# Jackknife inference for multiway clustering and CSDID in Stata: twowayjack and csdidjack

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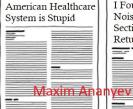
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### TYPES OF ECON PAPER









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We Spent Years in Archives of Genoese Republic and Wrote a Paper about Why Corruption is Bad Do People Respond to Incentives? Evidence from Swedish Admin Data Solving Covid-19 with Upper Hemi-Continuity

#### Overview

#### This talk will cover:

- Overview of two new Stata packages for jackknife clustering
- csdidjack
  - Available here Liu (2025)
  - Based on the paper MacKinnon, Nielsen, Webb, and Karim (2025)
  - Jackknife clustering for Callaway and Sant'Anna (2021)
- twowayjack
  - Available here Webb (2025)
  - based on the paper MacKinnon, Nielsen, and Webb (2024)
  - two-way cluster jackknife

### Staggered Adoption - $6 \times 3$ Rollout Matrix

- Setup: 6 regions, 3 time periods
- Each region is either treated or not
- Treatment timing is staggered:

### Estimands from 6-Region Rollout

- Follow the setup above
- 6 regions: A, B, C, D, E, F
- Treatment cohorts:
  - Group I: regions A, D (treated at t = 2)
  - Group II: regions B, E (treated at t = 3)
  - Group III: regions C, F (never treated)
- Define overall ATT:

$$ATT = \frac{1}{3}(ATT(I,2) + ATT(I,3) + ATT(II,3))$$
 (2)

### ATT Formulas and CSDID Estimator

• ATT(g, t) defined via difference-in-differences:

$$\begin{split} &\mathsf{ATT}(\mathsf{I},2) = (\mathsf{E}[Y_{\mathsf{I},2}] - \mathsf{E}[Y_{\mathsf{I},1}]) - (\mathsf{E}[Y_{\mathsf{III},2}] - \mathsf{E}[Y_{\mathsf{III},1}]), \\ &\mathsf{ATT}(\mathsf{I},3) = (\mathsf{E}[Y_{\mathsf{I},3}] - \mathsf{E}[Y_{\mathsf{I},1}]) - (\mathsf{E}[Y_{\mathsf{III},3}] - \mathsf{E}[Y_{\mathsf{III},1}]), \\ &\mathsf{ATT}(\mathsf{II},3) = (\mathsf{E}[Y_{\mathsf{II},3}] - \mathsf{E}[Y_{\mathsf{II},2}]) - (\mathsf{E}[Y_{\mathsf{III},3}] - \mathsf{E}[Y_{\mathsf{III},2}]). \end{split}$$

CSDID with 'simple' weights estimates:

$$\widehat{\mathsf{ATT}} = \frac{\widehat{\mathsf{ATT}}(\mathsf{I},2) + \widehat{\mathsf{ATT}}(\mathsf{I},3) + \widehat{\mathsf{ATT}}(\mathsf{II},3)}{3}.$$
 (3)

### Clustering in CSDID

- Default SEs in Callaway and Sant'Anna (2021) use influence functions
- Expressions are long (see Theorem 2), but derivation is not our focus
- Key result:

$$\sqrt{n}(\widehat{\mathsf{ATT}}_{t\geq (g-\delta)}^{dr,nev} - \mathsf{ATT}_{t\geq (g-\delta)}) \stackrel{d}{\longrightarrow} \mathsf{N}(\mathsf{0},\Sigma), \tag{4}$$

- ullet Where  $\Sigma = \mathrm{E}[\Psi(oldsymbol{W}_i)\Psi(oldsymbol{W}_i)']$  is from doubly robust estimator
- Normal approximation is used to compute P-values and Cls
- Callaway and Sant'Anna (2021, Remark 13): inference requires many clusters

### Problems with Clustering in CSDID

There are three main issues with clustering, by region, in CSDID on account of estimating the ATT(g,t) terms first

- Observations from the same region can appear in multiple separate ATT(g, t) estimates, such as region I in ATT(I, 2) and ATT(I, 3)
- Untreated observations from the same region and period can appear in multiple separate  $\mathsf{ATT}(g,t)$  estimates, such as region III in  $\mathsf{ATT}(\mathsf{I},3)$  and  $\mathsf{ATT}(\mathsf{II},3)$
- When not yet treated control units are specified, treated observations from the same region and period can be used twice as both a pre-period for a treated region, and a post-period for an untreated region

### Notation for the Cluster Jackknife

- ATT: full-sample CSDID estimate
- $\widehat{\mathsf{ATT}}^{(h)}$ : leave-one-cluster-out estimate
- H: total number of clusters
- CV<sub>3</sub> generalizes HC<sub>3</sub> from MacKinnon and White (1985)
- Attractive feature:
  - No need for  $\widehat{\mathrm{Var}}[\widehat{\mathsf{ATT}}(g,t)]$
- Standard error of ATT remains well-defined

The jackknife has received a lot of attention for clustering recently, see MacKinnon et al. (2023a,b); Hansen (2025a,b); MacKinnon et al. (2025); Hounyo and Lin (2025) among others.

### Cluster Jackknife for CSDID

- Alternative to Callaway and Sant'Anna (2021) standard errors
- We use the cluster jackknife for inference on  $\widehat{\mathsf{ATT}}$
- Jackknife omits one cluster h at a time:

$$\widehat{\mathsf{ATT}}^{(h)}$$
 omits cluster h

Resulting SE is:

$$CV_3(ATT) = \frac{H-1}{H} \sum_{h=1}^{H} \left( \widehat{ATT}^{(h)} - \widehat{ATT} \right)^2$$
 (5)

### Monte Carlo Design

- Simulations based on CPS MORG data, 1979–1999
- Outcome: log of weekly earnings for women
- Sample: 547,818 observations; earnings  $\geq$  \$20
- Placebo laws design inspired by Bertrand, Duflo, and Mullainathan (2004)
  - State-level staggered adoption in 2 cohorts
  - Early cohort (*J* states): treated in year 4
  - Late cohort (L states): treated in year 6
  - J = L; total treated states = J + L
- Treatment is absorptive and state-wide
- Each replication samples H states and 8 years
- Recent simulations in Mizushima and Powell (2025)
  - They use state-level unemployment rates
  - We use individual-level earnings
- Inference procedures: csdid, wboot, csdidjack

# Monte Carlo Design

Table: Values of H and J = L studied in our experiments

	H = 8	H = 16	H = 24	H = 32
J=L=1	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>
J = L = 2	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
J = L = 3	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$
J = L = 4		$\checkmark$	$\checkmark$	$\checkmark$
J = L = 6			$\checkmark$	$\checkmark$
J = L = 8			$\checkmark$	$\checkmark$
J = L = 10				$\checkmark$
J = L = 12				✓

# Rejection Frequencies: RIF (csdid)

	H = 8	H = 16	H = 24	H = 32
J=L=1	0.3046	0.3333	0.3558	0.3800
J=L=1 J=L=2	0.3040	0.3333	0.3330	0.3800
J=L=3	0.2146	0.1245	0.1371	0.1388
J = L = 4		0.1132	0.1204	0.1187
J = L = 6			0.0829	0.0954
J = L = 8			0.0950	0.0850
J = L = 10				0.0779
J = L = 12				0.0925

Notes: Nominal level is 5%.

# Rejection Frequencies: Multiplier Bootstrap (csdid)

	H = 8	<i>H</i> = 16	H = 24	H = 32
J=L=1	0.3079	0.3458	0.3725	0.3950
J = L = 2	0.1808	0.1887	0.1762	0.2004
J = L = 3	0.2125	0.1233	0.1408	0.1388
J = L = 4		0.1161	0.1200	0.1204
J = L = 6			0.0846	0.0967
J = L = 8			0.0929	0.0842
J = L = 10				0.0787
J = L = 12				0.0938

Notes: Nominal level is 5%.

# Rejection Frequencies: Jackknife (csdidjack)

	<i>H</i> = 8	H = 16	H = 24	H = 32
J=L=1	0.0938	0.1279	0.1450	0.1642
J = L = 2	0.0379	0.0763	0.0796	0.0929
J = L = 3	0.0533	0.0488	0.0600	0.0688
J = L = 4		0.0505	0.0621	0.0571
J = L = 6			0.0450	0.0571
J = L = 8			0.0425	0.0483
J = L = 10				0.0450
J = L = 12				0.0500

Notes: Nominal level is 5%.

### Minimum Wage and Teen Employment

- Adapted from Callaway and Sant'Anna (2021)
- County-level QWI data (2001–2007), 29 states
- Outcome: log of teen employment (lemp)
- Covariates: demographics + economics
  - Region dummies, % white, % HS diploma, poverty rate
  - County pop. and median income (quadratics)
- Estimation via csdid, calendar aggregation

#### Table: Effect of minimum wage on teen employment

Method	ATT	Std. error	P value	CI lower	CI upper
csdid	-0.0309	0.0076	0.000	-0.0457	-0.0160
csdidjack	-0.0309	0.0166	0.073	-0.0649	0.0031

### Software Packages

- Open-source implementations of CV<sub>3</sub> jackknife inference
- Available for both Stata and R users

### Stata: csdidjack (post-estimation for csdid)

- Supports agg(simple), agg(group), and agg(calendar)
- Install via:

```
net install csdidjack,
from("https://raw.githubusercontent.com/liu-yunhan/csdidjac
replace
```

- After estimating a model with csdid (Rios-Avila, Callaway, and Sant'Anna, 2021), run: csdidjack
- Returns CV<sub>3</sub> SEs, t-stats, P values, and Cls
- Docs: help csdidjack
- Source code: https://github.com/liu-yunhan/csdidjack

### Two-Way Cluster Jackknife

- Multiway clustering is very popular, introduced by Cameron et al. (2011) and Thompson (2011)
- Shown to be over-sized with few clusters in either dimension in MacKinnon et al. (2021)
- A (sort of) two-way version of the wild cluster bootstrap is proposed in that paper
- MacKinnon et al. (2024) proposes a two-way jackknife
- The paper also proposes a max(se) alternative to eigen-value corrections
- The paper describes twowayjack which will be the focus here
- That package basically makes three calls to summclust described in MacKinnon et al. (2023c)

# Two-Way Cluster-Robust Variance

- ullet OLS estimator:  $\hat{oldsymbol{eta}} = (oldsymbol{X}^{ op}oldsymbol{X})^{-1}oldsymbol{X}^{ op}oldsymbol{y}$
- Residuals:  $\hat{\boldsymbol{u}}$ , with cluster slices  $\hat{\boldsymbol{u}}_g$ ,  $\hat{\boldsymbol{u}}_h$ ,  $\hat{\boldsymbol{u}}_{gh}$
- From sandwich formula:

$$\operatorname{Var}(\hat{\boldsymbol{\beta}}) = (\boldsymbol{X}^{\top}\boldsymbol{X})^{-1}\boldsymbol{\Sigma}(\boldsymbol{X}^{\top}\boldsymbol{X})^{-1} = \boldsymbol{V}_{G} + \boldsymbol{V}_{H} - \boldsymbol{V}_{I}$$
 (6)

$$\mathbf{V}_{G} = (\mathbf{X}^{\top} \mathbf{X})^{-1} \left( \sum_{\sigma} \mathbf{\Sigma}_{\sigma} \right) (\mathbf{X}^{\top} \mathbf{X})^{-1}$$
 (7)

$$oldsymbol{V}_G = (oldsymbol{X}^ op oldsymbol{X})^{-1} igg( \sum_{g=1}^G oldsymbol{\Sigma}_g igg) (oldsymbol{X}^ op oldsymbol{X})^{-1}$$

$$oldsymbol{V}_H = (oldsymbol{X}^ op oldsymbol{X})^{-1} igg( \sum_{t=1}^H oldsymbol{\Sigma}_h igg) (oldsymbol{X}^ op oldsymbol{X})^{-1}$$

$$oldsymbol{V}_I = (oldsymbol{X}^ op oldsymbol{X})^{-1} igg( \sum_{g=1}^G \sum_{h=1}^H oldsymbol{\Sigma}_{gh} igg) (oldsymbol{X}^ op oldsymbol{X})^{-1}$$

(8)

(9)

### Two-Way Cluster-Jackknife CRVEs

- Standard CRVEs (e.g.,  $\hat{V}_G$ ) follow CV<sub>1</sub> form
- Jackknife estimators improve performance in small samples
- For  $J \in \{G, H, I\}$ , define leave-one-out estimator:

$$\hat{\boldsymbol{\beta}}^{(j)} = (\boldsymbol{X}^{\top} \boldsymbol{X} - \boldsymbol{X}_{j}^{\top} \boldsymbol{X}_{j})^{-1} (\boldsymbol{X}^{\top} \boldsymbol{y} - \boldsymbol{X}_{j}^{\top} \boldsymbol{y}_{j})$$
(10)

Cluster-jackknife variance for dimension J:

$$\hat{\mathbf{V}}_{J}^{\text{JK}} = \frac{J-1}{J} \sum_{j=1}^{J} (\hat{\beta}^{(j)} - \hat{\beta}) (\hat{\beta}^{(j)} - \hat{\beta})^{\top}$$
 (11)

Three-term jackknife CRVE:

$$\hat{\mathbf{V}}_{3}^{(3)} = \hat{\mathbf{V}}_{G}^{\mathrm{JK}} + \hat{\mathbf{V}}_{H}^{\mathrm{JK}} - \hat{\mathbf{V}}_{I}^{\mathrm{JK}}$$
(12)

• Related CRVEs:  $CV_3^{(2)}$ ,  $CV_3^{(3)}$ ,  $CV_3^{(max)}$ 

### Modified Wald Statistic: $W_{\min}$

- Problem:  $\hat{\boldsymbol{V}}_{1}^{(3)}$  may not be positive definite
- We propose:
  - Compute 3 Wald statistics: W<sub>3</sub>, W<sub>G</sub>, W<sub>H</sub>
  - Use smallest valid one:  $W_{\min}$

$$W_{3} = (R\hat{\beta} - \mathbf{r})^{\top} (R\hat{\mathbf{V}}_{1}^{(3)}R^{\top})^{-1} (R\hat{\beta} - \mathbf{r})$$

$$W_{G} = (R\hat{\beta} - \mathbf{r})^{\top} (R\hat{\mathbf{V}}_{G}R^{\top})^{-1} (R\hat{\beta} - \mathbf{r})$$

$$W_{H} = (R\hat{\beta} - \mathbf{r})^{\top} (R\hat{\mathbf{V}}_{H}R^{\top})^{-1} (R\hat{\beta} - \mathbf{r})$$
(13)

 $W_{\min} = \min \{ \max(W_3, 0), W_G, W_H \}$ 

(14)

# Tsetse Fly and African Development

- Alsan (2015) examines long-run effects of tsetse fly exposure
- Dependent variables: agricultural + technological outcomes
- Two-Way clustered inference using multiple CRVEs

Table: Selected P-values for Conventional and Jackknife CRVEs

Dependent Var.	β̂	HC <sub>1</sub>	CV <sub>(1)</sub>	$CV^{(G)}_{(1)}$	CV <sub>(3)</sub>	$CV_{(3)}^{(3)}$	CV <sub>(3)</sub>
Panel A: Conventional							
Large animals	-0.231	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
Intensive agriculture	-0.090	0.0080	0.0087	0.0020	0.0321	0.0003	0.0045
Plow use	-0.057	0.0096	0.0171	0.0149	0.1496	0.0715	0.0791
Panel B: Jackknife							
Large animals	-0.231	0.0000	0.0000	0.0000	0.0007	0.0000	0.0000
Intensive agriculture	-0.090	0.0092	0.0130	0.0044	0.0549	0.0027	0.0123
Plow use	-0.057	0.0124	0.0220	0.0207	0.2112	0.1365	0.1422

### Syntax: twowayjack Command

```
twowayjack depvar indepvar controls,
    cluster(var1 var2) [fevar(varlist) sample(cond)]
```

- depvar: dependent variable
- indepvar: main regressor of interest
- controls: other covariates (binary or continuous)
- cluster(varlist) (required): exactly two cluster vars
- fevar(varlist): fixed effects (like i.var)
  - Uses a generalized inverse (works with singular subsamples)
- sample(string): subset selection, e.g., sample(female==1)

#### More info:

http://qed.econ.queensu.ca/pub/faculty/mackinnon/twowayjack/

### Bibliography I

- Alsan, M. (2015). The effect of the tsetse fly on African development. American Economic Review 105, 382–410.
- Bertrand, M., E. Duflo, and S. Mullainathan (2004). How much should we trust differences-in-differences estimates? Quarterly Journal of Economics 119, 249–275.
- Callaway, B. and P. H. C. Sant'Anna (2021). Difference-in-differences with multiple time periods. <u>Journal of Econometrics</u> 225, 200–230.
- Cameron, A. C., J. B. Gelbach, and D. L. Miller (2011). Robust inference with multiway clustering. <u>Journal of Business & Economic Statistics</u> 29, 238–249.
- Hansen, B. E. (2025a). Jackknife standard errors for clustered regression. Working paper, University of Wisconsin.
- Hansen, B. E. (2025b). Standard errors for difference-in-difference regression. <u>Journal of Applied Econometrics</u> 40, 291–309.

### Bibliography II

- Hounyo, U. and J. Lin (2025). Jackknife variances for two-way clustering with serially correlated time effects. Working paper, SUNY Albany.
- Liu, Y. (2025). csdidjack: Cluster jackknife inference for callaway and sant'anna difference-in-differences (stata package). https://github.com/liu-yunhan/csdidjack. GitHub repository; Stata package.
- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2021). Wild bootstrap and asymptotic inference with multiway clustering. <u>Journal of Business</u> & Economic Statistics 39, 509–519.
- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2023a). Cluster-robust inference: A guide to empirical practice. <u>Journal of Econometrics</u> 232, 272–299.
- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2023b). Fast and reliable jackknife and bootstrap methods for cluster-robust inference. Journal of Applied Econometrics 38, 671–694.

### Bibliography III

- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2023c). Leverage, influence, and the jackknife in clustered regression models: Reliable inference using summclust. Stata Journal 23, 942–982.
- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2025). Cluster-robust jackknife and bootstrap inference for logistic regression models.

  <u>Econometric Reviews</u>. forthcoming.
- MacKinnon, J. G. and H. White (1985). Some heteroskedasticity consistent covariance matrix estimators with improved finite sample properties. Journal of Econometrics 29, 305–325.
- MacKinnon, J. G., M. Ø. Nielsen, and M. D. Webb (2024). Jackknife inference with two-way clustering. Technical report.
- MacKinnon, J. G., M. Ø. Nielsen, M. D. Webb, and S. Karim (2025). Improving inferences for callaway and sant'anna DiD using the cluster jackknife. Mimeo.

### Bibliography IV

- Mizushima, Y. and D. Powell (2025). Inference with modern difference-in-differences methods. Technical report, SSRN 5221387.
- Rios-Avila, F., B. Callaway, and P. H. C. Sant'Anna (2021). csdid: Difference-in-differences with multiple time periods in Stata. In <u>Stata</u> Conference, pp. 47.
- Thompson, S. B. (2011). Simple formulas for standard errors that cluster by both firm and time. <u>Journal of Financial Economics</u> 99, 1–10.
- Webb, M. D. (2025). twowayjack: Stata module for two-way cluster jackknife variance estimation.
  - https://github.com/mattdwebb/twowayjack. GitHub repository; Stata module.