

# The Effects of Single Mothers' Welfare Participation and Work Decisions on Children's Attainments

Hau Chyi<sup>1</sup> Orgul Demet Ozturk<sup>2</sup>

<sup>1</sup>WISE, Xiamen University

<sup>2</sup>University of South Carolina

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- Welfare system in the U.S.
  - Who are eligible?
  - What are the benefits?
  - 1996 reform: what changed and how?
- New restrictions on eligibility of TANF program.
  - 5-year welfare time limit and work requirement
- Implications for children's attainments through changes in mothers' behavior ?

## Related Literature

- Research on determinants of children's attainments are abundant:
  - Haveman and Wolfe (1995), Duncan and Hills (1997), Dahl and Lochner (2005) and Raquel (2007)
- Lack of information on causal effects of welfare on children's attainments (Currie (1998)).
- Issues:
  - Including children who were ineligible for welfare
  - OLS estimates may be biased
  - Multicollinearity between work and welfare decisions mostly ignored

# What Have We Done?

- Study effects of a low-skilled single mother's work and welfare decisions during her child's childhood on child's standardized math test score.
- Use IV method to control potential unobserved heterogeneity problem.
  - IV we propose: predicted quarters of work and welfare use estimated from low-skilled married mothers.
- A median welfare user (12 quarters) expects to gain 4.9 points more in test scores. Median work (14 quarters) is associated with 1.6 points more.

## Model Specification

Write a structural form of a child's attainment production function as:

$$\ln O_T = \ln A_0 + \gamma_1 \ln Y_T + \gamma_2 E_T + \gamma_3 W_T + \gamma_4 \ln A_0 W_T + \gamma_5 \ln A_0 E_T + \gamma_6 \text{testAge} + u$$

where:

- $\ln O_T$ : ln-PIAT math score of a child
- $\ln A_0$ : initial ability of the child, where:

$$\ln A_0 = \gamma_7 AFQT + \gamma_8 \text{gender} + \gamma_9 \text{race} + \gamma_{10} \text{ageless18} + \gamma_{11} \text{edu}$$

- $Y_T$ : accumulated family income during childhood.
- $E_T$ : total quarters of mother's work during childhood.
- $W_T$ : total quarters of welfare use.
- $u$ : unobserved characteristics.

## Model Specification - Cont.

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- Marginal productivity of mother's decisions varies with innate ability,  $\ln A_0$  (for example, Raquel (2007)).
- For example,

$$\frac{\partial \ln O_T}{\partial W_T} = \gamma_3 + \gamma_4 \times \ln A_0. \quad (1)$$

# Econometric Concerns

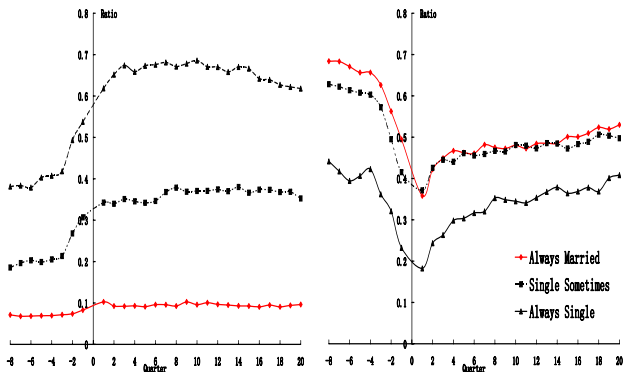
- Correlation between mothers' work and welfare decisions and the unobserved heterogeneity raises the issue of omitted variables bias.
- We will instrument for  $W$  and  $E$ .

## Econometric Concerns - Cont.

- IV we propose:
  - Predicted quarters of work and welfare use estimated from low-skilled married mothers.
- Why do we think it might work?



## Decision Patterns of NLSY Low-Skilled Mothers Based on Marital Status



(a) Welfare Use

(b) Labor Force Participation

Use the diagnostic functions of **-ivreg2-** to examine the validity of IVs.

# Constructing the Instruments

- Assume a mother makes two decisions of work ( $h_t=0, 1$ ) and welfare use ( $\omega_t=0, 1$ ) in each quarter.
- Let  $C_{ijt}$  represent utility from a single mother  $i$ 's  $j$ th alternative in quarter  $t$ ,

$$C_{ijt} = \beta_j' Z_{it} + u_{ijt}$$

where:

- $j = 1$  if mother chooses to ( $h_t=0, \omega_t = 0$ );
  - $j = 2$ : ( $h_t = 1, \omega_t = 0$ );
  - $j = 3$ : ( $h_t = 0, \omega_t = 1$ ), and  $j = 4$ : ( $h_t = 1, \omega_t = 1$ ).
  - Following Keane and Wolpin (2002),  $Z$  includes all  $X$  as well as annual state welfare benefit rules estimated by Ziliak (2007) and county characteristics.
- Assuming  $u_{ijt}$  follows multivariate normal distribution, we can estimate this model using **-mprobit-**.

# Constructing the Instruments - Cont.

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Potential instruments are:

$$\hat{E} = \sum_{t=1}^{20} \hat{\text{Pr}}(h_t), \text{ and}$$

$$\hat{W} = \sum_{t=1}^{20} \hat{\text{Pr}}(\omega_t).$$

1. Using two instruments ( $\hat{E}$  and  $\hat{W}$ ) for two endogenous variables ( $W$  and  $E$ ) means exact identification.

- To be able to test for overidentification, we use:

$$\sum_{t=1}^{20} \hat{\Pr}(h_t = 0, \omega_t = 0), \quad \sum_{t=1}^{20} \hat{\Pr}(h_t = 1, \omega_t = 0),$$
$$\sum_{t=1}^{20} \hat{\Pr}(h_t = 0, \omega_t = 1),$$

as instruments.

## Issues - Cont.

### 2. The model:

$$\ln O_T = \ln A_0 + \gamma_1 \ln Y + \gamma_2 E_T + \gamma_3 W_T + \gamma_4 \ln A_0 W_T \\ + \gamma_5 \ln A_0 E_T + \gamma_6 \text{testAge} + u,$$

implies we potentially need to instruments for  $(W, E, \ln A_0 W, \ln A_0 E)$ , which can be impractical.

- We only instrument for  $W$  and  $E$ , but use the **-orthogonal-** option in **-ivreg2-** to test whether  $\ln A_0 W$  and  $\ln A_0 E$  are exogenous.
- ### 3. Use **-cluster-** to control for intra-family correlation in $u$

## Use **-nlshr-** to Estimate the Same Model

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Another way to estimate the model is **-nlshr-**. Treat:

$$\ln O_T = \ln A_0 + \gamma_1 \ln Y + \gamma_2 E_T + \gamma_3 W_T + \gamma_4 \ln A_0 W_T \\ + \gamma_5 \ln A_0 E_T + \gamma_6 \text{testAge} + u$$

$$E_T = Z'h + \epsilon$$

$$W_T = Z'\omega + \nu$$

as a system of simultaneous equations. We can estimate this model by a nonlinear estimation method.

# Participation Pattern of the NLSY79 Low-Skilled Single Mothers

Child's age	Welfare	Part-time (300-1500)	Full-time ( $\geq 1500$ )
1	.67 (.47)	.25 (.43)	.17 (.38)
2	.69 (.46)	.31 (.46)	.23 (.42)
3	.70 (.47)	.33 (.47)	.25 (.43)
4	.68 (.47)	.34 (.48)	.27 (.44)
5	.65 (.48)	.36 (.48)	.28 (.45)

<sup>†</sup> Conditional on work

## First-Stage Results for NLSY Test Scores

	<i>E</i>	<i>W</i>
AFQT	.0031 (.0031)	.0122*** (.0044)
Gender	-.5366*** (.1057)	-1.3512*** (.2018)
.	.	.
<u>Interaction Between <i>E</i> and</u>		
AFQT	-.0006** (.0002)	-.0002 (.0002)
Gender	.0679*** (.0072)	.0314*** (.0104)
.	.	.
<u>Interaction Between <i>W</i> and</u>		
AFQT	-.0001 (.0002)	-.0009*** (.0003)
Gender	.0013 (.0057)	.1078*** (.0118)
.	.	.
<u>Instruments</u>		
$\sum_{t=1}^5 \widehat{\Pr}(h_t = 0, \omega_t = 0)$	.00001 (.0062)	-.0247** (.0098)
$\sum_{t=1}^5 \widehat{\Pr}(h_t = 0, \omega_t = 1)$	-.0817*** (.0139)	.0656*** (.0148)
$\sum_{t=1}^5 \widehat{\Pr}(h_t = 1, \omega_t = 0)$	.5603*** (.1086)	-.3581*** (.0971)
F Test	.0000	.0000
No. of Obs.	1,833	1,833

\*\*\*: significant at 1% significance level. \*\*: significant at 5% significance level.



## First Stage Instruments Validity - Correlation with Endogenous Variables

- Shea partial  $R^2$ , partial  $R^2$ , and F-test

Variable	Shea Partial $R^2$	Partial $R^2$	F(4,1812)	P-value
<i>E</i>	.0305	.2345	58.11	.0000
<i>W</i>	.0610	.4681	100.17	.0000

- Tests of joint significance of coefficients of endogenous regressors in main equation and overidentifying restrictions

Anderson-Rubin Wald test ( <i>F</i> <i>p</i> -value)	3491.85 .0000
Anderson-Rubin Wald test ( $\chi^2$ <i>p</i> -value)	14129.27 .0000
Stock-Wright LM statistic ( $\chi^2$ <i>p</i> -value)	231.74 .0000

- Underidentification Test

$H_0$ : Model is unidentified	56.703
<i>p</i> -value	.0000

## First Stage Instruments Validity - Cont.

	GMM2S	CUE
<b>Weak Identification test</b>		
$H_0$ : Instruments are weak	10.049	10.049
<b>Stock-Yogo weak ID test critical values:</b>		
5% maximal IV relative bias	11.04	
10% maximal IV relative bias	7.56	
20% maximal IV relative bias	5.57	
30% maximal IV relative bias	4.73	
10% maximal IV/LIML size	16.87	4.72
15% maximal IV/LIML size	9.93	3.39
20% maximal IV/LIML size	7.54	2.99
25% maximal IV/LIML size	6.28	2.79

## First Stage Instruments Validity - Cont.

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	GMM2S	CUE
<b><u>Overidentification test</u></b>		
$H_0$ : Instruments are orthogonal to errors	7.638	7.736
$p$ -value	.1058	.1013
<b><u>Endogeneity Test</u></b>		
$H_0$ : OLS estimator is consistent with IV estimator	39.041	39.041
$p$ -value	.0000	.0000

## Results for NLSY Test Scores

Chyi and Ozturk

	GMM2S	CUE	-nlstur-
$E$	.1191***	.1223***	.104***
( $\gamma_2$ )	(.0209)	(.0209)	(.0151)
$W$	.2894***	.2819***	.181***
( $\gamma_3$ )	(.0180)	(.0177)	(.0086)
$\ln A_0 \times W$			-.0486***
( $\gamma_4$ )			(.0010)
$\ln A_0 \times E$			-.0284***
( $\gamma_5$ )			(.0013)
<u>Initial Ability</u>			
AFQT	-.0033**	-.0033**	-.0039*
( $\gamma_7$ )	(.0016)	(.0016)	(.0016)
Gender	.4890***	.4731***	.392***
( $\gamma_8$ )	(.0714)	(.0706)	(.0591)
<u>Interaction Between <math>E</math> and</u>			
AFQT	.0001**	.0001**	
	(.0000)	(.0000)	
Gender	-.0125***	-.0122***	
	(.0024)	(.0024)	
<u>Interaction Between <math>W</math> and</u>			
AFQT	.0003***	.0003***	
	(.0001)	(.0001)	
Gender	-.0303***	-.0289***	
	(.0046)	(.0045)	

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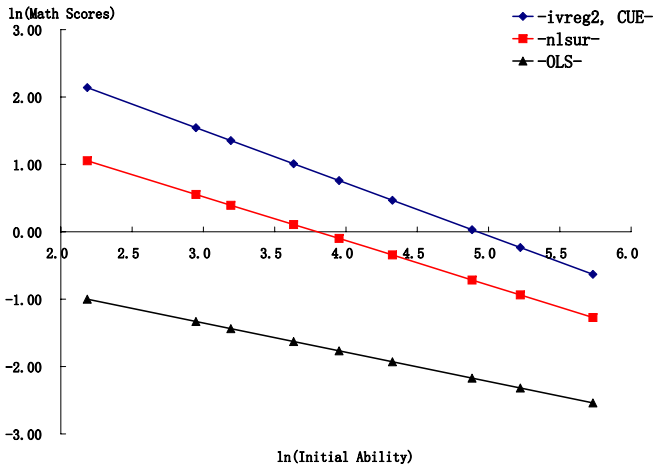
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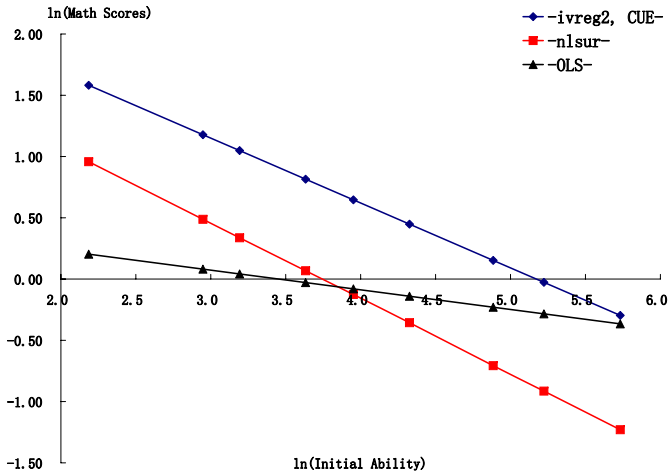
Sample Patterns Results

Concluding Remarks

## Total Effect of Welfare on Ability for a Median User (Welfare = 12 Quarters)



## Total Effect of Work on Ability for a Median User (Work=17 Quarters)



# Future Plans

- Incorporating longer-run results
- Separate effects of full- and part-time work