Title

xtpcse — Linear regression with panel-corrected standard errors

Syntax Remarks and examples References Menu Stored results Also see Description Methods and formulas Options Acknowledgments

Syntax

xtpcse depvar [indepvars] [if] [in] [weight] [, options]

options	Description
Model	
<u>nocon</u> stant	suppress constant term
<u>c</u> orrelation(<u>i</u> ndependent)	use independent autocorrelation structure
<u>c</u> orrelation(<u>a</u> r1)	use AR1 autocorrelation structure
<u>c</u> orrelation(psar1)	use panel-specific AR1 autocorrelation structure
<u>rho</u> type(<i>calc</i>)	specify method to compute autocorrelation parameter; seldom used
np1	weight panel-specific autocorrelations by panel sizes
<u>het</u> only	assume panel-level heteroskedastic errors
<u>i</u> ndependent	assume independent errors across panels
by/if/in	
<u>ca</u> sewise	include only observations with complete cases
\underline{p} airwise	include all available observations with nonmissing pairs
SE	
nmk	normalize standard errors by $N-k$ instead of N
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
<u>d</u> etail	report list of gaps in time series
display_options	control column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
<u>coefl</u> egend	display legend instead of statistics

A panel variable and a time variable must be specified; use xtset; see [XT] xtset.

indepvars may contain factor variables; see [U] 11.4.3 Factor variables.

depvar and indepvars may contain time-series operators; see [U] 11.4.4 Time-series varlists.

by and statsby are allowed; see [U] 11.1.10 Prefix commands.

iweights and aweights are allowed; see [U] 11.1.6 weight.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Menu

Statistics > Longitudinal/panel data > Contemporaneous correlation > Regression with panel-corrected standard errors (PCSE)

Description

xtpcse calculates panel-corrected standard error (PCSE) estimates for linear cross-sectional timeseries models where the parameters are estimated by either OLS or Prais–Winsten regression. When computing the standard errors and the variance–covariance estimates, xtpcse assumes that the disturbances are, by default, heteroskedastic and contemporaneously correlated across panels.

See [XT] xtgls for the generalized least-squares estimator for these models.

Options

Model

noconstant; see [R] estimation options.

correlation(corr) specifies the form of assumed autocorrelation within panels.

correlation(independent), the default, specifies that there is no autocorrelation.

correlation(ar1) specifies that, within panels, there is first-order autocorrelation AR(1) and that the coefficient of the AR(1) process is common to all the panels.

correlation(psar1) specifies that, within panels, there is first-order autocorrelation and that the coefficient of the AR(1) process is specific to each panel. psar1 stands for panel-specific AR(1).

rhotype(*calc*) specifies the method to be used to calculate the autocorrelation parameter. Allowed strings for *calc* are

regress	regression using lags; the default
freg	regression using leads
<u>tsc</u> orr	time-series autocorrelation calculation
dw	Durbin-Watson calculation

All above methods are consistent and asymptotically equivalent; this is a rarely used option.

- np1 specifies that the panel-specific autocorrelations be weighted by T_i rather than by the default $T_i 1$ when estimating a common ρ for all panels, where T_i is the number of observations in panel *i*. This option has an effect only when panels are unbalanced and the correlation(ar1) option is specified.
- hetonly and independent specify alternative forms for the assumed covariance of the disturbances across the panels. If neither is specified, the disturbances are assumed to be heteroskedastic (each panel has its own variance) and contemporaneously correlated across the panels (each pair of panels has its own covariance). This is the standard PCSE model.

hetonly specifies that the disturbances are assumed to be panel-level heteroskedastic only with no contemporaneous correlation across panels.

independent specifies that the disturbances are assumed to be independent across panels; that is, there is one disturbance variance common to all observations.

by/if/in

casewise and pairwise specify how missing observations in unbalanced panels are to be treated when estimating the interpanel covariance matrix of the disturbances. The default is casewise selection.

casewise specifies that the entire covariance matrix be computed only on the observations (periods) that are available for all panels. If an observation has missing data, all observations of that period are excluded when estimating the covariance matrix of disturbances. Specifying casewise ensures that the estimated covariance matrix will be of full rank and will be positive definite.

pairwise specifies that, for each element in the covariance matrix, all available observations (periods) that are common to the two panels contributing to the covariance be used to compute the covariance.

The casewise and pairwise options have an effect only when the panels are unbalanced and neither hetonly nor independent is specified.

SE

nmk specifies that standard errors be normalized by N - k, where k is the number of parameters estimated, rather than N, the number of observations. Different authors have used one or the other normalization. Greene (2012, 280) remarks that whether a degree-of-freedom correction improves the small-sample properties is an open question.

∫ Reporting

level(#); see [R] estimation options.

detail specifies that a detailed list of any gaps in the series be reported.

display_options: noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt), sformat(%fmt), and nolstretch; see [R] estimation options.

The following option is available with xtpcse but is not shown in the dialog box:

coeflegend; see [R] estimation options.

Remarks and examples

stata.com

xtpcse is an alternative to feasible generalized least squares (FGLS)—see [XT] xtgls—for fitting linear cross-sectional time-series models when the disturbances are not assumed to be independent and identically distributed (i.i.d.). Instead, the disturbances are assumed to be either heteroskedastic across panels or heteroskedastic and contemporaneously correlated across panels. The disturbances may also be assumed to be autocorrelated within panel, and the autocorrelation parameter may be constant across panels or different for each panel.

We can write such models as

$$y_{it} = \mathbf{x}_{it}\boldsymbol{\beta} + \epsilon_{it}$$

where i = 1, ..., m is the number of units (or panels); $t = 1, ..., T_i$; T_i is the number of periods in panel *i*; and ϵ_{it} is a disturbance that may be autocorrelated along *t* or contemporaneously correlated across *i*.

This model can also be written panel by panel as

$$\begin{bmatrix} \mathbf{y}_1 \\ \mathbf{y}_2 \\ \vdots \\ \mathbf{y}_m \end{bmatrix} = \begin{bmatrix} \mathbf{X}_1 \\ \mathbf{X}_2 \\ \vdots \\ \mathbf{X}_m \end{bmatrix} \boldsymbol{\beta} + \begin{bmatrix} \boldsymbol{\epsilon}_1 \\ \boldsymbol{\epsilon}_2 \\ \vdots \\ \boldsymbol{\epsilon}_m \end{bmatrix}$$

For a model with heteroskedastic disturbances and contemporaneous correlation but with no autocorrelation, the disturbance covariance matrix is assumed to be

$$E[\boldsymbol{\epsilon}\boldsymbol{\epsilon}'] = \boldsymbol{\Omega} = \begin{bmatrix} \sigma_{11}\mathbf{I}_{11} & \sigma_{12}\mathbf{I}_{12} & \cdots & \sigma_{1m}\mathbf{I}_{1m} \\ \sigma_{21}\mathbf{I}_{21} & \sigma_{22}\mathbf{I}_{22} & \cdots & \sigma_{2m}\mathbf{I}_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{m1}\mathbf{I}_{m1} & \sigma_{m2}\mathbf{I}_{m2} & \cdots & \sigma_{mm}\mathbf{I}_{mm} \end{bmatrix}$$

where σ_{ii} is the variance of the disturbances for panel *i*, σ_{ij} is the covariance of the disturbances between panel *i* and panel *j* when the panels' periods are matched, and **I** is a T_i by T_i identity matrix with balanced panels. The panels need not be balanced for xtpcse, but the expression for the covariance of the disturbances will be more general if they are unbalanced.

This could also be written as

$$E[\epsilon\epsilon'] = \Sigma_{m \times m} \otimes \mathbf{I}_{T_i \times T_i}$$

where Σ is the panel-by-panel covariance matrix and I is an identity matrix.

See [XT] **xtgls** for a full taxonomy and description of possible disturbance covariance structures.

xtpcse and xtgls follow two different estimation schemes for this family of models. xtpcse produces OLS estimates of the parameters when no autocorrelation is specified, or Prais–Winsten (see [TS] **prais**) estimates when autocorrelation is specified. If autocorrelation is specified, the estimates of the parameters are conditional on the estimates of the autocorrelation parameter(s). The estimate of the variance–covariance matrix of the parameters is asymptotically efficient under the assumed covariance structure of the disturbances and uses the FGLS estimate of the disturbance covariance matrix; see Kmenta (1997, 121).

xtgls produces full FGLS parameter and variance–covariance estimates. These estimates are conditional on the estimates of the disturbance covariance matrix and are conditional on any autocorrelation parameters that are estimated; see Kmenta (1997), Greene (2012), Davidson and MacKinnon (1993), or Judge et al. (1985).

Both estimators are consistent, as long as the conditional mean $(\mathbf{x}_{it}\beta)$ is correctly specified. If the assumed covariance structure is correct, FGLS estimates produced by xtgls are more efficient. Beck and Katz (1995) have shown, however, that the full FGLS variance-covariance estimates are typically unacceptably optimistic (anticonservative) when used with the type of data analyzed by most social scientists—10–20 panels with 10–40 periods per panel. They show that the OLS or Prais–Winsten estimates with PCSEs have coverage probabilities that are closer to nominal.

Because the covariance matrix elements, σ_{ij} , are estimated from panels *i* and *j*, using those observations that have common time periods, estimators for this model achieve their asymptotic behavior as the T_i s approach infinity. In contrast, the random- and fixed-effects estimators assume a different model and are asymptotic in the number of panels *m*; see [XT] **xtreg** for details of the random- and fixed-effects estimators.

Although xtpcse allows other disturbance covariance structures, the term PCSE, as used in the literature, refers specifically to models that are both heteroskedastic and contemporaneously correlated across panels, with or without autocorrelation.

Example 1: Controlling for heteroskedasticity and cross-panel correlation

Grunfeld and Griliches (1960) analyzed a company's current-year gross investment (invest) as determined by the company's prior year market value (mvalue) and the prior year's value of the company's plant and equipment (kstock). The dataset includes 10 companies over 20 years, from 1935 through 1954, and is a classic dataset for demonstrating cross-sectional time-series analysis. Greene (2012, 1112) reproduces the dataset.

To use xtpcse, the data must be organized in "long form"; that is, each observation must represent a record for a specific company at a specific time; see [D] **reshape**. In the Grunfeld data, company is a categorical variable identifying the company, and year is a variable recording the year. Here are the first few records:

```
. use http://www.stata-press.com/data/r13/grunfeld
```

```
. list in 1/5
```

	company	year	invest	mvalue	kstock	time
1.	1	1935	317.6	3078.5	2.8	1
2.	1	1936	391.8	4661.7	52.6	2
з.	1	1937	410.6	5387.1	156.9	3
4.	1	1938	257.7	2792.2	209.2	4
5.	1	1939	330.8	4313.2	203.4	5

To compute PCSEs, Stata must be able to identify the panel to which each observation belongs and be able to match the periods across the panels. We tell Stata how to do this matching by specifying the panel and time variables with xtset; see [XT] **xtset**. Because the data are annual, we specify the **yearly** option.

```
. xtset company year, yearly
panel variable: company (strongly balanced)
time variable: year, 1935 to 1954
    delta: 1 year
```

We can obtain OLS parameter estimates for a linear model of invest on mvalue and kstock while allowing the standard errors (and variance-covariance matrix of the estimates) to be consistent when the disturbances from each observation are not independent. Specifically, we want the standard errors to be robust to each company having a different variance of the disturbances and to each company's observations being correlated with those of the other companies through time. This model is fit in Stata by typing

Linear regression, correlated panels corrected standard errors (PCSE	
	000
Group variable: company Number of obs =	200
Time variable: year Number of groups =	10
Panels: correlated (balanced) Obs per group: min =	20
Autocorrelation: no autocorrelation avg =	20
max =	20
Estimated covariances = 55 R-squared =	0.8124
Estimated autocorrelations = 0 Wald chi2(2) =	637.41
Estimated coefficients = 3 Prob > chi2 =	0.0000
Panel-corrected	
invest Coef. Std. Err. z P> z [95% Conf.	Interval]
mvalue .1155622 .0072124 16.02 0.000 .101426	.1296983
kstock .2306785 .0278862 8.27 0.000 .1760225	.2853345
cons -42.71437 6.780965 -6.30 0.000 -56.00482	-29.42392

Example 2: Comparing the FGLS and PCSE approaches

xtgls will produce more efficient FGLS estimates of the models' parameters, but with the disadvantage that the standard error estimates are conditional on the estimated disturbance covariance. Beck and Katz (1995) argue that the improvement in power using FGLS with such data is small and that the standard error estimates from FGLS are unacceptably optimistic (anticonservative).

The FGLS model is fit by typing

. xtgls invest	t mvalue kstoo	ck, panels(c	correlated	1)		
Cross-sectiona	Cross-sectional time-series FGLS regression					
Coefficients: generalized least squares Panels: heteroskedastic with cross-sectional correlation Correlation: no autocorrelation						
Estimated cova	ariances	= 55	5	Number	of obs	= 200
Estimated auto	ocorrelations	= 0)	Number	of groups	= 10
Estimated coef	fficients	= 3	3	Time pe	riods	= 20
				Wald ch	i2(2)	= 3738.07
				Prob >	chi2	= 0.0000
invest	Coef.	Std. Err.	Z	P> z	[95% Conf	. Interval]
mvalue	.1127515	.0022364	50.42	0.000	.1083683	.1171347
kstock	.2231176	.0057363	38.90	0.000	.2118746	.2343605
_cons	-39.84382	1.717563	-23.20	0.000	-43.21018	-36.47746

The coefficients between the two models are close; the constants differ substantially, but we are generally not interested in the constant. As Beck and Katz observed, the standard errors for the FGLS model are 50%-100% smaller than those for the OLS model with PCSE.

If we were also concerned about autocorrelation of the disturbances, we could obtain a model with a common AR(1) parameter by specifying correlation(ar1).

. xtpcse inves (note: estimat					the range [·	-1,1])
Prais-Winsten	regression, o	correlated pa	anels com	rrected st	tandard erro	rs (PCSEs)
Group variable	1 0			Number o		= 200
Time variable: Panels:	5	ed (balanced))		of groups = group: min =	
Autocorrelatio	on: common Al	R(1)		-	avg :	= 20
					max	= 20
Estimated cova	riances	= 55		R-square	ed :	= 0.5468
Estimated auto	correlations	= 1		Wald ch:	i2(2) :	= 93.71
Estimated coef	ficients	= 3		Prob > o	chi2 ·	= 0.0000
	Pa	anel-correct	ed			
invest	Coef.	Std. Err.	Z	P> z	[95% Conf	. Interval]
mvalue	.0950157	.0129934	7.31	0.000	.0695492	.1204822
kstock	.306005	.0603718	5.07	0.000	.1876784	.4243317
_cons	-39.12569	30.50355	-1.28	0.200	-98.91154	20.66016
rho	.9059774					

The estimate of the autocorrelation parameter is high (0.906), and the standard errors are larger than for the model without autocorrelation, which is to be expected if there is autocorrelation.

4

Example 3: Controlling for cross-panel correlation and autocorrelation

Let's estimate panel-specific autocorrelation parameters and change the method of estimating the autocorrelation parameter to the one typically used to estimate autocorrelation in time-series analysis.

. xtpcse invest	t mvalue ksto	ock, correl	ation(psar	1) rhoty	pe(tsco	rr)	
Prais-Winsten r	regression, d	correlated	panels cor	rected s	tandard	error	s (PCSEs)
Group variable:	: company			Number	of obs	=	200
Time variable:	year			Number	of grou	os =	10
Panels:	correlate	ed (balance	d)	Obs per	group:	min =	20
Autocorrelation	n: panel-spe	ecific AR(1)	•	• •	avg =	20
						max =	20
Estimated covar	riances	= 5	5	R-squar	ed	=	0.8670
Estimated autoc	correlations	= 1	0	Wald ch	i2(2)	=	444.53
Estimated coeff	ficients	=	3	Prob >	chi2	=	0.0000
Panel-corrected							
invest	Coef.	Std. Err.	Z	P> z	L95%	Conf.	Interval]
mvalue	.1052613	.0086018	12.24	0.000	.0884		.1221205
kstock	.3386743	.0367568	9.21	0.000	.2666		.4107163
_cons	-58.18714	12.63687	-4.60	0.000	-82.9	5496	-33.41933
rhos =	.5135627	.87017 .	9023497	.63368	.857150	02	.8752707

Beck and Katz (1995, 121) make a case against estimating panel-specific AR parameters, as opposed to one AR parameter for all panels.

Example 4: Controlling for heteroskedasticity only; not quite PCSEs

We can also diverge from PCSEs to estimate standard errors that are panel corrected, but only for panel-level heteroskedasticity; that is, each company has a different variance of the disturbances. Allowing also for autocorrelation, we would type

. xtpcse inves (note: estimat					•		nge [-:	1,1])
Prais-Winsten	regression, h	heterosk	edast	ic panel	ls correc	ted sta	ndard	errors
Group variable Time variable:	1 0				Number Number	of obs of grou	= ns =	200 10
Panels:	heteroske		(bala	nced)		group:	-	20
Autocorrelatio	on: common Al	R(1)					avg =	20
.			4.0				max =	20
Estimated cova	111000	=	10		R-squar		=	0.5468
Estimated auto	correlations	=	1		Wald ch		=	01112
Estimated coef	ficients	=	3		Prob >	chi2	=	0.0000
	I	Het-corr	ected					
invest	Coef.	Std. E	lrr.	Z	P> z	[95%	Conf.	Interval]
mvalue	.0950157	.01308	372	7.26	0.000	.069	3653	.1206661
kstock	.306005	.0614	32	4.98	0.000	.185	6006	.4264095
_cons	-39.12569	26.169	35	-1.50	0.135	-90.4	1666	12.16529
rho	.9059774							

With this specification, we do not obtain what are referred to in the literature as PCSEs. These standard errors are in the same spirit as PCSEs but are from the asymptotic covariance estimates of OLS without allowing for contemporaneous correlation.

Stored results

xtpcse stores the following in e():

Scalars	
e(N)	number of observations
e(N_g)	number of groups
e(N_gaps)	number of gaps
e(n_cf)	number of estimated coefficients
e(n_cv)	number of estimated covariances
e(n_cr)	number of estimated correlations
e(n_sigma)	observations used to estimate elements of Sigma
e(mss)	model sum of squares
e(df)	degrees of freedom
e(df_m)	model degrees of freedom
e(rss)	residual sum of squares
e(g_min)	smallest group size
e(g_avg)	average group size
e(g_max)	largest group size
e(r2)	R-squared
e(chi2)	χ^2
e(p)	significance
e(rmse)	root mean squared error
e(rank)	rank of e(V)
e(rc)	return code
Macros	
e(cmd)	xtpcse
e(cmdline)	command as typed
e(depvar)	name of dependent variable
e(ivar)	variable denoting groups
e(tvar)	variable denoting time within groups
e(wtype)	weight type
e(wexp)	weight expression
e(title)	title in estimation output
e(panels)	contemporaneous covariance structure
e(corr)	correlation structure
e(rhotype)	type of estimated correlation
e(rho)	ρ
e(cons)	noconstant or ""
e(missmeth)	casewise or pairwise
e(balance)	balanced or unbalanced
e(chi2type)	Wald; type of model χ^2 test
e(vcetype)	title used to label Std. Err.
e(properties)	b V
e(predict)	program used to implement predict
e(marginsok)	predictions allowed by margins
e(asbalanced)	factor variables fvset as asbalanced
e(asobserved)	factor variables fvset as asobserved
Matrices	
e(b)	coefficient vector
e(Sigma)	$\widehat{\Sigma}$ matrix
e(rhomat)	vector of autocorrelation parameter estimates
e(V)	variance–covariance matrix of the estimators
Functions	
e(sample)	marks estimation sample
C(pambre)	marks estimation sample

Methods and formulas

If no autocorrelation is specified, the parameters β are estimated by OLS; see [R] regress. If autocorrelation is specified, the parameters β are estimated by Prais–Winsten; see [TS] prais.

When autocorrelation with panel-specific coefficients of correlation is specified (by using option correlation(psar1)), each panel-level ρ_i is computed from the residuals of an OLS regression across all panels; see [TS] **prais**. When autocorrelation with a common coefficient of correlation is specified (by using option correlation(ar1)), the common correlation coefficient is computed as

$$\rho = \frac{\rho_1 + \rho_2 + \dots + \rho_m}{m}$$

where ρ_i is the estimated autocorrelation coefficient for panel i and m is the number of panels.

The covariance of the OLS or Prais-Winsten coefficients is

$$\operatorname{Var}(\boldsymbol{\beta}) = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{\Omega}\mathbf{X}(\mathbf{X}'\mathbf{X})^{-1}$$

where Ω is the full covariance matrix of the disturbances.

When the panels are balanced, we can write Ω as

$$\mathbf{\Omega} = \mathbf{\Sigma}_{m imes m} \otimes \mathbf{I}_{T_i imes T_i}$$

where Σ is the *m* by *m* panel-by-panel covariance matrix of the disturbances; see *Remarks and examples*.

xtpcse estimates the elements of Σ as

$$\widehat{\Sigma}_{ij} = rac{\epsilon_i' \epsilon_j}{T_{ij}}$$

where ϵ_i and ϵ_j are the residuals for panels *i* and *j*, respectively, that can be matched by period, and where T_{ij} is the number of residuals between the panels *i* and *j* that can be matched by time period.

When the panels are balanced (each panel has the same number of observations and all periods are common to all panels), $T_{ij} = T$, where T is the number of observations per panel.

When panels are unbalanced, xtpcse by default uses casewise selection, in which only those residuals from periods that are common to all panels are used to compute \hat{S}_{ij} . Here $T_{ij} = T^*$, where T^* is the number of periods common to all panels. When pairwise is specified, each \hat{S}_{ij} is computed using all observations that can be matched by period between the panels *i* and *j*.

Acknowledgments

We thank the following people for helpful comments: Nathaniel Beck of the Department of Politics at New York University, Jonathan Katz of the Division of the Humanities and Social Science at California Institute of Technology, and Robert John Franzese Jr. of the Center for Political Studies at the Institute for Social Research at the University of Michigan.

References

- Beck, N. L., and J. N. Katz. 1995. What to do (and not to do) with time-series cross-section data. American Political Science Review 89: 634–647.
- Blackwell, J. L., III. 2005. Estimation and testing of fixed-effect panel-data systems. Stata Journal 5: 202-207.
- Davidson, R., and J. G. MacKinnon. 1993. Estimation and Inference in Econometrics. New York: Oxford University Press.
- Greene, W. H. 2012. Econometric Analysis. 7th ed. Upper Saddle River, NJ: Prentice Hall.
- Grunfeld, Y., and Z. Griliches. 1960. Is aggregation necessarily bad? Review of Economics and Statistics 42: 1-13.
- Hoechle, D. 2007. Robust standard errors for panel regressions with cross-sectional dependence. Stata Journal 7: 281–312.
- Judge, G. G., W. E. Griffiths, R. C. Hill, H. Lütkepohl, and T.-C. Lee. 1985. The Theory and Practice of Econometrics. 2nd ed. New York: Wiley.

Kmenta, J. 1997. Elements of Econometrics. 2nd ed. Ann Arbor: University of Michigan Press.

Also see

- [XT] **xtpcse postestimation** Postestimation tools for xtpcse
- [XT] **xtset** Declare data to be panel data
- [XT] **xtgls** Fit panel-data models by using GLS
- [XT] **xtreg** Fixed-, between-, and random-effects and population-averaged linear models
- [XT] **xtregar** Fixed- and random-effects linear models with an AR(1) disturbance
- [R] regress Linear regression
- [TS] **newey** Regression with Newey–West standard errors
- [TS] prais Prais–Winsten and Cochrane–Orcutt regression
- [U] 20 Estimation and postestimation commands