Stata Technical Bulletin

A publication to promote communication among Stata users

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an74	Stata 6, Stata 7, and the STB
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Stata 7 has been released, and this is the last issue of the STB that is explicitly Stata 6, which is to say, every insert in this issue will work equally well with Stata 6 or Stata 7. Future issues will contain inserts based on Stata 6 code and Stata 7 codes, and, over time, you should expect nearly all inserts to be in terms of Stata 7.

Submissions to the STB based on Stata 6 are still being accepted along with, of course, submissions based on Stata 7.

dm73.2	Contrasts for categorical variables: update

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Abstract: Enhancements to desmat and associated programs for models with categorical independent variables are described.

Keywords: contrasts, interactions, categorical variables.

The program desmat is used to create a design matrix for independent variables, allowing higher order interactions, and different types of contrasts (Hendrickx 1999, 2000). This update describes recent enhancements to desmat and its accompanying programs. The most important change to desmat is that it can now be used as a command prefix, similar to xi. When used as a command prefix, desmat generates a design matrix, quietly estimates the model, then calls desrep to present the results.

A second useful enhancement to desmat is that variables prefixed by an @ symbol will now be treated as continuous variables. This can be achieved now by assigning a pzat characteristic to the variable or by appending a contrast specification to the variable (Hendrickx 2000), but the new method will often be more convenient. For example, in

. desmat: regress weight @length rep78

length will be treated as a continuous variable, but dummies will be created for the variable rep78.

A third important enhancement to desmat is that a global macro D_CON can be used to specify a default contrast. This macro can be defined in the user's profile.do to set a new default contrast for all future Stata sessions. For example,

. global D_CON "dev(99)"

The deviation contrast with the highest category as reference will now be used as default in desmat models. This can be overridden by assigning a pzat characteristic to a variable, by prefixing to the variable with an @ to designate it as continuous, or by appending a contrast specification to the term.

desmat is still compatible with the original syntax when used as a command by itself. However, to permit new options and to make the command more in keeping with Stata syntax, the default contrast should be specified using the defcon option. For example,

. desmat vote*memb vot*educ*race educ*race*memb, dev(99)

Under the new syntax, this should be specified as follows, although the above syntax will still be accepted for reasons of compatibility

. desmat vote*memb vot*educ*race educ*race*memb, defcon(dev(99))

In previous versions, desmat printed information on variables deleted due to collinearity. This wasn't very informative, since the collinear variables were usually duplicate dummy variables produced by desmat. This output has now been made optional and can be requested using the colinf option.

Syntax for desmat

desmat model [, colinf defcon(contrast_specification)]

desmat: stata_procedure [using filename] [if exp] [in range] [weight] depvar model [, verbose

defcon(contrast_specification) desrep(desrep_options) procedure_options

fweights, pweights, aweights, and iweights are allowed, and the *model* consists of one or more terms separated by spaces. A term can be a single variable, two or more variables joined by periods, or two or more variables joined by asterisks. A period is used to specify an interaction effect as such, whereas an asterisk indicates hierarchical notation, in which both the interaction effect itself plus all possible nested interactions and main effects are included. All variables in the model are treated as categorical unless specified otherwise. A variable may be prefixed by an "@" to flag it as a continuous variable.

Options for desmat

When desmat is used as a command prefix to a Stata procedure, if or in options as well as *weights* may be specified in the usual manner and will be passed on to the procedure. Any options besides verbose, defcon, and desrep will be passed on as well.

- [using *filename*] specifies that the results will be written to a tab-delimited ASCII file. The default extension for *filename* is .out. See desrep below for further details.
- def con(*contrast_specification*) can be used to specify a different contrast than the indicator contrast with the first category as reference.

Options for desmat as a command prefix

- verbose specifies that intermediate results should be displayed. When verbose is not specified, desmat produces no output, estimates the model quietly, then calls desrep to display the results.
- desrep(desrep_options) allows the passing of options on to desrep after the model has been estimated but prior to the presentation of results. Note that most of these options can be specified using global macro variables. An exception could be the exp option. desrep displays linear coefficients even if the procedure prints exponential coefficients, for example, the odds ratios produced by logistic. In such a case, one can specify
 - . desmat: logistic vote memb educ*race [fw=pop], desrep(exp all)

to display odds ratios.

Options for desmat as a command by itself

For compatibility with earlier versions, a default contrast may be specified as an option rather than an argument for the defcon option when desmat is used as a command by itself.

colinf requests a report on which duplicate variables have been removed. When interaction terms are specified, desmat will often generate duplicate dummy variables. These duplicates are subsequently removed by dropping collinear variables. In some cases however, it can occur that variables are unexpectedly dropped.

The desrep command

desrep is a command for viewing the results of Stata estimation commands. It can be used after estimating any model but is particularly useful in conjunction with desmat. desrep is called by desmat when this is used in command prefix mode. In that case, options for formatting the output can be specified using the desrep option in desmat. desrep will print most model information but has not been tested for all Stata models. Note that the results of any Stata estimation procedure can be reprinted at a later point by submitting the command name with no arguments.

desrep has been enhanced to allow it to print z- or t-values, probabilities, and confidence intervals, as well as coefficients, standard errors, and symbols indicating significance. Global macro variables can be used to control what is printed by default. In addition, results can be written to a tab-delimited file.

Syntax for desrep

Options for desrep

- [using *filename*] specifies that the results will be written to a tab-delimited ASCII file. The default extension for filename is .out. If *filename* already exists, desrep will attempt to find a valid filename by appending a number (this is done using the included outshee2 program). The replace option can be used to overwrite an existing file.
- fw(#) specifies the number of columns used to display the estimates, standard errors, and other requested statistics. The default
 value is 10.
- ndec(#) specifies the number of decimal places. The default value is 3.

- sigcut(*numlist*) specifies the levels of significance to be used for symbols placed next to coefficients to indicate whether these are significant at a certain level. *numlist* should contain a list of values in descending order with the same number of elements as the string list in sigsym. For example, sigcut(.1.05.01.001) with sigsym(# * ** ***) will use the symbols # for p < .05, ** for p < .01, and *** for p < .001. The default for sigcut is (.05.01).
- sigsym(list) specifies the set of symbols corresponding with the levels of significance given by sigcut. The default for sigsym
 is (* **).
- sigsep(#) specifies the number of spaces between coefficients and symbols indicating significance. The default is zero.
- nrwd(#) specifies the number of columns reserved for numbering the effects. Specifying nrwd(0) can be used to suppress
 numbering. The default is 3.
- no modinfo specifies whether or not to print information on the model and goodness of fit. The default is modinfo.
- no sig specifies whether or not to display symbols for levels of significance. The default is sig.
- [no] se specifies whether or not to print standard errors. The default is se.
- zval requests printing of z values for models with a χ^2 statistic, and t values for models with an F statistic.
- prob requests printing of p-values.
- ci requests printing of confidence intervals.
- all requests all standard Stata output, that is, standard errors, z or t statistics, probabilities, and confidence intervals. Specifying all is, thus, equivalent to specifying zval prob ci.
- [no] trunc specifies whether or not very long labels should be cut off and the rightmost section displayed. notrunc will print estimates on a separate line. The default is trunc.
- exp specifies that desrep will report multiplicative parameters, for example, incident-rate ratios in Poisson regression, odds ratios in logistic regression. Note that if exp is not specified, desrep will produce the linear estimates even if the procedure produces multiplicative versions. Earlier versions of desrep allowed exp to be specified as the only argument. This is still allowed if exp is the only argument. If other options are specified, exp must be specified as an option.

The following two options apply only if using has been specified to write the data to a tab-delimited ASCII file.

- outraw specifies that results are written with their default formats, for example, %9.0g for floats. In addition, a tab will be inserted between coefficients and significance symbols. Otherwise, the variables are written with a fixed number of decimal places as specified by the ndec option, and significance symbols are appended to coefficients if sigsep is zero.
- replace specifies to overwrite any existing output file. If not specified, desrep appends a number to the filename if it already exists. If no valid name has been found after appending 1 to 20, the process stops and the output is not saved.

Macro variables to control layout

Macro variables can be used to alter the default for certain desrep options. The macro variables will still be overridden by options specified at the desrep command. The global variables can be specified once at the beginning of the Stata session or in the user's profile.do for all sessions. The following global variables may be defined:

D_FW	D_NRWD	D_CI
D_NDEC	D_SIG	D_ALL
D_SIGCUT	D_SE	D_TRUNC
D_SIGSYM	D_ZVAL	D_RAW
D_SIGSEP	D_PROB	D_REPL

For example, the following can be used to set the column width for estimates to 8, use 2 decimal places, and symbols and cutpoints for levels of significance:

```
. global D_NDEC 2
. global D_FW 8
. global D_SIGCUT ".1 .05 .01 .001"
. global D_SIGSYM "# * ** ***"
```

The showtrms command

showtrms produces a legend of the dummy variables produced by desmat, the terms these pertain to, and the contrasts used. The showtrms command has no options. It is called automatically when desmat is used as a command by itself or when the verbose option is used with desmat as a command prefix.

The destest command

destest is for use after estimating a model with a design matrix generated by desmat to perform a Wald test on model terms. Like desrep, destest can now write results to a tab-delimited file, symbols and cutpoints for levels of significance can be specified, and some aspects of the layout of results can be controlled through macro variables. In addition, destest now uses svytest if survey models have been estimated.

Syntax for destest

```
destest [termlist] [using filename] [, joint equal outraw replace ndec(#) sigcut(numlist)
    sigsym(list) sigsep(#) ]
```

Options for destest

The options ndec, sigcut, sigsym, sigsep, outraw, and replace have the same usage as in desrep.

joint specifies that destest will test whether all the effects in all the terms are jointly equal to zero.

equal specifies that destest will test whether the effects of each separate term are equal. The joint and equal options may be combined to test whether all effects are jointly equal, although this would be a somewhat peculiar hypothesis.

The global macro variables listed below can be used to specify different defaults for these options, either for only the current session or for all Stata sessions, by placing the global variables in the user's profile.do.

D_NDEC D_SIGSYM D_RAW D_SIGCUT D_SIGSEP D_REPL

Options specified in the destest command will override these global variables.

References

Hendrickx, J. 1999. dm73: Using categorical variables in Stata. Stata Technical Bulletin 52: 2–8. Reprinted in Stata Technical Bulletin Reprints, vol. 9, pp. 51–59.

— 2000. dm73.1: Contrasts for categorical variables: update. Stata Technical Bulletin 54: 7. Reprinted in Stata Technical Bulletin Reprints, vol. 9, pp. 60–61.

dm83	Renaming variables: changing suffixes		
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Abstract: rensfix is a command to rename variables, changing the suffix. It complements renpfix, an official Stata command to rename variables, changing the prefix.

Keywords: rensfix, renpfix, rename, variable names, data management.

Syntax

```
rensfix old_stub new_stub
```

Description

rensfix renames all variables whose names end with *old_stub*, so that they end instead with *new_stub*. If *new_stub* is not specified, *old_stub* is removed. It, therefore, matches the existing Stata command renpfix (see [R] rename), which renames variables, changing the prefix of each name.

In contrast to renpfix, however, rensfix will not rename any variable whose name ends in the suffix specified unless all new names implied are in fact legal names for new variables. Thus, either all names implied are acceptable, or rensfix warns you otherwise and makes no changes.

Examples

We illustrate rensfix using Stata's auto data. We begin by changing the variable rep78 to rep

```
. use auto
(1978 Automobile Data)
```

. ds make turn	price displ	mpg gratio	rep78 foreign	hdroom	trunk	weight	length
. rensfi	ix 78						
. ds make	price	mpg	rep	hdroom	trunk	weight	length
turn	displ	gratio	foreign				

and then change any variable name ending in e to end in 123

. rensfi	x e 123						
. ds mak123 turn	pric123 displ	mpg gratio	rep foreign	hdroom	trunk	weight	length

and then show what happens if rensfix would result in a name of more than 8 characters.

	: 123 12345 invalid n						
. ds mak123 turn	pric123 displ	mpg gratio	rep foreign	hdroom	trunk	weight	length

dm84 labjl: Adding numerical codes to value labels

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Abstract: To document fully analyses and to assure no numerical code misinterpretations are made, it is advisable to add value labels to all categorical variables as part of the documentation of a dataset. In analysis, one often wishes to make a particular calculation, listing, or analysis based on the numerical code of the variable. To facilitate the ease of having labels as well as numerical codes visible, the routine labjl will add the numerical code to the label as well as remove it afterwards.

Keywords: value label, categorical value codes, documentation.

Syntax

```
labjl varlist [, add remove noalign n(#) ]
```

Description

labjl adds the numeric code of a defined value label to each label for the variables in *varlist*. It can be used when a user wants to see the numeric code and the label in tables or other displays. If several variables are shown, the labels used by any of these will be changed. If a variable does not have a value label attached to it, nothing happens.

The routine can add the numerical value as well as restore the original label. The routine does not change any data values.

Options

add specifies that the value is to be added to the label (the default).

remove specifies that the value is to be removed from the label when the numerical code is equal to the first nonblank part of the label.

noalign specifies that the numeric codes will not be left aligned.

n(#) specifies that the user wants to increase the limit of codes. The default is the interval from 0 to 25.

Example

For a variable called sex, we use tabulate before and after using labjl.

. tabulate sex			
sex	-	Percent	Cum.
Female	490 3537		
Total	4027	100.00	
. labjl sex Numerical codes . tabulate sex	added to La	abel: sex	
	Freq.		Cum.
1 Female	490 3537	12.17 87.83	
Total	4027	100.00	

If one does not want to left align the codes, they can use the following:

. labjl sex, noalign Numerical codes added to Label: sex						
Freq.	Percent	Cum.				
490	12.17	12.17				
3537	87.83	100.00				
4027	100.00					
	added to Freq. 490 3537	added to Label: sex Freq. Percent 490 12.17 3537 87.83				

The numeric codes can be removed as in the next example.

. labjl sex, re Numerical codes		m Label: sex	
. tab sex			
sex	1	Percent	Cum.
Female Male	490 3537	12.17 87.83	12.17 100.00
Total	4027	100.00	

To add numerical codes to all variables for which value labels have been defined, one can use the code below.

```
. labjl _all /* add to all labels */
. labjl _all, remove /* remove from all labels */
```

dm85	listjl: List one variable in a condensed form
------	---

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Abstract: When checking datafiles during documentation it can be helpful to list id numbers in a condensed form for checking or finding of paper material. listjl does this for all observations or broken down by one different variable.

Keywords: data quality, id variable, observation id.

Syntax

```
listjl variable [if exp] [in range] [, by(variable) ]
```

Description

listjl will list the variable indicated in a condensed format, optionally broken down by one group variable.

Options

by(*variable*) specifies that the listing is to be broken down by the specified variable. When indicated, a frequency table of this variable will be shown.

Example

Here is an example of listing observations broken down by variable sex for the first 50 observations:

. listjl id in 1/50, by(sex) -> tabulation of sex sex Freq. Percent Cum. ---+-Κ 5 10.00 10.00 M 45 90.00 100.00 ------_ _ _ _ _ Total 50 100.00 Group: sex = K id : 8 34 35 41 42 Group: sex = M id : 1 2 4 5 6 7 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 36 37 38 39 40 43 44 45 46 47 48 49 50 51

Now, an example of a listing without the by option but using the if option:

. listjl id if id < 52 1 2 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51

dm86	Sampling without repl	acement: absolute sample	e sizes and keeping	g all observations
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Abstract: swor is a command for sampling without replacement which allows specification of absolute sample sizes and (optionally) keeping of nonsampled observations in memory. It complements the official Stata command sample.

Keywords: sample, sampling without replacement, data management.

Syntax

```
swor # [if exp] [in range] [, by(groupvars) generate(newvar) keep ]
```

Description

swor draws a pseudo-random sample of size # from the data in memory, by default discarding (optionally keeping) the remaining observations. Observations not meeting the optional if and in criteria are kept (sampled at 100%). # must be positive and no greater than the number of observations in each group to be sampled.

Options

by (groupvars) specifies that a sample of size # is to be drawn within each set of values of groupvars.

generate (newvar) generates newvar containing 1 for those observations included in the sample and 0 for those not included.

keep overrides the default dropping of nonsampled observations. keep must be combined with generate().

Discussion

The Stata command sample (see [R] sample) also carries out sampling without replacement, specified in percent to be sampled, rather than absolute number. See also Weesie (1997) for an extension of sample to sampling clusters of observations. Various bootstrap sampling commands allow sampling with replacement; see, in particular, [R] btstrap. Alternatively, check out the resample command of Gleason (1997, 1999).

Two features of sample are sometimes limitations. First, sample is designed to draw a sample as a specified percent of the observations in memory. Often the problem in practice is to draw a sample of a specified absolute size. Second, those observations not included in the sample are dropped from memory, although all observations not satisfying any if or in restrictions are kept. Sometimes it is desired to keep all nonsampled observations in memory.

swor is designed to meet these needs. The number to be specified is the absolute sample size, not a percent. All observations may be kept in memory using the keep option, in which case the sampled observations must be tagged by a new variable named in generate().

If you are serious about drawing random samples, you must first set the random number seed; see [R] generate.

Examples

First, we set the seed for reproducibility

. log using sampling . set seed 987654321

and then draw a sample of size 100

. swor 100

We can also keep all sex not equal to 0, but sample 100 from sex equal to 0

```
. swor 100 if sex == 0
```

or sample 100 from each group of sex

. swor 100, by(sex)

or sample 100 from each group of sex, but keep all the observations

. swor 100, by(sex) gen(sample) keep

Finally, we can sample 100 if sex is 0 and keep only those observations.

```
. swor 100 if sex == 0, gen(sample)
. keep if sample
```

References

Gleason, J. R. 1997. ip18: A command for randomly resampling a dataset. Stata Technical Bulletin 37: 17–22. Reprinted in Stata Technical Bulletin Reprints, vol. 7, pp. 77–83.

-----. 1999. ip18.1: Update to resample. Stata Technical Bulletin 52: 9–10. Reprinted in Stata Technical Bulletin Reprints, vol. 9, p. 119.

Weesie, J. 1997. dm46: Enhancement to the sample command. Stata Technical Bulletin 37: 6–7. Reprinted in Stata Technical Bulletin Reprints, vol. 7, pp. 37–38.

sbe36.1	Summary statistics for diagnostic tests	
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Abstract: An extensive revision of the diagtest command introduced in Tobias (2000) is introduced and illustrated.

Keywords: diagnostic test, sensitivity, specificity, predictive values, confidence intervals, contingency tables.

Introduction

The new command diagt is a complete revision of the earlier command diagtest (Tobias 2000). It should be regarded as succeeding it and replacing it. Both commands are used to assess a simple diagnostic test in comparison with a reference standard (or "gold standard"), assumed to be completely accurate. The diagnostic test is generally used because it is cheaper, quicker, or less invasive than the reference standard, but may not be as reliable. Results are typically presented in a 2×2 table and summarized as four percentages: sensitivity, specificity, positive predictive values, and negative predictive values, with their respective confidence intervals. diagti is an immediate version of diagt that does not require data to be entered.

The commands diagt and diagtest differ in the following ways:

- The exact binomial distribution is used instead of the normal approximation, based on command ci.
- An algebraic error that caused diagtest to give confidence intervals that were too wide has been corrected. Essentially, diagtest used the grand total instead of the row or column totals when calculating the standard errors.
- Only fweights are allowed, as with ci and binomial.
- The command format is changed. The outcome (the true disease status) is placed before the predictor (the diagnostic test). This makes it consistent with commands such as logistic, roctab, cs, and cc.

- The table layout is also changed. Rows represent disease status. As with commands cc and cs, rows represent true disease status, columns represent exposure (or test) result. Positive results are given in the top and left of the table, before negative ones.
- An immediate version is provided.
- The name has been changed. This is partly because the shorter name allows the immediate version to end in i, and partly to reduce the risk of people confusing the two command formats and so getting the wrong estimates.

Sensitivity is the proportion of true positives that are correctly identified by the test, and specificity the proportion of true negatives correctly identified. Typically, these are regarded as fixed properties of a particular test, independent of the prevalence of the disease. However, in medical practice, the result of the diagnostic test is all that is known. The positive predictive value (PPV) is the proportion of patients with positive test results who are correctly diagnosed. The negative predictive value (NPV) is the proportion of patients with negative test results who are correctly diagnosed. These values help a clinician trying to make a diagnosis for a particular patient.

Test result					
True disease status	Positive(+)				
Abnormal(+)	a	b	\implies Sensitivity = $a/(a+b)$		
Normal(-)	c	d	\implies Specificity = $d/(c+d)$		
	\Downarrow	\Downarrow			
	PPV = a/(a+c)	NPV = d/(b+d)			

Table 1. Definition of sensitivity, specificity and predictive values.

The predictive values of a test in clinical practice depend critically on the prevalence of the abnormality in the patients being tested; these values depend on the prevalence of the disease. Sometimes the prior likelihood of the current patient having the disease can be estimated from other signs and symptoms. This can be used instead of the prevalence.

The predictive values (PPV and NPV) can be calculated for any prevalence by using Bayes' theorem, as follows:

$$\begin{split} \text{PPV} &= \frac{\text{Sensitivity} \times \text{Prevalence}}{\text{Sensitivity} \times \text{Prevalence} + (1 - \text{Sensitivity}) \times (1 - \text{Prevalence})} \\ \text{NPV} &= \frac{\text{Specificity} \times (1 - \text{Prevalence})}{\text{Specificity} \times (1 - \text{Prevalence}) + (1 - \text{Specificity}) \times \text{Prevalence}} \end{split}$$

Syntax

diagt diagvar testvar [weight] [if exp] [in range] [, prev(#) level(#) tabulate_options]

diagti $\#_a \#_b \#_c \#_d$ [, prev(#) level(#) tabulate_options]

where *diagvar* is the variable which contains the real status of the patient, and where *testvar* is the variable which identifies the result of the diagnostic test. *testvar* and *diagvar* can have only two nonmissing values. The higher value must identify the positive result of the test or the diseased status of the patient.

For diagti, $\#_a$, $\#_b$, $\#_c$, and $\#_d$ are, respectively, the numbers of true positives (diseased subjects with correct positive test results), false negatives (diseased, but negative test), false positives (no disease, but positive test) and true negatives (no disease, negative test).

fweights are allowed.

Exact binomial confidence intervals are given, as with the command ci.

Options

prev(#) specifies the estimated prevalence, in percent, of the disease to be used in estimating the positive and negative predicted values using Bayes' theorem. If the prev option is used, the confidence interval is only displayed for the sensitivity and specificity values. Otherwise, the prevalence is estimated from the data.

level(#) specifies the confidence level, in percent, for confidence intervals. The default is level(95) or as set by set level.

All tabulate command options are available.

Example

The same example is considered here as in Tobias (2000) describing diagtest. Altman and Bland (1994a, 1994b) consider the relationship between the results of a liver scan test and the correct diagnosis (Drum and Christacapoulos 1972). The proportions that were correctly diagnosed by the scan were 89.53% for normal liver scan, and 62.79% for those with abnormal scan. The proportion of correct diagnoses among the patients with abnormal liver scan test was 87.83%, and among the patients with normal liver scans such proportion was 66.67%.

Here are summary results for the liver scan test and the correct diagnosis.

true diagnostic	g test [fw=n] diagnostic result Pos.	Neg.				
Abnormal Normal	231 32	27 54	258 86	i		
Total	263 al diagnosis def	81	344	:] . Inter.]
	edictive value edictive value	Pr(Pr(- ~D) 62 D +) 87	.79% .83%		72.98% 91.53%
Prevalence		Pr(D) 75	.00%	70.08%	79.49%

In the liver scan study, the percentage of abnormality was 75%. If the same test was used in a different clinical setting where the prevalence of abnormality was 0.25%, we would have a positive predictive value of 44.51% and a negative predictive value of 94.74%.

Now, we show summary results for the liver scan test and the correct diagnosis for a prevalence of abnormality of 25%.

	test [fw=n], p diagnostic result					
0	Pos.	0		al		
Abnormal	231 32	27	2			
+		4				
	263 1 diagnosis def				ed Abnormal))
			-		[95% Conf	f. Inter.]
 Sensitivity		Pr(89.53%	[95% Conf 	
Sensitivity Specificity						92.99%
Specificity	dictive value	Pr(- ~D)	62.79%	85.14% 51.70%	92.99%
Specificity Positive pre	dictive value dictive value	Pr(Pr(- ~D) D +)	62.79% 60.15%	85.14% 51.70% .%	92.99% 72.98%

The same results can be achieved without any data in memory using the immediate form of the command:

. diagti 231 True	L 27 32 54					
disease	Test resu	lt				
	Pos.	0 .				
Abnormal		27		258		
Normal	32	54		86		
Total	263	81		344		
Sensitivity		Pr(+ D)	89.53%	85.14%	92.99%
Specificity		Pr(- ~D)	62.79%	51.70%	72.98%
Positive pre	edictive value	Pr(D +)	87.83%	83.26%	91.53%
Negative predictive value		Pr(~D -)	66.67%	55.32%	76.76%
Prevalence		Pr(l)	75.00%	70.08%	79.49%

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sbe41	Ordinary case-cohort design and analysis	I
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Abstract: The case-cohort design is an efficient alternative to a full cohort analysis. Two new commands for ordinary case-cohort designs are presented. They randomly select a sample from a cohort, prepare the resulting dataset for analysis using a Cox regression model and compute the asymptotically consistent Self-Prentice variance estimator of the parameters.

Keywords: Cohort studies, nested case-control design, survival analysis, Cox regression model, variance estimation.

Introduction

Various designs have been proposed as useful alternatives to the standard full cohort analysis when data collection for any subject may be very expensive. In the case-cohort design (see Barlow et al. 1999, Clayton and Hills 1993, Langholz and Thomas 1990, 1991, and Rothman and Greenland 1998, for example), covariate information is assessed in a sample of subjects selected randomly from the entire cohort, the subcohort, and in all individuals who fail, whether they are in the subcohort or not. The case-cohort design has some advantages with respect to the nested case-control study mainly when the cohort under study is fixed (i.e., without staggered entry times), failures are rare, and there is little loss to follow-up. Unlike the nested case-control study, the case-cohort design allows one to use the same sample of subjects to analyze several failure time outcomes. Furthermore, the subcohort is chosen without regard to any time scale. Recently, simplified methods have appeared for parameter and variance estimation, thus, allowing the analysis of the case-cohort design using a Cox model suitably adapted. Here, we present two new Stata commands that assist the user in the fundamental steps of case-cohort design and analysis: stcascoh to sample the full cohort and prepare a dataset for analysis, and stselpre to calculate the variance as proposed by Self and Prentice.

Syntax for sampling cohort and preparing dataset

stcascoh [varlist] [if exp] [in range], alpha(#) [group(varnames) generate(varlist) eps(#)

<u>se</u>ed(#) <u>nosh</u>ow

stcascoh is for use with survival-time data. You must stset the data with an id() variable before using this command.

Description

stcascoh is used to create an appropriate dataset for analysis as a case-cohort study, drawing an α -fraction random sample of the full cohort and including all failures whether they occur in the random sample or not. To this aim, stcascoh expands observations which fall into two parts: 1) time interval $(t_0, t - \epsilon]$, and 2) time interval $(t - \epsilon, t]$. For cases included in the subcohort, both segments are retained in the final dataset, whereas for cases not in the subcohort just the last segment is retained.

The variables in the table below are added to the dataset.

_subco	coded 0 for subcohort member with no failure
	coded 1 for subcohort member who failed
	coded 2 for nonsubcohort member who failed (nonsubcohort case)
_wSelPre	log-weights of records as in the Self-Prentice method
_wBarlow	log-weights of records as in the Barlow method

The names of the new variables and the sampling fraction are saved as Stata characteristics as shown in the table below.

_dta[Subco]	subcohort membership variable name
_dta[wSelPre]	Self-Prentice log-weights variable name
_dta[wBarlow]	Barlow log-weights variable name
_dta[Alpha]	sampling fraction

varlist defines variables that will be retained in the final dataset. If varlist isn't specified, all variables are carried over into the resulting dataset. Observations not meeting if and in criteria are dropped even if they fail. Randomness in the sampling is obtained using Stata's uniform() function.

Options

alpha(#) specifies the sampling fraction. The sampling fraction can be expressed as real or integer.

group (varlist) specifies that the alpha sample is to be drawn within each set of values of varlist, thus, maintaining the proportion in each group.

generate (varlist) specifies other variable names for the three generated variables.

- eps(#) specifies a (typically small) number so that a case that is in the risk set at time t is represented in the expanded data by an "infinitesimal" episode (t - eps, t]. eps should be set to a number that is small compared to the measurement unit of time. The default value of eps is .001.
- seed(#) specifies a seed for random sampling. Providing the same seed means that the same subcohort is selected each time even if the definition of the failure event or time axis has been changed in stset.

noshow prevents stcascoh from showing the names of the key st variables.

Example

As an example, consider data contained in Appendix VIII of Breslow and Day (1987) concerning workers employed in a Welsh nickel refinery. Mortality for nasal cancer and sinus cancer has been analyzed using "time since first exposure" as analysis time. A preliminary description of the full cohort data is given below.

1

```
. use nickel, clear
 . stset dataout, f (tumnas) origin(dataass) enter(datain) id(id)
 . stdes
             failure _d: tumnas
     analysis time _t: (dataout-origin)
                  origin: time dataass
   enter on or after: time datain id: id
                                                    |----- per subject ------|
Category
                                       total
                                                         mean
                                                                            min median max
no. of subjects
                                 679
no. of records
                                          679
                                        1 1 1 1
17.98332 9.359375 18.29639 36.04663
                                                              1
                                                                                1
                                                                                                 1
(first) entry time

      (first) entry orac
      40.58155
      10.0111

      (final) exit time
      40.58155
      10.0111

      subjects with gap
      0
      .
      .

      time on gap if gap
      0
      .
      .
      .

      time at risk
      15344.223
      22.59827
      .3996582
      21.75623

      56
      .0824742
      0
      0

                                                   40.58158 10.04102 40.06299 75.59204
                                                                                                        48.6543
                                                                                                        1
                                                                                                               _ _ _
```

Now, we prepare this dataset for analysis as a case-cohort design using a sampling fraction of 0.3.

```
. stcascoh, a(0.3) seed(123)
       failure _d: tumnas
  analysis time _t: (dataout-origin)
           origin: time dataass
 enter on or after: time datain
              id: id
Sample composition
Subcohort
   member Censored Failure
                                  Total
                            39
      No
                436
                                      475
                187
                           17
      Yes
                                     204
 ----+----
               _____
                           ----+---
    Total 623 56
                                    679
Total sample = 243
No risk set with less than 4 controls
New stset definition
              id: id
failure event: _d ~= 0 & _d ~= . obs. time interval: (_t0, _t]
enter on or after: time _t0
exit on or before: failure
```

```
260 total obs.
0 exclusions
260 obs. remaining, representing
243 subjects
56 failures in single failure-per-subject data
4653.123 total analysis time at risk, at risk from t = 0
earliest observed entry t = 9.373047
last observed exit t = 75.59204
```

The output consists of

- 1. A table displaying the sample composition with respect to the full cohort. Note that from 679 subjects in the full cohort, 204 have been randomly sampled (subcohort). 39 more subjects who failed are added to the subcohort, so the total sample is 243 subjects.
- 2. A message declaring that in this sample no risk sets with three or fewer controls exist. Otherwise, a table illustrating risk sets with such few controls is displayed. This is a warning for the loss of efficiency of the design that may occur when the subcohort becomes small due to many failures or censorings. The sampling fraction α should be increased in such cases.
- 3. A new stset definition that fixes the entry and exit time to the present _t, _t0 and _d variables. This is necessary because nonsubcohort cases cannot rely on the original entry times. Note that after stcascoh, the total analysis time is reduced to 4653.123 starting from 15344.223 in the full cohort.

Syntax for estimating the model

stselpre is for use with survival-time data. Data must be prepared for case-cohort analysis by stcascoh before using this command.

Description

stselpre returns estimates and standard errors from proportional hazards fit to case-cohort data. Coefficients are estimated according to two methods: 1) the Self-Prentice method where risk sets use just the subcohort member at risk, and 2) the Prentice (1986) method where risk sets are augmented by nonsubcohort cases when they fail.

The asymptotic Self-Prentice method variance-covariance matrix and standard errors are computed using the simplification described in Therneau and Li (1999). The syntax of predict following stselpre is as in stcox.

Options

- nohr specifies that coefficients rather than hazard ratios are to be displayed. nohr may be typed at estimation or when replaying previously estimated results.
- level(#) specifies the confidence level for the confidence intervals of the coefficients. level may also be specified when replaying previously estimated results.
- self specifies that the Self-Prentice method coefficient vector is to be saved in e(b). By default, Prentice method coefficients are saved.
- breslow, efron, exactm, and exactp each specify a method for handling tied deaths that the underlying stcox command executes. efron is the default.

noshow prevents stselpre from displaying the identities of the key st variables above its output.

(Continued on next page)

Remarks

When a dataset is prepared, the parameter estimates can be easily obtained using a Cox model. However, their variance is somewhat complicated because of the correlation between risk sets induced by the sampling. Lin and Ying (1993) and independently Barlow (1994) proposed the use of the robust variance estimator for the case-cohort design as a simpler alternative to the asymptotically consistent estimator provided by Self and Prentice (1988). Recently, Therneau and Li (1999) proved that the Self and Prentice variance estimator can be obtained by correcting the standard variance estimate with a matrix derived from a subset of dfbeta residuals. Both estimates are now available in Stata. In estimating the model, three methods can be implemented: 1) Prentice, 2) Self and Prentice, and 3) Barlow. They differ in the composition of risk sets and in the weight ascribed to the nonsubcohort case and to the subcohort member. Both aspects can be handled by preparing an appropriate dataset and by using as offset terms, the log-weights stored in the variables created by stcascoh.

Example (continued)

In their analysis, Breslow and Day (1987) found three significant risk factors. Their final model includes four variables: 1) $\log(\text{age at first employment} - 10)$, 2) (year first employed - 1915)/100, 3) 2(year first employed - 1915)/100, and 4) $\log(\text{exposure} + 1)$. Here are the results in the full cohort:

```
. stcox afe_10 yfe_15 yfe2_15 logexp,nolog nohr
```

analysi		(dataout-orig time dataass time datain	in)			
Cox regres	ssion no t	ies				
No. of sub	jects =	679		Nui	mber of obs	= 679
No. of fai	ilures =	56				
Time at ri	isk = 153	44.22327				
				LR	chi2(4)	= 84.42
Log likeli	ihood = -2	85.22255		Pro	ob > chi2	= 0.0000
_t _d		Std. Err.	 z	P> z	[95% Conf	. Interval]
afe 10	2.155984	.4289709	5.026	0.000	1.315217	2.996752
					7084059	.5319132
		.5085606				
logexp	.7710877	.1746156	4.416	0.000	.4288474	1.113328

Now, we estimate the same model from a case-cohort design using the dataset previously prepared by stcascoh according to the various methods mentioned above and using the robust variance estimator. We begin with the Prentice method.

```
.stcox afe_10 yfe_15 yfe2_15 logexp, robust nohr nolog
         failure _d: _d
   analysis time _t: _t
 enter on or after: time _t0
                id: id
Cox regression -- no ties
No. of subjects =
                          243
                                                  Number of obs
                                                                           260
No. of failures =
                            56
               = 4653.122862
Time at risk
                                                  Wald chi2(4)
                                                                         42.90
                                                                   =
Log likelihood =
                                                  Prob > chi2
                                                                   =
                   -220.97225
                                                                        0.0000
                               (standard errors adjusted for clustering on id)
      _t
                        Robust
     _d |
               Coef.
                       Std. Err.
                                             P>|z|
                                                         [95% Conf. Interval]
                                       z
 afe_10 |
              1.9157
                       .4655684
                                     4.115
                                             0.000
                                                        1.003203
                                                                     2.828198
 yfe_15
            .1561891
                       .3807642
                                     0.410
                                             0.682
                                                         -.5900949
                                                                     .9024732
 yfe2_15 |
            -1.430739
                        .6503867
                                     -2.200
                                             0.028
                                                         -2.705474
                                                                     -.1560048
 logexp
           .7999919
                       .2140395
                                     3.738
                                             0.000
                                                         .3804821
                                                                     1.219502
```

Next, we use the Self and Prentice method.

```
. stcox afe_10 yfe_15 yfe2_15 logexp, offset(_wSelPre) robust nohr nolog
      failure _d: _d
 analysis time _t: _t
enter on or after: time _t0
             id: id
Cox regression -- no ties
No. of subjects =
                     243
                                        Number of obs =
                                                          260
No. of failures =
                     56
Time at risk
          = 4653.122862
                                        Wald chi2(4)
                                                    =
                                                        39.15
Log likelihood = -4119.5279
                                       Prob > chi2
                                                   =
                                                        0.0000
                       (standard errors adjusted for clustering on id)
         _____
    _t
                  Robust
    _d |
                                            [95% Conf. Interval]
           Coef. Std. Err.
                                   P>|z|
                              z
 4.010 0.000
                                         .9905537
 afe_10 | 1.937374 .4830806
                                                      2.884195
                 .4010318
                                                     .9679484
         .1819405
                                            -.6040675
                            0.454
                                   0.650
 yfe_15 |
yfe2_15 |
         -1.477223
                  .6956013
                            -2.124
                                    0.034
                                            -2.840576
                                                      -.1138694
          .8238937
                  .2278558
                          3.616 0.000
                                             .3773045
                                                     1.270483
 logexp
_wSelPre | (offset)
                       _____
```

Now, the Barlow method.

. stcox afe_10 yfe_15 yfe2_15 logexp, offset(_wBarlow) robust nohr nolog						
analysi	ailure _d: _ s time _t: _ n or after: 1 id: :	_t t time _t0				
Cox regres	ssion no t	ies				
No. of sub	ojects =	243		Nu	mber of obs	= 260
	ilures =					
Time at ri	isk = 465:	3.122862				
		075 00			ld chi2(4)	
Log likeli	ihood = -28	36.97533		Pr	ob > chi2	= 0.0000
	(standard errors adjusted for clustering on id)					
	Coef.		z	P> z	[95% Conf	. Interval]
afe_10	1.935024	.4790842	4.039	0.000	.996036	2.874012
yfe_15	.1779033	.3958307	0.449	0.653	5979106	.9537172
yfe2_15	-1.475154	.6836251	-2.158	0.031	-2.815035	1352738
01	.8216578 (offset)	.2236693	3.674	0.000	.3832741	1.260042

The first two methods can be implemented using stselpre as well. In this command, standard errors derive from the Self and Prentice model-based variance-covariance matrix. Note that they are similar to those calculated using the robust estimator.

```
.stselpre afe_10 yfe_15 yfe2_15 logexp, nohr
       failure _d: _d
  analysis time _t: _t
 enter on or after: time _t0
             id: id
Method for ties: efron
Self Prentice Variance Estimate for Case-Cohort Design
Self Prentice Scheme
            Coef. Std. Err. z P>|z|
      1
                                               [95% Conf. Interval]
..afe_101.937374.48885023.9630.000yfe_15.1819405.38065130.4780.633
                                           .9792455
                                                         2.895503
                                              -.5641223
                                                        .9280032
                  .6156814
yfe2_15 | -1.477223
                             -2.399
                                                        -.2705096
                                     0.016
                                              -2.683936
 logexp | .8238937 .2221188 3.709 0.000
                                              .3885489 1.259239
               . _ _ _ _ _ _ _ _
                         _____
                                                     _____
```

	1	Coef.	Std. Err.	z	P> z	=	. Interval]
afe_10	+- 	1.9157	.4888502	3.919	0.000	.9575717	2.873829
yfe_15	[.1561891	.3806513	0.410	0.682	5898736	.9022519
, fe2_15	1	-1.430739	.6156814	-2.324	0.020	-2.637453	224026
logexp	[.7999919	.2221188	3.602	0.000	.3646471	1.23533

Saved Results

stselpre saves in e() :

C 1

Sci	alars	
	e(N)	number of observations
	e(N_sub)	number of subjects
Ma	icros	
	e(cmd)	stselpre
	e(ties)	method for handling ties
	e(predict)	program used to implement predict
	e(scheme)	model name of coefficient vector saved
Ma	atrices	
	e(b)	coefficient vector of Prentice method (default). If self option is used,
		coefficient vector of Self and Prentice method are saved.
	e(V)	Self and Prentice model-based variance-covariance matrix
Fu	nctions	
	e(sample)	

Methods and formulas

The case-cohort design uses a pseudo-likelihood. Let $z_i(t)$ be the covariate vector and $Y_i(t)$ an at risk indicator for individual *i* at time *t*. Then, the pseudo-likelihood can be expressed as a weighted Cox regression model with the weights differently defined according to various analysis methods

$$\frac{Y_i(t)e^{z_i(t_j)\beta}}{Y_i(t)w_ie^{z_i(t_j)\beta} + \sum_{k \in S, \ k \neq i} Y_k(t_j)w_ke^{z_k(t_j)\beta}}$$

In the denominator, contributions of the failure and nonfailures (controls) at risk are given by the first and second terms respectively. In preparing a dataset for case–cohort analysis, all records with a failure are dissected in two time segments: 1) $(t_0, t - \epsilon]$ and 2) $(t - \epsilon, t]$. A case outside the subcohort isn't at risk until just before failure, so the first segment of nonsubcohort cases (and any other previous record of the same observation) is discarded from the sample. Both segments are retained for subcohort members who fail. Thus, the final dataset includes all the observations in the subcohort and just the final time segment records for subjects who fail but aren't in the subcohort. In such a dataset, implementing the Prentice method as in the formula above doesn't require that the weights be specified. In the other two methods, the weights must be specified. In Stata, the weights can be incorporated as an offset term; the logarithm of the weight must be used. The Self and Prentice method employs in the denominator just the subcohort cases setting the offset to -100, a value corresponding to a weight less than 10^{-40} that effectively allows exclusion of this observation from the denominator of the risk set.

The Barlow method requires that the offset be zero for all records corresponding to failures. Individuals who don't fail and the first time segment of subcohort members who do fail have offset $\log(1/\alpha)$ in an attempt to weight the controls in the denominator to the inverse of the sampling fraction.

Therneau and Li demonstrated that the Self and Prentice variance estimator for case cohort design can be calculated as:

$$V = I^{-1} + (1 - \alpha) D'_{SC} D_{SC}$$

where I^{-1} is the usual variance-covariance matrix returned by the Cox model, and D_{SC} is a subset of the matrix of dfbeta residuals that contains only records for the subcohort. (Note that Therneau and Li use a data setup slightly different than the one described in this section.)

Stata can calculate dfbeta residuals using efficient score residuals and I^{-1} . stdb, a Stata program at T. Lumley's web site (http://www.biostat.washington.edu/~thomas/), implements this calculus in a way not limited by the matsize constraints. When dfbeta residuals are at hand, it is straightforward to obtain the subset of the matrix through the usual matrix accum command.

Acknowledgment

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sbe42	Modeling the process of entry into the first marriage using Hernes model

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Abstract: This article describes the hernes command that fits the Hernes model of proportion of a cohort ever-married by age. The Hernes model has been widely applied in demographic studies. The author proposes to use the least squares method for model estimation and illustrates the use of the command with U.S. census data.

Keywords: Hernes model, first marriage, diffusion model.

Hernes (1972) developed a diffusion model for the process of entry into first marriage to explain the bell-shaped hazard rate of entry into marriage. In this model, he posits that two competing structural processes explain the time dependence in the process of entry into marriage. On one hand, with rising age t, there is an increasing proportion F(t) of a cohort that has already entered into first marriage, which in turn enhances the pressure to marry on those who are still unmarried. On the other hand, there is some sort of decreasing social attractiveness and, more importantly, a declining chance s(t) of contact between unmarried peers with increasing time t.

The diffusion model by Hernes can be expressed as

$$\frac{dF(t)}{dt} = s(t)F(t)(1 - F(t))$$
(1)

that is, the rate of change in the proportion married is a function of the proportion already married, the proportion not yet married, and the parameter of conversion that itself is a declining function of time.

We assume simply that each person starts out with a certain marriage potential, A_i , but that this potential declines with a constant proportion b for each time unit, where b is the same for all individuals. For the population as a whole, we then have

$$s(t) = Ab^t \tag{2}$$

where A is the average initial marriageability, and b < 1 is the constant of deterioration. Thus, over time, marriageability is a geometric progression; it decreases with a constant proportion for each time unit.

Inserting (2) into (1) we have

$$\frac{dF(t)}{dt} = Ab^t F(t)(1 - F(t)) \tag{3}$$

which can be transposed by integration, resulting in

$$-\log\frac{1-F(t)}{F(t)}\bigg|_{0}^{t} = \frac{Ab^{t}}{\log b}\bigg|_{0}^{t}$$

$$\tag{4}$$

When $F_0 = F(0)$ is a positive quantity, this expression can be written after exponentiation and rearrangement as

$$F(t) = \frac{1}{1 + \frac{(1 - F_0) \exp(A/\log b)}{F_0 \exp(Ab^t/\log b)}}$$
(5)

Since A and b are constants, we can always find a number such that

$$\log a = \frac{A}{\log b} \tag{6}$$

If this is substituted into (5), the equation for F(t) becomes

$$F(t) = \frac{1}{\frac{1 + (1 - F_0)a}{F_0 a^{b^t}}}$$
(7)

which, if we let $k = F_0/(a(1 - F_0))$, reduces to

$$F(t) = \frac{1}{1 + \frac{1}{k a^{b^{t}}}}$$
(8)

The curve corresponding to this equation looks somewhat like the logistic, but its inflection point is in general not midway between zero and its upper asymptote, so the limbs of the curve are not symmetric about the inflection point, as the logistic curve is constrained to be.

Note that F_0 is well defined and not equal to zero, but

$$F_0 = \frac{1}{1 + \frac{1}{ka}} \tag{9}$$

where k and a are estimated quantities. In practical terms, this means that in an empirical curve fit, we must take as t_0 the first year of the process. Note also that since b < 1, we have

$$\lim_{t \to \infty} F(t) = \frac{1}{1 + \frac{1}{k}}$$
(10)

Thus, the percentage ever married approaches (10) as an asymptote as the cohort ages.

To estimate the model for a given set of observed cumulative marriage rate (F(t)), we need a technique to estimate parameters F_0 , A, and b in formula (5), or equivalently, k, a, and b in (8) from which F_0 and A can be calculated. Once they are estimated, we can compute the predicted percentage married from the model for increasing values of t and compare these calculated values to the observed ones.

The quantity

$$g(t) = Ab^t \tag{11}$$

in equation (8) has the general form of the so-called Gompertz function, which can be easily estimated.

For that we rewrite (8) as

$$Ab^{t} = \frac{F(t)}{1 - F(t)} \tag{12}$$

and then use this procedure for the Gompertz function to find estimates for the parameters in equations (5) or (8).

Hernes proposed to use a simple procedure developed by Prescott (1922) for estimating the parameters of the Gompertz curve from the cumulative observations over time. Since the curve has three parameters, three equations are needed to find them. Equation (12) can be rewritten as

$$\log g(t) = \log k + \log ab^t \tag{13}$$

If we can divide the data into three equal sections, Prescott's procedure yields the estimates of the Hernes model from the equations

$$b^{T} = \frac{\sum_{3} \log g(t) - \sum_{2} \log g(t)}{\sum_{2} \log g(t) - \sum_{1} \log g(t)}$$
(14)

$$\log a = \left\{ \sum_{2} \log g(t) - \sum_{1} \log g(t) \right\} \frac{b-1}{(b^T - 1)^2}$$
(15)

$$\log k = \frac{1}{T} \left\{ \sum_{1} \log g(t) - \frac{b^T - 1}{b - 1} \log a \right\}$$
(16)

where \sum_1 stands for the sum of logarithms of observed cumulative percentages transformed by formula (12) of the first section, \sum_2 the corresponding sum of the second section, \sum_3 the sum of the third section, and T the number of observations in each of the three sections.

The above procedure has the advantage of easy calculation but does not provide the measurement of accuracy of estimated parameters. We here propose to use nonlinear least squares to estimate the Hernes model, which can be easily implemented by using Stata's nl command.

Syntax

```
hernes var_age var_rate [if exp] [in range] [, method(string) ]
```

Description

hernes generates five parameters for the Hernes model using given age-specific cumulative marriage rates: F_0 , A, a, b, and k. In addition, it yields the estimated age-specific cumulated marriage rates and age-specific differences between the observed and estimated cumulative marriage rates.

Options

method(*string*) specifies the method for estimating the Hernes model, either hernes for the Hernes method as described above or nl for the nonlinear least squares method. The default is the nonlinear least squares method.

Examples

We use the data of the cumulative first marriages for white women born in 1920–24 in the United States from the U.S. Bureau of Census to demonstrate the use of hernes to fit the Hernes model.

. use hernes (Cumulative Fi	irst Marr	iages for	White Women	Born in 1920-	-24 in the	US)
. describe						
Contains data obs:	from her 24	nes.dta		Cumulative	First Marr	isces for
005.	21					1920-24 in
vars:	2			18 Nov 2000	21:25	
size:	288 (99.9% of	memory free)			
1. age	float	%9.0g		Age in Year		
2. rate	float	%9.3f		Cumulative	First Marr	iage Rate
Sorted by:						
. summ						
Variable			Std. Dev.	Min	Max	
•			7.071068	15	38	
rate	24	.6524583	.3146823	.018	.916	

We first use the Hernes method:

. hernes age rate, method("hernes")

. list				
	age	rate	rate_hat	diff
1.	15	0.018	0.017	0.001
2.	16	0.046	0.043	0.003
3.	17	0.096	0.094	0.002
4.	18	0.176	0.173	0.003
5.	19	0.275	0.277	-0.002
6.	20	0.381	0.391	-0.010
7.	21	0.483	0.499	-0.016
8.	22	0.575	0.592	-0.017
9.	23	0.653	0.667	-0.014
10.	24	0.716	0.725	-0.009
11.	25	0.766	0.769	-0.003
12.	26	0.806	0.803	0.003
13.	27	0.833	0.829	0.004
14.	28	0.852	0.849	0.003
15.	29	0.867	0.864	0.003
16.	30	0.879	0.876	0.003
17.	31	0.887	0.886	0.001
18.	32	0.894	0.893	0.001
19.	33	0.900	0.900	0.000
20.	34	0.905	0.905	0.000
21.	35	0.909	0.909	0.000
22.	36	0.912	0.912	0.000
23.	37	0.914	0.915	-0.001
24.	38	0.916	0.917	-0.001
. retur	n list			
scalars	:			
	r(F0)	= .9298	3703505260212	
	r(k)	= 13.25	5930412458492	
	r(b)	= .8544	1559821043444	
	r(a)	= .0012	292205436846	
	r(A)	= 1.046	5201407690587	
and now the nl meth	nod			
. herne (obs =	s age rate, 24)	method('	'nl")	

Iteration 0: residual SS = .0010229 Iteration 1: residual SS = .0003782 Iteration 2: residual SS = .0003449Iteration 3: residual SS = .0003449Source SS df MS Number of obs = 24 F(3, 21) = 253609.83Model12.49407434.16469133Residual.00034485521.000016422 = 0.0000 = 1.0000 Prob > F R-squared 1.0000 ----**+**--Adj R-squared = Total | 12.4944188 24 .520600785 Root MSE = .0040524 Res. dev. = -199.5015 (hernes) _____ rate | Coef. Std. Err. t P>|t| [95% Conf. Interval] _____ _____ ----------.0000492 27.019 0.000 .0018716 460.795 0.000 .0012264 a | .0013287 b | .8624038 .001431 .8585117 .8662959 k 14.53891 .4107641 35.395 0.000 15.39314 13.68468 _____ _____ _____ _____ (SE's, P values, CI's, and correlations are asymptotic approximations) . list

	age	rate	rate_hat	diff
1.	15	0.018	0.019	-0.001
2.	16	0.046	0.046	0.000
3.	17	0.096	0.095	0.001
4.	18	0.176	0.172	0.004
5.	19	0.275	0.272	0.003
6.	20	0.381	0.382	-0.001
7.	21	0.483	0.488	-0.005
8.	22	0.575	0.581	-0.006
9.	23	0.653	0.657	-0.004
10.	24	0.716	0.717	-0.001
11.	25	0.766	0.763	0.003

12.	26	0.806	0.798	0.008
13.	27	0.833	0.826	0.007
14.	28	0.852	0.847	0.005
15.	29	0.867	0.863	0.004
16.	30	0.879	0.876	0.003
17.	31	0.887	0.887	0.000
18.	32	0.894	0.895	-0.001
19.	33	0.900	0.902	-0.002
20.	34	0.905	0.907	-0.002
21.	35	0.909	0.912	-0.003
22.	36	0.912	0.915	-0.003
23.	37	0.914	0.918	-0.004
24.	38	0.916	0.921	-0.005

As the above results show, both Hernes and least squares estimates fit the data very well, and the latter method yields a much better fit than the former. The largest deviations from the least squares procedure are found for ages 26 and 27 at which points the percentages married are overestimated by 0.8% and 0.7%, respectively. For the Hernes method, the largest difference is found for age 22 at which point the percentage married is overestimated by 1.72%. The degree of fit for the least squares method is seen more clearly in Figure 1, which plots the observed cumulative first marriages against age together with the fitted curve.



Figure 1. Observed and fitted first marriages versus age using nonlinear least squares.

The hernes command can also be applied conditionally using if and in expressions as shown by

	age rate if ag	ge<=24				
(obs = 10)						
	0: residual					
Iteration	1: residual	SS =	.0061118			
Iteration	2: residual	SS =	.0052664	:		
Iteration	3: residual	SS =	.0043897			
Iteration	4: residual	SS =	.0034274			
Iteration	5: residual	SS =	.0029379	1		
Iteration	6: residual	SS =	.001443			
Iteration	7: residual	SS =	.0000468			
Iteration	8: residual	SS =	.000045			
	9: residual					
	SS					Number of obs = 10
	•					F(3, 7) = 91576.69
Model	1.76635203	3	.588784	009		
	.000045006					R-squared = 1.0000
	+					Adj R-squared = 1.0000
Total	1.76639703	10	176630	703		Root MSE = $.0025356$
IUtai	1.70039703	10	.170035	103		Res. dev. $= -94.73426$
(1,						Res. dev. = -94.73420
(hernes)						
	Coof	C+ d	 Frr	+	D> +	[95% Conf. Interval]
				с 		
			0848	16.740	0.000	.0012187 .0016197
b	.86433	.0039	9088 2	21.123	0.000	.855087 .8735729
	14.52711					11.35555 17.69867

(SE's, P values, CI's, and correlations are asymptotic approximations)

Saved results

hernes saves the following scalars in r():

F_0
A
a
b
k

where these quantities are the parameters in equations (7) and (8).

References

Hernes, G. 1972. The Process of entry into first marriage. American Sociological Review 37: 173–182. Prescott, R. B. 1922. Law of growth in forecasting demand. Journal of the American Statistical Association 18: 471–479.

sg97.3	Update to formatting regression output	
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Abstract: An update to the outreg command is described.

Keywords: regression output.

I have fixed some small bugs in outreg, a program described in Gallup (1998, 1999, 2000) that writes regression output to a text file.

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- Gallup, J. L. 1998. sg97: Formatting regression output for published tables. Stata Technical Bulletin 46: 28–30. Reprinted in Stata Technical Bulletin Reprints, vol. 8, pp. 200–202.
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sg158	Random-effects ordered probit

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Abstract: The program reoprob that estimates a random-effects ordered probit model is presented and shown to be significantly faster than gllamm6. This increase in speed stems from the use of analytical first derivatives in the computation of the quasi-newton step.

Keywords: random-effects ordered probit, gllamm6, quasi-Newton algorithm.

Introduction

Recent developments in computing power have allowed the estimation of increasingly complex problems. One such class of estimators is allowing for individual specific effects when analyzing limited dependent variables. The first example of this in Stata is rfprobit introduced by Sribney (1995). This was followed by the inclusion of the random-effects option in xtprobit, and more recently by the creation of gllamm6 by Rabe-Hesketh, et al. (2000), which allows the computation of random-effects ordered probit models. However, the latter relies solely on the computation of the likelihood for the optimization, that is, the first derivatives and the Hessian are numerically approximated, and thus can be very slow, even for relatively simple problems. I propose a program, reoprob, which makes use of the analytical first derivatives and, thus, considerably improves performance. Using gllamm6 as a benchmark, I will show that this new program finds the "correct" solution and that it is substantially faster.

Syntax

```
reoprob depvar varlist [if exp] [in range], i(varname) [quadrat(#) level(#) maximize_options]
```

This command shares the features of all estimation commands. reoprob typed without arguments redisplays previous results.

Options

i (varname) is not optional, it specifies the variable corresponding to an independent unit (for example, a subject id).

- quadrat(#) specifies the number of points to use for Gaussian-Hermite quadrature. It is optional, and the default is 12. Increasing this value improves accuracy, but also increases computation time. Computation time is roughly proportional to its value.
- level (#) specifies the confidence level, in percent, for confidence intervals. The default is level (95) or as set by set level.
- maximize_options controls the maximization process and the display of information; see [R] maximize. nolog suppresses the display of the likelihood iterations. Use the trace option to view parameter convergence. The ltol(#) and tol(#) options can be used to loosen the convergence criterion (respectively 1e-7 and 1e-6 by default) during specification searches. iter(#) specifies the maximum number of iterations.

Remarks

The problem of interest can be describe as wanting to estimate

$$y_{it}^* = \beta' x_{it} + \epsilon_{it}, \qquad i = 1, \dots, N, \ t = 1, \dots, T$$
$$\epsilon_{it} = v_{it} + u_i$$
$$\operatorname{Var}(\epsilon_{it}) = \sigma_v^2 + \sigma_u^2 = 1 + \sigma_u^2$$
$$\operatorname{Corr}(\epsilon_{it}, \epsilon_{is}) = \rho = \frac{\sigma_u^2}{1 + \sigma_v^2}$$

where y^* is unobserved. Instead, the analyst observes

$$y_{it} = \begin{cases} 0 & \text{if } y_{it}^* \leq \mu_0, \\ 1 & \text{if } \mu_0 < y_{it}^* \leq \mu_1 \\ 2 & \text{if } \mu_1 < y_{it}^* \leq \mu_2 \\ \vdots \\ J & \text{if } \mu_{J-1} < y_{it}^* \end{cases}$$

Define $a_{it} = \mu_{j-1} - \beta' x_{it}$ and $b_{it} = \mu_j - \beta' x_{it}$ if $y_{it} = j$, where $\mu_{-1} = -\infty$ and $\mu_J = \infty$. Then, the log-likelihood function is $L = \sum_{i=1}^{N} \ln \left(P\left(y_{i1}, y_{i2}, \dots, y_{iT}\right) \right)$ where, by simply generalizing the argument made in Butler and Moffitt (1982), one can show that

$$P(y_{i1}, y_{i2}, \dots, y_{iT}) = \int_{a_{i1}}^{b_{i1}} \dots \int_{a_{iT}}^{b_{iT}} f(\epsilon_{i1}, \dots, \epsilon_{iT}) d\epsilon_{iT} \dots d\epsilon_{i1}$$
$$= \int_{a_{i1}}^{b_{i1}} \dots \int_{a_{iT}}^{b_{iT}} \int_{-\infty}^{\infty} \prod_{t=1}^{T} f(v_{it}|u_i) f(u_i) du_i dv_{iT} \dots dv_{i1}$$
$$= \int_{-\infty}^{\infty} \prod_{t=1}^{T} \left[F(b_{it}|u_i) - F(a_{it}|u_i) \right] du_i$$

in which $f(\cdot)$ and $F(\cdot)$ represent the pdf and cdf of the normal distribution function, respectively. As Butler and Moffitt (1982) demonstrated, this is amenable to Gaussian quadrature. Of course, this is sufficient to estimate such a model as one can use numerical approximation to the first and second derivatives to compute quasi-Newton steps. This, however, makes every step fairly long to compute, even for a relatively small sample. This can be improved upon since the first derivatives can also be approximated by Gauss-Hermite quadrature. Using the convention that $f_{it}^j = f(\mu_j - \beta' x_{it})$, $F_{it}^j = F(\mu_j - \beta' x_{it})$, $L_i = P(y_{i1}, y_{i2}, \ldots, y_{iT})$, and an indicator function 1 {statement} which takes value 1 if the statement is true and 0 otherwise, the first derivative with respect to a parameter k is given by

$$\frac{\partial L}{\partial k} = \frac{\partial \sum_{i} \ln L_{i}}{\partial k} = \sum_{i} \frac{1}{L_{i}} \frac{\partial L_{i}}{\partial k}$$

and thus for our parameters of interest

$$\begin{split} \frac{\partial L_i}{\partial \beta} &= \int_{-\infty}^{\infty} f(u_i) \sum_{t=1}^{T} \frac{f_{it}^{j-1} - f_{it}^j}{F_{it}^j - F_{it}^{j-1}} x_{it} \prod_{t=1}^{T} \left[F(b_{it}|u_i) - F(a_{it}|u_i) \right] du_i \\ \frac{\partial L_i}{\partial \mu_j} &= \int_{-\infty}^{\infty} f(u_i) \sum_{t=1}^{T} \frac{f_{it}^{j-1} \mathbf{1}\{y_{it} = j\} - f_{it}^j \mathbf{1}\{y_{it} = j-1\}}{F_{it}^j - F_{it}^{j-1}} \prod_{t=1}^{T} \left[F(b_{it}|u_i) - F(a_{it}|u_i) \right] du_i \\ \frac{\partial L_i}{\partial \rho} &= \int_{-\infty}^{\infty} f(u_i) \sum_{t=1}^{T} \frac{f_{it}^{j-1} - f_{it}^j}{F_{it}^j - F_{it}^{j-1}} \frac{\sqrt{1-\rho}}{\sqrt{2\rho}(1-\rho)} \prod_{t=1}^{T} \left[F(b_{it}|u_i) - F(a_{it}|u_i) \right] du_i \end{split}$$

Taking advantage of knowing the analytical first derivatives will result in substantial speed improvements, as will be shown below.

Examples

To demonstrate and test reoprob, I will investigate the effect of income, schooling, and political freedom on the degree of bureaucratic corruption in non-OECD countries. To this end, I will use data from 87 non-OECD countries over a 16 year period (1982–1997) on the level of bureaucratic corruption produced by the International Country Risk Guide. Not all years are available for every country, however. The corruption index (CI) ranges from 0 to 6. It is reported on a monthly basis, but I am using annual averages. Lower scores indicate "high government officials are likely to demand special payments" and that "illegal payments are generally expected throughout lower levels of government" in the form of "bribes connected with import and export licenses, exchange controls, tax assessment, police protection, or loans." Although the index does take noninteger values (because of the averaging), 90% of the values are integers and thus the rest are recoded to the smallest integer. Income and schooling are from the Global Development Network Growth Database developed by the World Bank. Income is taken to be GDP per capita, and education is measured as the ratio of total enrollment in primary school, regardless of age, to the population of the age group that officially corresponds to the primary school level. Estimates are based on the International Standard Classification of Education. Political freedom (PF) is given by the Gastil index of political rights. The Gastil index ranges from 1 to 7, one being the highest degree of political freedom.

For the purpose of comparison, however, I will first look at a simplified problem. First, I will reduce the number of values for the dependent variable to 3, that is, CI3 is 0 if CI is 0 or 1, it is 1 if CI is 2 or 3, and is 3 if CI is 4 or 5. The only regressor will be income. This will be estimated using 12 points for the quadrature. Using a Pentium III 450 mhz with 256 megs of RAM on a Windows NT 4.0 workstation platform, reoprob took 2 minutes 37 seconds to converge to the result presented below.

```
. use stb
. describe
Contains data from stb.dta
 obs:
              1,068
                   6
                                              27 Nov 2000 14:04
vars:
              29,904 (97.1% of memory free)
size:
  1. y
                       %9.0g
                float
  2. ps
                float
                       %9.0g
  3. pol
                float
                      %9.0g
  4. corr6
                float
                      %9.0g
  5. corr3
                       %9.0g
                float
                float %9.0g
  6. id
                                              group(id)
Sorted by: id
. reoprob corr3 y, i(id) quad(12)
Fitting constant-only model:
Iteration 0:
              log likelihood = -677.80343
               \log likelihood = -600.94473
Iteration 1:
              log likelihood = -591.25914
Iteration 2:
                                            (not concave)
              log likelihood = -577.09022
Iteration 3:
              log likelihood = -561.8791
Iteration 4:
Iteration 5:
               log likelihood = -560.88178
              log likelihood = -560.88048
Iteration 6:
              log likelihood = -560.88048
Iteration 7:
Fitting full model:
Iteration 0:
              log likelihood = -669.98703
```

Iteration Iteration Iteration Iteration Iteration Iteration	2: log like 3: log like 4: log like 5: log like 6: log like	elihood = -60 elihood = -58 elihood = -57 elihood = -56 elihood = -58 elihood = -58 elihood = -58	37.38208 74.74158 50.16828 59.90922 59.90892	(not conca (not conca		
	fects Ordered			LR c	er of obs = hi2(1) =	1.94
Log likel:	ihood = -559.9	90892 		Prob	> chi2 =	0.1633
	Coef.				[95% Conf.	Interval]
eq1 y	 0308618	.0202292	-1.526	0.127	0705104	.0087868
_	 -1.066998				-1.323274	8107222
_cut2	i				2.123557	2.720488
rho _cons	.7618085	.0238483	31.944	0.000	.7150667	.8085504

Using gllamm6 proves to be substantially slower; it converges to exactly the same coefficient estimates in 8 minutes 43 seconds, over 3 times slower.

Estimating the complete model yields similar results. Regressing CI on income, education, and PF, it takes 13 minutes and 14 seconds for reoprob to converge versus 44 minutes 35 seconds for gllamm6; again more than three times slower. Moreover, in this specific case, reoprob stops at a "better" coefficient estimate. This, however, should not be expected to be true in general. There may well be problems for which the opposite is true, it is simply a question of the stopping criterion being affected by the differences in the analytical and numerical gradients. These results are presented in the table of determinants of corruption in non-OECD countries given below.

	reoprob	gllamm6
income	-0.074	-0.034
	(0.014)***	(0.017)*
education	-0.006	-0.002
	(0.002)***	(0.002)
PF	0.134	0.198
	(0.032)***	(0.029)***
cut1	-3.360	-1.694
	(0.239)***	$(0.278)^{***}$
cut2	-1.728	-0.025
	$(0.228)^{***}$	(0.273)
cut3	0.341	2.073
	(0.222)	$(0.272)^{***}$
cut4	1.876	3.637
	(0.221)***	(0.283)***
cut5	3.004	4.754
	(0.241)***	(0.308)***
rho	0.755	
	(0.015)***	
var(1)		1.980
		(0.170)***
Observations	1068	1068
Log Likelihood	-1087.556	-1091.551

Also worth observing is that even though the two programs have stopped at a slightly different point, all coefficient estimates are of the same sign.

Hence, this paper has shown that reoprob computes the likelihood for a random-effects probit correctly. Furthermore, it has provided examples of the considerable increase in speed that may be achieved.

References

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sg159	Confidence intervals for correlations		
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Abstract: The commands ci2 and cii2 are introduced and illustrated. They perform as Stata's ci and cii, but also give confidence intervals for Pearson's product moment correlation and Spearman rank correlation, based on Fisher's transformation.

Keywords: correlation coefficient, Fisher's transformation, Spearman's rank correlation.

Stata's ci command and its immediate version cii together provide confidence intervals for a number of statistics based on standard distributions. These include means (normal distribution), proportions (binomial), and expected frequencies (poisson).

Syntax of ci and cii

ci [varlist] [weight] [if exp] [in range] [, level(#) binomial poisson exposure(varname)
 by(varlist_2) total]
cii #_{obs} #_{mean} #_{sd} [, level(#)] (normal variable)
cii #_{obs} #_{succ} [, level(#)] (binomial variable)
cii #_{exposure} #_{events} [, poisson level(#)] (Poisson variable)

aweights and fweights are allowed; see [U] 14.1.6 weight.

Brief review of correlation confidence intervals

I will give a reminder of the algebra of correlations, following Altman (1991). For paired data, (x_i, y_i) , Pearson's r, the product-moment correlation coefficient, is calculated as

$$r = \frac{\sum_{i} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i} (x_i - \bar{x})^2 \sum_{i} (y_i - \bar{y})^2}}$$

The sampling distribution of Pearson's r is not normal, but we can transform r to get a quantity called z, which does have an asymptotic normal sampling distribution. This is known as Fisher's transformation

$$z = \frac{1}{2} \log\left(\frac{1+r}{1-r}\right)$$

The standard error of z is approximately $s_z = 1/\sqrt{n-3}$, where n is the sample size, so for example, we can construct a 95% probability interval for z as $z_l = z - 1.96s_z$ to $z_u = z + 1.96s_z$, which when we transform back via $r = (e^{2z} - 1)/(e^{2z} + 1)$ gives a 95% confidence interval for the population correlation coefficient as $(e^{2z_l} - 1)/(e^{2z_l} + 1)$ to $(e^{2z_u} - 1)/(e^{2z_u} + 1)$.

For nonnormal data, Spearman's rank correlation can be used. For n larger than about 10, Fisher's transformation again gives an approximately normal sampling distribution and a suitable confidence interval.

The new commands ci2 and ci12 behave exactly as ci and ci1, except for the extra options corr and spearman. When these are used, confidence intervals for Pearson's product moment or Spearman's rank correlations are produced.

Syntax for ci2 and cii2

ci2 varl var2 [weight] [if exp] [in range] [, level(#) {corr | spearman}] cii2 # $_n$ # $_r$ [, level(#) corr]

It is important to include the corr and spearman options. Without them, these formats are invalid. ci2 (as ci) will give confidence intervals for the mean of the two variables; cii2 (as cii) will give a confidence interval for a binomial distribution, correcting $\#_r$ to give the proportion corresponding to nearest whole number of events.

Examples

We begin with cii2 operating as cii, and as for correlations.

. cii2 18 .7921 -- Binomial Exact --Variable [95% Conf. Interval] Obs Mean Std. Err. _____ _____ 18 .7777778 .0979908 .5236138 .9359131 . cii2 18 .7921, corr Confidence interval for correlation, based on Fisher's transformation. Correlation = 0.792 on 18 observations (95% CI: 0.516 to 0.919)

Next, we use ci2 for weight and mpg for Stata's auto data using both the corr and spearman options.

```
. use auto
(1978 Automobile Data)
. ci2 weight mpg, corr
Confidence interval for Pearson's product-moment correlation
of weight and mpg, based on Fisher's transformation.
Correlation = -0.807 on 74 observations (95% CI: -0.874 to -0.710)
. ci2 weight mpg, spearman
Confidence interval for Spearman's rank correlation
of weight and mpg, based on Fisher's transformation.
Correlation = -0.858 on 74 observations (95% CI: -0.908 to -0.782)
```

Finally, we use spearman on the first 10 observations.

. ci2 weight mpg in 1/10, spearman Confidence interval for Spearman's rank correlation of weight and mpg, based on Fisher's transformation. Correlation = -0.606 on 10 observations (95% CI: -0.894 to 0.039) Warning: This method may not give valid results with small samples (n<= 10) for rank correlations.

Saved results

Whichever command is used for correlations, the following are saved in r():

r(n)	number of observations
r(r)	correlation
r(1b)	lower bound
r(ub)	upper bound
r(corr)	(ci2 only) correlation type

Otherwise, results are saved as for ci and cii.

Reference

Altman D. G. 1991. Relationship between two continuous variables. In Practical Statistics for Medical Research, ed. D. G. Altman, 277-321. London: Chapman and Hall.

ssa14	Global and multiple causes-of-death life tables from complete or aggregated vital data
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Abstract: The command lifetabl for performing a wide variety of life table analyses is introduced and illustrated.

Keywords: life table analysis, vital statistics, causes of death, survival analysis.

The life table is one of the fundamental tools of vital statistics analysis, either when used from an epidemiological standpoint or from the perspective of actuarial science. As we know it today, the method was formally established in the transition of the 17th to the 18th century by Edmund Halley (1693) and John Graunt (1665), and afterwards became a focus of attention to many other distinguished men of science, such as Benjamin Gompertz (1825), in the first quarter of the 19th century. Although interest in mortality records can be traced back to the 3rd century Roman Empire mortality registries, the systematic compilation and publication of mortality statistics only began by the end of the 19th century. For instance, the first American official life table ever published came to light in 1900 (Selvin 1991).

Life table construction and analysis provides an alternative to standardization as an appropriate method to describe the pattern of the survival experience of a large population or of one of its subgroups, given only that we possess a set of age-specific mortality rates, or more elementary data allowing their computation, such as number of deaths, and midyear population estimates for each age strata (Armitage and Berry 1994; Chiang 1984). Some developments of this approach are also useful to evaluate the impact of competing risks as they act upon a group, as well as to obtain data to draw survival curves, survival probabilities, and hazard functions (Selvin 1991).

Generally, a distinction is made between cohort (or generation) life tables and current life tables. While the former variant aims at describing the actual observed survival experience of a group or cohort of individuals born at about the same time (a generation cohort) followed up through time, the latter type describes the survival pattern of a population group subject throughout life to the age-specific death rates currently observed in a particular community, as though no significant cohort effects, for example, generation variability influences exert their actions.

Both these two life table forms are quite useful in the context of epidemiological or vital statistics studies. While the current life table technique provides an alternative method to standardization when comparing the mortality experience or the burden of disease of different groups, the generation life table approach is particularly useful in the context of occupational health studies; namely, to investigate the patterns of observed mortality in specific professional groups followed up over a long period of time (Armitage and Berry 1994).

Another commonly-made distinction separates abridged from complete life tables. While an abridged life table typically displays data by 5- or 10-year age intervals, a complete life table exhibits data for every single year of age until the closing category which, until recently, was most of times 85+, that is, 85 and over years of age. In this sense, the abridged life table is constructed by reference to a "standard" complete table, whose significant internal relationships are transposed to the simplified version. Being an approximation, its use is mainly justified by computational constraints, or by lack or scarcity of the data. On the other hand, a complete life table may also be aggregated into 5- or 10-year age groups (Anderson 1999).

Chiang (1984), as well as others (for example, Armitage and Berry 1994; Anderson 1999) emphasize that the technique of construction of life tables, such as those published by life assurance offices or national sources of vital statistics, is a rather complex one. However, Hill and Hill (1991), as well as Selvin (1991) describe quite simple construction strategies which, being simplified and accessible to almost anyone, may prove quite useful either for pedagogic purposes, for epidemiological research, or for surveillance.

Syntax

lifetabl varlist [if exp] [in range], strata(age_level_var) [rates(ratesvar) deaths(deathsvar)
pop(popvar) by(byvar) nyears(age_interval_length_var) radix(#) sclist(varlist) allrx
weights(#1[#2[#3[#4]]]) pyll(#) keep label(labelvar) multiplier(#) not noo allsct
sconly noyll saving(filename) replace grphs ge gp gs gh gsc lograte graph_options]

Description

The lifetabl command allows the computation of life tables for whole populations, or their subgroups, based on vital statistics data, following the method described by Selvin (1991). Furthermore, it also permits the user to produce the so-called "multiple specific causes of death analysis," as well as several indicators of potential years of life lost due to specific causes of death, and also a number of graphics describing several aspects of the global and cause-specific survival experience of the groups considered.

lifetabl allows the construction of life tables based on data for single years of age, or aggregated for several years, following the general method provided by Selvin. According to this approach, a population life table, as well as several derived statistics, such as the at-birth, e_0 , and age-specific, e_j , expectation of life estimates or the corresponding survival probabilities or hazard rates (and functions), can be generated if we dispose of a set of observed age-specific mortality rates (or data allowing their computation, such as the number of recorded deaths and number of persons at risk for each age interval). The command options provided allow not only the computation of general life tables (for all causes of death at once, that is, single-cause life tables), according to desired if or in clauses, but also for specific population strata, for example, sex groups discriminated by means of a by option.

In addition to the tables just mentioned, lifetabl also allows the analysis of the impact of multiple specific causes of death (option sclist) on the pattern of human mortality. Up to 20 different variables registering the number of deaths related to particular causes in each age strata may be added through the sc option. The resulting output will then include tables with absolute values (and rates) for a number of indicators of potential years of life lost connected to the causes of death considered: $PYLL(x)_i$, which is Potential Years of Life Lost until age x due to cause i, $PYLL(x)u_i$, "uncorrected" Potential Years of Life Lost until age x, due to cause i; PEYLL, Period Expected Years of Life Lost; SEYLL, Standard Expected Years of Life Lost (Murray and Lopez 1996), together with tables displaying the following statistics: at birth, and lifetime (beyond age x), conditional probabilities of death for each specific cause (P_{xi}) , the probability of death by cause i given survival to age x), absolute risk of dying by each cause, given a certain age, in the following interval (q_{xi}) ; the cumulative distributions of deaths by cause and age (F_{xi}) ; and the probabilities of death after a certain age x, given that the death is caused by each of the specific categories considered (S_{xi}) .

Moreover, if requested by the option allsct, the program will also display tables for observed number of deaths by each cause and age level (Dxi), for the life table expected number of deaths, by each cause at each age level x (dxi), and, finally, for the life table expected total number of deaths by each cause occurring after each age x (Wxi).

Throughout the program output, the notation used for the labeling of life table columns, as well as indicators such as those just described (letters and expressions between parenthesis above), strictly follows the conventions adopted by Selvin (1991). On the other hand, the output labeling for statistics related with the potential years of life lost group of indicators derives from the suggestions of Murray and Lopez (1996). See the *Methods and formulas* section below for further details on the procedures and definitions.

With the lifetabl command, it is also possible to produce five different groups of graphics. Options ge, gp, gs, gh, and gsc allow users to request the graphs of, respectively, expectation of life function(s), cumulative distribution(s) of expected deaths, survival function(s), hazard rate function(s), as well as other graphics related to the specific causes of death included in the command. Option grphs requests all five graphics at once.

Since the program has several options to control the extent and type of outputs (for example, not, noo, noyll, allsct) and can produce very long series of tables or a large number of graphics, particularly when the by or grphs options are used together, we strongly recommend the user to begin by exploring the program with one of the example databases included with this insert.

Minimal specification

In order to produce a life table with the lifetabl routine, it is necessary to specify at least

1. Through the command option strata a numeric or string variable, coded in such a way as to adequately describe the different age strata (for example 1, 2, 3, ... j if the strata variable is numeric, or "[00-01[", "[01-02[", ... "j" if the variable is string type),

and one of

- 2a. A variable containing observed strata specific mortality rates (option rates)
- 2b. Two variables coded with, respectively, the number of death events registered for each age during the time interval considered (option deaths), and the number of persons in the same age levels (usually the mid-period population estimates; option pop).

Regarding the strata option, the values used to designate the successive age intervals must be unique within if or in subgroups and must also keep the natural order of the successive levels when sorted by the program. For example, a string variable coded "[0-1[", "[1-2[", "[2-3[", ..., "[30-31[", "[31-32[", and so on, would not conform to this requirement since the third level, "[2-3[" would always appear after "[19-20[" after a sorting. When in doubt, perhaps a safer alternative is provided by the use of a naturally ordered numeric variable to designate the successive strata in this option, together with a string variable, which may be declared through option label to provide labels for the output. This alternative instructs the program to use as labels in the output the first seven characters of the strings contained in*labelvar*.

If the program is run through the specification of observed rates (rates(ratesvar)), these must be constructed in order to represent number of events for 1, 10, 100, 1,000, 10,000, 10,000, or 1,000,000 persons. If the rates multiplier is other than 100,000 (the default value), the exact value to which the recorded rates are referred to must be explicitly declared through the option multip(#). Use of this last option is allowed only when option rates(ratesvar) is also utilized. However, regardless of the power of ten of the rates used, the figures shown in the life table column Rx for the life-table age-specific mortality rates are always referred to number of events per 100,000 individuals.

By the use of option radix(#), where radix stands for l_0 , the arbitrary number for people entering the life table's first age level, it is also possible to choose a value different from the default of 100,000. Although the radix is an essential element from which all the life table is derived, this option rarely will need to be used, since the default will be adequate for the majority of circumstances.

Another important technical detail of the life table construction regards the evaluation of the contribution made to the total time lived by a cohort who entered any age interval (l_0, l_1, \ldots, l_x) by those who die in that same period (d_0, d_1, \ldots, d_x) . Generally, it is assumed that, on average, those who die during each age period were alive for a time of approximately half of the total interval length. However, for life tables in which the interval lengths considered are equal to one year for ages following birth (complete life tables), that approximation is not valid. Indeed, during the first few years of life, deaths tend to occur not symmetrically around the midpoint of the interval, thus originating an overestimation of the same interval life table stationary population (L_r) . Usually this problem is dealt with by some form of correction made to the general rule above. One of the methods available, reported, and adopted by Selvin (1991) is the specification of weights other than 0.5 for the contribution of the death cases to the total time lived in the interval in the first four years of life. The lifetabl option weights allows the specification of such weights. If the option is ignored and the interval lengths of the life table intervals are all of one year, the weights automatically used by the program will be those empirically determined by Chiang (1984) and reported by Selvin (1991) for, respectively, the first four years of life: 0.113, 0.430, 0.450, and 0.470. At all subsequent intervals and in all circumstances, the contribution of each death to total time lived in the age segment is considered to be equivalent to one half the period length (that is, 0.5 years for complete life tables or half the interval length for tables with different aggregation of ages). On the other hand, if any of the life table age intervals extends itself for more than one year, the program automatically makes this parameter equal to 0.5 at all age levels, unless otherwise explicitly required by the declaration of a different set of one to four values for the first four periods through option weights. One other option, nyears(numvar), allows the user to inform the program about the name of the numeric variable which registers, in years, the length of each age interval. If this option is not used, the program assumes that all age periods are of one year length.

It is also possible to retain and/or save for further analysis or transformation several variables produced in the background during the construction of the life table (options keep and saving(*filename*)). Unless one of the two options just mentioned is included in the command line, the original data will always be restored (or reconstructed) at the end of the processing, thus protecting any user variables with names similar to the ones listed below in the original file. Kept variable names and their content are the following: Rx (life table mortality rates per 100,000 persons), $_qx$ (probability of dying in the x age interval), $_dx$ (expected number of deaths in the age interval), $_px$ (probability of surviving the age interval), $_lx$ (number of people alive at the beginning of the age interval), $_Lx$ (cumulative years lived through age x), $_Tx$ (total time lived beyond age x), $_ExpYL$ (expected years of life at age x), $_Surv$ (survival probability), $_SurvVar$ (Greenwood variance for $_Surv$), and $_Hrate$ (hazard rate).

If specific causes of death are also being considered in the analysis requested at the command line, three other sets of variables, respectively suffixed 1, 2, ... i (the number of the last specific cause of death included in the sc option), will also be retained: $_qxi$ (risks of dying of cause *i* in the age interval *x*), $_Wxi$ (expected total number of deaths by cause *i* after the beginning of the age interval *x*), and $_Fxi$ (cumulative distribution of deaths by cause *i*, through age).

Other available resources

Stata already has several quite extended and useful commands, the set of st algorithms, which can be applied to the analysis of "cohort" type, follow-up data. With some of these st commands, it is also possible to produce several variants of the classic life table here presented, provided the original data are recorded at the individual level (single observations followed-up through fixed or variable length time intervals). However, with the available st commands, it is not possible to produce life tables for whole populations based on vital statistics data aggregated at the level of age groups as shown in the examples provided below.

Options

strata(age_level_var) allows the specification of a numeric or string variable coding the different age strata. This option must always be specified. If the variable used is numeric, the values representing the successive age strata must be monotonically ascending numbers, because during processing, this variable will be subject to an ascending sort, and the concrete values recorded will be used as labels for the strata (for example, 0, 1, 2, ..., 90 for, respectively, the intervals [0-1[, [1-2[, [2-3[, ... [90+[). If the alternative possibility of specifying a string variable is utilized, the same also applies. Therefore, care must be taken in order to use strings which, after being sorted, keep in the correct order the corresponding age strata. A perhaps safer alternative is the use of a numeric variable with ascending integers to designate the successive age levels in this option together with a string variable to provide labels for the different age strata in the output through option label. In every circumstance, the (within if, in, or by subgroups) variable describing the age strata cannot have repeated, neither missing nor null, values.

- rates(ratesvar) designates a variable for stratum-specific observed mortality rates. Use of this option is mandatory, unless the following two options are used instead. The age-specific rates can be expressed in terms of several population multipliers (powers of ten). However, if the specific power of 10 for which the rates are referred is not 100,000 (the default), its value must be specified through the option multiplier.
- deaths (deathsvar) specifies a numeric variable containing the number of observed deaths in each of the age strata.
- pop(*popvar*) designates a numeric variable with the number of persons at risk at each of the age strata (for example, the mid-year population estimate). This option must always be used in conjunction with the previous one whenever option rates() is not available nor specified simultaneously.
- by(*byvar*) requests that all computations and outputs, graphics included, are produced for every subgroup defined by the nonmissing categories of one (and only one) numeric variable, *byvar*.
- nyears(*age_interval_length_var*) allows the user to declare a numeric variable specifying the length, in years, of the successive age strata. When this option is not used, it is assumed that all age intervals are equal to one year (in other words, it is assumed by the program that the life table being calculated is a complete life table). The (within subgroup) value for the last interval (an open one) is always (re)set to one.
- radix(#) allows the user to modify the life table number of persons at risk at exactly age 0; that is, the size of the life table conventional cohort (radix or l_0). The default value, assumed whenever this option is not used, is again 10^5 .
- sclist (varlist) specifies a list of from one to 20 numeric variables registering the cause-specific number of observed deaths in each of the age strata (and, eventually, for each of the by() subgroups). Use of this option will always be followed by a "multiple causes-of-death" analysis, consisting in the output of a number of additional tables. These will include estimates for the 1) at birth, and lifetime (beyond age x) conditional probabilities of death for each specific cause (Pr(death by cause i | age x)), 2) absolute risk of dying by each cause, given a certain age, during the following interval (q_{xi}) , 3) cumulative distributions of deaths by cause and age (F_{xi}) , and 4) probabilities of death after a certain age x, given that the death is caused by each of the specific categories considered. Whenever this option is utilized, it is safer and wiser to also use option deaths(deathsvar) to explicitly declare the total number of deaths observed to occur in each age strata. However, this requirement is not absolute because, in the absence of an explicit declaration of the total number of deaths in each age level (by all causes), the program automatically assumes that the (row) sum of the variables included in option sclist (varlist) equals the just-mentioned total. Of course, if that is not the case, the results may be compromised. So, when the deaths(deathsvar) option is not being used, care must be taken to assure that this assumption holds, for instance by including in the sclist(varlist) option, one variable for a residual specific cause-of-death category corresponding to the remaining, not otherwise explicitly considered, causes of death. Finally, as an alternative to the specification of the absolute number of observed deaths by specific causes, the variables for specific causes of death may also contain previously calculated age (and/or group) specific rates of death. It is only necessary that these rates are all referred to the same number of persons (power of ten) as the ones eventually included in the option rates (ratesvar), and that another option, allrx (signifying all specific causes are in rates) is also used to inform the program of this particular circumstance.
- allrx declares that the variables included in option sclist(varlist) contain specific rates instead of absolute numbers of deaths by each of the specific causes, which is the default for this program. If this option is used together with option rates(ratesvar), the user is advised to also specify options pop(popvar), and/or deaths(deathsvar), provided the data are available in order to allow the deduction of all the parameters necessary to produce the standard output. If neither of these is available (that is, if strictly only rates are declared), the program will not be able to calculate the potential years of life lost indicators.
- weights(#1[#2[#3[#4]]]) allows specification of the contribution made for the total time lived on each of the first four life table periods by the cases registered as deaths occurring in these same time intervals. The quantities specified must be expressed in terms of the proportion of the total interval presumably lived by any person ultimately deceased anytime during the same interval. The weights option allows the modification of the default values for one, or all, of the first four periods of living. By default, the weights used by lifetabl are those used by Selvin (1991) which, apparently, were taken from Chiang (1984). In fact, they are equivalent to an explicit specification of this option as weights(0.113 0.430 0.450 0.470). The variable number of parameters passed to the program is interpreted according to their order, as pertaining respectively to the first, second, third, and fourth age intervals. If fewer than four of these parameters are specified, the program assumes that the omitted parameters are the ones at the end of the list, and attributes to them the default value

of 0.50 (for instance, w(0.30) will be interpreted as weights(0.30 0.50 0.50 0.50)). Concerning all the time periods following the fourth, it is also always assumed that each death contributes to the total time lived in each age level by the cohort of people alive at its beginning with a time equal to one half of the respective interval length.

- pyll(#) provides the possibility of modification of the upper age limit utilized in the calculation of the indicator "potential years of life lost" until age #. The default value used by lifetabl is pyll(65), following the convention adopted by the U.S. Centers for Disease Control and Prevention, and also by a number of other national and international agencies. In this option, as well as in all outputs of the program, we also complied with the Murray and Lopez (1996) suggestion of always explicitly indicating the upper age limit used in the calculations.
- keep instructs the program to retain several of the variables generated during the life table construction procedure. By default, lifetabl restores the original dataset after processing. However, when option keep is included, the user data is left behind, unchanged, and a new datafile, with an added set of variables, but truncated according to any if or in expressions also utilized in the command, is kept in memory. By default, this new working file is saved under the name _SaVeD_.dta, thus replacing any equally named pre-existent file. The variables added to the original set are

_Rx	Life table mortality rates, per 10^5 persons
_qx	Probability of dying in interval
_dx	Expected number of deaths in interval
_px	Probability of surviving the interval
_lx	Number of people alive at the beginning of the interval
_Lx	Cumulative years lived through x
_Tx	Total time lived beyond x
_ExpYL	Expected years of life at age x
_Surv	Survival probability
_SurvVar	Greenwood variance for _Surv
_HRate	Hazard rate

- label(labelvar) specifies a string variable to be used in the outputs in the substitution of conventional ordered values in the naming of the successive age levels. In contrast with the truly optional use of this label option, the user is always obliged to (also) specify one variable (which may be the same) through option strata(age_level_var), in order to clearly indicate the correct ordering of the age levels. Due to the output space available, the strings stored in labelvar will appear truncated in the output if they are longer than 7 characters.
- multiplier(#) specifies the number of persons for which the mortality rates declared by the ratesvar in option rates are referred. Allowed values are powers 0 through 6 of ten. The default value for the rates multiplier, assumed whenever this option is not used, is 10⁵.
- not suppresses the display of tables, which may be useful if the user is mainly interested in the production of graphs or in comparing subgroup life expectancies.
- noo completely suppresses the written outputs. Following this option, only graphs will be displayed provided they have been requested in the same command line.
- allsct is used in combination with sclist (varlist) to instruct the program to display three additional tables related with the multiple cause-of-death analysis. These supplementary tables exhibit the observed number of deaths by each cause and age level (D_{xi}) , the life table expected number of deaths by each cause at each age level $x (d_{xi})$, and the life table expected total number of deaths by each cause occurring after each age $x (W_{xi})$.
- sconly instructs lifetabl to restrict the output only to results related with the multiple causes-of-death analysis.
- noyll allows the user to request that all output related with the potential years of life lost indicators not be displayed.
- saving(filename) allows the user to specify the name of a new filename to save the results. The name for the file must be fewer than eight characters, according to the general naming rules. This option may be combined with replace to allow the program to substitute any existing file with the same name.
- replace instructs lifetabl to overwrite any existing file similarly named when saving (filename) is specified.
- grphs specifies the production of all the five available groups of graphics. The same graphs may instead be produced individually by using the next five options.
- ge requests the display of a graphed expectation of life function (expectation for the mean years of remaining life to be lived, at each age), for one or more of the subgroups considered.
- gp requests the graph of the cumulative (proportional) distribution(s) of expected deaths.

gs requests the production of a graph with the survival function, or functions, if subgroups are being considered.

gh requests a graph of the hazard rate function, or functions, if subgroups are being considered.

gsc requests a set of graphs related with the specific causes of death included in option sclist(varlist).

lograte requests a graph of the log hazard rate(s) when the gh or grphs options are specified.

Examples

The examples provided below use three different data files allowing a complete exploration of the lifetabl command. The first dataset, named lifetabl.dta, was prepared with data taken from Selvin (1991, 245–248) and contains several variables related to California male and female mortality in 1980. The second file, mcauses.dta, stores Portuguese mortality data from several years (1993–1998) disaggregated on sex. This file also includes variables registering the number of observed deaths in each year-sex-age-strata due to some specific causes of death. The third data file included in this insert, 4deaths.dta, stores data on California male mortality in 1980 related to four specific categories (lung cancer, ischemic heart disease, motor vehicle accidents, and all other causes). It was also prepared with data taken from Selvin (1991, 264) with the purpose of allowing a cross-validation of the lifetabl command outputs by replicating the numeric results published by that author.

```
use lifetabl
(California Mortality: 1980, males & females. Source: Selvin, 1991)
 describe
Contains data from lifetabl.dta
                  182
                                                  California Mortality (1980,
  obs:
                                                    males & females. Source:
                                                    Selvin,1991)
                                                  19 Sep 2000 13:35
vars:
                   11
                7,826 (99.1% of memory free)
 size:
   1. strata
                 byte
                         %9.0g
                                                  Age strata order
   2. agelab
                 str7
                         %9s
                                                  Labels for the age strata
                         %5.0f
   3. deaths
                 int
                                                  Number of observed deaths
                         %9.0g
                                                  Resident population
                 float
   4. pop
                         %9.0g
   5. sex
                 bvte
                                      sex
                                                  sex
   6. Rx100000
                 float
                         %9.0g
                                                  Rate: deaths by 10<sup>5</sup> residents
                                                  Rate: deaths by 10<sup>4</sup> residents
   7. Rx10000
                 float
                         %9.0g
                                                  Rate: deaths by 10<sup>3</sup> residents
                         %9.0g
   8. Rx1000
                 float
   9. Rx100
                 float
                         %9.0g
                                                  Rate: deaths by 10<sup>2</sup> residents
                         %9.0g
  10. Rx10
                 float
                                                  Rate: deaths by 10 residents
  11. Rx1
                 float
                         %9.0g
                                                  Rate: deaths by 1 resident
```

Sorted by: sex strata

The string variable agelab, as well as strata of byte type, codifies information for the 91 age strata in both sexes.

Suppose we want to produce a complete life table for the male population.

		, s(strata)						
Radix: 100000 Nr of age strata: 91 Weights (first 4 strata): .113, .430, .450, .470 Rx multiplier:								
Strata	Rx	qx	dx	lx	Lx	Ex	Sx	
1	1671.3	0.01668	1647	100000	98521	69.61	1.000	
2	104.5	0.00104	103	98353	98295	69.77	0.984	
3	63.5	0.00063	62	98251	98216	68.84	0.983	
4	53.0	0.00053	52	98188	98161	67.89	0.982	
5	37.0	0.00037	36	98136	98118	66.92	0.981	
6	49.8	0.00050	49	98100	98076	65.95	0.981	
7	39.3	0.00039	39	98051	98032	64.98	0.981	
8	51.7	0.00052	51	98013	97987	64.00	0.980	
9	37.8	0.00038	37	97962	97944	63.04	0.980	
10	39.1	0.00039	38	97925	97906	62.06	0.979	
(output omitted)								
80	7969.1	0.07664	2640	34443	33123	7.67	0.344	
81	8962.7	0.08578	2728	31803	30439	7.27	0.318	
82	10319.1	0.09813	2853	29075	27648	6.90	0.291	
83	10820.9	0.10265	2692	26222	24876	6.60	0.262	
84	11811.1	0.11153	2624	23530	22218	6.30	0.235	
85	12856.8	0.12080	2525	20906	19643	6.02	0.209	

86 87 88 89 90	14290.7 15102.7 14887.5 17599.7 16666.7	0.13338 0.14042 0.13856 0.16176 0.15385	2452 2237 1897 1908 1521	18380 15929 13692 11795 9887	17155 14810 12744 10841 9126	5.78 5.60 5.43 5.22 5.13	0.184 0.159 0.137 0.118 0.099
91	20102.6	1.00000	8366	8366	41616	4.97	0.084
Life Expectancy at birth : 69.607 (years) Crude Mortality Rate : 14.366 (deaths by 10 ³ persons)							

From left to right the columns exhibit for each of the age strata numbered in the first column: Rx, the life table mortality rate; qx, the probability of dying in the age period for those alive at its beginning; dx, the life table number of expected deaths in each stratum, given the radix; 1x, the life table number of people alive at the beginning of each age period; Lx, the life table total number of years lived in the age period by those alive at its beginning (the life table person-years or stationary population); Ex, the expected (mean) years of remaining life for each stratum; and, finally, Sx, which informs about the mean probability of surviving until the beginning of each particular stratum.

At the end of the output appears the life table estimate of the crude mortality rate (always expressed in terms of deaths by 10^3 persons), and also the life table estimate of the "at birth" life expectancy statistic.

Notice because we have redundant data in our dataset (observed rates together with number of observed deaths plus population, for each strata), that exactly the same output could have been produced by

. lifetabl if sex==1 , s(strata) d(deaths) p(pop)

and also by the alternative command lines

```
. lifetabl if sex==1 , s(agelab) d(deaths) p(pop)
. lifetabl if sex==1 , s(agelab) r(Rx100000)
. lifetabl if sex==1 , s(agelab) r(Rx1000) multip(1000)
```

since our string variable agelab was constructed in order to reproduce the natural order of the age strata after being sorted. The last example also illustrates the use of observed age-specific mortality rates referred to a number of people other than the 100,000 default value.

Because we have never specified a variable to label the successive age intervals, the age strata were labeled as 1, 2, 3, ... j (their total). Following the classical division of a population from age 0 to 90+, the strata numbers should be interpreted in this example as $1 = [0 \text{ to } 1], 2 = [1 \text{ to } 2], \ldots, 91 = [90 + [$. Notice further that we could also have requested

. lifetabl , s(agelab) d(deaths) p(pop) label(agelab) by(sex)

thus obtaining 2 life tables, one for each sex, in which the age levels would appear labeled with the contents of the string variable agelab.

Until now, it was not necessary to use the option nyears (*age_interval_length_var*) due to the fact that we have been dealing with complete life tables. Automatically, the program assumes these conditions hold whenever not finding an explicit nyears (*age_interval_length_var*) option modifying the default assumption.

Let us also consider the request of one or more of the available graphs. It is only necessary to add, to any variation of the commands considered so far, the respective option(s). For example, the command

. lifetabl , s(agelab) r(Rx100000) grphs by(sex)

produces, in addition to two life tables for both sex groups (which could have been suppressed provided that we also included in the command line the option noo), the following five graphs.

(Continued on next page)



Example 2

Next, we illustrate the use of lifetabl in the context of the analysis of multiple causes of death. We use the mcauses dataset.

```
. use mcauses
(Portuguese Mortality in 5 categories: 1993-98, females & males. Source: INE,1999)
```
. describe			
Contains data f	rom mca	uses.dta	
obs:	216		Portuguese Mortality in 5 categories: 1993-98, females & males. Source: INE,1999
vars:	13		20 Sep 2000 12:34
size:	6,912 (99.3% of memory free)	-
1. year	int	%9.0g	Calendar year
2. strata	byte	%9.0g	Age level order
agelab	str5	%9s	Age level labels
nyears	byte	%9.0g	Age level length in years
5. sex	byte	%9.0g	Sex : $0 = females; 1 = males$
6. pop	float	%9.0g	Mid-year population
7. deaths	int	%9.0g	Total number of deaths
sc_infec	int	%9.0g	Deaths by infections
9. sc_tumor	int	%9.0g	Deaths by cancer
10. sc_circ	int	%9.0g	Deaths by cardiovascular diseases
11. sc_acid	int	%9.0g	Deaths by external causes
12. AllOthrC	int	%9.0g	deaths-(sum(4 sc vars))

Sorted by: year sex strata

Note that some of the variables have exactly the same name and meaning as the similar ones in the data file used previously (strata, agelab, sex, pop, deaths). However, the data stored in this file is a bit more complex than the data of the lifetabl.dta file we used before. Now, we are dealing with data pertaining to several calendar years (1993–1998, coded by the variable year), disaggregated by sex, and we also dispose of a set of variables codifying the absolute number of observed deaths related to four diagnostic groups (the sc_* variables registering, respectively, infectious diseases, cancer, cardiovascular diseases, and deaths by external causes), plus one other variable (AllOthrC) registering deaths linked with aetiologies different from those otherwise explicitly considered. One other feature of this dataset is that the age intervals are bigger than one year in length. In fact, data within each year-sex group is available only for (since birth, successive) five year intervals. Thus, we are not dealing with the standard conditions required for the computation of a complete life table. However, since we do possess one variable codifying the length of each age strata (nyears), it is still possible to approximately estimate the life table(s), provided that we use option nyears(varname) to instruct the program that we are dealing with nonequal or nonequal-to-one year age lags.

For instance, if we were (again) simply interested in the calculation of male and female life tables for the calendar year 1995, we would use

adix: 1	.00000		LIFE	TABLE			
rofag	ge strata:						
eights	(first 4 s	trata): .5	00, .500,	.500, .500	Rx mı	ltiplier:	100000
trata	Rx	qx	dx	lx	Lx	Ex	Sx
00-04	165.5	0.00824	165	100000	99588	79.12	1.000
05-09	26.7	0.00133	133	99835	99769	74.27	0.998
10-14	24.1	0.00120	120	99702	99642	69.36	0.997
15-19	37.8	0.00189	188	99582	99488	64.44	0.996
20-24	52.9	0.00264	262	99394	99263	59.56	0.994
25-29	62.9	0.00314	311	99131	98976	54.71	0.991
30-34	78.0	0.00389	385	98820	98628	49.88	0.988
35-39	96.8	0.00483	475	98435	98198	45.06	0.984
40-44	159.8	0.00796	779	97960	97570	40.27	0.980
45-49	209.9	0.01044	1015	97181	96673	35.57	0.972
50-54	322.5	0.01600	1538	96166	95397	30.92	0.962
55-59	493.7	0.02438	2307	94628	93474	26.38	0.946
60-64	769.0	0.03772	3483	92320	90579	21.98	0.923
65-69	1237.9	0.06004	5334	88838	86171	17.74	0.888
70-74	2365.1	0.11165	9323	83504	78843	13.72	0.835
75-79	4494.3	0.20201	14986	74181	66688	10.13	0.742
80-84	8985.2	0.36685	21716	59195	48337	7.06	0.592
85+	21290.5	1.00000	37479	37479	176038	4.70	0.375

	ge strata:		00, .500,	.500, .500	Rx mu	iltiplier:	100000
Strata	R x	qx	dx	lx	Lx	Ex	Sx
00-04	207.3	0.01031	206	100000	99484	71.86	1.00
05-09	40.0	0.00200	199	99794	99694	67.03	0.99
10-14	41.5	0.00207	207	99594	99491	62.16	0.99
15-19	123.2	0.00614	610	99388	99083	57.28	0.99
20-24	193.0	0.00960	949	98778	98303	52.62	0.98
25-29	235.7	0.01172	1146	97829	97256	48.10	0.97
30-34	260.5	0.01294	1251	96683	96057	43.64	0.96
35-39	300.4	0.01491	1423	95432	94721	39.18	0.95
40-44	363.7	0.01802	1694	94009	93162	34.74	0.94
45-49	500.7	0.02472	2282	92315	91174	30.33	0.92
50-54	681.2	0.03349	3015	90033	88525	26.04	0.90
55-59	1119.9	0.05447	4740	87017	84647	21.85	0.87
60-64	1768.5	0.08468	6967	82278	78794	17.97	0.82
65-69	2776.5	0.12981	9776	75310	70422	14.40	0.75
70-74	4398.7	0.19815	12985	65534	59041	11.17	0.65
75-79	7144.3	0.30308	15927	52549	44585	8.31	0.52
80-84	12882.5	0.48721	17843	36622	27701	5.84	0.36
85+	24875.8	1.00000	18779	18779	75492	4.02	0.18

The successive age strata have now been labeled with the contents of variable agelab, and, as anticipated, the program made a background reset of the arguments of the weights option to a constant value of 0.50. Nevertheless, this default behavior may always be modified by means of an explicit use of the weight option. We had to include an if restriction to the data being analyzed because the mcauses.dta data file stores figures from several years. Had we preferred to obtain life tables for all the calendar years, and for each of the genders one at a time, we would only have had to change accordingly the if expression, as well as the content of the by option. Of course, we would also have had to be prepared to deal with a very long list of tables.

Next, we illustrate the study of multiple causes of death by means of life-table-derived methods which provide an opportunity to isolate the impact of specific causes on the pattern of observed human mortality. The command below restricts the scope of the analysis to the observed male gender mortality in 1995.

. lifetabl if year==1995 & sex==1 , s(strata) d(deaths) p(pop) ny(nyears) . > l(agelab) sc(sc_infec sc_tumor sc_circ sc_acid AllOthrC)

We present the resulting output, stripped of its first part (a life table equal to the last one in the previous example). Of course, if we had chosen to also include option sconly (which stands for "specific causes related output only") in the above command line, we would have achieved a result similar the one shown below.

output omitted) Years of Life	Lost (YLL) due t	o specific cau	ises of death	
C. of death	PYLL(65)	PYLL (65)u	PEYLL	SEYL
sc_infec	32253	35085	48863	6078
sc_tumor	41440	50945	171222	23545
sc_circ	32795	40945	213076	30139
sc_acid	93360	101450	142275	17710
AllOthrC	108088	121165	270368	35902
C. of death	s of Life Lost PYLL(65)	PYLL (65)u	PEYLL	SEYL
sc_infec	7.7209	8.3989	199.1563	247.731
sc_tumor	9.9202	12.1955	697.8684	959.661
sc_circ	7.8507	9.8017	868.4573	1228.420
sc_acid	22.3491	24.2857	579.8859	721.826
	25.8748	29,0052	1101.9686	1463.334

* per 10^3 persons under 65 years: PYLL(65) and PYLL(65)u
* per 10^3 population members: PEYLL and SEYLL

Lifetime (at birth) prob. of death

C. of death	 -+-	Prob.
sc_infec sc_tumor sc_circ sc_acid AllOthrC	 	0.02237 0.21290 0.38801 0.06763 0.31734

Multiple Causes Life Table(s)

. _ _ _ _ _ _ _ _ _ .

Global and cause-specific probabilities of death in interval

	qx	qx1	qx2	qx3	qx4	 qx5
Strata	Total Risk	sc_infec	sc_tumor	sc_circ	sc_acid	AllOthrC
00-04	0.01031	0.00077	0.00026	0.00010	0.00105	0.00813
05-09	0.00200	0.00009	0.00023	0.00004	0.00101	0.00063
10-14	0.00207	0.00009	0.00021	0.00003	0.00094	0.00080
15-19	0.00614	0.00018	0.00035	0.00024	0.00390	0.00148
20-24	0.00960	0.00123	0.00038	0.00022	0.00535	0.00242
25-29	0.01172	0.00267	0.00060	0.00041	0.00497	0.00307
30-34	0.01294	0.00272	0.00092	0.00099	0.00460	0.00371
35-39	0.01491	0.00239	0.00195	0.00164	0.00415	0.00477
40-44	0.01802	0.00145	0.00337	0.00299	0.00429	0.00592
45-49	0.02472	0.00139	0.00654	0.00500	0.00419	0.00761
50-54	0.03349	0.00141	0.00983	0.00797	0.00412	0.01016
55-59	0.05447	0.00120	0.01729	0.01406	0.00514	0.01677
60-64	0.08468	0.00150	0.02740	0.02603	0.00531	0.02443
65-69	0.12981	0.00199	0.03995	0.04576	0.00581	0.03631
70-74	0.19815	0.00218	0.05307	0.07991	0.00755	0.05543
75-79	0.30308	0.00223	0.06668	0.13789	0.00797	0.08831
80-84	0.48721	0.00330	0.08272	0.23738	0.01269	0.15113
85+	1.00000	0.00532	0.11875	0.47913	0.01919	0.37763
	Fx	Fx1	F x 2	Fx3	Fx4	Fx5
Age	Tot Pr Dth	sc_infec	sc_tumor	sc_circ	sc_acid	AllOthrC
0	0.00000	0.00000	0.00000	0.00000	0.00000	0.00000
5	0.00206	0.03426	0.00123	0.00027	0.01545	0.02563
10	0.00406	0.03827	0.00232	0.00036	0.03032	0.02761
15	0.00612	0.04232	0.00332	0.00044	0.04415	0.03013
20	0.01222	0.05016	0.00496	0.00105	0.10141	0.03475
25	0.02171	0.10465	0.00671	0.00162	0.17952	0.04229
30	0.03317	0.22126	0.00944	0.00267	0.25142	0.05175
35	0.04568	0.33897	0.01361	0.00513	0.31719	0.06305
40	0.05991	0.44101	0.02236	0.00917	0.37579	0.07740
45	0.07685	0.50177	0.03726	0.01640	0.43544	0.09494
50	0.09967	0.55893	0.06560	0.02830	0.49262	0.11709
55	0.12983	0.61574	0.10715	0.04679	0.54751	0.14591
60	0.17722	0.66261	0.17782	0.07832	0.61371	0.19190
65	0.24690	0.71787	0.28371	0.13353	0.67829	0.25526
70	0.34466	0.78494	0.42504	0.22234	0.74294	0.34142
75	0.47451	0.84889	0.58839	0.35730	0.81611	0.45589
80	0.63378	0.90134	0.75297	0.54406	0.87803	0.60213
85	0.81221	0.95539	0.89526	0.76811	0.94672	0.77653

Lifetime, and beyond age x, cond. prob. of death: Pr(Dth by cause | x)

					·		
			Px1	P x 2	Px3	Px4	Px5
Age		Dths aft x	sc_infec	sc_tumor	sc_circ	sc_acid	AllOthrC
0	1	100825	0.02219	0.21115	0.38483	0.06708	0.31475
5		99794	0.02165	0.21307	0.38871	0.06672	0.30985

10	1	99594	0.02160	0.21327	0.38945	0.06585	0.30984
15		99388	0.02156	0.21350	0.39023	0.06504	0.30968
20		98778	0.02151	0.21446	0.39240	0.06152	0.31010
25		97829	0.02048	0.21616	0.39598	0.05672	0.31067
30		96683	0.01802	0.21812	0.40025	0.05236	0.31124
35		95432	0.01550	0.22005	0.40450	0.04839	0.31157
40		94009	0.01330	0.22140	0.40895	0.04491	0.31144
45		92315	0.01207	0.22203	0.41342	0.04136	0.31112
50		90033	0.01096	0.22095	0.41877	0.03811	0.31121
55		87017	0.00988	0.21844	0.42503	0.03517	0.31148
60		82278	0.00917	0.21274	0.43465	0.03175	0.31168
65		75310	0.00838	0.20249	0.44642	0.02889	0.31382
70		65534	0.00734	0.18678	0.46043	0.02653	0.31891
75		52549	0.00643	0.16676	0.47455	0.02367	0.32859
80		36622	0.00603	0.14361	0.48307	0.02252	0.34477
85	1	18779	0.00532	0.11875	0.47913	0.01919	0.37763

Probability of death after age x given death by cause (all & sp causes)

Sx4 S	Sx4	Sx3	Sx2	Sx1	Sx	
acid AllOth	sc_acid	sc_circ	sc_tumor	sc_infec	All causes	Age
00000 1.000	1.00000	1.00000	1.00000	1.00000	1.00000	0
98455 0.974	0.98455	0.99973	0.99877	0.96574	0.99794	5
96968 0.972	0.96968	0.99964	0.99768	0.96173	0.99594	10
95585 0.969	0.95585	0.99956	0.99668	0.95768	0.99388	15
39859 0.965	0.89859	0.99895	0.99504	0.94984	0.98778	20
32048 0.957	0.82048	0.99838	0.99329	0.89535	0.97829	25
74858 0.948	0.74858	0.99733	0.99056	0.77874	0.96683	30
68281 0.936	0.68281	0.99488	0.98639	0.66103	0.95432	35
62421 0.922	0.62421	0.99083	0.97764	0.55899	0.94009	40
6456 0.905	0.56456	0.98360	0.96274	0.49823	0.92315	45
50738 0.882	0.50738	0.97170	0.93440	0.44107	0.90033	50
15249 0.854	0.45249	0.95321	0.89285	0.38426	0.87017	55
38629 0.808	0.38629	0.92168	0.82218	0.33739	0.82278	60
32171 0.744	0.32171	0.86647	0.71629	0.28213	0.75310	65
25706 0.658	0.25706	0.77766	0.57496	0.21506	0.65534	70
L8389 0.544	0.18389	0.64270	0.41161	0.15111	0.52549	75
L2197 0.397	0.12197	0.45594	0.24703	0.09866	0.36622	80
0.223 0.223	0.05328	0.23189	0.10474	0.04461	0.18779	85

The first section of this output comprises two tables for, respectively, the absolute estimates for potential years of life lost in relation with each of the specific causes of death considered (first table), and the very same statistics transformed in rates per 1,000 persons at risk (second table).

Four different statistics are displayed: 1) PYLL(x), for the potential years of life lost until age x; a sum of the time lags separating the moment of each death (considered to correspond, on average, to the midpoint of each age interval), and a conventional, variable, upper age limit x; 2) PYLL(x)u, which is basically the same statistic, but noncorrected (u stands for uncorrected) for the estimated time lived in each age interval by those who die in it (this odd version of the statistic always provides higher estimates than PYLL(x) because it follows the noncredible assumption that all deaths occur at the beginning of each age interval, was only included in the program output in order to allow, by comparison, an evaluation of the impact and the possible bias linked to the discrete nature of the age interval lengths being considered); 3) PEYLL, which stands for period expected years of life lost; a popular alternative to PYLL(x), calculated for the whole life span, and where the years of life lost due to a death occurring at each age interval are made equal to the local expectation of life; and 4) SEYLL, which designates the standard expected years of life lost, a completely different type of indicator, standardized in nature, and thus, from the beginning, conceived with the aim of allowing between-population comparisons (its general definition is similar to that of PEYLL but, differently, the estimates for the age specific expectations of life are substituted from those of a reference population; in our program the "Coale and Demeny West Level 26" standard population, adapted from Murray and Lopez (1996), a population segment which exhibits an at-birth expectation of life of 82.5 years, and whose life expectation structure is applied by our program indifferently to both sexes).

In regard to PYLL(x), we must also add that a wide range of potential limits to life have been used, ranging from 60 to 85 (Murray and Lopez 1996). Although some authors, such as Dempsey (1947) argued that the limit to life should be set equal to the life expectancy at birth for any given population, others have sustained, on the basis of equally weak statistical arguments, that the same limit should be set to some other values, for some bigger, for others lower than life expectancy, no definitive

answer to the problem can be provided. So, while our program by default sets this limit to 65, the user remains free to modify it by means of option pyll.

The next table, entitled "Lifetime (at birth) prob. of death" shows an extract from the third of the next four tables presented and grouped together under the general heading "Multiple Causes Life Table(s)". The figures represent the life table estimates for the at-birth probability of dying due to each of the specific causes under study. For example, it can be seen that while the expectation for Portuguese male newborn of a future death related to a cardiovascular problem is almost 39%, its chances for a future death by accident (plus suicide or homicide) round to 7%.

The remaining tables describe, respectively, the risks of dying in each age interval by means of any of the specific causes (q_{xi}) , of the cumulative distributions of the deaths (again, for all reasons, and for the specific causes of death at each time, F_{xi}), of the lifetime, and beyond age x, conditional probabilities of death (that is, the probabilities of dying due to a certain cause after reaching any age x, P_{xi}), and finally, of the conditional probabilities of dying after any age provided that death is caused by any of the listed reasons (that is, the survival probabilities conditional on the causes of death, S_{xi}).

Tables with other useful information could also have been requested, had we decided to include the further option allsct. Since the interpretation of this kind of output is straightforward, we limit ourselves to showing some other possible examples the user may want to try, namely to illustrate the fact that it is also possible to obtain graphed versions of the probability functions. For instance, the following command line, quite similar to the previous one (only the two new options added, gsc and noo), would make the program suppress all written output and, instead, produce a series of 12 graphs, all related with the specific causes of death.

```
. lifetabl if year==1995 & sex==1 , s(strata) d(deaths) p(pop) ny(nyears)
. > l(agelab) sc(sc_infec sc_tumor sc_circ sc_acid AllOthrC) gsc noo
```

We show below some of these graphs, which we saved, one at a time, and later reused by means of the command graph using. The first four show the risk of death through age functions for the four specific groups of causes being studied. One obvious feature is the obvious relative increase in risk of dying by external causes and infections after adolescence, followed by a posterior decrease in the same risks, during the thirties and forties, and again an increase much later in life. Also characteristically, the corresponding patterns for cancer and cardiovascular diseases are quite different from these; risks increase monotonically mainly after the forties, for both types of conditions, but with a somewhat more delayed pattern for cardiovascular affections.



Figure 6. Risk of death through age functions for different groups of causes.

The next two graphs display the cumulative distributions of age at death and the survival probabilities conditional on the cause-of-death for all causes taken together. These two reciprocal sets of functions clearly show (again) that both the external causes of death, and the infectious diseases, detach themselves as important causes of premature death. It is perhaps appropriate to remember that, although these two groups of conditions, even when taken together, sum to a relatively low absolute risk (a global lifetime risk around 9%), they also have already shown to be responsible for a total of 125,613 years of life lost, even when considering a low conventional upper life limit of 65 years (PYLL (65)).

(Continued on next page)

Figure 7. Cumulative distributions of age at death functions.

Finally, we also show a series of four other graphs produced, illustrating the conditional probability of death due to affections related to any of the specific cause groups given age x (that is, the future risk of dying due to any of the causes, for those that already have attained age x).



Figure 8. Future risk of dying due to individual causes, given survival to x.

Note that only the relative proportion of dying by means of one of the cardiovascular related affections seems to (definitively) increase monotonically throughout the life span.

The reader may find it useful to explore some further examples we provide below (with outputs omitted) exploring the third database included in this insert, 4deaths.dta. Once again, most of the examples and illustrations included by Selvin (1991) may be fully reproduced with the lifetabl command provided only the user has enough patience and is willing to discount for quite small differences related to computational precision and rounding options.

```
. use 4deaths
. describe
. lifetabl , s(strata) l(agelab) r(Rx100000) ny(nyears)
. lifetabl , s(strata) l(agelab) p(pop) d(deaths) ny(nyears)
. lifetabl , s(strata) l(agelab) p(pop) d(deaths) ny(nyears) noo grphs log
 lifetabl , s(strata) r(Rx100000) ny(nyears) sc(lungcan ihd motor allother) sco
. lifetabl , s(strata) r(Rx100000) ny(nyears) sc(lungcan ihd motor allother) noo gsc
. lifetabl , s(strata) r(Rx100000) ny(nyears) sc(Rlung Rihd Rmotor Rallothr) allrx
 lifetabl , s(strata) r(Rx100000) ny(nyears) sc(Rlung Rihd Rmotor Rallothr) allrx p(pop)
. lifetabl , s(strata) r(Rx100000) ny(nyears) sc(Rlung Rihd Rmotor Rallothr) allrx d(death)
. lifetabl , s(strata) d(deaths) p(pop) ny(nyears) sc(Rlung Rihd Rmotor Rallothr) allrx
. lifetabl , s(strata) d(deaths) p(pop) ny(nyears) sc(Rlung Rihd Rmotor) allrx
. generate Rx1000 = (deaths / pop) * 1000
. label variable Rx1000 "Global death rate, per 1000"
. save 4deaths.dta, replace
. lifetabl , s(agelab) r(Rx1000) ny(nyears) m(1000)
. lifetabl , s(agelab) r(Rx1000) ny(nyears) m(1000) sc(lungcan ihd motor allother) allsct
. lifetabl , s(agelab) r(Rx100000) ny(nyears) sc(lungcan ihd motor allother) grphs noo
. lifetabl , s(agelab) r(Rx100000) ny(nyears)
. lifetabl , s(agelab) r(Rx100000) ny(nyears) radix(10000)
 lifetabl , s(agelab) r(Rx100000) ny(nyears) w(0.3 0.4)
. lifetabl , s(agelab) r(Rx100000) ny(nyears) not gs gh log
```

One final comment on potential years of life lost

Under the (not so realistic) assumption of the possibility of a complete elimination of any chosen cause of death, it is also possible to obtain one other type of summary statistic related to the potential years of life lost concept, but quite different from those described so far. It is only necessary to calculate, one after the other, two life tables: the first, a standard one, and the second, a slightly modified version in which the total number of deaths variable is reduced by a number equal to the deaths caused by the specific cause chosen. Afterwords, making a simple difference between the two estimates obtained for the expectation of life at birth will generate a statistic which may be interpreted as the mean number of additional years of living gained by each person if the specific cause of death under scrutiny could be eliminated (or, saying it otherwise, a summary measure of the mean number of years of life each one looses due to the existence of that particular cause of death). Consider the example below:

```
. use mcauses
(Portuguese Mortality in 5 categories: 1993-98, females & males. Source: INE, 1999)
. lifetabl if sex==1 & year==1995, s(agelab) ny(nyears) p(pop) d(deaths) not
  Global statistics (all causes of death)
  Life Expectancy at birth : 71.862
                                                        (years)
                                                        (deaths by 10<sup>3</sup> persons)
      Crude Mortality Rate : 13.916
. gen dthsdiff = deaths - sc_acid
. lifetabl if sex==1 & year==1995, s(agelab) ny(nyears) p(pop) d(dthsdiff) not
  Global statistics (all causes of death)
  Life Expectancy at birth : 73.734
                                                        (vears)
      Crude Mortality Rate : 13.562
                                                        (deaths by 10<sup>3</sup> persons)
. display 73.734 - 71.862
1.872
```

Thus, according to the 1995 Portuguese data, the complete prevention of all deaths related with accidents, homicides, and suicides (sc_acid) would result in an average increase in the life expectation of each male of 1.9 years. It can be verified that similar summary measures for cancer and cardiovascular related deaths amount to, respectively, 2.8 and 5.0 years, while the impact of infectious diseases attains no more than 0.6 years.

Methods and formulas

The all life table is generated from q_x , the calculated risk of dying in each age interval for those alive at its beginning,

$$q_x = \frac{R_x n_x}{1 + n_x w_x R_x}$$

where R_x represents the observed mortality rates, n_x the length of the age interval, and w_x the factor defining the proportion of the interval during which those that die remain, on average, alive. In the last age interval q_x is always made equal to 1.0 because all of those reaching the beginning of that last, open age interval, will die during it. Throughout the program, p_x , the probability of surviving until the end of any age interval for those alive at its beginning is taken from $1 - q_x$.

Survivor function (l_x)

The life table radix, l_0 , is set at 100,000. For ages greater than 0, the number of survivors remaining at exactly age x is calculated as

$$l_x = l_{x-1}(1 - q_{x-1}) = l_{x-1} - d_{x-1}$$

Life table decrement function (d_x)

The number of deaths d_x occurring in each age interval (for example, between ages x, and $x + n_x$) is calculated from the survivor function

$$d_x = l_x q_x$$

Notice that d_x in the last interval, d_{xlast} , is equal to l_{xlast} since q_{xlast} is always set to 1.

Stationary population (L_x)

The stationary population is calculated under the assumption that the survivor function declines linearly during each age interval

$$L_x = \frac{(l_x + l_{x+1})}{2} = l_x - d_x + (d_x w_x)$$

Person years lived at and above age x (T_x)

 T_x is calculated by summing L_x values at and above age x (of course, at the last age interval, T_x is equal to L_x):

$$T_x = \sum_{i=x}^{\text{xlast}} L_{x_i} L_{x_{i+1}} \cdots l_{x_{\text{xlast}}}$$

Life expectancy at age x (e_x)

Life expectancy at exactly each age x is taken from

$$e_x = \frac{T_x}{l_x}$$

If x = 0, then $e_x = e_0$, the at-birth life expectancy.

Life table estimate for the crude mortality rate (R_c)

The life table estimate for this parameter is taken from

$$R_c = \frac{1}{T_0/l_0} = \frac{1}{e_0}$$

Survival probabilities (S_x)

The life table estimate for this parameter is taken from

$$S_x = \frac{l_x}{\text{radix}} = \frac{l_x}{l_0}$$

Hazard rate(s) (HRate)

The life table estimate(s), corresponding to the approximation

$$-\frac{(S_{x+1}-S_x)}{(S_{x+1}+S_x)/2}$$

is (are) estimated by

$$\frac{d_x}{n_x(l_x - w_x d_x)}$$

Potential years of life lost until age x (PYLL(x))

This quantity, which is calculated in reference to a user-defined upper age limit L (that is, x = L) is obtained by means of the formula

$$PYLL(L) = \sum_{x=0}^{L} d_x (L - x_m)$$

where x_m represents the age interval midpoint (that is, $(x + (x + n_x))/2$). Due to the discrete treatment of the age dimension, if the upper age limit L was not defined in order to correspond to any age interval's lower or upper limit, the correct number of deaths for the relevant subsection of the time interval is estimated by assuming a uniform distribution of deaths during the interval.

Period expected years of life lost (PEYLL)

This quantity is computed until the last age to which people survive

$$PEYLL = \sum_{x=0}^{xlast} d_x e_x$$

In this formula, e_x represents the age-specific expectation of life.

Standard expected years of life lost (SEYLL)

This summary measure is again computed until the last age to which people survive

$$\mathrm{SEYLL} = \sum_{x=0}^{\mathrm{xlast}} d_x e_x^S$$

where e_x^S represents the standard population age-specific expectation of life. The lifetabl command automatically computes this statistic in reference to Coale and Demeny's "West Level 26" age-specific expectations of life for females, which we decided to apply indifferently to every group analyzed. These reference estimates were published by Murray and Lopez (1996), but only for five-year spaced ages from 0 to 100 years. In order to allow their use in the context of complete life tables construction and analysis with our program, we had to estimate values for intermediate years by linear interpolation. The following table presents the final result (the numbers from Murray and Lopez are those for years that are a multiple of five).

Age	e_x								
0	82.50	20	63.08	40	43.53	60	24.83	80	8.90
1	81.84	21	62.10	41	42.57	61	23.95	81	8.36
2	80.87	22	61.12	42	41.61	62	23.07	82	7.83
3	79.90	23	60.13	43	40.64	63	22.20	83	7.29
4	78.92	24	59.15	44	39.68	64	21.32	84	6.76
5	77.95	25	58.17	45	38.72	65	20.44	85	6.22
6	76.96	26	57.19	46	37.77	66	19.59	86	5.83
7	75.97	27	56.21	47	36.83	67	18.74	87	5.43
8	74.97	28	55.23	48	35.88	68	17.90	88	5.04
9	73.98	29	54.25	49	34.94	69	17.05	89	4.64
10	72.99	30	53.27	50	33.99	70	16.20	90	4.25
11	72.00	31	52.29	51	33.07	71	15.42	91	3.98
12	71.00	32	51.31	52	32.14	72	14.63	92	3.71
13	70.01	33	50.34	53	31.22	73	13.85	93	3.43
14	69.01	34	49.36	54	30.29	74	13.06	94	3.16
15	68.02	35	48.38	55	29.37	75	12.28	95	2.89
16	67.03	36	47.41	56	28.46	76	11.60	96	2.71
17	66.04	37	46.44	57	27.55	77	10.93	97	2.53
18	65.06	38	45.47	58	26.65	78	10.25	98	2.36
19	64.07	39	44.50	59	25.74	79	9.58	99	2.18
								100	2.00

Table 1. Coale and Demeny's "West Level 26" age-specific expectations of life for females.Modified from Murray and Lopez (1996, 17).

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STB categories and insert codes

Inserts in the STB are presently categorized as follows:

Gener	ral Categories:		
an	announcements	ip	instruction on programming
сс	communications & letters	OS	operating system, hardware, &
dm	data management		interprogram communication
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gr	graphics	tt	teaching
gr in	instruction	ZZ	not elsewhere classified
Statis	tical Categories:		
sbe	biostatistics & epidemiology	ssa	survival analysis
sed	exploratory data analysis	ssi	simulation & random numbers
sg	general statistics	SSS	social science & psychometrics
smv	multivariate analysis	sts	time-series, econometrics
snp	nonparametric methods	svy	survey sampling
sqc	quality control	sxd	experimental design
sqv	analysis of qualitative variables	SZZ	not elsewhere classified
srd	robust methods & statistical diagnostics		

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