# Heterogeneous difference-in-differences estimation

StataCorp LLC

September 01, 2023

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The effect of a treatment or exposure on an outcome

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The effect of a treatment or exposure on an outcome

 Average treatment effect (ATE) and average treatment effect on the treated (ATET)

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The effect of a treatment or exposure on an outcome

- Average treatment effect (ATE) and average treatment effect on the treated (ATET)
- teffects: cross-sectional data selection on observables
- didregress and xtdidregress: repeated-measures selection on unobservables
- Estimation, inference, visualization, diagnostics, and tests

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The effect of a treatment or exposure on an outcome

- Average treatment effect (ATE) and average treatment effect on the treated (ATET)
- teffects: cross-sectional data selection on observables
- didregress and xtdidregress: repeated-measures selection on unobservables
- Estimation, inference, visualization, diagnostics, and tests
- One treatment effect. That assumes that the treatment does not change over groups or time. Homogeneous treatment effects
- New: Heterogeneous treatment effects for selection on unobservables. Heterogeneous Difference in differences (DID). Multiple ATETs

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# Starting point: Why heterogeneous treatment effects?

DID with different groups treated at different times

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- DID with different groups treated at different times
- With multiple treatment times the ATET for DID was obtained via

$$y_{it} = \beta_0 + D_{it}\beta_1 + \gamma_t + \gamma_g + e_{it}$$

- $\beta_1$  is the ATET
- A generalization of the well understood 2 by 2 model.

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# Starting point: Why heterogeneous treatment effects?

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$$y_{it} = \beta_0 + D_{it}\beta_1 + \gamma_t + \gamma_g + e_{it}$$

- $\beta_1$  is the ATET
- A generalization of the well understood 2 by 2 model.
- Two-way fixed-effects (TWFE) was criticized in the last six years
- Why:
  - Homogeneity (well understood)
  - 2 Hidden cost of generalizing of 2 by 2

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## What happens when we go beyond the 2 by 2 model?

- ATET might be different for groups treated at different times
- Within groups, ATET might change over time
- If this is the case:

$$y_{it} = \beta_0 + D_{it} \beta_1 + \gamma_t + \gamma_g + e_{it}$$

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## What happens when we go beyond the 2 by 2 model?

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$$y_{it} = \beta_0 + D_{it}\beta_1 + \gamma_t + \gamma_g + e_{it}$$

- Weighted average
  - Borusyak, Jaravel, and Spiess (2018)
  - de Chaisemartin and D'Haultfoeuille (2020)
  - Goodman-Bacon (2021) (estat bdecomp)

### Bacon decomposition

•  $\beta_1$  is a weighted average of (2 by 2) estimates

$$y_{it} = \beta_0 + D_{it} \beta_1 + \gamma_t + \gamma_g + e_{it}$$

- 2 by 2 estimates using:
  - Never treated groups
  - Early treated groups

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## Bacon decomposition

•  $\beta_1$  is a weighted average of (2 by 2) estimates

$$y_{it} = \beta_0 + D_{it} \beta_1 + \gamma_t + \gamma_g + e_{it}$$

- 2 by 2 estimates using:
  - Never treated groups
  - Early treated groups
- Some of the comparisons are valid comparisons. Some are not.
- Validity: satisfying a parallel-trends assumption.

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#### Let's see it work

- What a 2 by 2 model looks like
- What a DID model with multiple treatment times looks like graphically
  - homogeneous treatment
  - heterogeneous treatment
- What the Bacon decomposition tells us
  - homogeneous treatment
  - heterogeneous treatment

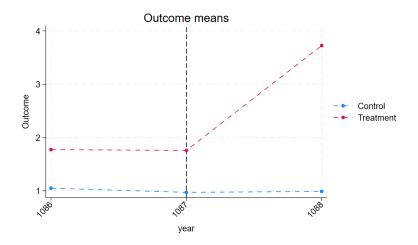
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#### Let's see it work

- What a 2 by 2 model looks like
- What a DID model with multiple treatment times looks like graphically
  - homogeneous treatment
  - heterogeneous treatment
- What the Bacon decomposition tells us
  - homogeneous treatment
  - heterogeneous treatment
- Build our understanding of heterogeneous DID

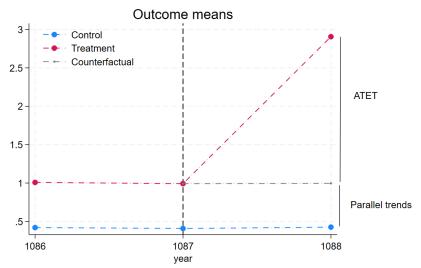
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## 2 by 2 framework: estat trendplots



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## 2 by 2 framework: Parallel(Common)-trends assumption



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## Homogeneous treatment with multiple treatment times I

- 10 time periods
- Treatment occurs for some groups at time 3 (Earlier treated)
- For others at time 6 (Later treated)
- Some units remain untreated

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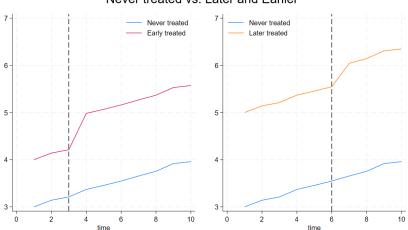
## Homogeneous treatment with multiple treatment times I

- 10 time periods
- Treatment occurs for some groups at time 3 (Earlier treated)
- For others at time 6 (Later treated)
- Some units remain untreated
- What are the comparisons used by TWFE

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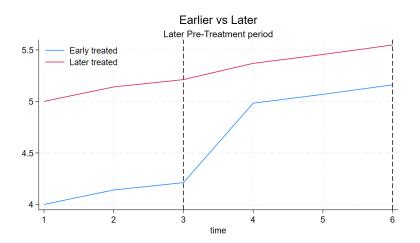
# Homogeneous treatment with multiple treatment times I

#### Never treated vs. Later and Earlier

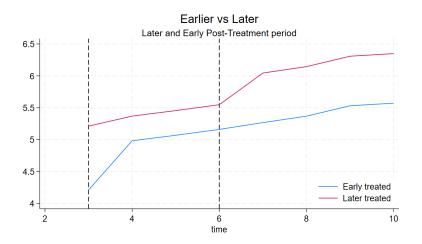


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# Homogeneous treatment with multiple treatment times II



# Homogeneous treatment with multiple treatment times III



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#### Homogeneous treatment: estat bdecomp

```
. estat bdecomp, summaryonly
DID treatment-effect decomposition
ATET = 4.041694
                                                   Number of obs
                                                                      = 100,000
                                                   Number of groups
                                                                        10,000
                                                   Number of cohorts =
ATET decomposition summary
                                          ATET component
                                                                        Weight
Treated vs never treated
                                               4.0435917
                                                                       0.865605
Treated earlier vs later
                                               4.0245287
                                                                      0.057598
Treated later vs earlier
                                               4.0331799
                                                                       0.076797
```

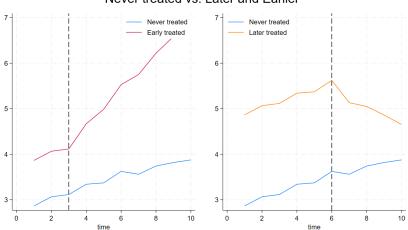
Note: Number of cohorts includes never treated.

Note: The ATET reported by xtdidregress is a weighted average of the ATET components. If any component is substantially different from the ATET reported by xtdidregress and the weight is large, consider accounting for treatment-effect heterogeneity by using xthdidregress.

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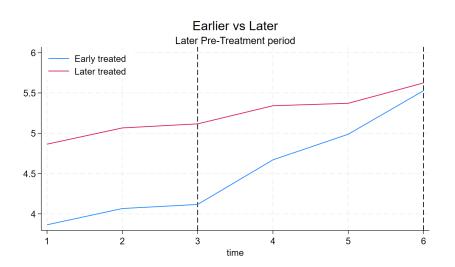
## Heterogeneous treatment effect I





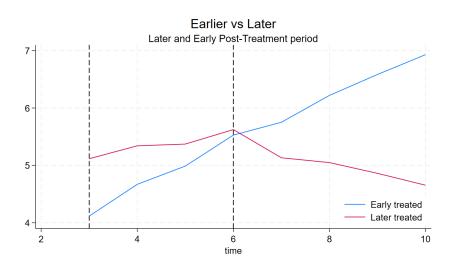
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## Heterogeneous treatment effect II



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#### Heterogeneous treatment effect III



#### Heterogeneous treatment: estat bdecomp

```
. estat bdecomp, summaryonly
DID treatment-effect decomposition
ATET = 1.389688
                                                    Number of obs
                                                                       = 50,000
                                                    Number of groups
                                                                       = 5,000
                                                    Number of cohorts =
ATET decomposition summary
                                          ATET component
                                                                        Weight
Treated vs never treated
                                               1.9728088
                                                                       0.860939
Treated earlier vs later
                                               4.3441312
                                                                       0.059597
Treated later vs earlier
                                              -7.1439268
                                                                       0.079463
```

Note: Number of cohorts includes never treated.

Note: The ATET reported by xtdidregress is a weighted average of the ATET components. If any component is substantially different from the ATET reported by xtdidregress and the weight is large, consider accounting for treatment-effect heterogeneity by using xthdidregress.

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# What would the aggregated effect be with "good" comparison groups?

. estat aggregation Overall ATET

Number of obs = 50,000 (Std. err. adjusted for 50 clusters in state)

У	ATET	Robust std. err.	z	P> z	[95% conf.	interval]
tr (1 vs 0)	3.654175	.962046	3.80	0.000	1.768599	5.53975

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#### What have we learned?

- With multiple treatment times, traditional DID assumes homogeneity
- 2 by 2 comparisons are well defined, but not all are useful
  - Comparison group matters
  - Time of comparison matters
- With multiple treatment times, it is important to assess heterogeneity
- If we suspect heterogeneity or do not want to assume homogeneity,

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#### What have we learned?

- With multiple treatment times, traditional DID assumes homogeneity
- 2 by 2 comparisons are well defined, but not all are useful
  - Comparison group matters
  - Time of comparison matters
- With multiple treatment times, it is important to assess heterogeneity
- If we suspect heterogeneity or do not want to assume homogeneity, use hdidregress and xthdidregress

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#### Heterogeneous treatment effects approaches

- Solution 1: Callaway and Sant'Anna (2021)
  - Use valid comparison groups
  - Split the problem into 2 by 2 comparisons
  - Compute ATET(g, t), where g is the cohort and t is the time
- Solution 2: Wooldridge (2021)
  - (Do not blame the messenger) Include heterogeneity in your regression
  - Add the adequate interactions with cohort and time
  - Compute ATET(g, t), where g is the cohort and t is the time
  - Computing ATET(g) or ATET(t) is also possible
- Other solutions exist. Good surveys are Roth et al. (2022) and de Chaisemartin and D'Haultfoeuille (forthcoming)

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#### Framework I

$$Y_{it} = Y_{it}(0) + \sum_{g=2}^{T} [Y_{it}(g) - Y_{it}(0)] G_{ig}$$

- Y<sub>it</sub> observed outcome
- $Y_{it}(0)$  potential outcome of not being treated
- Gig is an indicator for treatment group
- ullet g is the time at which a group of individuals is treated (cohort)
- $Y_{it}(g)$  potential outcome for cohort g



#### Framework II

- Treatment is staggered
- Parallel trends
- No anticipation
- Overlap

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## Callaway and Sant'Anna

- Regression adjustment (RA)
- Inverse-probability weighting (IPW)
- Augmented inverse-probability weighting (AIPW)

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#### **RA**

$$ATET(g,t) = E\left\{\frac{G_g}{E\left(G_g\right)}\left[Y_t - Y_{g-1} - m_{gt}\left(X\right)\right]\right\}$$

- $m_{gt}(X) = E(Y_t Y_{g-1}|X, C = 1)$
- C=1 is the never treated group  $(G_g=\infty)$



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#### **RA**

$$ATET(g,t) = E\left\{\frac{G_g}{E(G_g)}\left[Y_t - Y_{g-1} - m_{gt}(X)\right]\right\}$$

- ATET(g, t) is calculated using two groups: g and C = 1, never treated
- Outcomes are computed for two points in time



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#### **RA**

$$ATET(g,t) = E\left\{\frac{G_g}{E(G_g)}\left[Y_t - Y_{g-1} - m_{gt}(X)\right]\right\}$$

- ATET(g, t) is calculated using two groups: g and C = 1, never treated
- Outcomes are computed for two points in time
- 2 by 2 idea
- This is done for all g and all t
- We could have other 2 by 2 comparisons, i.e, using the not yet treated
- Identification assumptions are the same but need to hold for each 2 by 2



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# Heuristically

- keep if time is t or g-1
- 2 keep if cohort is g or cohort is C=1
- **3** generate  $Y_t Y_{g-1} \equiv \Delta Y$
- lacktriangledown regress  $\Delta Y$  on X for C=1 and predict,  $\widehat{m}_{gt}(X)$
- **5** generate  $\Delta Y \widehat{m}_{gt}(X) = \widehat{TE}$
- **6** summarize  $\widehat{TE}$  if cohort is g
  - This is done for each g and t
  - Doing it for all is a GMM problem, Callaway and Sant'Anna use influence functions.

$$ATET(g,t) = E\left\{ \left( \frac{G_g}{E(G_g)} - \frac{\frac{p_g(X)}{1 - p_g(X)}}{E\left[\frac{p_g(X)}{1 - p_g(X)}\right]} \right) [Y_t - Y_{g-1}] \right\}$$

- $p_g(X) = P(G_g = 1|X, G_g + C = 1)$ , i.e., conditional on the sample we keep
- Steps are similar to before with the additional computation of  $\widehat{p}_g(X)$  and the quotient  $\frac{\widehat{p}_g(X)}{\widehat{E}\left[\frac{\widehat{p}_g(X)}{\widehat{1-\widehat{p}_c}(X)}\right]}$



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### **AIPW**

$$ATET(g,t) = E\left\{ \left( \frac{G_g}{E\left(G_g\right)} - \frac{\frac{p_g(X_1)}{1 - p_g(X_1)}}{E\left[\frac{p_g(X_1)}{1 - p_g(X_1)}\right]} \right) \left[ Y_t - Y_{g-1} - m_{gt}\left(X_2\right) \right] \right\}$$

- Notice  $m_{gt}(X_2)$ . Emphasizes we could have different covariates
- AIPW is doubly robust. You may incorrectly specify at least one of  $m_{gt}(X_2)$  or  $p_g(X_1)$  and still recover ATET(g,t)



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$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig}\alpha_g + \sum_{s=q}^{T} f_s\alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it}G_{ig}f_s\tau_{gs}$$

- ullet q is the first treatment time and  $q \dots T$  the post period
- $f_s$  is 1 if the time period is s and 0 otherwise
- ullet We have group and time effects  $lpha_{m{g}}$  and  $lpha_{m{s}}$

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$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig}\alpha_g + \sum_{s=q}^{T} f_s\alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it}G_{ig}f_s\tau_{gs}$$

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- Heterogeneity is captured by interacting group and time effects
- $\tau_{gs} \equiv ATET(g, t)$

$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig}\alpha_g + \sum_{s=q}^{T} f_s\alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it}G_{ig}f_s\tau_{gs}$$

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- $\tau_{gs} \equiv ATET(g,t)$
- We use all our data and do not partition them
- If I have covariates, they enter fully interacted

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$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig}\alpha_g + \sum_{s=q}^{T} f_s\alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it}G_{ig}f_s\tau_{gs}$$

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- Heterogeneity is captured by interacting group and time effects
- $\tau_{gs} \equiv ATET(g,t)$
- We use all our data and do not partition them
- If I have covariates, they enter fully interacted
- Extended two-way fixed effects

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### Let's see it work

. webuse akc, clear

(Fictional dog breed and AKC registration data)

. describe

Contains data from https://www.stata-press.com/data/r18/akc.dta

Observations: 1,410 Fictional dog breed and AKC registration data

Variables: 5 1 Feb 2023 14:23

Variable name	Storage type	Display format	Value label	Variable label
year	int	%10.0g		Year
breed	int	%34.0g	Breed	Dog breed
movie	byte	%9.0g		Was a movie protagonist
best	byte	%9.0g		Won best in show in past 10 years
registered	int	%9.0g		Number of AKC registrations

Sorted by: breed

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### Let's see it work

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registered	int	%9.0g		Number of AKC registrations

Sorted by: breed

• Out of the 113 contests, the Terrier group has won 47 times

## Staggered treatment

. tabulate year movie

	Was a mov protagoni		
Year	0	1	Total
2031	141	0	141
2032	141	0	141
2033	141	0	141
2034	137	4	141
2035	137	4	141
2036	134	7	141
2037	119	22	141
2038	119	22	141
2039	119	22	141
2040	119	22	141
Total	1,307	103	1,410

### Specification: Panel/Longitudinal

xthdidregress estimator (registered best) (movie), group(breed)

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## Specification: Panel/Longitudinal

```
xthdidregress estimator (registered best) (movie), group(breed)
```

- You need to xtset with panel ID and time variable
- estimator is one of:
  - ra
  - twfe
  - ipw
  - aipw

### Output I

```
. xtset breed year
. xthdidregress ra (registered best) (movie), group(breed)
note: variable _did_cohort, containing cohort indicators formed by treatment variable
     movie and group variable breed, was added to the dataset.
Computing ATET for each cohort and time:
Cohort 2034 (9): ..... done
Cohort 2036 (9): ..... done
Cohort 2037 (9): ..... done
Treatment and time information
Time variable: vear
Time interval: 2031 to 2040
              _did_cohort = 0
Control:
Treatment:
              _did_cohort > 0
                   _did_cohort
Number of cohorts
```

Number of obs	
Never treated	1190
2034	40
2036	30
2037	150

### Output II

. xthdidregress ra (registered best) (movie), group(breed)
 (output omitted)

Heterogeneous-treatment-effects regression Number of obs = 1,410 Number of panels = 141

Estimator: Regression adjustment

Panel variable: breed

Treatment level: breed

Control group: Never treated

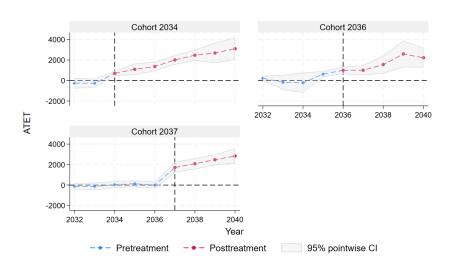
(Std. err. adjusted for 141 clusters in breed)

			<b>(</b>	:			,
Cohort	;	ATET	Robust std. err.	z	P> z	[95% conf.	interval]
2034							
	year						
	2032	-254.8927	266.1024	-0.96	0.338	-776.4439	266.6584
	2033	-257.5329	217.9389	-1.18	0.237	-684.6852	169.6194
	2034	701.1318	127.0935	5.52	0.000	452.0331	950.2304
	2035	1099.044	282.0704	3.90	0.000	546.196	1651.892
	2036	1367.632	225.8702	6.05	0.000	924.9343	1810.329
	2037	2008.294	237.2396	8.47	0.000	1543.313	2473.275
	2038	2472.624	278.2949	8.88	0.000	1927.176	3018.072
	2039	2689.615	504.3324	5.33	0.000	1701.142	3678.088
	2040	3110.97	568.916	5.47	0.000	1995.915	4226.025
(out	nut omit	tod)					

(output omitted)

Note: ATET computed using covariates.

### Graphical representation: estat atetplot



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### How to interpret my results

- I might want an average over all the ATET(g, t)
- I might want to know the effect of treatment within each group
- I might want to know the effect of treatment within a particular year
- I might want to see how the effect evolves with the duration of treatment

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### Overall

. estat aggregation, overall Overall ATET

Number of obs = 1,410

(Std. err. adjusted for 141 clusters in breed)

registered	ATET	Robust std. err.	z	P> z	[95% conf.	interval]
movie (1 vs 0)	2093.318	122.5752	17.08	0.000	1853.075	2333.561

### Cohort Tabular

. estat aggregation, cohort graph  $\operatorname{sci}$ 

ATET over cohort

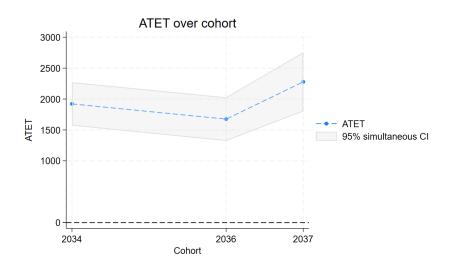
Number of obs = 1,410

Replications = 999 (Std. err. adjusted for 141 clusters in breed)

Cohort	Observed ATET	Bootstrap std. err.	Simultaneous [95% conf. interval]
2034	1921.33	126.9843	1570.576 2272.084
2036	1675.093	127.749	1322.227 2027.959
2037	2278.136	173.1852	1799.767 2756.504

Note: Simultaneous confidence intervals provide inference across all aggregations simultaneously.

# Cohort Graphical



### Cohort list

. estat aggregation, cohort(2036 2034)

ATET over cohort Number of obs = 1,410

(Std. err. adjusted for 141 clusters in breed)

Cohort	ATET	Robust std. err.	z	P> z	[95% conf.	interval]
2034	1921.33	187.2787	10.26	0.000	1554.271	2288.389
2036	1675.093	130.4929	12.84		1419.332	1930.855

#### Time Tabular

. estat aggregation, time graph sci

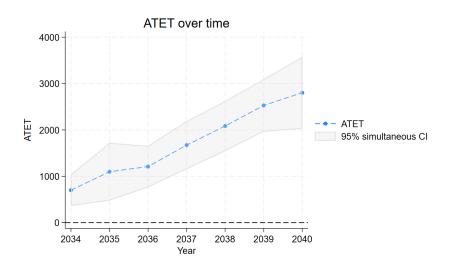
ATET over time Number of obs = 1,410 Replications = 999

(Std. err. adjusted for 141 clusters in breed)

Time	Observed ATET	Bootstrap std. err.	Simultaneous [95% conf. interval]
2034	701.1318	135.4942	360.2741 1041.989
2035	1099.044	247.3894	476.6955 1721.392
2036	1209.68	177.7654	762.4823 1656.878
2037	1672.655	206.0035	1154.42 2190.891
2038	2084.658	214.6857	1544.581 2624.735
2039	2528.847	225.004	1962.813 3094.882
2040	2802.171	308.5624	2025.932 3578.41

Note: Simultaneous confidence intervals provide inference across all aggregations simultaneously.

# Time Graphical



#### **Duration Tabular**

. estat aggregation, dynamic graph Duration of exposure ATET

Number of obs = 1,410 (Std. err. adjusted for 141 clusters in breed)

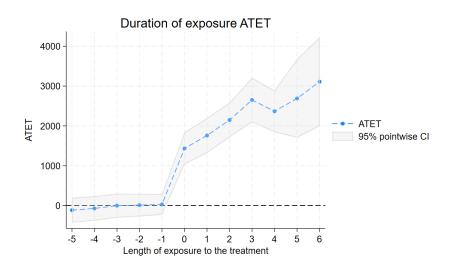
Exposure	ATET	Robust std. err.	z	P> z	[95% conf.	interval]
-5	-114.582	160.0972	-0.72	0.474	-428.3668	199.2028
-4	-70.65034	156.3185	-0.45	0.651	-377.029	235.7283
-3	9117242	153.0999	-0.01	0.995	-300.982	299.1585
-2	12.79653	144.8216	0.09	0.930	-271.0486	296.6417
-1	30.71473	132.8508	0.23	0.817	-229.668	291.0975
0	1434.409	206.3277	6.95	0.000	1030.014	1838.804
1	1759.461	224.0229	7.85	0.000	1320.385	2198.538
2	2147.486	221.903	9.68	0.000	1712.564	2582.408
3	2651.452	284.8928	9.31	0.000	2093.073	3209.832
4	2366.805	267.4253	8.85	0.000	1842.661	2890.949
5	2689.615	504.3324	5.33	0.000	1701.142	3678.088
6	3110.97	568.916	5.47	0.000	1995.915	4226.025

Note: Exposure is the number of periods since the first treatment time.

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### **Duration Graphical**



#### Costs

$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig} \alpha_g + \sum_{s=q}^{T} f_s \alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it} G_{ig} f_s \tau_{gs}$$

- Number of parameters increases with t, g, and covariates
- This is true for Callaway and Sant'Anna for each 2 by 2 subset



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#### Costs

$$Y_{it} = \eta + \sum_{g=q}^{T} G_{ig}\alpha_g + \sum_{s=q}^{T} f_s\alpha_s + \sum_{g=q}^{T} \sum_{s=g}^{T} D_{it}G_{ig}f_s\tau_{gs}$$

- Number of parameters increases with t, g, and covariates
- This is true for Callaway and Sant'Anna for each 2 by 2 subset
- twfe gives us a chance to address this at estimation with hettype()



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### Cohort heterogeneity

```
. xthdidregress twfe (registered best) (movie), group(breed) hettype(cohort) (output omitted)

Computing ATETs using margins ...
(output omitted)

Heterogeneous-treatment-effects regression

Number of obs = 1,410

Number of panels = 141
```

Estimator: Two-way fixed effects

Panel variable: breed

Treatment level: breed Control group: Never treated

Heterogeneity: Cohort

(Std. err. adjusted for 141 clusters in breed)

Cohort	ATET	Robust std. err.	t	P> t	[95% conf.	interval]
2034	1662.492	108.002	15.39	0.000	1448.966	1876.017
2036	1978.645	54.21043	36.50	0.000	1871.468	2085.822
2037	2276.223	70.63244	32.23	0.000	2136.579	2415.867

Note: ATET computed using covariates.

### Time heterogeneity

```
. xthdidregress twfe (registered best) (movie), group(breed) hettype(time) (output omitted)
Computing ATETs using margins ...
```

Computing ATETs using margins ...

(output omitted)

Heterogeneous-treatment-effects regression Number of obs = 1,410 Number of panels = 141

Estimator: Two-way fixed effects

Panel variable: breed Treatment level: breed

Control group: Never treated

Heterogeneity: Time

(Std. err. adjusted for 141 clusters in breed)

Time	ATET	Robust std. err.	t	P> t	[95% conf.	interval]
year						
2034	368.7667	177.8305	2.07	0.040	17.18625	720.3472
2035	825.1479	269.4845	3.06	0.003	292.3625	1357.933
2036	1262.367	85.71962	14.73	0.000	1092.895	1431.839
2037	1692.904	165.318	10.24	0.000	1366.061	2019.746
2038	2110.763	162.5539	12.99	0.000	1789.386	2432.141
2039	2554.188	241.3463	10.58	0.000	2077.033	3031.342
2040	2829.94	243.2751	11.63	0.000	2348.972	3310.908

Note: ATET computed using covariates.

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## Parting thoughts

- Continued interest and development in causal inference/treatment effects
- Heterogeneous DID
- Estimation and postestimation tools displayed in tabular and graphical forms
- Different ways of thinking about heterogeneity