

Estimating effects from extended regression models

David M. Drukker

Executive Director of Econometrics
Stata

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Extended regression models

Extended regression model (ERM) is a Stata term for a class of regression models

- The outcome can be continuous (linear), probit, ordered probit, or censored (tobit)
- Some of the covariates may be endogenous
 - The endogenous covariates may be continuous, probit, or ordered probit
- Endogenous sample-selection may be modeled
- Exogenous or endogenous treatment assignment may be modeled
- The new-in-Stata-15 commands `eregress`, `eprobit`, `eoprobit`, and `eintreg` fit ERMs

Extended regression models

- Some of the covariates may be endogenous
 - The endogenous covariates may be continuous, binary, or ordinal
 - Polynomial terms and interaction terms constructed from the endogenous covariates are allowed
 - Interactions among the endogenous covariates and interactions between the endogenous covariates and the exogenous covariates are allowed

Outline

- I cannot do justice to ERMs in this short talk
- I discuss examples in which I
 - define some of the terms that I have already used
 - illustrate some command syntax
 - illustrate how to estimate some effects using postestimation commands

- Fictional data on wellness program from large company

```
. use wprogram
```

```
. describe
```

Contains data from wprogram.dta

```
obs:      3,000
```

```
vars:      6
```

```
size:     72,000
```

```
28 Jul 2017 07:13
```

variable name	storage type	display format	value label	variable label
wchange	float	%9.0g	changel	Weight change level
age	float	%9.0g		Years over 50
over	float	%9.0g		Overweight (tens of pounds)
phealth	float	%9.0g		Prior health score
prog	float	%9.0g	yesno	Participate in wellness program
wtprog	float	%9.0g	yesno	Offered work time to participate in program

Sorted by:

- Three levels of wchange

```
. tabulate wchange prog
```

Weight change level	Participate in wellness program		Total
	No	Yes	
Loss	239	909	1,148
No change	468	605	1,073
Gain	593	186	779
Total	1,300	1,700	3,000

- Data are observational
- Table does not account for how observed covariates and/or unobserved errors that affect program participation also affect the outcome variable

- I want a model that
 - allows observed covariates to affect both `wchange` and assignment to `prog`
 - allows the errors that affect assignment to `prog` to be correlated with the errors that affect `wchange`
 - I suspect that unobservables that increase program participation are negatively correlated with unobservables that affect weight gain
- In other words, I want allow `prog` to be endogenous

If prog is endogenous, I must model the dependence.

Consider

$$wchange = \begin{cases} \text{"Loss"} & \text{if } \beta_1 \text{prog} + \mathbf{x}\boldsymbol{\beta} + \epsilon \leq \text{cut1} \\ \text{"No change"} & \text{if } \text{cut1} < \beta_1 \text{prog} + \mathbf{x}\boldsymbol{\beta} + \epsilon \leq \text{cut2} \\ \text{"Gain"} & \text{if } \text{cut2} < \beta_1 \text{prog} + \mathbf{x}\boldsymbol{\beta} + \epsilon \end{cases}$$

$$\text{prog} = (\mathbf{x}\boldsymbol{\gamma} + \gamma_1 \text{wtime} + \eta > 0)$$

ϵ and η are correlated and joint normal

$$\mathbf{x}\boldsymbol{\beta} = \beta_2 \text{age} + \beta_3 \text{over} + \beta_4 \text{phealth}$$

$$\mathbf{x}\boldsymbol{\gamma} = \gamma_2 \text{age} + \gamma_3 \text{over} + \gamma_4 \text{phealth}$$

- wtime is an instrumental variable
 - It is included in the model for treatment
 - It is excluded from the model for the potential outcomes of wchange

$$wchange = \begin{cases} \text{"Loss"} & \text{if } \beta_1 prog + \mathbf{x}\boldsymbol{\beta} + \epsilon \leq cut1 \\ \text{"No change"} & \text{if } cut1 < \beta_1 prog + \mathbf{x}\boldsymbol{\beta} + \epsilon \leq cut2 \\ \text{"Gain"} & \text{if } cut2 < \beta_1 prog + \mathbf{x}\boldsymbol{\beta} + \epsilon \end{cases}$$

$$prog = (\mathbf{x}\boldsymbol{\gamma} + \gamma_1 wtime + \eta > 0)$$

ϵ and η are correlated and joint normal

$$\mathbf{x}\boldsymbol{\beta} = \beta_2 age + \beta_3 over + \beta_4 phealth$$

$$\mathbf{x}\boldsymbol{\gamma} = \gamma_2 age + \gamma_3 over + \gamma_4 phealth$$

Fit by: `eoprobit wchange age over phealth ,`
`endog(prog = age over phealth wtime, probit)`

```

. eoprobit wchange age over phealth , ///
> endog(prog = age over phealth wtprog, probit) ///
> vsquish nolog
Extended ordered probit regression      Number of obs      =      3,000
                                         Wald chi2(4)        =      409.97
Log likelihood = -4401.0952             Prob > chi2         =      0.0000

```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
wchange						
age	.2155906	.0705048	3.06	0.002	.0774037	.3537776
over	.4349946	.0387185	11.23	0.000	.3591078	.5108814
phealth	-.4933361	.0411866	-11.98	0.000	-.5740603	-.412612
prog						
Yes	-.3624996	.1031408	-3.51	0.000	-.5646519	-.1603473
prog						
age	-.9341234	.0840002	-11.12	0.000	-1.098761	-.7694861
over	-1.058621	.0514252	-20.59	0.000	-1.159412	-.9578294
phealth	.9001108	.0504804	17.83	0.000	.801171	.9990507
wtprog	1.631615	.0780834	20.90	0.000	1.478574	1.784656
_cons	.0090842	.0535434	0.17	0.865	-.095859	.1140274
/wchange						
cut1	-.5897304	.0781626			-.7429264	-.4365345
cut2	.5029323	.068292			.3690825	.6367821
corr(e.prog, e.wchange)	-.3478179	.0604422	-5.75	0.000	-.4603282	-.2243109

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corr(e.prog, e.wchange)	-.3478179	.0604422	-5.75	0.000	-.4603282	-.2243109

- The coefficient on wtprog and its standard error give the impression that the instrument is relevant

cut2	.5099323	.068292				
corr(e.prog, e.wchange)	-.3478179	.0604422	-5.75	0.000	-.4603282	-.2243109

- The nonzero correlation between e.prog and e.wchange indicates that prog is endogenous
- Those who are more likely to participate are more likely to lose weight

```

. margins r.prog, ///
> predict(fix(prog) outlevel("Loss")) ///
> predict(fix(prog) outlevel("No change")) ///
> predict(fix(prog) outlevel("Gain")) ///
> contrast(nowald)

```

Contrasts of predictive margins

Model VCE : OIM

1._predict : Pr(wchange==Loss), predict(fix(prog) outlevel("Loss"))

2._predict : Pr(wchange==No change), predict(fix(prog) outlevel("No change"))

3._predict : Pr(wchange==Gain), predict(fix(prog) outlevel("Gain"))

	Delta-method			
	Contrast	Std. Err.	[95% Conf. Interval]	
prog@_predict				
(Yes vs No) 1	.1259899	.0356631	.0560914	.1958883
(Yes vs No) 2	-.0185024	.0055583	-.0293965	-.0076084
(Yes vs No) 3	-.1074874	.0306512	-.1675628	-.0474121

- When everyone joins the program instead of when no one participants in the program,
 - On average, the probability of “Loss” goes up by .13
 - On average, the probability of “No change” goes down by .02
 - On average, the probability of “Gain” goes down by .11

- `fix(prog)` gets us the effect of the program that is not contaminated by the selection effect/correlation between ϵ and η that increases the participation among people more likely to lose weight
- `predict(fix(prog))` tells margins to specify `fix(prog)` to predict when computing each predicted probability
- `fix(prog)` causes the value of `prog` not to affect ϵ , even though they are correlated
 - `fix(prog)` specifies that the part of ϵ that is correlated with y_2 be integrated out

- This type of prediction is sometimes called the structural prediction or an average structural function; see Blundell and Powell (2003), Blundell and Powell (2004), Wooldridge (2010), and Wooldridge (2014),
- The difference between the mean of the average of the structural predictions when $\text{prog}=1$ and the mean of the average of the structural predictions when $\text{prog}=0$ is an average treatment effect (Blundell and Powell (2003) and Wooldridge (2014))

Standard errors for population versus sample

- The delta-method standard errors reported by `margins` hold the covariates fixed at their sample values
 - The delta-method standard errors are for a sample-average treatment effect instead of a population-averaged treatment effect
 - The sample-averaged treatment effect is for those individuals that showed up in that run of the treatment
 - The population-averaged treatment effect is for a random draw of individuals from the population
- To get standard errors for the population-average treatment effect, specify `vce(robust)` to the estimation command and specify `vce(unconditional)` to `margins`


```

. quietly eoprobit wchange age over phealth ,          ///
>     endog(prog = age over phealth wtprog, probit) ///
>     vce(robust)

. margins r.prog,          ///
>     predict(fix(prog) outlevel("Loss"))          ///
>     predict(fix(prog) outlevel("No change"))     ///
>     predict(fix(prog) outlevel("Gain"))          ///
>     contrast(nowald) vce(unconditional)

```

Contrasts of predictive margins

```

1._predict   : Pr(wchange==Loss), predict(fix(prog) outlevel("Loss"))
2._predict   : Pr(wchange==No change), predict(fix(prog) outlevel("No
change"))
3._predict   : Pr(wchange==Gain), predict(fix(prog) outlevel("Gain"))

```

	Unconditional		
	Contrast	Std. Err.	[95% Conf. Interval]
prog@_predict			
(Yes vs No) 1	.1259899	.0349061	.0575753 .1944045
(Yes vs No) 2	-.0185024	.0054389	-.0291624 -.0078424
(Yes vs No) 3	-.1074874	.0300866	-.1664561 -.0485188

```

. matrix b = r(b)

```

More about ERM commands

- The commands `eregress`, `eprobit`, and `eintreg` fit ERMs handle continuous-and-unbounded, binary, and censored/corner outcomes
- Look at

<http://www.stata.com/manuals/erm.pdf>

for more examples and a wealth of details

- Blundell, R. W., and J. L. Powell. 2003. Endogeneity in nonparametric and semiparametric regression models. In *Advances in Economics and Econometrics: Theory and Applications, Eighth World Congress*, ed. M. Dewatripont, L. P. Hansen, and S. J. Turnovsky, vol. 2, 312–357. Cambridge: Cambridge University Press.
- . 2004. Endogeneity in semiparametric binary response models. *Review of Economic Studies* 71: 655–679.
- Wooldridge, J. M. 2010. *Econometric Analysis of Cross Section and Panel Data*. 2nd ed. Cambridge, Massachusetts: MIT Press.
- . 2014. Quasi-maximum likelihood estimation and testing for nonlinear models with endogenous explanatory variables. *Journal of Econometrics* 182: 226–234.