auxiliary	X	

# Step 1: Imputation model

- We used command **mi impute**.
- A total of  $m=30$  imputed datasets, with 20 iterations, were generated.
  - $m$  was chosen to be larger than the highest percentage of missing values among the variables (Targeted therapy=20.14%), according to the rule of thumb by White et al (2011).
- In the chained equations, each variable was regressed on all other variables
  - **logistic regression models** were applied to **binary outcome variables** (ER, PR, HER2, chemotherapy, radiotherapy, endocrine therapy, targeted therapy, screening status), while
  - **ordinal regression** was used for **categorical outcome variables** (grade, nodal involvement N, surgery type, T stage, educational level).
- The imputation models were **stratified by age at diagnosis** (using the **by option in mi estimate**)
  - thus corresponding to including **all pairwise interactions of age at diagnosis** (<40, 40-44, 45-49, 50-54, 55-59, 60-64, 65-69, 70-74, 75-79, ≥80) with **each** covariate in the model.
  - **Important to include age-interactions! As our analysis model were modelling age-varying incidence rates.**

## Step 2: Analysis model and pooling

- We combined the (imputed) variables ER, PR, HER2 and grade into the **surrogate subtype variable** using the **mi passive:** command.
  - Using mi passive: we can create a new variable from the imputed variables.
  - Such a new variable can be used in mi commands.
- To each of the  $m$  imputed datasets, we fitted the **analytical Poisson model** with 2-year age groups as covariates; and saved the estimated parameters and standard errors.
  - This generated  $m$  sets of parameter estimates (and standard errors).
- To estimate **pooled parameters**, we manually applied Rubin's rules to the  $m$  parameters:
  - Rubin's rule #1: **Pooled parameter** is the mean of the estimated parameters for the imputed data sets (i.e. taking average of  $m$  parameters).
  - Rubin's rule #2: **Standard error of the pooled parameter**; incl. both within-between imputations variances.
- This is typically done by **mi estimate**. **I will come back to why we did not use mi estimate.**

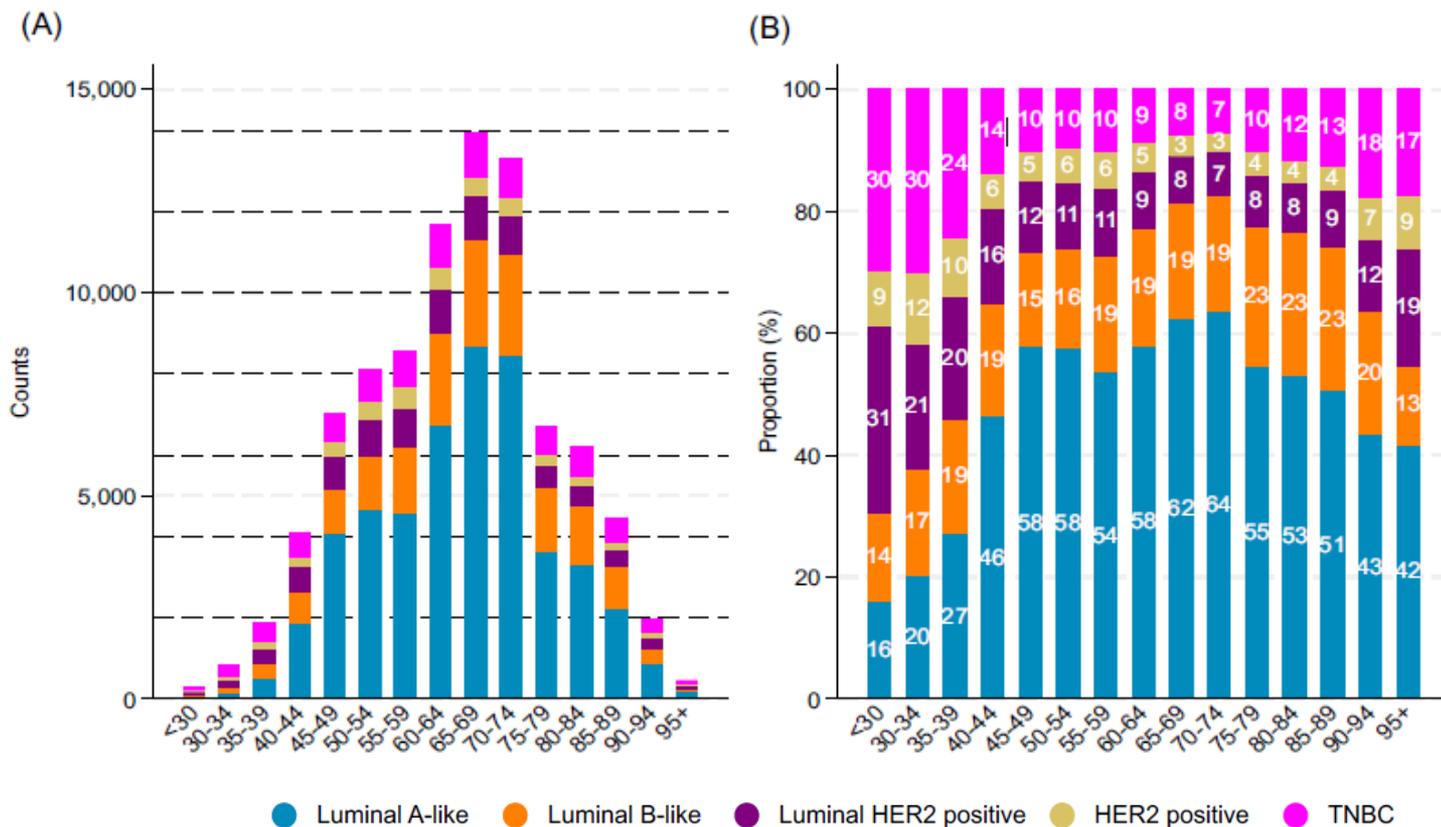


**FIGURE 2** Breast cancer incidence rates of known and unknown subtype by age at diagnosis (A) and comparison of incidence rate ratios

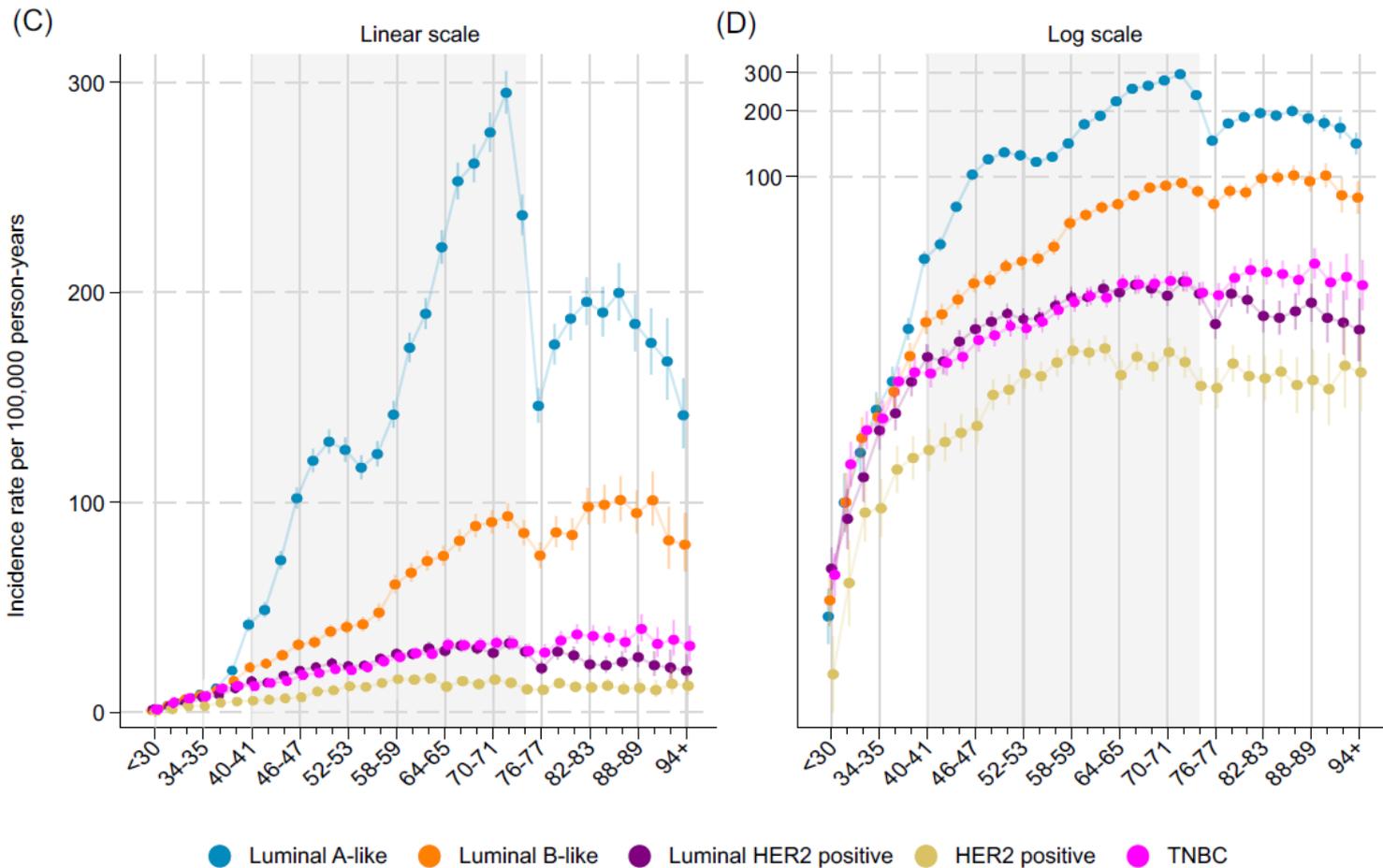
## Appropriately estimating cancer incidence – without loss of cases

- A key strength of this analysis is that we included all women with missing subtype.
- Important as we were interested in the **absolute incidence rate** (not just relative rates):
  - If women with missing subtype are excluded - subtype-incidence rates will be underestimated.
- Relative effects are likely less impacted – at least in younger ages.
  
- The parameter estimates from the Poisson model represent
  - **Intercept**: rate in reference age
  - **Coefficients for covariates** (age effect): rate ratios (vs. the reference age)
  
- From these parameter estimates from the Poisson model, we can obtain at different ages
  - **Incidence rates** – directly from the parameters in the model.
  - **Proportions, counts** – by multiplying rate fractions of total rate (%) with the known N.
  - “pool-last-principle”: to obtain **pooled** incidence rates & proportions:
    - transform rates/proportions from params in each imputed dataset >> then pooled them.

# Results: Pooled counts and proportions post-estimated from parameters in Poisson model.

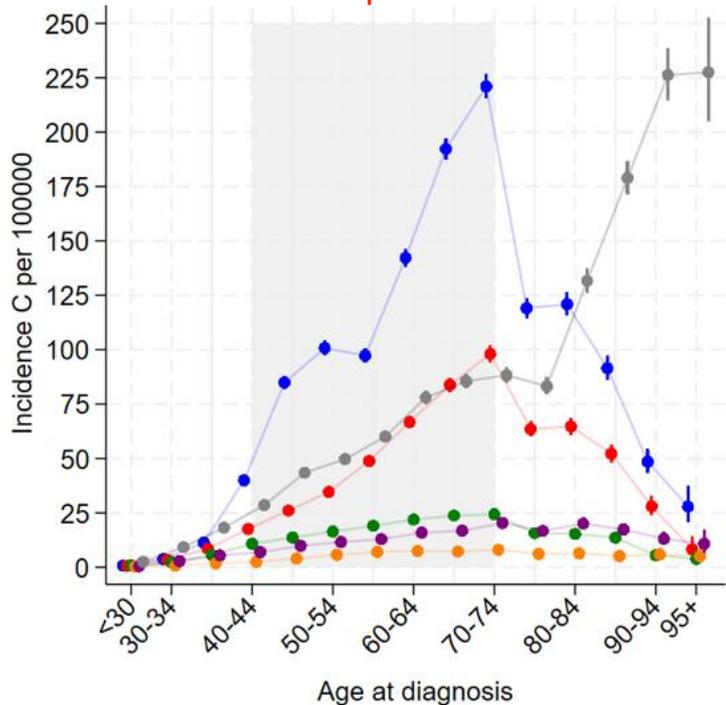


# Results: Pooled incidence rates from parameters in Poisson model

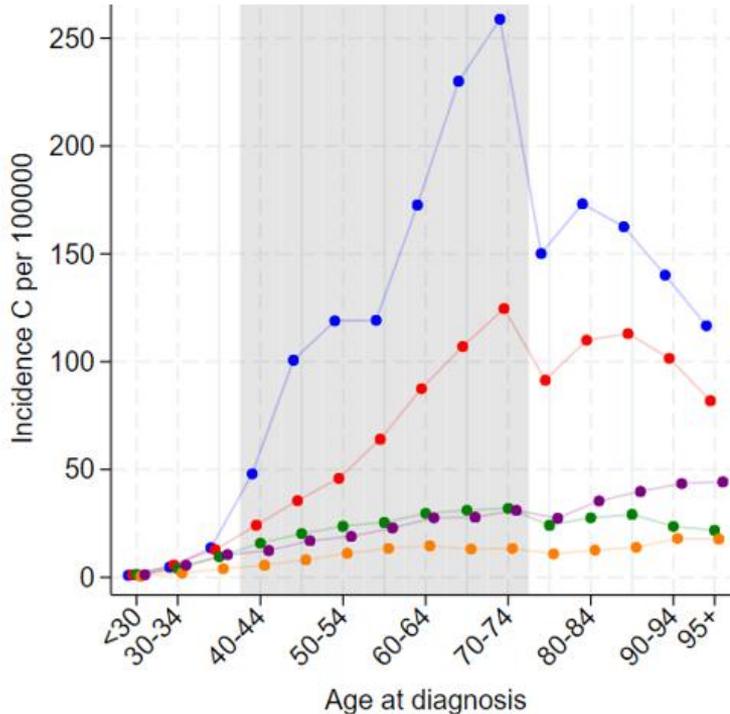


Results not in the published paper! Absolute rates are higher in imputed analysis, esp. older ages.

Complete case



Imputation



- Luminal A-like
- Luminal B-like
- Luminal HER2 positive
- HER2 positive
- TNBC
- Missing

- Luminal A-like
- Luminal B-like
- Luminal HER2 positive
- HER2 positive
- TNBC

# Why we could not use **mi estimate** to obtain the pooled estimates

- MICE only works on individual-level data: We applied Poisson regression to individual level data.
- We only imputed the case dataset.
  - We then added the counts of “population-at-risk” for each individual, as an offset (in “pop\_at\_risk” variable).
  - E.g. `. poisson d_subtype1 i.age, exposure(pop_at_risk)`
- For each subtype: We restricted the case dataset to those with that subtype.
  - E.g. For the estimation of subtype 1 incidence – we only included the women with subtype 1.
- However, since we imputed the “outcome” (subtype):
  - Number of outcomes will differ for different  $m$  datasets.
    - Imputation  $m=1$ : 45000 Lum A
    - Imputation  $m=2$ : 44000 Lum A. etc.
  - This created **imputed datasets of different sizes for each subtype-specific model**.
  - As far as we could work out, **mi estimate** requires imputed datasets of the same size (same number of obs).
- In many applications of MICE, the interest is in imputing a covariate (exposure/treatment, confounder, etc.) – this will not change the size of the imputed datasets.

## In conclusion

- This is one of the first studies to estimate subtype-specific BC incidence using MICE.
- MICE was important to avoid underestimation of incidence rates – up to 15.5% in our data.
- Essential to include a broad imputation model that captures the underlying missing data mechanism.
  - We had access to a wide range of clinical variables.
- Also important to include the correlation structures from the analysis model in the imputation model.
- **mi package** was a very powerful tool – it enabled us to estimate rates and impute the data.
  - Yet we faced challenges when using **mi estimate** for imputed datasets of different sizes.
- This is an example of **imputing the outcome** – while most examples in literature focus on imputing covariates (exposure/treatment, confounder) in regression models.



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