20 Estimation and postestimation commands

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20.1 All estimation commands work the same way

All Stata commands that fit statistical models—commands such as `regress`, `logit`, `sureg`, and so on—work the same way. Most single-equation estimation commands have the syntax

```
command varlist [if] [in] [weight] [ , options]
```

and most multiple-equation estimation commands have the syntax

```
command (varlist) (varlist) ... (varlist) [if] [in] [weight] [ , options]
```

Adopt a loose definition of single and multiple equation in interpreting this. For instance, `heckman` is a two-equation system, mathematically speaking, yet we categorize it, syntactically, with single-equation commands because most researchers think of it as a linear regression with an adjustment for the censoring. The important thing is that most estimation commands have one or the other of these two syntaxes.

In single-equation commands, the first variable in the `varlist` is the dependent variable, and the remaining variables are the independent variables, with some exceptions. For instance, `mixed` allows special variable prefixes to identify random factors.

Prefix commands may be specified in front of an estimation command to modify what it does. The syntax is

```
prefix: command ...
```

where the prefix commands are

<table>
<thead>
<tr>
<th>Prefix command</th>
<th>Description</th>
<th>Manual entry</th>
</tr>
</thead>
<tbody>
<tr>
<td>by</td>
<td>repeat command on subsets of data</td>
<td>[D] by</td>
</tr>
<tr>
<td>statsby</td>
<td>collect results across subsets of data</td>
<td>[D] statsby</td>
</tr>
<tr>
<td>rolling</td>
<td>time-series rolling estimation</td>
<td>[TS] rolling</td>
</tr>
<tr>
<td>*svy</td>
<td>estimation for complex survey data</td>
<td>[SVY] svy</td>
</tr>
<tr>
<td>*mi estimate</td>
<td>multiply imputed data and multiple imputation</td>
<td>[MI] mi estimate</td>
</tr>
<tr>
<td>*nestreg</td>
<td>nested model statistics</td>
<td>[R] nestreg</td>
</tr>
<tr>
<td>*stepwise</td>
<td>stepwise estimation</td>
<td>[R] stepwise</td>
</tr>
<tr>
<td>*xi</td>
<td>interaction expansion</td>
<td>[R] xi</td>
</tr>
<tr>
<td>*fp</td>
<td>fractional polynomials</td>
<td>[R] fp</td>
</tr>
<tr>
<td>*mfp</td>
<td>multiple fractional polynomials</td>
<td>[R] mfp</td>
</tr>
</tbody>
</table>

*Available for some but not all estimation commands

Two other prefix commands—`bootstrap` and `jackknife`—also work with estimation commands—see [R] bootstrap and [R] jackknife—but usually it is easier to specify the estimation-command option `vce(bootstrap)` or `vce(jackknife)`.

Also, all estimation commands—whether single or multiple equation—share the following features:

1. You can use the standard features of Stata’s syntax—`if exp` and `in range`—to specify the estimation subsample; you do not have to make a special dataset.

2. You can retype the estimation command without arguments to redisplay the most recent estimation results. For instance, after fitting a model with `regress`, you can see the estimates again by typing `regress` by itself. You do not have to do this immediately—any number of commands can occur between the estimation and the replaying, and, in fact, you can even replay the last estimates after the data have changed or you have dropped the data altogether. Stata never forgets (unless you type `discard`; see [P] discard).
3. You can specify the \texttt{level()} option at the time of estimation, or when you redisplay results if that makes sense, to specify the width of the confidence intervals for the coefficients. The default is \texttt{level(95)}, meaning 95\% confidence intervals. You can reset the default with \texttt{set level}; see \cite{Rlevel}.

4. You can use the postestimation command \texttt{margins} to display model results in terms of marginal effects ($dy/dx$ or even $df(y)/dx$), which can be displayed as either derivatives or elasticities; see \cite{Rmargins}.

5. You can use the postestimation command \texttt{margins} to obtain tables of estimated marginal means, adjusted predictions, and predictive margins; see \cite{U20.16} Obtaining conditional and average marginal effects and see \cite{Rmargins}.

6. You can use the postestimation command \texttt{pwcompare} to obtain pairwise comparisons across levels of factor variables. You can compare estimated cell means, marginal means, intercepts, marginal intercepts, slopes, or marginal slopes—collectively called margins. See \cite{U20.17} Obtaining pairwise comparisons, \cite{Rmargins}, and \cite{Rpwcompare}.

7. You can use the postestimation command \texttt{contrast} to obtain contrasts, which is to say, to compare levels of factor variables and their interactions. This command can also produce ANOVA-style tests of main effects, interactions effects, simple effects, and nested effects; and it can be used after most estimation commands. See \cite{U20.18} Obtaining contrasts, tests of interactions, and main effects, \cite{Rcontrast}, and \cite{Rmargins,contrast}.

8. You can use the postestimation command \texttt{marginsplot} to graph any of the results produced by \texttt{margins}, and because \texttt{margins} can replicate any result produced by \texttt{pwcompare} and \texttt{contrast}, you can graph any result produced by them, too. See \cite{Rmarginsplot}.

9. You can use the postestimation command \texttt{estat} to obtain common statistics associated with the model. Which statistics are available are documented in the postestimation section following the documentation of the estimation command, for instance, in \cite{Rregress} estimating following \cite{Rregress}.

You can always use the postestimation command \texttt{estat vce} to obtain the variance–covariance matrix of the estimators (VCE), presented as either a correlation matrix or a covariance matrix. (You can also obtain the estimated coefficients and covariance matrix as vectors and matrices and manipulate them with Stata’s matrix capabilities; see \cite{U14.5} Accessing matrices created by Stata commands.)

10. You can use the postestimation command \texttt{predict} to obtain predictions, residuals, influence statistics, and the like, either for the data on which you just estimated or for some other data. You can use postestimation command \texttt{predictnl} to obtain point estimates, standard errors, etc., for customized predictions. See \cite{Rpredict} and \cite{Rpredictnl}.

11. You can use the postestimation command \texttt{forecast} to perform dynamic and static forecasts, with optional forecast confidence intervals. This includes the ability to produce forecasts from multiple estimation commands, even when estimates imply simultaneous systems. An example of a simultaneous system is when $y2$ predicts $y1$ in estimation 1 and $y1$ predicts $y2$ in estimation 2. \texttt{forecast} provides many facilities for creating comparative forecast scenarios. See \cite{TSforecast}.

12. You can refer to the values of coefficients and standard errors in expressions (such as with \texttt{generate}) by using standard notation; see \cite{U13.5} Accessing coefficients and standard errors. You can refer in expressions to the values of other estimation-related statistics by using \texttt{e(resultname)}. For instance, all commands define \texttt{e(N)} recording the number of observations in the estimation subsample. After estimation, type \texttt{ereturn list} to see a list of all that is
available. See the Stored results section in the estimation command’s documentation for their definition.

An especially useful e() result is e(sample): it returns 1 if an observation was used in the estimation and 0 otherwise, so you can add if e(sample) to the end of other commands to restrict them to the estimation subsample. You could type, for instance, summarize if e(sample).

13. You can use the postestimation command test to perform tests on the estimated parameters (Wald tests of linear hypotheses), testnl to perform Wald tests of nonlinear hypotheses, and lrtest to perform likelihood-ratio tests. You can use the postestimation command lincom to obtain point estimates and confidence intervals for linear combinations of the estimated parameters and the postestimation command nlcom to obtain nonlinear combinations.

14. You can specify the coeflegend option at the time of estimation or when you redisplay results to see how to type your coefficients in postestimation commands such as test and lincom (see [R] test and [R] lincom) and in expressions.

15. You can use the statsby prefix command (see [D] statsby) to fit models over each category in a categorical variable and collect the results in a Stata dataset.

16. You can use the postestimation command estimates to store estimation results by name for later retrieval or for displaying/comparing multiple models by using estimates, or for saving them in a file; see [R] estimates.

17. You can use the postestimation command _estimates to hold estimates, perform other estimation commands, and then restore the prior estimates. This is of particular interest to programmers. See [P] _estimates.

18. You can use the postestimation command suest to obtain the joint parameter vector and variance–covariance matrix for coefficients from two different models by using seemingly unrelated estimation. This is especially useful for testing the equality, say, of coefficients across models; see [R] suest.

19. You can use the postestimation command hausman to perform Hausman model-specification tests by using hausman; see [R] hausman.

20. With some exceptions, you can specify the vce(robust) option at the time of estimation to obtain the Huber/White/robust alternate estimate of variance, or you can specify the vce(cluster clustvar) option to relax the assumption of independence of the observations. See [R] vce_option.

Most estimation commands also allow a vce(vcetype) option to specify other alternative variance estimators—which ones are allowed are documented with the estimator—and usually vce(opg), vce(bootstrap), and vce(jackknife) are available.

### 20.2 Standard syntax

You can combine Stata’s if exp and in range with any estimation command. Estimation commands also allow by varlist:, where it would be sensible.

#### Example 1

We have data on 74 automobiles that record the mileage rating (mpg), weight (weight), and whether the car is domestic or foreign produced (foreign). We can fit a linear regression model of mpg on weight and the square of weight, using just the foreign-made automobiles, by typing
. use http://www.stata-press.com/data/r13/auto2
(1978 Automobile Data)
. regress mpg weight c.weight#c.weight if foreign

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>428.256889</td>
<td>2</td>
<td>214.128444</td>
</tr>
<tr>
<td>Residual</td>
<td>489.606747</td>
<td>19</td>
<td>25.7687762</td>
</tr>
<tr>
<td>Total</td>
<td>917.863636</td>
<td>21</td>
<td>43.7077922</td>
</tr>
</tbody>
</table>

F( 2, 19) = 8.31
Prob > F = 0.0026
R-squared = 0.4666
Adj R-squared = 0.4104
Root MSE = 5.0763

We use the factor-variable notation c.weight#c.weight to add the square of weight to our regression; see [U] 11.4.3 Factor variables.

We can run separate regressions for the domestic and foreign-produced automobiles with the by varlist: prefix:
. by foreign: regress mpg weight c.weight#c.weight

-> foreign = Domestic

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 52</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>905.395466</td>
<td>2</td>
<td>452.697733</td>
<td>F( 2, 49) = 91.64</td>
</tr>
<tr>
<td>Residual</td>
<td>242.046842</td>
<td>49</td>
<td>4.93973146</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>1147.44231</td>
<td>51</td>
<td>22.4988688</td>
<td>R-squared = 0.7891</td>
</tr>
</tbody>
</table>

| Coef. | Std. Err. | t     | P>|t| | [95% Conf. Interval] |
|-------|-----------|-------|------|----------------------|
| weight | -.0131718 | .0032307 | -4.08 | 0.000 | -.0196642 -.0066794 |
| c.weight#c.weight | 1.11e-06 | 4.95e-07 | 2.25 | 0.029 | 1.19e-07 2.11e-06 |
| _cons  | 50.74551 | 5.162014 | 9.83 | 0.000 | 40.37205 61.11896 |

-> foreign = Foreign

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 22</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>428.256889</td>
<td>2</td>
<td>214.128444</td>
<td>F( 2, 19) = 8.31</td>
</tr>
<tr>
<td>Residual</td>
<td>489.606747</td>
<td>19</td>
<td>25.7687762</td>
<td>Prob &gt; F = 0.0026</td>
</tr>
<tr>
<td>Total</td>
<td>917.863636</td>
<td>21</td>
<td>43.7077922</td>
<td>R-squared = 0.4666</td>
</tr>
</tbody>
</table>

| Coef. | Std. Err. | t     | P>|t| | [95% Conf. Interval] |
|-------|-----------|-------|------|----------------------|
| weight | -.0132182 | .0275711 | -0.48 | 0.637 | -.0709252 .0444888 |
| c.weight#c.weight | 5.50e-07 | 5.41e-06 | 0.10 | 0.920 | -.0000108 .0000119 |
| _cons  | 52.33775 | 34.1539 | 1.53 | 0.142 | -19.14719 123.8227 |

Although all estimation commands allow if exp and in range, only some allow the by varlist: prefix. For by(), the duration of Stata’s memory is limited: it remembers the last set of estimates only. This means that, if we were to use any of the other features described below, they would use the last regression estimated, which right now is mpg on weight and square of weight for the Foreign subsample.

We can instead collect the statistics from each of the by-groups using the [D] statsby prefix.

. statsby, by(foreign): regress mpg weight c.weight#c.weight
(command: regress mpg weight c.weight#c.weight
(by: foreign
Statsby groups
1 2 3 4 5

statsby runs the regression first on Domestic cars then on Foreign cars and saves the coefficients by overwriting our dataset. Do not worry; if the dataset has not been previously saved, statsby will refuse to run unless we also specify the clear option.)
Here is what we now have in memory.

```
. list
  foreign  _b_weight  _stat_2  _b_cons
        1. Domestic  -.0131718  1.11e-06  50.74551
        2. Foreign   -.0132182  5.50e-07  52.33775
```

These are the coefficients from the two regressions above. `statsby` does not know how to name the coefficient for `c.weight#c.weight` so it labels the coefficient with the generic name `_stat_2`. We can also save the standard errors and other statistics from the regressions; see [D] `statsby`.

### 20.3 Replaying prior results

When you type an estimation command without arguments, it redisplay prior results.

#### Example 2

To perform a regression of `mpg` on the variables `weight` and `displacement`, we could type

```
. use http://www.stata-press.com/data/r13/auto2, clear
(1978 Automobile Data)
. regress mpg weight displacement
```

```plaintext
Source |        SS   df      MS
------|-----------|--------|-----------
Model  | 1595.40969 2  797.704846
Residual | 848.049768 71  11.9443629
Total  | 2443.45946 73  33.4720474
```

| mpg  | Coef. | Std. Err. | t     | P>|t|   | [95% Conf. Interval] |
|------|-------|-----------|-------|-------|----------------------|
| weight | -0.0065671 | 0.0011662 | -5.63 | 0.000 | -0.0088925 -0.0042417 |
| displacement | 0.0052808 | 0.0098696 | 0.54  | 0.594 | -0.0143986 0.0249602 |
| _cons  | 40.08452  | 2.02011  | 19.84 | 0.000 | 36.05654 44.11251   |

We now go on to do other things, summarizing data, listing observations, performing hypothesis tests, or anything else. If we decide that we want to see the last set of estimates again, we type the estimation command without arguments.

```
. regress
```

```plaintext
Source |        SS   df      MS
------|-----------|--------|-----------
Model  | 1595.40969 2  797.704846
Residual | 848.049768 71  11.9443629
Total  | 2443.45946 73  33.4720474
```

| mpg  | Coef. | Std. Err. | t     | P>|t|   | [95% Conf. Interval] |
|------|-------|-----------|-------|-------|----------------------|
| weight | -0.0065671 | 0.0011662 | -5.63 | 0.000 | -0.0088925 -0.0042417 |
| displacement | 0.0052808 | 0.0098696 | 0.54  | 0.594 | -0.0143986 0.0249602 |
| _cons  | 40.08452  | 2.02011  | 19.84 | 0.000 | 36.05654 44.11251   |
This feature works with every estimation command, so we could just as well have done it with, say, \texttt{stcox} or \texttt{logit}.

### 20.4 Cataloging estimation results

Stata keeps only the results of the most recently fit model in active memory. You can use Stata’s \texttt{estimates} command, however, to temporarily store estimation results for displaying, comparing, cross-model testing, etc., during the same session. You can also save estimation results to disk, but that will be the subject of the next section. You may temporarily store up to 300 sets of estimation results.

#### Example 3

Continuing with our automobile data, we fit four models and \texttt{estimates store} them. We fit the models quietly to keep the output to a minimum.

```stata
. quietly regress mpg weight displ
. estimates store r_base
. quietly regress mpg weight displ foreign
. estimates store r_alt
. quietly qreg mpg weight displ
. estimates store q_base
. quietly qreg mpg weight displ foreign
. estimates store q_alt
```

We saved the four models under the names \texttt{r_base}, \texttt{r_alt}, \texttt{q_base}, and \texttt{q_alt} but, if we forget, we can ask to see a directory of what is stored:

```stata
. estimates dir
```

<table>
<thead>
<tr>
<th>name</th>
<th>command</th>
<th>depvar</th>
<th>npar</th>
<th>title</th>
</tr>
</thead>
<tbody>
<tr>
<td>r_base</td>
<td>regress</td>
<td>mpg</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>r_alt</td>
<td>regress</td>
<td>mpg</td>
<td>4</td>
<td></td>
</tr>
<tr>
<td>q_base</td>
<td>qreg</td>
<td>mpg</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>q_alt</td>
<td>qreg</td>
<td>mpg</td>
<td>4</td>
<td></td>
</tr>
</tbody>
</table>

We can ask that any of the previous models be replayed:

```stata
. estimates replay r_base
```

#### Model \texttt{r_base}

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 74</th>
<th>F(  2,  71) = 66.79</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1595.40969</td>
<td>2</td>
<td>797.704846</td>
<td>Prob &gt; F = 0.0000</td>
<td>R-squared = 0.6529</td>
</tr>
<tr>
<td>Residual</td>
<td>848.049768</td>
<td>71</td>
<td>11.9443629</td>
<td>Adj R-squared = 0.6432</td>
<td>Root MSE = 3.4561</td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

| mpg       | Coef.    | Std. Err. | t     | P>|t|  | [95% Conf. Interval] |
|-----------|----------|-----------|-------|------|---------------------|
| weight    | -0.0065671 | 0.0011662 | -5.63 | 0.000 | -0.0088925 to -0.0042417 |
| displacement | 0.0052808 | 0.0098696 | 0.54  | 0.594 | -0.0143986 to 0.0249602 |
| _cons     | 40.08452   | 2.02011   | 19.84 | 0.000 | 36.05654 to 44.11251  |
Or we can ask to see all the models in a combined table:

```
. estimates table _all
```

<table>
<thead>
<tr>
<th>Variable</th>
<th>r_base</th>
<th>r_alt</th>
<th>q_base</th>
<th>q_alt</th>
</tr>
</thead>
<tbody>
<tr>
<td>weight</td>
<td>-.00656711</td>
<td>-.00677449</td>
<td>-.00581172</td>
<td>-.00595056</td>
</tr>
<tr>
<td>displacement</td>
<td>.00528078</td>
<td>.00192865</td>
<td>.0042841</td>
<td>.00018552</td>
</tr>
<tr>
<td>foreign</td>
<td>-1.6006312</td>
<td>-2.1326005</td>
<td></td>
<td></td>
</tr>
<tr>
<td>_cons</td>
<td>40.084522</td>
<td>41.847949</td>
<td>37.559865</td>
<td>39.213348</td>
</tr>
</tbody>
</table>

estimates displayed just the coefficients, but we could ask for other statistics. Finally, we can also select one of the stored estimates to be made active, meaning things are just as if we had just fit the model:

```
. estimates restore r_alt
(results r_alt are active now)
```

```
. regress
```

```
Source | SS | df | MS | Number of obs = 74
--- | --- | --- | --- | ---
Model | 1619.71935 | 3 | 539.906448 | F( 3, 70) = 45.88 Prob > F = 0.0000
Residual | 823.740114 | 70 | 11.7677159 | R-squared = 0.6629 Adj R-squared = 0.6484
Total | 2443.45946 | 73 | 33.4720474 | Root MSE = 3.4304

| mpg | Coef. | Std. Err. | t | P>|t| | [95% Conf. Interval] |
--- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
weight | -.0067745 | .0011665 | -5.81 | 0.000 | -.0091011 | -.0044479 |
displacement | .0019286 | .0100701 | 0.19 | 0.849 | -.0181556 | .0220129 |
foreign | -1.6006312 | 1.113648 | -1.44 | 0.155 | -3.821732 | .6204699 |
_cons | 41.84795 | 2.350704 | 17.80 | 0.000 | 37.15962 | 46.53628 |
```

You can do a lot more with estimates; see [R] estimates. In particular, estimates makes it easy to perform cross-model tests, such as the Hausman specification test.

### 20.5 Saving estimation results

estimates can also save estimation results into a file.

```
. estimates save alt
file alt.ster saved
```

That saved the active estimation results, the ones we just estimated or, in our case, the ones we just restored. Later, even in another Stata session, we could reload our estimates:
. estimates use alt
. regress

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 74</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1619.71935</td>
<td>3</td>
<td>539.906448</td>
<td>F( 3, 70) = 45.88</td>
</tr>
<tr>
<td>Residual</td>
<td>823.740114</td>
<td>70</td>
<td>11.7677159</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td>R-squared = 0.6629</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Adj R-squared = 0.6484</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1619.71935</td>
<td>3</td>
<td>539.906448</td>
<td>Root MSE = 3.4304</td>
</tr>
<tr>
<td>Residual</td>
<td>823.740114</td>
<td>70</td>
<td>11.7677159</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td></td>
</tr>
</tbody>
</table>

There is one important difference between storing results in memory and saving them in a file: \(e(sample)\) is lost. We have not discussed \(e(sample)\) yet, but it allows us to identify the observations among those currently in memory that were used in the estimation. For instance, after estimation, we could type

```
. summarize mpg weight displ foreign if e(sample)
```

and see the summary statistics of the relevant data. We could do that after an \texttt{estimates restore}, too. But we cannot do it after an \texttt{estimates use}. Part of the reason is that we might not even have the relevant data in memory. Even if we do, however, here is what will happen:

```
. summarize mpg weight displ foreign if e(sample)
```

<table>
<thead>
<tr>
<th>Variable</th>
<th>Obs</th>
<th>Mean</th>
<th>Std. Dev.</th>
<th>Min</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>mpg</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>weight</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>displ</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>foreign</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Stata will just assume that none of the data in memory played a role in obtaining the estimation results.

There is more worth knowing. You could, for instance, type \texttt{estimates describe} to see the command line that produced the estimates. See \texttt{[R] estimates}.

### 20.6 Specifying the estimation subsample

You specify the estimation subsample—the sample to be used in estimation—by specifying the \texttt{if} \texttt{exp} and/or \texttt{in range} modifiers with the estimation command.

Once an estimation command has been run or previous estimates restored, Stata remembers the estimation subsample, and you can use the modifier \texttt{if e(sample)} on the end of other Stata commands. The term \texttt{estimation subsample} refers to the set of observations used to produce the active estimation results. That might turn out to be all the observations (as it was in the above example) or some of the observations:
. regress mpg weight 5.rep78 if foreign

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 21</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>F( 2, 18) = 10.21</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Model</td>
<td>423.317154</td>
<td>2</td>
<td>211.658577</td>
<td></td>
</tr>
<tr>
<td>Residual</td>
<td>372.96856</td>
<td>18</td>
<td>20.7204756</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>796.285714</td>
<td>20</td>
<td>39.8142857</td>
<td></td>
</tr>
</tbody>
</table>

| Variable  | Coef.   | Std. Err. | t    | P>|t| [95% Conf. Interval] |
|-----------|---------|-----------|------|------------------------|
| mpg       | -.0131402 | .0029684 | -4.43| 0.000 | -.0193765 -.0069038 |
| weight    |          |          |      |           |                    |
| rep78     | 5.052676  | 2.13492  | 2.37 | 0.029 | .5673764 9.537977 |
| _cons     | 52.86088  | 6.540147 | 8.08 | 0.000 | 39.12054 66.60122 |

. summarize mpg weight 5.rep78 if e(sample)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Obs</th>
<th>Mean</th>
<th>Std. Dev.</th>
<th>Min</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>mpg</td>
<td>21</td>
<td>25.28571</td>
<td>6.309856</td>
<td>17</td>
<td>41</td>
</tr>
<tr>
<td>weight</td>
<td>21</td>
<td>2263.333</td>
<td>364.7099</td>
<td>1760</td>
<td>3170</td>
</tr>
<tr>
<td>rep78</td>
<td>21</td>
<td>.4285714</td>
<td>.5070926</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

Twenty-one observations were used in the above regression and we subsequently obtained the means for those same 21 observations by typing `summarize ... if e(sample)`. There are two reasons observations were dropped: we specified `if foreign` when we ran the regression, and there were observations for which `5.rep78` was missing. The reason does not matter; `e(sample)` is true if the observation was used and false otherwise.

You can use `if e(sample)` on the end of any Stata command that allows an `if` expression.

Here Stata has a shorthand command that produces the same results as `summarize ... if e(sample)`:

. estat summarize, label

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Std. Dev.</th>
<th>Min</th>
<th>Max</th>
<th>Label</th>
</tr>
</thead>
<tbody>
<tr>
<td>mpg</td>
<td>25.28571</td>
<td>6.309856</td>
<td>17</td>
<td>41</td>
<td>Mileage (mpg)</td>
</tr>
<tr>
<td>weight</td>
<td>2263.333</td>
<td>364.7099</td>
<td>1760</td>
<td>3170</td>
<td>Weight (lbs.)</td>
</tr>
<tr>
<td>rep78</td>
<td>.4285714</td>
<td>.5070926</td>
<td>0</td>
<td>1</td>
<td>Repair Record 1978</td>
</tr>
</tbody>
</table>

See [R] `estat summarize`.

### 20.7 Specifying the width of confidence intervals

You can specify the width of the confidence intervals for the coefficients using the `level()` option at estimation or when you play back the results.
To obtain narrower, 90% confidence intervals when we fit the model, we type

```
. regress mpg weight displ, level(90)
```

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 74</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1595.40969</td>
<td>2</td>
<td>797.704846</td>
<td>F( 2, 71) = 66.79</td>
</tr>
<tr>
<td>Residual</td>
<td>848.049768</td>
<td>71</td>
<td>11.9443629</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td>R-squared = 0.6529</td>
</tr>
</tbody>
</table>

```
mpg   Coef. Std. Err.    t   P>|t|   [90% Conf. Interval]
weight   -.0065671   .0011662  -5.63   0.000   -.0085108   -.0046234
displacement   .0052808   .0098696    0.54   0.594  -.0111679    .0217294
_cons   40.08452   2.02011   19.84   0.000   36.43419   43.73485
```

If we subsequently typed `regress`, without arguments, 95% confidence intervals would be reported. If we initially fit the model with 95% confidence intervals, we could later type `regress, level(90)` to redisplay results with 90% confidence intervals.

Also, we could type `set level 90` to make 90% intervals our default; see [R] level.

Stata allows noninteger confidence intervals between 10.00 and 99.99, with a maximum of two digits following the decimal point. For instance, we could type

```
. regress mpg weight displ, level(92.5)
```

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 74</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1595.40969</td>
<td>2</td>
<td>797.704846</td>
<td>F( 2, 71) = 66.79</td>
</tr>
<tr>
<td>Residual</td>
<td>848.049768</td>
<td>71</td>
<td>11.9443629</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td>R-squared = 0.6529</td>
</tr>
</tbody>
</table>

```
mpg   Coef. Std. Err.    t   P>|t|   [92.5% Conf. Interval]
weight   -.0065671   .0011662  -5.63   0.000   -.0086745   -.0044597
displacement   .0052808   .0098696    0.54   0.594  -.0125535    .023115
_cons   40.08452   2.02011   19.84   0.000   36.43419   43.73485
```

## 20.8 Formatting the coefficient table

You can change the formatting of the coefficient table with the `sformat()`, `pformat()`, and `cformat()` options. The `sformat()` option changes the output format of test statistics; `pformat()` changes p-values; and `cformat()` changes coefficients, standard errors, and confidence limits. We can reduce the number of decimal places by specifying `%f` fixed-width formats:
The option `cformat(%6.3f)`, for example, fixes a width of six characters with three digits to the right of the decimal point. For more information on formats, see [U] 12.5.1 Numeric formats.

The formatting options may also be specified when replaying results, so you can try different formats without refitting the model:

```
. regress mpg weight displacement, cformat(%7.4f)
```

```
. regress mpg weight displacement
```

```
20.9 Obtaining the variance–covariance matrix

Typing `estat vce` displays the variance–covariance matrix of the estimators in active memory.

> Example 5

In example 2, we typed `regress mpg weight displacement`. The full variance–covariance matrix of the estimators can be displayed at any time after estimation:
Typing `estat vce` with the `corr` option presents this matrix as a correlation matrix:

```
. estat vce, corr
Correlation matrix of coefficients of regress model

<table>
<thead>
<tr>
<th></th>
<th>weight</th>
<th>displacement</th>
<th>_cons</th>
</tr>
</thead>
<tbody>
<tr>
<td>weight</td>
<td>1.0000</td>
<td>-0.8949</td>
<td>0.8806</td>
</tr>
<tr>
<td>displacement</td>
<td>1.0000</td>
<td>0.5960</td>
<td>1.0000</td>
</tr>
<tr>
<td>_cons</td>
<td>-0.8806</td>
<td>0.5960</td>
<td>1.0000</td>
</tr>
</tbody>
</table>
```

See [R] estat vce.

Also, Stata’s matrix commands understand that `e(V)` refers to the matrix:

```
. matrix Vinv = invsym(e(V))
```

See [U] 14.5 Accessing matrices created by Stata commands.

## 20.10 Obtaining predicted values

Our discussion below, although cast in terms of predicted values, applies equally to the other statistics generated by `predict`; see [R] predict.

When Stata fits a model, whether it is regression or anything else, it internally stores the results, including the estimated coefficients and the variable names. The predict command allows you to use that information.
Example 6

Let’s perform a linear regression of mpg on weight and the square of weight:

```
. regress mpg weight c.weight#c.weight
```

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 74</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1642.52197</td>
<td>2</td>
<td>821.260986</td>
<td>F( 2, 71) = 72.80</td>
</tr>
<tr>
<td>Residual</td>
<td>800.937487</td>
<td>71</td>
<td>11.2808097</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>2443.45946</td>
<td>73</td>
<td>33.4720474</td>
<td>R-squared = 0.6722</td>
</tr>
</tbody>
</table>

| mpg     | Coef.  | Std. Err. | t     | P>|t|     | [95% Conf. Interval] |
|---------|--------|-----------|-------|---------|---------------------|
| weight  | -.0141581 | .0038835 | -3.65 | 0.001   | -.0219016 -.0064145 |
| c.weight#c.weight | 1.32e-06 | 6.26e-07 | 2.12  | 0.038   | 7.67e-08 2.57e-06  |
| _cons   | 51.18308 | 5.767884 | 8.87  | 0.000   | 39.68225 62.68392 |

After the regression, predict is defined to be

\[-0.0141581 \text{weight} + 1.32 \cdot 10^{-6} \text{weight}^2 + 51.18308\]

(Actually, it is more precise because the coefficients are internally stored at much higher precision than shown in the output.) Thus we can create a new variable—call it fitted—equal to the prediction by typing predict fitted and then use scatter to display the fitted and actual values separately for domestic and foreign automobiles:

```
. predict fitted
(option xb assumed; fitted values)
. scatter mpg fitted weight, by(foreign, total) c(. l) m(o i) sort
```

```
. predict r, resid
```

predict can calculate much more than just predicted values. For predict after linear regression, predict can calculate residuals, standardized residuals, Studentized residuals, influence statistics, etc. In any case, we specify what is to be calculated via an option, so if we wanted the residuals stored in new variable r, we would type

```
. predict r, resid
```
The options that may be specified following `predict` vary according to the estimation command previously used; the `predict` options are documented along with the estimation command. For instance, to discover all the things `predict` can do following `regress`, see `[R] regress`.

### 20.10.1 Using predict

The use of `predict` is not limited to linear regression. `predict` can be used after any estimation command.

#### Example 7

You fit a logistic regression model of whether a car is manufactured outside the United States on the basis of its weight and mileage rating using either the `logistic` or the `logit` command; see `[R] logistic` and `[R] logit`. We will use `logit`.

```stata
. use http://www.stata-press.com/data/r13/auto2, clear
. logit foreign weight mpg
Iteration 0: log likelihood = -45.03321
Iteration 1: log likelihood = -29.238536
Iteration 2: log likelihood = -27.244139
Iteration 3: log likelihood = -27.175277
Iteration 4: log likelihood = -27.175156
Iteration 5: log likelihood = -27.175156

Logistic regression Number of obs = 74
LR chi2(2) = 35.72
Prob > chi2 = 0.0000
Log likelihood = -27.175156 Pseudo R2 = 0.3966

foreign Coef. Std. Err. z P>|z| [95% Conf. Interval]
weight -.0039067 .0010116 -3.86 0.000 -.0058894 -.001924
mpg -.1685869 .0919175 -1.83 0.067 -.3487418 .011568
_cons 13.70837 4.518709 3.03 0.002 4.851859 22.56487
```

After `logit`, `predict` without options calculates the probability of a positive outcome (we learned that by looking at `[R] logit`). To obtain the predicted probabilities that each car is manufactured outside the United States, we type

```stata
. predict probhat
(option pr assumed; Pr(foreign))
. summarize probhat
Variable Obs Mean Std. Dev. Min Max
probhat 74 .2972973 .3052979 .000729 .8980594
```

```stata
. list make mpg weight foreign probhat in 1/5

<table>
<thead>
<tr>
<th>make</th>
<th>mpg</th>
<th>weight</th>
<th>foreign</th>
<th>probhat</th>
</tr>
</thead>
<tbody>
<tr>
<td>AMC Concord</td>
<td>22</td>
<td>2,930</td>
<td>Domestic</td>
<td>.1904363</td>
</tr>
<tr>
<td>AMC Pacer</td>
<td>17</td>
<td>3,350</td>
<td>Domestic</td>
<td>.0957767</td>
</tr>
<tr>
<td>AMC Spirit</td>
<td>22</td>
<td>2,640</td>
<td>Domestic</td>
<td>.4220815</td>
</tr>
<tr>
<td>Buick Century</td>
<td>20</td>
<td>3,250</td>
<td>Domestic</td>
<td>.0862625</td>
</tr>
<tr>
<td>Buick Electra</td>
<td>15</td>
<td>4,080</td>
<td>Domestic</td>
<td>.0084948</td>
</tr>
</tbody>
</table>
```


20.10.2 Making in-sample predictions

`predict` does not retrieve a vector of prerecorded values—it calculates the predictions on the basis of the recorded coefficients and the data currently in memory. In the above examples, when we typed things like

```
. predict probhat
```

`predict` filled in the prediction everywhere that it could be calculated.

Sometimes we have more data in memory than were used by the estimation command, either because we explicitly ignored some of the observations by specifying an `if` expression with the estimation command or because there are missing values. In such cases, if we want to restrict the calculation to the estimation subsample, we would do that in the usual way by adding `if e(sample)` to the end of the command:

```
. predict probhat if e(sample)
```

20.10.3 Making out-of-sample predictions

Because `predict` makes its calculations on the basis of the recorded coefficients and the data in memory, `predict` can do more than calculate predicted values for the data on which the estimation took place—it can make out-of-sample predictions, as well.

If you fit your model on a subset of the observations, you could then predict the outcome for all the observations:

```
. logit foreign weight mpg if rep78 > 3
. predict pall
```

If you do not specify `if e(sample)` at the end of the `predict` command, `predict` calculates the predictions for all observations possible.

In fact, because `predict` works from the active estimation results, you can use `predict` with any dataset that contains the necessary variables.

Example 8

Continuing with our previous `logit` example, assume that we have a second dataset containing the `mpg` and `weight` of a different sample of cars. We have just fit your model and now continue:

```
. use otherdat, clear
(Different cars)
. predict probhat
(option pr assumed; Pr(foreign))
. summarize probhat foreign

Variable |     Obs  Mean    Std. Dev.     Min      Max
---------|--------|--------|-----------------|--------|--------
   probhat |     12  .2505068   .3187104  .0084948  .8920776
  foreign  |     12  .1666667   .3892495      0      1
```

> Example 8

Continuing with our previous `logit` example, assume that we have a second dataset containing the `mpg` and `weight` of a different sample of cars. We have just fit your model and now continue:
Example 9

There are many ways to obtain out-of-sample predictions. Above, we estimated on one dataset and then used another. If our first dataset had contained both sets of cars, marked, say, by the variable `difcars` being 0 if from the first sample and 1 if from the second, we could type

```
. logit foreign weight mpg if difcars==0
   same output as above appears
. predict probhat
   (option pr assumed; Pr(foreign))
. summarize probhat foreign if difcars==1
   same output as directly above appears
```

If we just had a few additional cars, we could even input them after estimation. Assume that our data once again contain only the first sample of cars, and assume that we are interested in an additional sample of only two rather than 12 cars; we could type

```
. use http://www.stata-press.com/data/r13/auto2
   (1978 Automobile Data)
. keep make mpg weight foreign
. logit foreign weight mpg
   same output as above appears
   input
   make   mpg   weight  foreign
   75. "Merc. Zephyr"   20  2830   0
   76. "VW Dasher"   23  2160   1
   . predict probhat
   (option pr assumed; Pr(foreign))
   obtain all the predictions
. list in -2/l
   make   mpg   weight  foreign  probhat
   75. Merc. Zephyr   20  2,830 Domestic  .3275397
   76. VW Dasher 23  2,160 Foreign  .8009743
```

20.10.4 Obtaining standard errors, tests, and confidence intervals for predictions

When you use `predict`, you create, for each observation in the prediction sample, a statistic that is a function of the data and the estimated model parameters. You also could have generated your own customized predictions by using `generate`. In either case, to get standard errors, Wald tests, and confidence intervals for your predictions, use `predictnl`. For example, if we wanted the standard errors for our predicted probabilities, we could type

```
. drop probhat
. predictnl probhat = predict(), se(phat_se)
. list in 1/5
```

<table>
<thead>
<tr>
<th>make</th>
<th>mpg</th>
<th>weight</th>
<th>foreign</th>
<th>probhat</th>
<th>phat_se</th>
</tr>
</thead>
<tbody>
<tr>
<td>AMC Concord</td>
<td>22</td>
<td>2,930</td>
<td>Domestic</td>
<td>.1904363</td>
<td>.0658387</td>
</tr>
<tr>
<td>AMC Pacer</td>
<td>17</td>
<td>3,350</td>
<td>Domestic</td>
<td>.0957767</td>
<td>.0536297</td>
</tr>
<tr>
<td>AMC Spirit</td>
<td>22</td>
<td>2,640</td>
<td>Domestic</td>
<td>.4220815</td>
<td>.0892845</td>
</tr>
<tr>
<td>Buick Century</td>
<td>20</td>
<td>3,250</td>
<td>Domestic</td>
<td>.0862625</td>
<td>.0461928</td>
</tr>
<tr>
<td>Buick Electra</td>
<td>15</td>
<td>4,080</td>
<td>Domestic</td>
<td>.0084948</td>
<td>.0093079</td>
</tr>
</tbody>
</table>
Comparing this output to our previous listing of the first five predicted probabilities, you will notice that the output is identical, except that we now have an additional variable, phat_se, which contains the estimated standard error for each predicted probability.

We first had to drop probhat because predictnl will regenerate it. Note also the use of predict() within predictnl—it specified that we wanted to generate a point estimate (and standard error) for the default prediction after logit; see [R] predictnl for more details.

### 20.11 Accessing estimated coefficients

You can access coefficients and standard errors after estimation by referring to \_b[name] and \_se[name]; see [U] 13.5 Accessing coefficients and standard errors.

#### Example 10

Let’s return to linear regression. We are doing a study of earnings of men and women at a particular company. In addition to each person’s earnings, we have information on their educational attainment and tenure with the company. We type the following:

```
. regress lnearn ed tenure i.female female#(c.ed c.tenure)
```

(output omitted)

If you are not familiar with the # notation, see [U] 11.4.3 Factor variables.

We now wish to predict everyone’s income as if they were male and then compare these as-if earnings with the actual earnings:

```
. generate asif = \_b[\_cons] + \_b[ed]*ed + \_b[tenure]*tenure
```

#### Example 11

We are analyzing the mileage of automobiles and are using a slightly more sophisticated model than any we have used so far. As we have previously, we will fit a linear regression model of mpg on weight and the square of weight, but we also add the interaction of foreign with weight, the car's gear ratio (gear_ratio), and foreign interacted with gear_ratio. We will use factor-variable notation to create the squared term and the interactions; see [U] 11.4.3 Factor variables.
. use http://www.stata-press.com/data/r13/auto2, clear
(1978 Automobile Data)
. regress mpg weight c.weight#c.weight i.foreign#c.weight gear_ratio
> i.foreign#c.gear_ratio

If you are not experienced in both regression technology and automobile technology, you may find it
difficult to interpret this regression. Putting aside issues of statistical significance, we find that mileage
decreases with a car’s weight but increases with the square of weight; decreases even more rapidly
with weight for foreign cars; increases with higher gear ratio; and increases even more rapidly with
higher gear ratio in foreign cars.

Thus do foreign cars yield better or worse gas mileage? Results are mixed. As the foreign cars’
weight increases, they do more poorly in relation to domestic cars, but they do better at higher gear
ratios. One way to compare the results is to predict what mileage foreign cars would have if they
were manufactured domestically. The regression provides all the information necessary for making
that calculation; mileage for domestic cars is estimated to be

$$-0.012 \text{ weight} + 9.81 \cdot 10^{-7} \text{ weight}^2 + 1.160 \text{ gear\_ratio} + 44.6$$

We can use that equation to predict the mileage of foreign cars and then compare it with the true
outcome. The _b[] function simplifies reference to the estimated coefficients. We can type

. gen asif=_b[weight]*weight + _b[c.weight#c.weight]*c.weight#c.weight +
> _b[gear\_ratio]*gear\_ratio + _b[_cons]

_b[weight] refers to the estimated coefficient on weight, _b[c.weight#c.weight] to the estimated
coefficient on c.weight#c.weight, and so on.
We might now ask how the actual mileage of a Honda compares with the \texttt{asif} prediction:

\begin{verbatim}
. list make asif mpg if strpos(make,"Honda")
\end{verbatim}

\begin{verbatim}
<table>
<thead>
<tr>
<th>make</th>
<th>asif</th>
<th>mpg</th>
</tr>
</thead>
<tbody>
<tr>
<td>Honda Accord</td>
<td>26.52597</td>
<td>25</td>
</tr>
<tr>
<td>Honda Civic</td>
<td>30.62202</td>
<td>28</td>
</tr>
</tbody>
</table>
\end{verbatim}

Notice the way we constructed our \texttt{if} clause to select Hondas. \texttt{strpos()} is the string function that returns the location in the first string where the second string is found or, if the second string does not occur in the first, zero. Thus any recorded \texttt{make} that contains the string "Honda" anywhere in it would be listed; see \texttt{[D] functions}.

We find that both Honda models yield slightly lower gas mileage than the \texttt{asif} domestic car–based prediction. (We do not endorse this model as a complete model of the determinants of mileage, nor do we single out the Honda for any special scorn. In fact, please note that the observed values are within the root mean squared error of the average prediction.)

We might wish to compare the overall average \texttt{mpg} and the \texttt{asif} prediction over all foreign cars in the data:

\begin{verbatim}
. summarize mpg asif if foreign
\end{verbatim}

\begin{verbatim}
Variable | Obs | Mean   | Std. Dev. | Min | Max |
----------|-----|--------|-----------|-----|-----|
mpg       | 22  | 24.77273 | 6.611187  | 14  | 41  |
asif      | 22  | 26.67124 | 3.142912  | 19.70466 | 30.62202 |
\end{verbatim}

We find that, on average, foreign cars yield slightly lower mileage than our \texttt{asif} prediction. This might lead us to ask if any foreign cars do better than the \texttt{asif} prediction:

\begin{verbatim}
. list make asif mpg if foreign & mpg>asif, sep(0)
\end{verbatim}

\begin{verbatim}
<table>
<thead>
<tr>
<th>make</th>
<th>asif</th>
<th>mpg</th>
</tr>
</thead>
<tbody>
<tr>
<td>BMW 320i</td>
<td>24.31697</td>
<td>25</td>
</tr>
<tr>
<td>Datsun 210</td>
<td>28.96818</td>
<td>35</td>
</tr>
<tr>
<td>Mazda GLC</td>
<td>29.32015</td>
<td>30</td>
</tr>
<tr>
<td>Subaru</td>
<td>28.85993</td>
<td>35</td>
</tr>
<tr>
<td>Toyota Corolla</td>
<td>27.01144</td>
<td>31</td>
</tr>
<tr>
<td>VW Diesel</td>
<td>28.90355</td>
<td>41</td>
</tr>
</tbody>
</table>
\end{verbatim}

We find six such automobiles.
20.12 Performing hypothesis tests on the coefficients

20.12.1 Linear tests

After estimation, `test` is used to perform tests of linear hypotheses on the basis of the variance–covariance matrix of the estimators (Wald tests).

> Example 12

(test has many syntaxes and features, so do not use this example as an excuse for not reading [R] `test`.) Using the automobile data, we perform the following regression:

```
. use http://www.stata-press.com/data/r13/auto2, clear
(1978 Automobile Data)
. generate weightsq=weight^2
. regress mpg weight weightsq foreign
```

```
Source | SS       df       MS           Number of obs = 74
       |          |             | F( 3, 70) = 52.25
Model  | 1689.15372  3  563.05124 Prob > F = 0.0000
Residual | 754.30574  70  10.7757963 R-squared = 0.6913
        |          |             | Adj R-squared = 0.6781
Total  | 2443.45946  73  33.4720474 Root MSE = 3.2827

mpg     Coef.     Std. Err.      t    P>|t|     [95% Conf. Interval]
weight  -.0165729   .0039692   -4.18   0.000    -.0244892   -.0086567
weightsq  1.59e-06   6.25e-07    2.55   0.013     3.45e-07   2.84e-06
foreign  -2.2035   1.059246   -2.08   0.041    -4.3161   -.0909002
_cons    56.53884    6.197383    9.12   0.000     44.17855    68.89913
```

We can use the `test` command to calculate the joint significance of `weight` and `weightsq`:

```
. test weight weightsq
   ( 1) weight = 0
   ( 2) weightsq = 0
F( 2, 70) = 60.83 Prob > F = 0.0000
```

We are not limited to testing whether the coefficients are zero. We can test whether the coefficient on foreign is \(-2\) by typing

```
. test foreign = -2
   ( 1) foreign = -2
F( 1, 70) =   0.04 Prob > F = 0.8482
```

We can even test more complicated hypotheses because `test` can perform basic algebra. Here is an absurd hypothesis:

```
. test 2*(weight+weightsq)=-3*(foreign-(weight-weightsq))
   ( 1) - weight + 5*weightsq + 3*foreign = 0
F( 1, 70) =   4.31 Prob > F = 0.0416
```

test simplified the algebra of our hypothesis and then presented the test results. We discover that the hypothesis may be absurd but we cannot reject it at the 1% or even 4% level. We can also use `test`’s `accumulate` option to combine this test with another test:
. test foreign+weight=0, accum
( 1) - weight + 5*weightsq + 3*foreign = 0
( 2) weight + foreign = 0
F( 2, 70) = 9.12
Prob > F = 0.0003

There are limitations. test can test only linear hypotheses. If we attempt to test a nonlinear hypothesis, test will tell us that it is not possible:

. test weight/foreign=0
not possible with test
r(131);

Testing nonlinear hypotheses is discussed in [U] 20.12.4 Nonlinear Wald tests below.

20.12.2 Using test

test bases its results on the estimated variance–covariance matrix of the estimators (that is, performs a Wald test), so it can be used after any estimation command. For maximum likelihood estimation, you will have to decide whether you want to perform tests on the basis of the information matrix instead of constraining the equation, reestimating it, and then calculating the likelihood-ratio test (see [U] 20.12.3 Likelihood-ratio tests). Because test bases its results on the information matrix, its results have the same standing as the asymptotic z statistic presented in the coefficient table.

Example 13

Let’s examine the repair records of the cars in our automobile data as rated by Consumer Reports:

. tabulate rep78 foreign

<table>
<thead>
<tr>
<th>Repair Record 1978</th>
<th>Car type</th>
<th>Domestic</th>
<th>Foreign</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Poor</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>Fair</td>
<td>8</td>
<td>0</td>
<td>8</td>
<td></td>
</tr>
<tr>
<td>Average</td>
<td>27</td>
<td>3</td>
<td>30</td>
<td></td>
</tr>
<tr>
<td>Good</td>
<td>9</td>
<td>9</td>
<td>18</td>
<td></td>
</tr>
<tr>
<td>Excellent</td>
<td>2</td>
<td>9</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>48</td>
<td>21</td>
<td>69</td>
<td></td>
</tr>
</tbody>
</table>

The values are coded 1–5, corresponding to Poor, Fair, Average, Good, and Excellent. We will fit this variable by using a maximum-likelihood ordered logit model (the nolog option suppresses the iteration log, saving us some paper):
. ologit rep78 price foreign weight weightsq displ, nolog

Ordered logistic regression
Number of obs = 69
LR chi2(5) = 33.12
Prob > chi2 = 0.0000
Log likelihood = -77.133082 Pseudo R2 = 0.1767

| Coef. | Std. Err. | z     | P>|z| | [95% Conf. Interval] |
|-------|-----------|-------|------|----------------------|
| rep78 | -0.000034 | 0.0001188 | -0.29 | 0.775 | -0.0002669 | 0.000199 |
| price | -0.000034 | 0.0001188 | -0.29 | 0.775 | -0.0002669 | 0.000199 |
| foreign | 2.685647 | 0.9320404 | 2.88 | 0.004 | 0.8588817 | 4.512413 |
| weight | -0.0037447 | 0.0025609 | -1.46 | 0.144 | -0.0087639 | 0.0012745 |
| weightsq | 7.87e-07 | 4.50e-07 | 1.75 | 0.080 | -9.43e-08 | 1.67e-06 |
| displacement | -0.0108919 | 0.0076805 | -1.42 | 0.156 | -0.0259455 | 0.0041617 |

We now wonder whether all our variables other than foreign are jointly significant. We test the hypothesis just as we would after linear regression:

. test weight weightsq displ price
   ( 1) [rep78]weight = 0
   ( 2) [rep78]weightsq = 0
   ( 3) [rep78]displacement = 0
   ( 4) [rep78]price = 0
   chi2( 4) = 3.63
   Prob > chi2 = 0.4590

To compare this with the results performed by a likelihood-ratio test, see [U] 20.12.3 Likelihood-ratio tests. Here results differ little.

## 20.12.3 Likelihood-ratio tests

After maximum likelihood estimation, you can obtain likelihood-ratio tests by fitting both the unconstrained and constrained models, storing the results using estimates store, and then running lrtest. See [R] lrtest for the full details.

Example 14

In [U] 20.12.2 Using test above, we fit an ordered logit on rep78 and then tested the significance of all the explanatory variables except foreign.

To obtain the likelihood-ratio test, sometime after fitting the full model, we type estimates store full_model_name, where full_model_name is just a label that we assign to these results.

. ologit rep78 price foreign weight weightsq displ
   (output omitted)
. estimates store myfullmodel

This command saves the current model results with the name myfullmodel.
Next we fit the constrained model. After that, typing `lrtest myfullmodel .` compares the current model with the model we saved:

```
. ologit rep78 foreign
Iteration 0:  log likelihood = -93.692061
Iteration 1:  log likelihood = -79.696089
Iteration 2:  log likelihood = -79.034005
Iteration 3:  log likelihood = -79.029244
Iteration 4:  log likelihood = -79.029243
Ordered logistic regression
Number of obs = 69
LR chi2(1) = 29.33
Prob > chi2 = 0.0000
Log likelihood = -79.029243 Pseudo R2 = 0.1565
```

|            | Coef.    | Std. Err. | z   | P>|z|   | [95% Conf. Interval] |
|------------|----------|-----------|-----|-------|----------------------|
| rep78      |          |           |     |       |                      |
| foreign    |          |           |     |       |                      |
| /cut1      | -3.158382| .7222469  | 4.81| 0.000 | 1.765658  4.197442   |
| /cut2      | -1.362642| .3557343  | 3.85| 0.000 | 0.98622  -1.739069   |
| /cut3      | 1.232161 | .3431227  | 3.55| 0.000 | 0.549653  1.90467    |
| /cut4      | 3.246209 | .5556657  | 5.83| 0.000 | 2.157124 4.335293    |

```
. lrtest myfullmodel .
Likelihood-ratio test  LR chi2(4) = 3.79
(Assumption: . nested in myfullmodel)  Prob > chi2 = 0.4348
```

When we tested the same constraint with `test` (which performed a Wald test), we obtained a $\chi^2$ of 3.63 and a significance level of 0.4590. We used . (the dot) to specify the results in active memory, although we also could have stored them with `estimates store` and referred to them by name instead. Also, the order in which you specify the two models to `lrtest` doesn’t matter; `lrtest` is smart enough to know the full model from the constrained model.

Two other postestimation commands work in the same way as `lrtest`, meaning that they accept names of stored estimation results as their input: `hausman` for performing Hausman specification tests and `suest` for seemingly unrelated estimation. We do not cover these commands here; see [R] `hausman` and [R] `suest` for more details.

## 20.12.4 Nonlinear Wald tests

`testnl` can be used to test nonlinear hypotheses about the parameters of the active estimation results. `testnl`, like `test`, bases its results on the variance–covariance matrix of the estimators (that is, performs a Wald test), so it can be used after any estimation command; see [R] `testnl`.

### Example 15

We fit the model

```
. regress price mpg weight foreign
(output omitted)
```
and then type

```
    . testnl (38*_b[mpg]^2 = _b[foreign]) (_b[mpg]/_b[weight]=4)
```

(1)  38*_b[mpg]^2 = _b[foreign]
(2)  _b[mpg]/_b[weight] = 4

\[
\begin{align*}
\chi^2(2) &= 0.04 \\
\text{Prob} &> \chi^2 = 0.9806
\end{align*}
\]

We performed this test on linear regression estimates, but tests of this type could be performed after any estimation command.

### 20.13 Obtaining linear combinations of coefficients

`lincom` computes point estimates, standard errors, \( t \) or \( z \) statistics, \( p \)-values, and confidence intervals for a linear combination of coefficients after any estimation command. Results can optionally be displayed as odds ratios, incidence-rate ratios, or relative-risk ratios.

**Example 16**

We fit a linear regression:

```
    . use http://www.stata-press.com/data/r13/regress, clear
    . regress y x1 x2 x3
```

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 148</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>3259.3561</td>
<td>3</td>
<td>1086.45203</td>
<td>F( 3, 144) = 96.12</td>
</tr>
<tr>
<td>Residual</td>
<td>1627.56282</td>
<td>144</td>
<td>11.3025196</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>4886.91892</td>
<td>147</td>
<td>33.2443464</td>
<td>R-squared = 0.6670</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Adj R-squared = 0.6600</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Root MSE = 3.3619</td>
</tr>
</tbody>
</table>

|         | Coef.    | Std. Err. | t       | P>|t|  | [95% Conf. Interval] |
|---------|----------|------------|---------|-------|---------------------|
| x1      | 1.457113 | 1.07461    | 1.36    | 0.177 | -1.20218 3.581161   |
| x2      | 2.221682 | .8610358   | 2.58    | 0.011 | .5197797 3.923583   |
| x3      | -.006139 | .0005543   | -11.08  | 0.000 | -.0072345 -.0050435 |
| _cons   | 36.10135 | 4.382693   | 8.24    | 0.000 | 27.43863 44.76407   |

Suppose that we want to see the difference of the coefficients of \( x2 \) and \( x1 \). We type

```
    . lincom x2 - x1
    ( 1)  - x1 + x2 = 0
```

|         | Coef.    | Std. Err. | t       | P>|t|  | [95% Conf. Interval] |
|---------|----------|------------|---------|-------|---------------------|
| (1)     | .7645682 | .9950282   | 0.77    | 0.444 | -1.20218 2.731316   |

`lincom` is handy for computing the odds ratio of one covariate group relative to another.
### Example 17

We estimate the parameters of a logistic model of low birthweight:

```
. use http://www.stata-press.com/data/r13/lbw3
  (Hosmer & Lemeshow data)
. logit low age lwd i.race smoke ptd ht ui
Iteration 0:  log likelihood =  -117.336
Iteration 1:  log likelihood =  -99.3982
Iteration 2:  log likelihood =  -98.780418
Iteration 3:  log likelihood =  -98.777998
Iteration 4:  log likelihood =  -98.777998
Logistic regression                              Number of obs =  189
LR chi2(8) =  37.12                             Prob > chi2 = 0.0000
Log likelihood =  -98.777998                    Pseudo R2 = 0.1582

  low |       Coef.       Std. Err.     z  P>|z|      [95% Conf. Interval]
-----|------------------|------------------|-----|--------|------------------|------------------|
  age |   -.0464796   .0373888     -1.24  0.214   -.1197603   .0268011
 lwd |   .8420615   .4055338      2.08  0.038   .0472299   1.636893
 race|                  |                  |    |        |                |                |
  black |   1.073456   .5150753      2.08  0.037   .0639273   2.082985
  other |   .815367   .4452979      1.83  0.067  -.0874008   1.688135
  smoke |   .8071996   .404446      2.00  0.046   .0145001   1.599899
   ptd |  1.281678   .4682699      2.77  0.006   .3759478   2.187408
    ht |  1.435227   .6482694      2.21  0.027   .1646414   2.705813
    ui |  .6576256   .4666192      1.41  0.159  -.2569313   1.572182
 _cons | -1.216781   .9556797     -1.27  0.203  -.3089878   .656317

Level 1 of race designates white, level 2 designates black, and level 3 designates other.

If we want to obtain the odds ratio for black smokers relative to white nonsmokers (the reference group), we type

```
. lincom 2.race + smoke, or
   ( 1) [low]2.race + [low]smoke = 0
```

```
   low |  Odds Ratio   Std. Err.    z    P>|z|   [95% Conf. Interval]
-----|--------------|------------------|-----|--------|------------------|------------------|
     (1) |   6.557805   4.744692     2.60  0.009   1.588176   27.07811
```

lincom computed \( \exp(\beta_{race=2} + \beta_{smoke}) = 6.56 \).

### 20.14 Obtaining nonlinear combinations of coefficients

lincom is limited to estimating linear combinations of coefficients, for example, \( 2.race + smoke \), or exponentiated linear combinations, as in the above. For general nonlinear combinations, use `nlcom`.
Example 18

Continuing our previous example: suppose that we wanted the ratio of the coefficients (and standard errors, Wald test, confidence interval, etc.) of blacks and races other than white and black:

```
    . nlcom _b[2.race]/_b[3.race]
    _nl_1: _b[2.race]/_b[3.race]
```

```
    low       Coef. Std. Err.   z    P>|z|   [95% Conf. Interval]
    _nl_1    1.316531   .7359262  1.79  0.074   -.1258574    2.75892
```

The Wald test given is that of the null hypothesis that the nonlinear combination is zero versus the two-sided alternative—this is probably not informative for a ratio. If we would instead like to test whether this ratio is one, we can rerun `nlcom`, this time subtracting one from our ratio estimate.

```
    . nlcom _b[2.race]/_b[3.race] - 1
    _nl_1: _b[2.race]/_b[3.race] - 1
```

```
    low       Coef. Std. Err.   z    P>|z|   [95% Conf. Interval]
    _nl_1    .3165314    .7359262   0.43  0.667   -1.125857    1.75892
```

We can interpret this as not much evidence that the “ratio minus 1” is different from zero, meaning that we cannot reject the null hypothesis that the ratio equals one.

When using `nlcom`, we needed to refer to the model coefficients by their “proper” names, for example, `_b[2.race]`, and not by the shorthand `2.race`, such as when using `lincom`. If we had typed

```
    . nlcom 2.race/3.race
```

Stata would have reported an error.

If you have difficulty determining what to type for a coefficient when using `lincom` or `nlcom` replay your results using the `coeflegend` option. Here are the results for our current estimates,

```
    . logit, coeflegend
    Logistic regression  Number of obs = 189
    LR chi2(8) = 37.12
    Prob > chi2 = 0.0000
    Log likelihood = -98.777998  Pseudo R2 =  0.1582
```

```
    low       Coef. Legend
    age    -.0464796   _b[age]
    lwd    .8420615   _b[lwd]
    race
        black    1.073456   _b[2.race]
        other    .815367   _b[3.race]
    smoke    .8071996   _b[smoke]
    ptd    1.281678   _b[ptd]
    ht    1.435227   _b[ht]
    ui    .6576256   _b[ui]
    _cons    -1.216781   _b[_cons]
```
20.15 Obtaining marginal means, adjusted predictions, and predictive margins

predict uses the current estimation results (the coefficients and the VCE) to estimate the value of statistics for observations in the data. lincom and nlcom use the current estimation results to estimate a specific linear or nonlinear expression of the coefficients. The margins command combines aspects of both and estimates margins of responses.

margins answers the question “What does my model have to say about such-and-such a group or such-and-such a person”, where such-and-such might be

- my estimation sample or another sample
- a sample with the values of some covariates fixed
- a sample evaluated at each level of a treatment
- a population represented by a complex survey sample
- someone who looks like the fifth person in my sample
- someone who looks like the mean of the covariates in my sample
- someone who looks like the median of the covariates in my sample
- someone who looks like the 25th percentile of the covariates in my sample
- someone who looks like some other function of the covariates in my sample
- a standardized population
- a balanced experimental design
- any combination of the above
- any comparison of the above

margins answers these questions either conditionally on fixed values of all covariates or averaged over the observations in a sample. It answers these questions about almost any predictions or any other response that you can calculate as a function of your estimated parameters—linear responses, probabilities, hazards, survival times, odds ratios, risk differences, etc. It answers these questions in terms of the response given covariate levels, or in terms of the change in the response for a change in levels (also known as marginal effects). It answers these questions providing standard errors, test statistics, and confidence intervals; and those statistics can take the covariates as given or adjust for sampling, also known as predictive margins and survey statistics.

A margin is a statistic based on a response for a fitted model calculated over a dataset in which some of or all the covariates are fixed at values different from what they really are.

Margins go by different names in different fields, and they can estimate many interesting statistics related to a fitted model. We discuss some common uses below; see [R] margins for more applications.

20.15.1 Obtaining estimated marginal means

A classic application of margins is to estimate the expected marginal means from a linear estimator as though the design for the covariates were balanced—assuming an equal number of observations for each unique combination of levels for the factor-variable covariates. These means have a long history in the study of ANOVA and MANOVA but are of limited use with nonexperimental data. For a discussion, see Obtaining margins as though the data were balanced in [R] margins and example 4 in [R] anova.

Estimated marginal means are also called “least-squares means”.

Consider an analysis of variance of the change in systolic blood pressure as determined by one of four drug treatments and adjusting for the patient’s disease (Afifi and Azen 1979).

```
. use http://www.stata-press.com/data/r13/systolic
(Systolic Blood Pressure Data)
. tabulate drug disease

<table>
<thead>
<tr>
<th>Drug Used</th>
<th>Patient’s Disease</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td>6</td>
<td>4</td>
<td>5</td>
<td>15</td>
</tr>
<tr>
<td>2</td>
<td></td>
<td>5</td>
<td>4</td>
<td>6</td>
<td>15</td>
</tr>
<tr>
<td>3</td>
<td></td>
<td>3</td>
<td>5</td>
<td>4</td>
<td>12</td>
</tr>
<tr>
<td>4</td>
<td></td>
<td>5</td>
<td>6</td>
<td>5</td>
<td>16</td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>19</td>
<td>19</td>
<td>20</td>
<td>58</td>
</tr>
</tbody>
</table>
```

```
. anova systolic drug##disease

Number of obs = 58  R-squared = 0.4560
Root MSE = 10.5096  Adj R-squared = 0.3259

<table>
<thead>
<tr>
<th>Source</th>
<th>Partial SS</th>
<th>df</th>
<th>MS</th>
<th>F</th>
<th>Prob &gt; F</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>4259.33851</td>
<td>11</td>
<td>387.212591</td>
<td>3.51</td>
<td>0.0013</td>
</tr>
<tr>
<td>drug</td>
<td>2997.47186</td>
<td>3</td>
<td>999.157287</td>
<td>9.05</td>
<td>0.0001</td>
</tr>
<tr>
<td>disease</td>
<td>415.873046</td>
<td>2</td>
<td>207.936523</td>
<td>1.88</td>
<td>0.1637</td>
</tr>
<tr>
<td>drug#disease</td>
<td>707.266259</td>
<td>6</td>
<td>117.87771</td>
<td>1.07</td>
<td>0.3958</td>
</tr>
<tr>
<td>Residual</td>
<td>5080.81667</td>
<td>46</td>
<td>110.452536</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>9340.15517</td>
<td>57</td>
<td>163.862371</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
```

Despite having randomized on drug, we see in the tabulation that our data are not balanced—for example, 12 patients were administered drug 3, whereas 16 were administered drug 4. The diseases are also not balanced across drugs. To estimate the marginal mean for each level of drug while treating the design as though it were balanced, we type

```
. margins drug, asbalanced

Adjusted predictions          Number of obs = 58
Expression : Linear prediction, predict()
at : drug (asbalanced)
disease (asbalanced)

|         | Margin  | Std. Err. | t     | P>|t|   [95% Conf. Interval] |
|---------|---------|-----------|-------|-------|------------------------|
| drug    |         |           |       |       |                        |
| 1       | 25.994444| 2.751008 | 9.45  | 0.000 | 20.45695 31.53194   |
| 2       | 26.55556| 2.751008 | 9.65  | 0.000 | 21.01806 32.09305  |
| 3       | 9.744444| 3.100558 | 3.14  | 0.003 | 3.503344 15.98554  |
| 4       | 13.54444| 2.637123 | 5.14  | 0.000 | 8.236191 18.8527    |
```

Assuming everyone in the sample were treated with drug 4 and that the diseases were equally distributed across the drug treatments, the expected mean change in pressure resulting from treatment with drug 4 is 13.54. Because we are treating the data as balanced, we could also say that 13.54 is the expected mean change resulting from drug 4 for any sample where an equal number of patients has each of the three diseases.

If we want an estimate of the mean that uses the distribution of diseases observed in the sample, we would remove the asbalanced option:
We can now say that a pressure change of 13.56 is expected if everyone in the sample is given drug 4 and the distribution of diseases is as observed in the sample.

The second set of margins are not usually called estimated marginal means because they do not impose a balanced design when estimating the mean. They are adjusted predictions that just happen to be means because the response is linear.

Neither of these values is the average pressure change for those taking drug 4 in our sample because margins treats everyone in the sample as having taken drug 4. Treating everyone as though they have taken each drug is what makes the means comparable. We are essentially standardizing on the values of all the other covariates in our model (in this example, just disease).

To obtain the observed mean for those taking drug 4, we must tell margins to treat drug 4 as its sample, which we do with the over() option.

```
. summarize systolic if drug==4
Variable |      Obs  Mean    Std. Dev.   Min    Max
---------+---------------------------------------
systolic |      16  13.5    9.323805    -5    27

. margins, over(drug)
Predictive margins Number of obs = 58
Expression : Linear prediction, predict()

<table>
<thead>
<tr>
<th></th>
<th>Delta-method</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Margin</td>
<td>Std. Err.</td>
<td>t</td>
<td>P&gt;</td>
<td>t</td>
</tr>
<tr>
<td>drug</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>26.06667</td>
<td>2.713577</td>
<td>9.61</td>
<td>0.000</td>
<td>20.60452</td>
</tr>
<tr>
<td>2</td>
<td>25.53333</td>
<td>2.713577</td>
<td>9.41</td>
<td>0.000</td>
<td>20.07119</td>
</tr>
<tr>
<td>3</td>
<td>8.75</td>
<td>3.033872</td>
<td>2.88</td>
<td>0.006</td>
<td>2.643133</td>
</tr>
<tr>
<td>4</td>
<td>13.5</td>
<td>2.62741</td>
<td>5.14</td>
<td>0.000</td>
<td>8.211298</td>
</tr>
</tbody>
</table>
```

The margin in the last line of the table matches the mean from summarize.

For many questions, we prefer one of the first two estimates of margins to the last one. If we compare drugs 3 and 4 from the last results, the 8.75 and 13.5 include both the effect from the drug and the differing distribution of diseases among patients taking drug 3 and drug 4 in our sample. Our first set of margins, those from margins drug, asbalanced, assumed that for both drug 3 and drug 4, we had an equal number of patients with each disease. Our second set of margins, those from margins drug, assumed that for both drug 3 and drug 4, we wanted the observed distribution of patients from the whole sample. By assuming a common distribution of diseases across the drugs, our first two sets of margins remove the effect of disease when we compare across drugs.
20.15.2 Obtaining adjusted predictions

We will use the term adjusted predictions to refer to margins that are evaluated at fixed values for all covariates. The `margins` command has a great deal of flexibility in letting you choose what those fixed values are. Consider a model of high blood pressure as a function of sex, age group, and body mass index (BMI, a common measure of weight relative to height; variable `bmi`). We will allow the effect of age to differ for males and females by interacting the age group and sex variables. We will also allow the effect of BMI to differ across all combinations of age group and sex by specifying a full factorial model.
```
use http://www.stata-press.com/data/r13/nhanes2
.logistic highbp sex##agegrp##c.bmi

Logistic regression
Number of obs = 10351
LR chi2(23) = 2521.83
Prob > chi2 = 0.0000
Log likelihood = -5789.851 Pseudo R2 = 0.1788

. logistic highbp sex##agegrp##c.bmi
  Logistic regression
  Number of obs = 10351
  LR chi2(23) = 2521.83
  Prob > chi2 = 0.0000
  Log likelihood = -5789.851 Pseudo R2 = 0.1788

  hibp | Odds Ratio Std. Err. z  P>|z|   [95% Conf. Interval]
----------|-----------------+------------------+---------+----------+-----------------------------+
  sex |                +------------------+---------+----------+-----------------------------+
    Female | .4012124 .2695666 -1.36 0.174 .107515 1.497199

  agegrp |                +------------------+---------+----------+-----------------------------+
    30-39 |  .8124869  .6162489 -0.27 0.784  .1837399 3.592768
    40-49 | 1.346976  1.101181  0.36 0.716  .2713222 6.687051
    50-59 | 5.415758  4.254136  2.15 0.032  1.161532 25.2515
    60-69 | 16.31623 10.09529  4.51 0.000  4.852423 54.86321
        70+ | 161.2491 130.7332  6.27 0.000   32.9142 789.9717

  sex#agegrp |                +------------------+---------+----------+-----------------------------+
    Female # |                +------------------+---------+----------+-----------------------------+
    30-39 | 1.441256  1.44721  0.36 0.716  .2013834 10.31475
    40-49 |  6.29497  6.575021  1.76 0.078  .8126879 48.75998
    50-59 |  4.377185  4.43183  1.46 0.145  .6016818 31.84366
    60-69 |  1.790026 1.502447  0.69 0.488  .3454684 9.27492
    70+ |  1.958758 2.165763 -1.47 0.140  .924297  41.0562

  bmi |                +------------------+---------+----------+-----------------------------+
        Female | .9809543 .0250973 -0.75 0.452  .9329775 1.031398

  sex#c.bmi |                +------------------+---------+----------+-----------------------------+
    Female |                +------------------+---------+----------+-----------------------------+
    30-39 | 1.021812  .0299468  0.74 0.462   .9647712 1.082225
    40-49 | 1.00982  .0315328  0.31 0.754   .9498702 1.073554
    50-59 |  .979291  .0298836 -0.69 0.493  .9224373 1.039649
    60-69 |  .9413883  .0228342 -2.49 0.013  .8976813  9.872234
        70+ |  .8738056  .0278416 -4.23 0.000  .8209061  .930114

  sex#agegrp#c.bmi |                +------------------+---------+----------+-----------------------------+
    Female # |                +------------------+---------+----------+-----------------------------+
    30-39 | 1.000676  .0377954  0.02 0.986  .9292736 1.077564
    40-49 |  .9702656  .0382854 -0.76 0.444  .8980559 1.048281
    50-59 |  .9852929  .0380345 -0.38 0.701  .9134969 1.062732
    60-69 |  1.028896  .0330473  0.89 0.375  .9661212  1.09575
    70+ |  1.12236  .0480541  2.70 0.007  1.032019 1.220609

  _cons | .0052191 .0024787 -11.07 0.000  .0020575  .0132388

```
We can evaluate the probability of having high blood pressure for each age group while holding the proportion of males and females and the value of bmi to its average by specifying the covariate agegrp to margins and including the option atmeans:

```
. margins agegrp, atmeans
Adjusted predictions Number of obs = 10351
Model VCE : OIM
Expression : Pr(highbp), predict()
at : 1.sex = .4748333 (mean)
     2.sex = .5251667 (mean)
     1.agegrp = .2241329 (mean)
     2.agegrp = .1566998 (mean)
     3.agegrp = .1228867 (mean)
     4.agegrp = .1247222 (mean)
     5.agegrp = .2763018 (mean)
     6.agegrp = .0952565 (mean)
     bmi = 25.5376 (mean)
```

The header of the table showed us the mean values of each covariate. These are the values at which the probabilities were evaluated. The mean values for the levels of agegrp appear in the header even though they were not used. agegrp assumed the values 1, 2, 3, 4, 5, and 6, as shown in the table. The means of the levels of agegrp are shown because we might have asked for more margins in the table, for example, margins sex agegrp.

The modeled probability is just below 25% for those under 40 years of age, and then increases fairly rapidly to 52% in the 50–59 age group. Above age 59, the probability remains under 67%. It is often easier for nonstatisticians to interpret the statistics computed by margins than the coefficients of a fitted model.

### 20.15.3 Obtaining predictive margins

Rather than evaluate the probability of having high blood pressure at one fixed point (the means), as we did above, we can evaluate the probability at the covariate values for each observation in our data and average those probabilities. Here is the modeled probability averaged over our sample:

```
. margins
Predictive margins Number of obs = 10351
Model VCE : OIM
Expression : Pr(highbp), predict()
```

```
<table>
<thead>
<tr>
<th></th>
<th>Delta-method</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Margin</td>
<td>Std. Err.</td>
<td>z</td>
<td>P&gt;</td>
<td>z</td>
</tr>
<tr>
<td>_cons</td>
<td>.4227611</td>
<td>.0042939</td>
<td>98.46</td>
<td>0.000</td>
<td>.4143451 .4311771</td>
</tr>
</tbody>
</table>
```
If we fix the level of \texttt{agegrp} to 1, compute the probability for each observation, and then average those probabilities, the result is the predictive margin for level 1 of \texttt{agegrp}. \texttt{margins}, by default, computes these margins for each level of each variable specified on the command line. Let’s compute the predictive margins for \texttt{agegrp}:

\begin{verbatim}
. margins agegrp
Predictive margins                  Number of obs   =        10351
Model VCE  : OIM
Expression : Pr(highbp), predict()

<table>
<thead>
<tr>
<th></th>
<th>Delta-method</th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Margin</td>
<td>Std. Err.</td>
<td>z</td>
<td>P&gt;</td>
</tr>
<tr>
<td>agegrp</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20-29</td>
<td>0.2030932</td>
<td>0.0087166</td>
<td>23.30</td>
<td>0.000</td>
</tr>
<tr>
<td>30-39</td>
<td>0.2829091</td>
<td>0.010318</td>
<td>27.42</td>
<td>0.000</td>
</tr>
<tr>
<td>40-49</td>
<td>0.3769536</td>
<td>0.0128744</td>
<td>29.28</td>
<td>0.000</td>
</tr>
<tr>
<td>50-59</td>
<td>0.5153439</td>
<td>0.0136201</td>
<td>37.84</td>
<td>0.000</td>
</tr>
<tr>
<td>60-69</td>
<td>0.5641065</td>
<td>0.0151371</td>
<td>43.18</td>
<td>0.000</td>
</tr>
<tr>
<td>70+</td>
<td>0.6535679</td>
<td>0.0151371</td>
<td>43.18</td>
<td>0.000</td>
</tr>
</tbody>
</table>
\end{verbatim}

One way of looking at predictive margins is that they answer the question “What would the average response (probability) be in my sample if everyone were in one age group?” Another way of looking at predictive margins is that they standardize the effect of being in an age group with the distribution of other covariate values in our sample. The margins above are comparable because only the level of \texttt{agegrp} is changing across the margins. They represent our sample because all the other covariates take on their values in the sample when the margins are evaluated.

The predictive margins in this table differ from the adjusted predictions we estimated in \[\text{U} \] 20.15.2 Obtaining adjusted predictions because the probability is a nonlinear function of the coefficients in a logistic model; see \textit{Example 3: Average response versus response at average} in \[\text{R} \] \texttt{margins} for details.

Our analysis so far has been a bit naïve. The dataset we are using is from the Second National Health and Nutrition Examination Survey (NHANES II). It has weights to make it representative of the population from which it was drawn as well as other survey characteristics—strata and primary sampling units. The data have already been \texttt{svyset}; see \[\text{SVY} \] \texttt{svyset}. We should take note of these characteristics and use the \texttt{svy} prefix when fitting our model.

\begin{verbatim}
. svy: logistic highbp sex##agegrp##c.bmi
(output omitted)
\end{verbatim}

If we were to repeat the command \texttt{margins agegrp}, we would see that our point estimates differ only a little, but our standard errors are generally larger.

We are not restricted to margining over a single factor variable. Let’s see if the pattern of high blood pressure over age groups differs for men and women. We do that by specifying the interaction of \texttt{sex} and \texttt{agegrp} to \texttt{margins}. We add the \texttt{vce(unconditional)} option to accommodate the survey design.
```
.margins sex#agegrp, vce(unconditional)
Predictive margins Number of obs = 10351
Expression : Pr(highbp), predict()

| sex#agegrp       | Linearized Margin | Std. Err. | t    | P>|t|   | [95% Conf. Interval] |
|------------------|-------------------|-----------|------|-------|----------------------|
| Male#20-29       | .2931664          | .0204899  | 14.31| 0.000 | .251377 .3349557     |
| Male#30-39       | .3664032          | .0241677  | 15.16| 0.000 | .3171128 .4156936    |
| Male#40-49       | .3945619          | .0240343  | 16.42| 0.000 | .3455435 .4435802    |
| Male#50-59       | .5376423          | .0295377  | 18.20| 0.000 | .4773997 .5978849    |
| Male#60-69       | .5780997          | .0224681  | 25.73| 0.000 | .5322756 .6239237    |
| Male#70+         | .6507023          | .0209322  | 31.09| 0.000 | .6080109 .6933938    |
| Female #20-29    | .1069761          | .0135978  | 7.87 | 0.000 | .0792432 .1347091    |
| Female #30-39    | .1898006          | .0143975  | 13.18| 0.000 | .1604367 .2191646    |
| Female #40-49    | .3250246          | .0236775  | 13.73| 0.000 | .276734 .3733152     |
| Female #50-59    | .4855339          | .03364    | 14.43| 0.000 | .4169247 .5541431    |
| Female #60-69    | .5441773          | .0186243  | 29.22| 0.000 | .5061928 .5821618    |
| Female#70+       | .6195342          | .0275568  | 22.48| 0.000 | .5633317 .6757367    |
```

Each line in the table corresponds to holding both `sex` and `agegrp` to fixed values while using the observed level of `bmi` to evaluate the probability and then averaging over the observations in the sample. To calculate the results in the first line of the table, `margins` fixed `sex = 1` and `agegrp = 1`, evaluated the probability for each observation, and then averaged the probabilities. All these margins reflect the observed distribution of `bmi` in the sample.

The first six lines represent males, and the second six lines represent females. Comparing males with females for the same age groups, males are almost three times as likely to have high blood pressure in the first age group ($0.293/0.107 = 2.7$), they are almost twice as likely in the second age group, and while the relative gap narrows, it is not until above age 70 that the probability for males drops below the probability for females.

Can the pattern of probabilities be affected by controlling one’s `bmi`? Let’s reevaluate the probabilities while holding `bmi` to two levels—20 (which is well within the normal range) and 30 (which is at the boundary between overweight and obese). We add the option `at(bmi=(20 30))` to set `bmi` first to 20 and then to 30.
. margins sex#agegrp, at(bmi=(20 30)) vce(unconditional)

Adjusted predictions
Expression : Pr(highbp), predict()
Number of obs = 10351

<p>|        | Marginal Std. Err. | t     | P&gt;|t|  | [95% Conf. Interval] |
|--------|--------------------|-------|------|----------------------|
| _at#sex#agegrp |                   |       |      |                      |
|        | Male # 1 #         |       |      |                      |
| 20-29  | .1392353 .0217328  | 6.41  | 0.000| .094911 .1835596    |
| 1 #    | Male # 2 #         |       |      |                      |
| 30-39  | .1714727 .0241469  | 7.10  | 0.000| .1222249 .2207205   |
| 1 #    | Male # 3 #         |       |      |                      |
| 40-49  | .1914061 .0366133  | 5.23  | 0.000| .1167329 .2660794   |
| 1 #    | Male # 4 #         |       |      |                      |
| 50-59  | .3380778 .0380474  | 8.89  | 0.000| .2604797 .4156759   |
| 1 #    | Male # 5 #         |       |      |                      |
| 60-69  | .4311378 .0371582  | 11.60 | 0.000| .3553532 .5069225   |
| 1 #    | Female # 1 #       |       |      |                      |
| 20-29  | .0439911 .0061833  | 7.11  | 0.000| .0313802 .056602    |
| 1 #    | Female # 2 #       |       |      |                      |
| 30-39  | .075806 .0134771   | 5.62  | 0.000| .0483193 .1032926   |
| 1 #    | Female # 3 #       |       |      |                      |
| 40-49  | .1941274 .0231872  | 8.37  | 0.000| .1468367 .2414181   |
| 1 #    | Female # 4 #       |       |      |                      |
| 50-59  | .3493224 .0405082  | 8.62  | 0.000| .2667055 .4319394   |
| 1 #    | Female # 5 #       |       |      |                      |
| 60-69  | .3897998 .0226443  | 17.21 | 0.000| .3436165 .4359831   |
| 1 #    | Female # 6 #       |       |      |                      |
| 70+    | .4599175 .0338926  | 13.57 | 0.000| .3907931 .5290419   |
| 2 #    | Male # 1 #         |       |      |                      |
| 20-29  | .4506376 .0370654  | 12.16 | 0.000| .3750422 .526233    |
| 2 #    | Male # 2 #         |       |      |                      |
| 30-39  | .569466 .04663     | 12.21 | 0.000| .4743635 .6645686   |
| 2 #    | Male # 3 #         |       |      |                      |
| 40-49  | .6042078 .039777   | 15.19 | 0.000| .5230821 .6853334   |
| 2 #    | Male # 4 #         |       |      |                      |
| 50-59  | .7268547 .0339618  | 21.40 | 0.000| .657589 .7961203    |
| 2 #    | Male # 5 #         |       |      |                      |
| 60-69  | .7131811 .0271145  | 26.30 | 0.000| .6578807 .7684816   |</p>
<table>
<thead>
<tr>
<th></th>
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<th>.0357432</th>
<th>19.15</th>
<th>0.000</th>
<th>.611435</th>
<th>.7572323</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2#Female#20–29</td>
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<td>.024609</td>
<td>6.66</td>
<td>0.000</td>
<td>.1136282</td>
<td>.2140088</td>
</tr>
<tr>
<td></td>
<td>2#Female#30–39</td>
<td>.3038899</td>
<td>.0271211</td>
<td>11.20</td>
<td>0.000</td>
<td>.2485761</td>
<td>.3592037</td>
</tr>
<tr>
<td></td>
<td>2#Female#40–49</td>
<td>.4523337</td>
<td>.0364949</td>
<td>12.39</td>
<td>0.000</td>
<td>.3779019</td>
<td>.5267655</td>
</tr>
<tr>
<td></td>
<td>2#Female#50–59</td>
<td>.6132219</td>
<td>.0376898</td>
<td>16.27</td>
<td>0.000</td>
<td>.536353</td>
<td>.6900908</td>
</tr>
<tr>
<td></td>
<td>2#Female#60–69</td>
<td>.68786</td>
<td>.0274712</td>
<td>25.04</td>
<td>0.000</td>
<td>.631832</td>
<td>.7438879</td>
</tr>
<tr>
<td></td>
<td>2#Female#70+</td>
<td>.7643662</td>
<td>.0343399</td>
<td>22.26</td>
<td>0.000</td>
<td>.6943296</td>
<td>.8344029</td>
</tr>
</tbody>
</table>

That is a lot of margins, but they are in sets of six age groups. The first six margins are men with a BMI of 20, the second six are women with a BMI of 20, the third six are men with a BMI of 30, and the last six are women with a BMI of 30. These margins tell a more complete story. The probability of high blood pressure is much lower for both men and women who maintain a BMI of 20. More interesting is that the relationship between men and women differs depending on BMI. While young men who maintain a BMI of 20 are still twice as likely as young women to have high blood pressure (0.139/0.044) and youngish men are over 50% more likely (0.171/0.076), the gap narrows substantially for men in the four older groups. The story is worse for those with a BMI of 30. Both men and women with a high BMI have a substantially increased risk of high blood pressure, with men ages 50–69 almost 10 percentage points higher than women. Before you dismiss these differences as caused by the usual attenuation of the logistic curve in the tails, recall that when we fit the model, we allowed the effect of bmi to be different for each combination of sex and agegrp.

You may have noticed that the header of the prior results says “Adjusted predictions” rather than “Predictive margins”. That is because our model has only three covariates, and we have fixed the values of each. margins is no longer averaging over the data, but is instead evaluating the margins at fixed points that we have requested. It lets us know that by changing the header.

We could post the results of margins and form linear combinations or perform tests about any of the assertions above; see Example 10: Testing margins—contrasts of margins in [R] margins.

There is much more to know about margins and the margins command. Consider the headings for the Remarks and examples section of [R] margins:

* Introduction
  * Obtaining margins of responses
    * Example 1: A simple case after regress
    * Example 2: A simple case after logistic
    * Example 3: Average response versus response at average
    * Example 4: Multiple margins from one command
    * Example 5: Margins with interaction terms
    * Example 6: Margins with continuous variables
    * Example 7: Margins of continuous variables
    * Example 8: Margins of interactions
    * Example 9: Decomposing margins
    * Example 10: Testing margins—contrasts of margins
    * Example 11: Margins of a specified prediction
    * Example 12: Margins of a specified expression
    * Example 13: Margins with multiple outcomes (responses)
20.16 Obtaining conditional and average marginal effects

Marginal effects measure the change in a response given a change in a covariate, which is to say that marginal effects are derivatives. As used here, marginal effects can also be the discrete change in a response as an indicator goes from 0 to 1. Some authors reserve the term marginal effect for the continuous change and use partial effect for the discrete change. We will not make that distinction. Regardless, marginal effects are most often used to make it easier to interpret how changes in covariates affect a nonlinear response from a fitted model—a probability, a censored dependent variable, a survival time, a hazard, etc.

Marginal effects can either be evaluated at a specified point for all the covariates in our model (conditional marginal effects) or be evaluated at the observed values of the covariates in a dataset and then averaged (average marginal effects).

To Stata, marginal effects are just margins whose response happens to be the derivative of another response. Those interested in marginal effects will be interested in all or most of [R] margins.
20.16.1 Obtaining conditional marginal effects

We call a marginal effect conditional when we fix the values of all the covariates and then take the derivative of the response with respect to a covariate. The mean of all covariates is often used as the fixed point, and this is sometimes called the marginal effect at the means.

Consider a simple probit model of union membership for women as a function of having graduated from college (collgrad), living in the South (south), tenure on the job (tenure), and the interaction of south and tenure. We are interested in how being in the South affects union membership. We fit the model by using an extract from 1988 of the U.S. National Longitudinal Survey of Labor Market Experience (see [XT] xt).

```
. use http://www.stata-press.com/data/r13/nlsw88b, clear
  (NLSW, 1988 extract)
. probit union i.collgrad i.south tenure south#c.tenure
Iteration 0:  log likelihood =  -1042.6816
Iteration 1:  log likelihood =  -997.71809
Iteration 2:  log likelihood =  -997.60984
Iteration 3:  log likelihood =  -997.60983
Probit regression                       Number of obs  =       1868
Model VCE : OIM                         LR chi2(4)    =     90.14
Expression : Pr(union), predict()       Prob > chi2   =     0.0000
Log likelihood =  -997.60983            Pseudo R2     =     0.0432

             Coef.  Std. Err.      z    P>|z|     [95% Conf. Interval]
------------- -------- ------------- ------ -------- ------------------
collgrad     .2783278   .0726167     3.83  0.000     0.1360018    .4206539
not grad    -          -           -          -           -          -
1.south     -.2534964   .1050552    -2.41  0.016    -.4594008   -.0475921
tenure      .0362944   .0068205     5.32  0.000     .0229264    .0496624
south#   tenure     -.0239785   .0119533    -2.01  0.045   -.0474066   -.0005504
1.south#  c.tenure    -0.8497418   .0664524   -12.79  0.000    -.9799862   -.7194974
_cons       -.8497418   .0664524   -12.79  0.000    -.9799862   -.7194974
```

Clearly, being located in the South decreases union membership. Using the dydx() and atmeans options of margins, we can ask how much it decreases membership by evaluating the marginal effect of being southern at the mean of all covariates:

```
. margins, dydx(south) atmeans
Conditional marginal effects                       Number of obs  =       1868
Model VCE : OIM
Expression : Pr(union), predict()
dy/dx w.r.t. : 1.south
at          : 0.collgrad    =    .7521413 (mean)
             1.collgrad    =    .2478587 (mean)
             0.south       =    .5744111 (mean)
             1.south       =    .4255889 (mean)
             tenure       =    6.571065 (mean)
             1.south#  tenure    =    6.571065 (mean)

                      Delta-method
      dy/dx      Std. Err.      z    P>|z|     [95% Conf. Interval]
------------- -------- ------------- ------ -------- ------------------
  1.south     -.1236055   .0194311   -6.36  0.000    -.1616896   -.0855215
```

Note: dy/dx for factor levels is the discrete change from the base level.
At the means of all the covariates, southern women are 12 percentage points less likely to be members of a union. This marginal effect includes both the direct effect of `i.south` and the interaction `south#c.tenure`.

As `margins` reports below the table, this change in the response is for the discrete change of going from not southern (0) to southern (1).

The header of `margins` tells us where the marginal effect was estimated. This margin fixes `tenure` to be 6.6 years. There is nothing special about this point. We could also evaluate the marginal effect at the median of `tenure`:

```
. margins, dydx(south) atmeans at((medians) _continuous)
```

### Conditional marginal effects

| 1.south | Delta-method dy/dx | Std. Err. | z     | P>|z|  | [95% Conf. Interval] |
|---------|---------------------|-----------|-------|------|----------------------|
| -0.1061338 | 0.0201722 | -5.26 | 0.000 | -0.1456706 | -0.066597 |

With `tenure` at its median of 4.67, the marginal effect is about 2 percentage points less than it was at the mean of 6.6.

When examining conditional marginal effects, it is often useful to evaluate them at a range of values for the covariates. We can do that by asking both for values of the indicator covariate `collgrad` and for a range of values for `tenure`:
. margins collgrad, dydx(south) at(tenure=(0(5)25))

Conditional marginal effects

Model VCE : OIM
Expression : Pr(union), predict()
dy/dx w.r.t. : 1.south

|            | dy/dx   | Std. Err. | z      | P>|z|   | [95% Conf. Interval] |
|------------|---------|-----------|--------|-------|---------------------|
| 1.south    |         |           |        |       |                     |
| 1._at      | tenure=0| -0.0627725| 0.0254161| -2.47 | 0.014              | -0.112587 -0.0129579 |
| 2._at      | tenure=5| -0.0791483| 0.0321151| -2.46 | 0.014              | -0.1420928 -0.162038 |
| 3._at      | tenure=10| -0.1031957| 0.0189184| -5.45 | 0.000              | -0.140275 -0.0661164 |
| 4._at      | tenure=15| -0.1256566| 0.0232385| -5.41 | 0.000              | -0.1712031 -0.0801101 |
| 5._at      | tenure=20| -0.1496772| 0.022222| -6.73 | 0.000              | -0.1932392 -0.1061151 |
| 6._at      | tenure=25| -0.2008801| 0.036154 | -5.56 | 0.000              | -0.271407 -0.1300196 |

Note: dy/dx for factor levels is the discrete change from the base level.

We now have a more complete picture of the effect that being in the South has on union participation. For those with no tenure and without a college degree (the first line in the table), being in the South decreases union participation by only 6 percentage points. For those with 25 years of tenure and with a college degree (the last line in the table), being in the South decreases participation by almost 33 percentage points. We can read the effect for any combination of tenure and college graduation status from the other lines in the table.

### 20.16.2 Obtaining average marginal effects

To compute average marginal effects, the marginal effect is first computed for each observation in the dataset and then averaged. If the sample over which we compute the average marginal effect represents a population, then we have estimated the marginal effect for the population.

We continue with our example of labor union participation.

. use http://www.stata-press.com/data/r13/nlsw88b
(NLSW, 1988 extract)
. probit union i.collgrad i.south tenure south#c.tenure
(output omitted)
To estimate the average marginal effect for each of our regressors, we type

```
.margins, dydx(*)
```

**Average marginal effects**

<table>
<thead>
<tr>
<th>Expression</th>
<th>Number of obs = 1868</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model VCE</td>
<td>OIM</td>
</tr>
<tr>
<td>Expression</td>
<td>Pr(union), predict()</td>
</tr>
<tr>
<td>dy/dx w.r.t.</td>
<td>1.collgrad 1.south tenure</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Delta-method</th>
</tr>
</thead>
<tbody>
<tr>
<td>dy/dx Std. Err. z P&gt;</td>
</tr>
<tr>
<td>-----------------------------</td>
</tr>
<tr>
<td>collgrad not grad</td>
</tr>
<tr>
<td>0.0878847 .0238065 3.69 0.000 .0412248 .1345447</td>
</tr>
<tr>
<td>1.south</td>
</tr>
<tr>
<td>-.126164 .0191504 -6.59 0.000 -.1636981 -.0886299</td>
</tr>
<tr>
<td>tenure</td>
</tr>
<tr>
<td>.0083571 .0016521 5.06 0.000 .005119 .0115951</td>
</tr>
</tbody>
</table>

**Note:** dy/dx for factor levels is the discrete change from the base level.

For this sample, the average marginal effect is very close to the marginal effect at the mean that we computed earlier. That is not always true; it depends on the distribution of the other covariates. The results also tell us that on average, for populations like the one from which our sample was drawn, union participation increases 0.8 percentage points for every year of tenure on the job. College graduates are, on average, 8.8 percentage points more likely to participate.

In the examples above, we treated the covariates in the sample as fixed and known. We could have accounted for the fact that this sample was drawn from a population and the covariates represent just one sample from that population. We do that by adding the `vce(robust)` or `vce(cluster clustvar)` option when fitting the model and the `vce(unconditional)` option when estimating the margins; see **Obtaining margins with survey data and representative samples** in [R] `margins`. It makes little difference in the examples above.

### 20.17 Obtaining pairwise comparisons

`pwcompare` performs pairwise comparisons across the levels of factor variables. `pwcompare` can compare estimated cell means, marginal means, intercepts, marginal intercepts, slopes, or marginal slopes—collectively called margins. `pwcompare` reports comparisons as contrasts (differences) of margins along with significance tests or confidence intervals for the contrasts. The tests and confidence intervals can be adjusted for multiple comparisons.

`pwcompare` is for use after an estimation command in which you have used factor variables in specifying the model. You could not use `pwcompare` after typing

```
.regress yield fertilizer1-fertilizer5
```

but you could use `pwcompare` after typing

```
.regress yield i.fertilizer
```

Below we fit a linear regression of wheat yield on type of fertilizer, and then we compare the mean yields for each pair of fertilizers and obtain *p*-values and confidence intervals adjusted for multiple comparisons using Tukey’s honestly significant difference.
. use http://www.stata-press.com/data/r13/yield
(Artificial wheat yield dataset)
. regress yield i.fertilizer

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 200</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1078.84207</td>
<td>4</td>
<td>269.710517</td>
<td>F( 4, 195) = 5.33</td>
</tr>
<tr>
<td>Residual</td>
<td>9859.55334</td>
<td>195</td>
<td>50.561812</td>
<td>Prob &gt; F = 0.0004</td>
</tr>
<tr>
<td>Total</td>
<td>10938.3954</td>
<td>199</td>
<td>54.9668111</td>
<td>Adj R-squared = 0.0801</td>
</tr>
</tbody>
</table>

| yield | Coef.  | Std. Err. | t    | P>|t| | [95% Conf. Interval] |
|-------|--------|-----------|------|-----|-----------------------|
| fertilizer |       |           |      |     |                       |
| 10-08-22 | 3.62272 | 1.589997  | 2.28 | 0.024 | .4869212 6.758518 |
| 16-04-08 | .4906299 | 1.589997 | 0.31 | 0.758 | -2.645169 3.626428 |
| 18-24-06 | 4.922803 | 1.589997 | 3.10 | 0.002 | 1.787005 8.058602 |
| 29-03-04 | -1.238328 | 1.589997 | -0.78 | 0.437 | -4.374127 1.89747 |
| _cons | 41.36243 | 1.124298 | 36.79 | 0.000 | 39.14509 43.57977 |
. pwcompare fertilizer, effects mcompare(tukey)
Pairwise comparisons of marginal linear predictions
Margins : asbalanced

<table>
<thead>
<tr>
<th>Number of Comparisons</th>
</tr>
</thead>
<tbody>
<tr>
<td>fertilizer 10</td>
</tr>
</tbody>
</table>

| Tukey Contrast Std. Err. t P>|t| [95% Conf. Interval] |
|-------------------------|-----------------|------|---------------------|
| fertilizer 10-08-22 vs 10-10-10 3.62272 1.589997 2.28 0.156 -.7552913 8.000731 |
| 10-10-10 16-04-08 vs .4906299 1.589997 0.31 0.998 -3.887381 4.868641 |
| 10-10-10 18-24-06 vs 4.922803 1.589997 3.10 0.019 .5447922 9.300815 |
| 10-08-22 16-04-08 vs -1.238328 1.589997 -0.78 0.936 -5.616339 3.139683 |
| 10-08-22 18-24-06 vs -3.13209 1.589997 -1.97 0.285 -7.510101 1.245921 |
| 10-08-22 29-03-04 vs 1.300083 1.589997 0.82 0.925 -3.077928 5.678095 |
| 10-08-22 16-04-08 vs -4.861048 1.589997 -3.06 0.021 -9.239059 -.4830368 |
| 18-24-06 16-04-08 vs 4.432173 1.589997 2.79 0.046 .0541623 8.810185 |
| 16-04-08 29-03-04 vs -1.728958 1.589997 -1.09 0.813 -6.106969 2.649053 |
| 29-03-04 18-24-06 vs -6.161132 1.589997 -3.87 0.001 -10.53914 -1.78312 |

See [R] pwcompare and [R] margins, pwcompare.

### 20.18 Obtaining contrasts, tests of interactions, and main effects

contrast estimates and tests contrasts—comparisons of levels of factor variables. It also performs joint tests of these contrasts and can produce ANOVA-style tests of main effects, interaction effects, simple effects, and nested effects. It can be used after most estimation commands.

contrast provides a set of “contrast operators” such as r., ar., and p.. These operators are prefixed onto variable names—for example, r.varname—to specify the contrasts to be performed. The operators can be used with the contrast and margins commands.

Below we fit a regression of cholesterol level on age group category.
. regress chol i.agegrp

The reported coefficients on `i.agegrp' will themselves be contrasts, namely, contrasts on the reference category. After estimation, if we wanted to compare the cell mean of each age group with that of the previous group, we would perform a reverse-adjacent contrast by typing

. contrast ar.agegrp

That is exactly what we will do:

. use http://www.stata-press.com/data/r13/cholesterol
(Artificial cholesterol data)
. regress chol i.agegrp

<table>
<thead>
<tr>
<th>Source</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>Number of obs = 75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>14943.3997</td>
<td>4</td>
<td>3735.84993</td>
<td>F( 4, 70) = 35.02</td>
</tr>
<tr>
<td>Residual</td>
<td>7468.21971</td>
<td>70</td>
<td>106.688853</td>
<td>Prob &gt; F = 0.0000</td>
</tr>
<tr>
<td>Total</td>
<td>22411.6194</td>
<td>74</td>
<td>302.859722</td>
<td>R-squared = 0.6668</td>
</tr>
</tbody>
</table>

| chol     | Coef.     | Std. Err. | t    | P>|t| | [95% Conf. Interval] |
|----------|-----------|-----------|------|------|---------------------|
| agegrp   |           |           |      |      |                     |
| 20-29    | 8.203575  | 3.771628  | 2.18 | 0.033| 0.6812991 15.72585 |
| 30-39    | 21.54105  | 3.771628  | 5.71 | 0.000| 14.01878 29.06333 |
| 40-59    | 30.15067  | 3.771628  | 7.99 | 0.000| 22.6284 37.67295 |
| 60-79    | 38.76221  | 3.771628  | 10.28| 0.000| 31.23993 46.28448 |
| _cons    | 180.5198  | 2.666944  | 67.69| 0.000| 175.2007 185.8388 |

. contrast ar.agegrp

Contrasts of marginal linear predictions
Margins : asbalanced

<table>
<thead>
<tr>
<th>df</th>
<th>F</th>
<th>P&gt;F</th>
</tr>
</thead>
<tbody>
<tr>
<td>agegrp</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(20-29 vs 10-19)</td>
<td>1</td>
<td>4.73</td>
</tr>
<tr>
<td>(30-39 vs 20-29)</td>
<td>1</td>
<td>12.51</td>
</tr>
<tr>
<td>(40-59 vs 30-39)</td>
<td>1</td>
<td>5.21</td>
</tr>
<tr>
<td>(60-79 vs 40-59)</td>
<td>1</td>
<td>5.21</td>
</tr>
<tr>
<td>Joint</td>
<td>4</td>
<td>35.02</td>
</tr>
<tr>
<td>Denominator</td>
<td>70</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Contrast</th>
<th>Std. Err.</th>
<th>[95% Conf. Interval]</th>
</tr>
</thead>
<tbody>
<tr>
<td>agegrp</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(20-29 vs 10-19)</td>
<td>8.203575</td>
<td>3.771628</td>
</tr>
<tr>
<td>(30-39 vs 20-29)</td>
<td>13.33748</td>
<td>3.771628</td>
</tr>
<tr>
<td>(40-59 vs 30-39)</td>
<td>8.60962</td>
<td>3.771628</td>
</tr>
<tr>
<td>(60-79 vs 40-59)</td>
<td>8.611533</td>
<td>3.771628</td>
</tr>
</tbody>
</table>

We could use orthogonal polynomial contrasts to test whether there is a linear, quadratic, or even higher-order trend in the estimated cell means.
> contrast p.agegrp, noeffects

Contrasts of marginal linear predictions

|        | df | F      | P>F
|--------|----|--------|---
| agegrp |    |        |   |
| (linear) | 1  | 139.11 | 0.0000 |
| (quadratic) | 1  | 0.15   | 0.6962 |
| (cubic)   | 1  | 0.37   | 0.5448 |
| (quartic) | 1  | 0.43   | 0.5153 |
| Joint     | 4  | 35.02  | 0.0000 |

Denominator | 70

You are not limited to using contrast in one-way models. Had we fit

> regress chol agegrp##race

we could contrast to obtain tests of the main effects and interaction effects.

> contrast agegrp##race

These results would be the same as would be reported by anova. We mention this because you can use contrast after any estimation command that allows factor variables and works with margins. You could type

> logistic highbp agegrp##race

> contrast agegrp##race

See [R] contrast and [R] margins, contrast.

## 20.19 Graphing margins, marginal effects, and contrasts

Using marginsplot, you can graph any of the results produced by margins, and because margins can replicate any of the results produced by pwcompare and contrast, you can graph any of the results produced by them, too.

In [U] 20.15.3 Obtaining predictive margins, we did the following:

> use http://www.stata-press.com/data/r13/nhanes2
> svy: logistic highbp sex#agegrp##c.bmi
> margins sex#agegrp, vce(unconditional)
We can now graph those results by typing

```
.marginsplot, xdimension(agegrp)
```

Variables that uniquely identify margins: sex agegrp

See [R] marginsplot. Mitchell (2012) shows how to make similar graphs for a variety of predictions and models.

### 20.20 Dynamic forecasts and simulations

The `forecast` suite of commands lets you obtain forecasts from forecast models, collections of equations that jointly determine the outcomes of one or more endogenous variables. You fit stochastic equations using estimation commands such as `regress` or `var`, then you add those results to your forecast model. You can also specify identities that define variables in terms of other variables, and you can also specify exogenous variables whose values are already known or otherwise determined by factors outside your model. `forecast` then solves the resulting system of equations to obtain forecasts.

`forecast` works with time-series and panel datasets, and you can obtain either dynamic or static forecasts. Dynamic forecasts use previous periods’ forecast values wherever lags appear in the model’s equations and thus allow you to obtain forecasts for multiple periods in the future. Static forecasts use previous periods’ actual values wherever lags appear in the model’s equations, so if you use lags, you cannot make predictions much beyond the end of the time horizon in your dataset. However, static forecasts are useful during model development.

You can incorporate outside information into your forecasts, and you can specify a future path for some of the model’s variables and obtain forecasts for the other variables conditional on that path. These features allow you to produce forecasts under different scenarios, and they allow you to explore how different policy interventions would affect your forecasts.

`forecast` also has the capability to produce confidence intervals around the forecasts. You can have `forecast` account for the sampling variance of the estimated parameters in the stochastic equations. There are two ways to account for an additive stochastic error term in the stochastic equations. You can request either that `forecast` assume the error terms are normally distributed and take draws from a random-number generator or that `forecast` take random samples from the pool of static-forecast residuals.

See [TS] forecast.
20.21 Obtaining robust variance estimates

Estimates of variance refer to estimated standard errors or, more completely, the estimated variance–covariance matrix of the estimators of which the standard errors are a subset, being the square root of the diagonal elements. Call this matrix the variance. All estimation commands produce an estimate of variance and, using that, produce confidence intervals and significance tests.

In addition to the conventional estimator of variance, there is another estimator that has been called by various names because it has been derived independently in different ways by different authors. Two popular names associated with the calculation are Huber and White, but it is also known as the sandwich estimator of variance (because of how the calculation formula physically appears) and the robust estimator of variance (because of claims made about it). Also, this estimator has an independent and long tradition in the survey literature.

The conventional estimator of variance is derived by starting with a model. Let’s start with the regression model

\[ y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2) \]

although it is not important for the discussion that we are using regression. Under the model-based approach, we assume that the model is true and thereby derive an estimator for \( \beta \) and its variance.

The estimator of the standard error of \( \hat{\beta} \) we develop is based on the assumption that the model is true in every detail. \( y_i \) is not exactly equal to \( x_i \beta \) (so that we would only need to solve an equation to obtain precisely that value of \( \beta \)) because the observed \( y_i \) has noise \( \epsilon_i \) added to it, the noise is Gaussian, and it has constant variance. That noise leads to the uncertainty about \( \beta \), and it is from the characteristics of that noise that we are able to calculate a sampling distribution for \( \hat{\beta} \).

The key thought here is that the standard error of \( \hat{\beta} \) arises because of \( \epsilon \) and is valid only because the model is absolutely, without question, true; we just do not happen to know the particular values of \( \beta \) and \( \sigma^2 \) that make the model true. The implication is that, in an infinite-sized sample, the estimator \( \hat{\beta} \) for \( \beta \) would converge to the true value of \( \beta \) and that its variance would go to 0.

Now here is another interpretation of the estimation problem: We are going to fit the model

\[ y_i = x_i b + e_i \]

and, to obtain estimates of \( b \), we are going to use the calculation formula

\[ \hat{b} = (X'X)^{-1}X'y \]

We have made no claims that the model is true or any claims about \( e_i \) or its distribution. We shifted our notation from \( \beta \) and \( \epsilon_i \) to \( b \) and \( e_i \) to emphasize this. All we have stated are the physical actions we intend to carry out on the data. Interestingly, it is possible to calculate a standard error for \( \hat{b} \) here. At least, it is possible if you will agree with us on what the standard error measures are.

We are going to define the standard error as measuring the standard error of the calculated \( \hat{b} \) if we were to repeat the data collection followed by estimation over and over again.

This is a different concept of the standard error from the conventional, model-based ideas, but it is related. Both measure uncertainty about \( b \) (or \( \beta \)). The regression model–based derivation states from where the variation arises and so can make grander statements about the applicability of the measured standard error. The weaker second interpretation makes fewer assumptions and so produces a standard error suitable for one purpose.

There is a subtle difference in interpretation of these identically calculated point estimates. \( \hat{\beta} \) is the estimate of \( \beta \) under the assumption that the model is true. \( \hat{b} \) is the estimate of \( b \), which is merely what the estimator would converge to if we collected more and more data.
Is the estimate of \( b \) unbiased? If we mean, “Does \( b = \beta \)?” that depends on whether the model is true. \( \hat{b} \) is, however, an unbiased estimate of \( b \), which admittedly is not saying much.

What if \( x \) and \( e \) are correlated? Don’t we have a problem then? We may have an interpretation problem—\( b \) may not measure what we want to measure, namely, \( \beta \)—but we measure \( \hat{b} \) to be such and such and expect, if the experiment and estimation were repeated, that we would observe results in the range we have reported.

So, we have two different understandings of what the parameters mean and how the variance in their estimators arises. However, both interpretations must confront the issue of how to make valid statistical inference about the coefficient estimates when the data do not come from either a simple random sample or the distribution of \((x_i, \epsilon_i)\) is not independent and identically distributed (i.i.d.). In essence, we need an estimator of the standard errors that is robust to this deviation from the standard case.

Hence, the name the robust estimate of variance; its associated authors are Huber (1967) and White (1980, 1982) (who developed it independently), although many others have extended its development, including Gail, Tan, and Piantadosi (1988); Kent (1982); Royall (1986); and Lin and Wei (1989). In the survey literature, this same estimator has been developed; see Kish and Frankel (1974), Fuller (1975), and Binder (1983). Most of Stata’s estimation commands can produce this alternative estimate of variance and do so via the `vce(robust)` option.

Halbert Lynn White Jr. (1950–2012) was born in Kansas City. After receiving economics degrees at Princeton and MIT, he taught and researched econometrics at the University of Rochester and, from 1979, at the University of California in San Diego. He also co-founded an economics and legal consulting firm known for its rigorous use of econometrics methods. His 1980 paper on heteroskedasticity introduced the use of robust covariance matrices to economists and passed 16,000 citations in Google Scholar in 2012. His 1982 paper on maximum likelihood estimation of misspecified models helped develop the now-common use of quasi–maximum likelihood estimation techniques. Later in his career, he explored the use of neural networks, nonparametric models, and time-series modeling of financial markets.

Among his many awards and distinctions, White was made a fellow of the American Academy of Arts and Sciences and the Econometric Society, and he won a fellowship from the John Simon Guggenheim Memorial Foundation. Had he not died prematurely, many scholars believe he would have eventually been awarded the Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel.

Aside from his academic work, White was an avid jazz musician who played with well-known jazz trombonist and fellow University of California at San Diego teacher Jimmy Cheatham.

Peter Jost Huber (1934– ) was born in Wohlen (Aargau, Switzerland). He gained mathematics degrees from ETH Zürich, including a PhD thesis on homotopy theory, and then studied statistics at Berkeley on postdoctoral fellowships. This visit yielded a celebrated 1964 paper on robust estimation, and Huber’s later monographs on robust statistics were crucial in directing that field. Thereafter his career took him back and forth across the Atlantic, with periods at Cornell, ETH Zürich, Harvard, MIT, and Bayreuth. His work has touched several other major parts of statistics, theoretical and applied, including regression, exploratory multivariate analysis, large datasets, and statistical computing. Huber also has a major long-standing interest in Babylonian astronomy.
20.21.1 Interpreting standard errors

Without `vce(robust)`, we get one measure of variance:

```
. use http://www.stata-press.com/data/r13/auto7
(1978 Automobile Data)
. regress mpg weight foreign
```

```
Source          SS       df       MS          Number of obs =    74
               | F(  2,  71) =  69.75
Model          1619.2877  2   809.643849  Prob > F =    0.0000
Residual      824.171761  71   11.608053   R-squared =    0.6627
       Total     2443.45946  73  33.4720474   Adj R-squared =    0.6532

mpg          Coef. Std. Err.     t    P>|t|     [95% Conf. Interval]
weight      -.0065879   .0006371 -10.34   0.000   -.0078583   -.0053175
foreign    -1.650029   1.075994  -1.53   0.130   -3.7955    .4954422
_cons        41.6797    2.165547  19.25   0.000   37.36172   45.99768
```

With `vce(robust)`, we get another:

```
. regress mpg weight foreign, vce(robust)
```

```
Linear regression                                Number of obs =    74
               F(  2,   71) =  73.81
               Prob > F =    0.0000
               R-squared =    0.6627
               Root MSE =    3.4071

mpg          Coef. Std. Err.     t    P>|t|     [95% Conf. Interval]
weight      -.0065879   .0005462 -12.06   0.000   -.007677    -.0054988
foreign    -1.650029   1.132566  -1.46   0.150   -3.908301    .6082424
_cons        41.6797    1.797553  23.19   0.000    38.09548   45.26392
```

Either way, the point estimates are the same. (See [R] `regress` for an example where specifying `vce(robust)` produces strikingly different standard errors.)

How do we interpret these results? Let’s consider the model-based interpretation. Suppose that

\[ y_i = x_i \beta + \epsilon_i, \]

where \((x_i, \epsilon_i)\) are independently and identically distributed (i.i.d.) with variance \(\sigma^2\). For the model-based interpretation, we also must assume that \(x_i\) and \(\epsilon_i\) are uncorrelated. With these assumptions and a few technical regularity conditions, our first regression gives us consistent parameter estimates and standard errors that we can use for valid statistical inference about the coefficients. Now suppose that we weaken our assumptions so that \((x_i, \epsilon_i)\) are independently and—but not necessarily—identically distributed. Our parameter estimates are still consistent, but the standard errors from the first regression can no longer be used to make valid inference. We need estimates of the standard errors that are robust to the fact that the error term is not identically distributed. The standard errors in our second regression are just what we need. We can use them to make valid statistical inference about our coefficients, even though our data are not identically distributed.

Now consider a non–model-based interpretation. If our data come from a survey design that ensures that \((x_i, \epsilon_i)\) are i.i.d., then we can use the nonrobust standard errors for valid statistical inference
about the population parameters $b$. For this interpretation, we do not need to assume that $x_i$ and $e_i$ are uncorrelated. If they are uncorrelated, the population parameters $b$ and the model parameters $\beta$ are the same. However, if they are correlated, then the population parameters $b$ that we are estimating are not the same as the model-based $\beta$. So, what we are estimating is different, but we still need standard errors that allow us to make valid statistical inference. So, if the process that we used to collect the data caused $(x_i,e_i)$ to be independently but not identically distributed, then we need to use the robust standard errors to make valid statistical inference about the population parameters $b$.

20.21.2 Correlated errors: cluster–robust standard errors

The robust estimator of variance has one feature that the conventional estimator does not have: the ability to relax the assumption of independence of the observations. That is, if you specify the `vce(cluster clustvar)` option, it can produce “correct” standard errors (in the measurement sense), even if the observations are correlated.

For the automobile data, it is difficult to believe that the models of the various manufacturers are truly independent. Manufacturers, after all, use common technology, engines, and drive trains across their model lines. The VW Dasher in the above regression has a measured residual of $-2.80$. Having been told that, do you really believe that the residual for the VW Rabbit is as likely to be above 0 as below? (The residual is $-2.32$.) Similarly, the measured residual for the Chevrolet Malibu is 1.27. Does that provide information about the expected value of the residual of the Chevrolet Monte Carlo (which turns out to be 1.53)?

We need to be careful about picking examples from data; we have not told you about the Datsun 210 and 510 (residuals $+8.28$ and $-1.01$) or the Cadillac Eldorado and Seville (residuals $-1.99$ and $+7.58$), but you should, at least, question the assumption of independence. It may be believable that the measured $\text{mpg}$ given the weight of one manufacturer’s vehicles is independent of other manufacturers’ vehicles, but it is at least questionable whether a manufacturer’s vehicles are independent of one another.

In commands with the `vce(robust)` option, another option—`vce(cluster clustvar)`—relaxes the independence assumption and requires only that the observations be independent across the clusters:

```
. regress mpg weight foreign, vce(cluster manufacturer)
```

```
Linear regression

Number of obs = 74
F( 2, 22) = 90.93
Prob > F = 0.0000
R-squared = 0.6627
Root MSE = 3.4071

(Std. Err. adjusted for 23 clusters in manufacturer)

| mpg  | Robust Coef. | Std. Err. | t     | P>|t|  | [95% Conf. Interval] |
|------|--------------|-----------|-------|------|----------------------|
| weight | -.0065879    | .0005339  | -12.34 | 0.000 | -.0076952 to -.0054806 |
| foreign| -1.650029    | 1.039033  | -1.59  | 0.127 | -3.804852 to .5047939 |
| _cons | 41.6797      | 1.844559  | 22.60  | 0.000 | 37.85432 to 45.50508  |
```

It turns out that, in these data, whether or not we specify `vce(cluster clustvar)` makes little difference. The VW and Chevrolet examples above were not representative; had they been, the confidence intervals would have widened. (In the above, `manuf` is a variable that takes on values such as “Chev.” or “VW”, recording the manufacturer of the vehicle. This variable was created from variable `make`, which contains values such as “Chev. Malibu” or “VW Rabbit”, by extracting the first word.)
As a demonstration of how well clustering can work, in [R] regress we fit a random-effects model with \texttt{regress, vce(robust)} and then compared the results with ordinary least squares and the GLS random-effects estimator. Here we will simply summarize the results.

We start with a dataset on 4,711 women aged 14–46 years. Subjects appear an average of 6.056 times in the data; there are a total of 28,534 observations. The model we use is log wage on age, age-squared, and job tenure. The focus of the example is the estimated coefficient on tenure. We obtain the following results:

<table>
<thead>
<tr>
<th>Estimator</th>
<th>Point estimate</th>
<th>Confidence interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Inappropriate) least squares</td>
<td>.039</td>
<td>[.038, .041]</td>
</tr>
<tr>
<td>Robust clustered</td>
<td>.039</td>
<td>[.036, .042]</td>
</tr>
<tr>
<td>GLS random effects</td>
<td>.026</td>
<td>[.025, .027]</td>
</tr>
</tbody>
</table>

Notice how well the robust clustered estimate does compared with the GLS random-effects model. We then run a Hausman specification test, obtaining $\chi^2(3) = 336.62$, which casts grave doubt on the assumptions justifying the use of the GLS estimator and hence on the GLS results. At this point, we will simply quote our comments:

Meanwhile, our robust regression results still stand, as long as we are careful about the interpretation. The correct interpretation is that, if the data collection were repeated (on women sampled the same way as in the original sample), and if we were to refit the model, 95% of the time we would expect the estimated coefficient on tenure to be in the range [.036, .042].

Even with robust regression, we must be careful about going beyond that statement. Here the Hausman test is probably picking up something that differs within and between person, which would cast doubt on our robust regression model in terms of interpreting [.036, .042] to contain the rate of return for keeping a job, economywide, for all women, without exception.

The formula for the robust estimator of variance is

$$
\hat{\mathcal{V}} = \hat{\mathcal{V}} \left( \sum_{j=1}^{N} u_j' u_j \right) \hat{\mathcal{V}}
$$

where $\hat{\mathcal{V}} = (-\partial^2 \ln L / \partial \beta^2)^{-1}$ (the conventional estimator of variance) and $u_j$ (a row vector) is the contribution from the $j$th observation to $\partial \ln L / \partial \beta$.

In the example above, observations are assumed to be independent. Assume for a moment that the observations denoted by $j$ are not independent but that they can be divided into $M$ groups $G_1, G_2, \ldots, G_M$ that are independent. The robust estimator of variance is

$$
\hat{\mathcal{V}} = \hat{\mathcal{V}} \left( \sum_{k=1}^{M} u_k^{(G)}' u_k^{(G)} \right) \hat{\mathcal{V}}
$$

where $u_k^{(G)}$ is the contribution of the $k$th group to $\partial \ln L / \partial \beta$. That is, application of the robust variance formula merely involves using a different decomposition of $\partial \ln L / \partial \beta$, namely, $u_k^{(G)}$, $k = 1, \ldots, M$ rather than $u_j$, $j = 1, \ldots, N$. Moreover, if the log-likelihood function is additive in the observations denoted by $j$

$$
\ln L = \sum_{j=1}^{N} \ln L_j
$$
then \( u_j = \frac{\partial \ln L_j}{\partial \beta} \), so

\[
\mathbf{u}^{(G)}_K = \sum_{j \in G_k} \mathbf{u}_j
\]

That is what the \texttt{vce(cluster clustvar)} option does. (This point was first made in writing by Rogers [1993], although he considered the point an obvious generalization of Huber [1967] and the calculation—implemented by Rogers—had appeared in Stata a year earlier.)

\section*{Technical note}

What is written above is asymptotically correct but ignores a finite-sample adjustment to \( \hat{V} \). For maximum likelihood estimators, when you specify \texttt{vce(robust)} but not \texttt{vce(cluster clustvar)}, a better estimate of variance is

\[
\hat{V}^* = \left\{ \frac{N}{N - 1} \right\} \hat{V}
\]

When you also specify the \texttt{vce(cluster clustvar)} option, this becomes

\[
\hat{V}^* = \left\{ \frac{M}{M - 1} \right\} \hat{V}
\]

For linear regression, the finite-sample adjustment is \( \frac{N}{N - k} \) without \texttt{vce(cluster clustvar)}—where \( k \) is the number of regressors—and \( \left\{ \frac{M}{M - 1} \right\} \left\{ \frac{N - 1}{N - k} \right\} \) with \texttt{vce(cluster clustvar)}. Also, two data-dependent modifications to the calculation for \( \hat{V}^* \), suggested by MacKinnon and White (1985), are also provided by \texttt{regress}; see \texttt{[R] regress}. Angrist and Pischke (2009, chap. 8) is devoted to robust covariance matrix estimation and offers practical guidance on the use of \texttt{vce(robust)} and \texttt{vce(cluster clustvar)} in both cross-sectional and panel-data applications.

\section{20.22 Obtaining scores}

Many of the estimation commands that provide the \texttt{vce(robust)} option also provide the ability to generate equation-level score variables via the \texttt{predict} command. With the \texttt{score} option, \texttt{predict} returns an important ingredient into the robust variance calculation that is sometimes useful in its own right. As explained in \section{20.21 Obtaining robust variance estimates} above, ignoring the finite-sample corrections, the robust estimate of variance is

\[
\hat{V} = \hat{V} \left( \sum_{j=1}^{N} u'_j u_j \right)
\]

where \( \hat{V} = \left( -\frac{\partial^2 \ln L}{\partial \beta^2} \right)^{-1} \) is the conventional estimator of variance. Let’s consider likelihood functions that are additive in the observations

\[
\ln L = \sum_{j=1}^{N} \ln L_j
\]

then \( u_j = \frac{\partial \ln L_j}{\partial \beta} \). In general, function \( L_j \) is a function of \( x_j \) and \( \beta \), \( L_j(\beta; x_j) \). For many likelihood functions, however, it is only the linear form \( x_j \beta \) that enters the function. In those cases,

\[
\frac{\partial \ln L_j(x_j \beta)}{\partial \beta} = \frac{\partial \ln L_j(x_j \beta)}{\partial (x_j \beta)} \frac{\partial (x_j \beta)}{\partial \beta} = \frac{\partial \ln L_j(x_j \beta)}{\partial (x_j \beta)} x_j
\]

By writing \( u_j = \frac{\partial \ln L_j(x_j \beta)}{\partial (x_j \beta)} \), this becomes simply \( u_j x_j \). Thus the formula for the robust estimate of variance can be rewritten as

\[
\hat{V} = \hat{V} \left( \sum_{j=1}^{N} u_j^2 x'_j x_j \right)
\]
We refer to \( u_j \) as the equation-level score (in the singular), and it is \( u_j \) that is returned when you use `predict` with the `score` option. \( u_j \) is like a residual in that

1. \( \sum_j u_j = 0 \) and
2. correlation of \( u_j \) and \( x_j \), calculated over \( j = 1, \ldots, N \), is 0.

In fact, for linear regression, \( u_j \) is the residual, normalized,

\[
\frac{\partial \ln L_j}{\partial (x_j \beta)} = \frac{\partial}{\partial (x_j \beta)} \ln f\left\{ \frac{(y_j - x_j \beta)}{\sigma} \right\} = \frac{(y_j - x_j \beta)}{\sigma}
\]

where \( f() \) is the standard normal density.

Example 19

`probit` provides both the `vce(robust)` option and `predict`, `score`. Equation-level scores play an important role in calculating the robust estimate of variance, but we can use `predict`, `score` regardless of whether we specify `vce(robust)`:  

```stata
. use http://www.stata-press.com/data/r13/auto2
. probit foreign mpg weight
Iteration 0: log likelihood = -45.03321
Iteration 1: log likelihood = -27.914626
Iteration 2: log likelihood = -26.858074
Iteration 3: log likelihood = -26.844197
Iteration 4: log likelihood = -26.844189
Iteration 5: log likelihood = -26.844189
Probit regression Number of obs = 74
LR chi2(2) = 36.38
Prob > chi2 = 0.0000
Log likelihood = -26.844189 Pseudo R2 = 0.4039

foreign Coef. Std. Err. z P>|z| [95% Conf. Interval]
mpg -.1039503 .0515689 -2.02 0.044 -.2050235 -.0028772
weight -.0023355 .0005661 -4.13 0.000 -.003445 -.0012261
_cons 8.275464 2.554142 3.24 0.001 3.269437 13.28149

. predict double u, score
. summarize u
   Variable | Obs Mean Std. Dev. Min Max
-------------+--------------------------------------------------
    u | 74  -6.66e-14    .5988325  -1.655439   1.660787

. correlate u mpg weight
(obs=74)
   u   mpg   weight
    u  1.0000     .
    mpg  0.0000  1.0000
   weight -0.0000 -0.8072  1.0000

. list make foreign mpg weight u if abs(u)>1.65
    +-------------+-------------+-------+-------+------+
    | make      | foreign | mpg   | weight|     u   |
    +-------------+-------------+-------+-------+------+
    24.    Ford Fiesta | Domestic  | 28    | 1,800 | -1.6554395
    64.    Peugeot 604 | Foreign  | 14    | 3,420 | 1.6607871
```


The light, high-mileage Ford Fiesta is surprisingly domestic, whereas the heavy, low-mileage Peugeot 604 is surprisingly foreign.

Technical note

For some estimation commands, one score is not enough. Consider a likelihood that can be written as $L_j(x_j, z_j, \beta_1, \beta_2)$, a function of two linear forms (or linear equations). Then $\partial \ln L_j / \partial \beta$ can be written $(\partial \ln L_j / \partial \beta_1, \partial \ln L_j / \partial \beta_2)$. Each of the components can in turn be written as $[\partial \ln L_j / \partial (\beta_1 x)] x = u_1 x$ and $[\partial \ln L_j / \partial (\beta_2 z)] z = u_2 z$. There are then two equation-level scores, $u_1$ and $u_2$, and, in general, there could be more.

Stata’s `streg, distribution(weibull)` command is an example of this: it estimates $\beta$ and a shape parameter, $\ln p$, the latter of which can be thought of as a degenerate linear form $(\ln p) z$ with $z = 1$. `predict, scores` after this command requires that you specify two new variable names, or you can specify `stub*`, which will generate two variables, `stub1` and `stub2`; the first will be defined containing $u_1$ — the score associated with $\beta$ — and the second will be defined containing $u_2$ — the score associated with $\ln p$.

Technical note

Using Stata’s matrix commands—see [P] `matrix`—we can make the robust variance calculation for ourselves and then compare it with that made by Stata.

```
. use http://www.stata-press.com/data/r13/auto2, clear
   (1978 Automobile Data)
. quietly probit foreign mpg weight
. predict double u, score
. matrix accum S = mpg weight [iweight=u^2*74/73]
   (obs=26.53642547)
. matrix rV = e(V)*S*e(V)
. matrix list rV
   symmetric rV[3,3]
   foreign: foreign: foreign:
     mpg    weight   _cons
  foreign:mpg .00352299
  foreign:weight .00002216  2.434e-07
  foreign:_cons -.14090346  -.00117031    6.4474174
. quietly probit foreign mpg weight, vce(robust)
. matrix list e(V)
   symmetric e(V)[3,3]
   foreign: foreign: foreign:
     mpg    weight   _cons
  foreign:mpg .00352299
  foreign:weight .00002216  2.434e-07
  foreign:_cons -.14090346  -.00117031    6.4474174
```

The results are the same.

There is an important lesson here for programmers. Given the scores, conventional variance estimates can be easily transformed to robust estimates. If we were writing a new estimation command, it would not be difficult to include a `vce(robust)` option.

It is, in fact, easy if we ignore clustering. With clustering, it is more work because the calculation involves forming sums within clusters. For programmers interested in implementing robust variance calculations, Stata provides an `_robust` command to ease the task. This is documented in [P] `_robust`. 
To use _robust, you first produce conventional results (a vector of coefficients and covariance matrix) along with a variable containing the scores $u_j$ (or variables if the likelihood function has more than one stub). You then call _robust, and it will transform your conventional variance estimate into the robust estimate. _robust will handle the work associated with clustering and the details of the finite-sample adjustment, and it will even label your output so that the word Robust appears above the standard error when the results are displayed.

Of course, this is all even easier if you write your commands with Stata’s ml maximum likelihood optimization, in which case you merely pass the vce(robust) option on to ml. ml will then call _robust itself and do all the work for you.

Technical note

For some estimation commands, predict, score computes parameter-level scores $\partial L_j/\partial \beta$ instead of equation-level scores $\partial L_j/\partial x_j \beta$. Those commands are

- asclogit
- asmprobit
- asroprobit
- nlogit
- stcox
- stcrreg
- mixed

These models share the characteristic that there are multiple observations per independent event.

In making the robust variance calculation, what are really needed are parameter-level scores $\partial L_j/\partial \beta$, and so you may be asking yourself why predict, score does not always produce parameter-level scores. In the usual case we can obtain them from equation-level scores via the chain rule, and fewer variables are required if we adopt this approach. In the cases above, however, the likelihood is calculated at the group level and is not split into contributions from the individual observations. Thus the chain rule cannot be used and we must use the parameter level scores directly.

_robust can be tricked into using them if each parameter appears to be in its own equation as a constant. This requires resetting the row and column stripes on the covariance matrix before _robust is called. The equation names for each row and column must each be unique and the variable names must all be _cons.

20.23 Weighted estimation

[U] 11.1.6 weight introduced the syntax for weights. Stata provides four kinds of weights: fweights, or frequency weights; pweights, or sampling weights; aweights, or analytic weights; and iweights, or importance weights. The syntax for using each is the same. Type

```
.regress y x1 x2
```

and you obtain unweighted estimates; type

```
.regress y x1 x2 [pweight=pop]
```

and you obtain (in this example) pweighted estimation.

The sections below explain how each type of weight is used in estimation.
20.23.1 Frequency weights

Frequency weights—\texttt{fweight}s—are integers and are nothing more than replication counts. The weight is statistically uninteresting, but from a data processing perspective it is important. Consider the following data

\[
\begin{array}{ccc}
22 & 1 & 0 \\
22 & 1 & 0 \\
22 & 1 & 1 \\
23 & 0 & 1 \\
23 & 0 & 1 \\
23 & 0 & 1 \\
\end{array}
\]

and the estimation command

\texttt{. regress y x1 x2}

Equivalent is the following, more compressed data

\[
\begin{array}{cccc}
22 & 1 & 0 & 2 \\
22 & 1 & 1 & 1 \\
23 & 0 & 1 & 3 \\
\end{array}
\]

and the corresponding estimation command

\texttt{. regress y x1 x2 [fweight=pop]}

When you specify frequency weights, you are treating each observation as one or more real observations.

⚠️ Technical note

You might occasionally run across a command that does not allow weights at all, especially among user-written commands. \texttt{expand} (see \texttt{[D] expand}) can be used with such commands to obtain frequency-weighted results. The \texttt{expand} command duplicates observations so that the data become self-weighting. Suppose that you want to run the command \texttt{usercmd}, which does something or other, and you would like to type \texttt{usercmd y x1 x2 [fw=pop]}. Unfortunately, \texttt{usercmd} does not allow weights. Instead, you type

\texttt{. expand pop}

\texttt{. usercmd y x1 x2}

to obtain your result. Moreover, there is an important principle here: the results of running any command with frequency weights should be the same as running the command on the unweighted, expanded data. Unweighted, duplicated data and frequency-weighted data are merely two ways of recording identical information.
20.23.2 Analytic weights

Analytic weights—analytic is a term we made up—statistically arise in one particular problem: linear regression on data that are themselves observed means. That is, think of the model

\[ y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2) \]

and now think about fitting this model on data \((\bar{y}_j, \bar{x}_j)\) that are themselves observed averages. For instance, a piece of the underlying data for \((y_i, x_i)\) might be \((3, 1), (4, 2),\) and \((2, 2)\), but you do not know that. Instead, you have one observation \{\((3 + 4 + 2)/3, (1 + 2 + 2)/3\)\} = \((3, 1.67)\) and know only that the \((3, 1.67)\) arose as the average of 3 underlying observations. All your data are like that.

`regress` with `aweights` is the solution to that problem:

```
. regress y x [aweights=pop]
```

There is a history of misusing such weights. A researcher does not have cell-mean data but instead has a probability-weighted random sample. Long before Stata existed, some researchers were using `aweights` to produce estimates from such samples. We will come back to this point in [U] 20.23.3 Sampling weights below.

Anyway, the statistical problem that `aweights` resolve can be written as

\[ y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2/w_i) \]

where the \(w_i\) are the analytic weights. The details of the solution are to make linear regression calculations using the weights as if they were `fweights` but to normalize them to sum to \(N\) before doing that.

Most commands that allow `aweights` handle them in this manner. That is, if you specify `aweights`, they are

1. normalized to sum to \(N\) and then
2. inserted in the calculation formulas in the same way as `fweights`.

20.23.3 Sampling weights

Sampling weights—probability weights or `pweights`—refer to probability-weighted random samples. Actually, what you specify in `[pweight=...]` is a variable recording the number of subjects in the full population that the sampled observation in your data represents. That is, an observation that had probability \(1/3\) of being included in your sample has `pweight 3`.

Some researchers have used `aweights` with this kind of data. If they do, they are probably making a mistake. Consider the regression model

\[ y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2) \]

Begin by considering the exact nature of the problem of fitting this model on cell-mean data—for which `aweights` are the solution: heteroskedasticity arising from the grouping. The error term \(\epsilon_i\) is homoskedastic (meaning that it has constant variance \(\sigma^2\)). Say that the first observation in the data is the mean of 3 underlying observations. Then

\[ y_1 = x_1 \beta + \epsilon_1, \quad \epsilon_i \sim N(0, \sigma^2) \]
\[ y_2 = x_2 \beta + \epsilon_2, \quad \epsilon_i \sim N(0, \sigma^2) \]
\[ y_3 = x_3 \beta + \epsilon_3, \quad \epsilon_i \sim N(0, \sigma^2) \]
and taking the mean

\[
(y_1 + y_2 + y_3)/3 = \left\{ (x_1 + x_2 + x_3)/3 \right\} \beta + (\epsilon_1 + \epsilon_2 + \epsilon_3)/3
\]

For another observation in the data—which may be the result of summing of a different number of observations—the variance will be different. Hence, the model for the data is

\[
y_j = x_j \beta + \epsilon_j, \quad \epsilon_j \sim N(0, \sigma^2/N_j)
\]

This makes intuitive sense. Consider 2 observations, one recording means over two subjects and the other means over 100,000 subjects. You would expect the variance of the residual to be less in the 100,000-subject observation; that is, there is more information in the 100,000-subject observation than in the two-subject observation.

Now instead say that you are fitting the same model, \(y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2)\), on probability-weighted data. Each observation in your data is one subject, but the different subjects have different chances of being included in your sample. Therefore, for each subject in your data

\[
y_i = x_i \beta + \epsilon_i, \quad \epsilon_i \sim N(0, \sigma^2)
\]

That is, there is no heteroskedasticity problem. The use of the aweighted estimator cannot be justified on these grounds.

As a matter of fact, from the argument just given, you do not need to adjust for the weights at all, although the argument does not justify not making an adjustment. If you do not adjust, you are holding tightly to the assumed truth of your model. Two issues arise when considering adjustment for sampling weights:

1. the efficiency of the point estimate \(\hat{\beta}\) of \(\beta\) and
2. the reported standard errors (and, more generally, the variance matrix of \(\hat{\beta}\)).

Efficiency argues in favor of adjustment, and that, by the way, is why many researchers have used aweights with pweighted data. The adjustment implied by pweights to the point estimates is the same as the adjustment implied by aweights.

With regard to the second issue, the use of aweights produces incorrect results because it interprets larger weights as designating more accurately measured points. For pweights, however, the point is no more accurately measured—it is still just one observation with one residual \(\epsilon_j\) and variance \(\sigma^2\). In [U] 20.21 Obtaining robust variance estimates above, we introduced another estimator of variance that measures the variation that would be observed if the data collection followed by the estimation were repeated. Those same formulas provide the solution to pweights, and they have the added advantage that they are not conditioned on the model’s being true. If we have any hopes of measuring the variation that would be observed were the data collection followed by estimation repeated, we must include the probability of the observations being sampled in the calculation.

In Stata, when you type

\[.\text{regress y x1 x2 [pw=pop]}\]

the results are the same as if you had typed

\[.\text{regress y x1 x2 [pw=pop], vce(robust)}\]
That is, specifying \texttt{pweight}s implies the \texttt{vce(robust)} option and, hence, the robust variance calculation (but weighted). In this example, we use \texttt{regress} simply for illustration. The same is true of \texttt{probit} and all of Stata’s estimation commands. Estimation commands that do not have a \texttt{vce(robust)} option (there are a few) do not allow \texttt{pweight}s.

\texttt{pweight}s are adequate for handling random samples where the probability of being sampled varies. \texttt{pweight}s may be all you need. If, however, the observations are not sampled independently but are sampled in groups—called clusters in the jargon—you should specify the estimator’s \texttt{vce(cluster clustvar)} option as well:

\begin{verbatim}
. regress y x1 x2 [pw=pop], vce(cluster block)
\end{verbatim}

There are two ways of thinking about this:

1. The robust estimator answers the question of which variation would be observed were the data collection followed by the estimation repeated; if that question is to be answered, the estimator must account for the clustered nature of how observations are selected. If observations 1 and 2 are in the same cluster, then you cannot select observation 1 without selecting observation 2 (and, by extension, you cannot select observations like 1 without selecting observations like 2).

2. If you prefer, you can think about potential correlations. Observations in the same cluster may not really be independent—that is an empirical question to be answered by the data. For instance, if the clusters are neighborhoods, it would not be surprising that the individual neighbors are similar in their income, their tastes, and their attitudes, and even more similar than two randomly drawn persons from the area at large with similar characteristics, such as age and sex.

Either way of thinking leads to the same (robust) estimator of variance.

Sampling weights usually arise from complex sampling designs, which often involve not only unequal probability sampling and cluster sampling but also stratified sampling. There is a family of commands in Stata designed to work with the features of complex survey data, and those are the commands that begin with \texttt{svy}. To fit a linear regression model with stratification, for example, you would use the \texttt{svy:regress} command.

\texttt{Non-svy} commands that allow \texttt{pweight}s and clustering give essentially identical results to the \texttt{svy} commands. If the sampling design is simple enough that it can be accommodated by the non-\texttt{svy} command, that is a fine way to perform the analysis. The \texttt{svy} commands differ in that they have more features, and they do all the little details correctly for real survey data. See \texttt{[SVY] survey} for a brief discussion of some of the issues involved in the analysis of survey data and a list of all the differences between the \texttt{svy} and non-\texttt{svy} commands.

Not all model estimation commands in Stata allow \texttt{pweight}s. This is often because they are computationally or statistically difficult to implement.

\subsection{20.23.4 Importance weights}

Stata’s \texttt{iweight}s—importance weights—are the emergency exit. These weights are for those who want to take control and create special effects. For example, programmers have used \texttt{regress} with \texttt{iweight}s to compute iteratively reweighted least-squares solutions for various problems.
iweights are treated much like aweights, except that they are not normalized. Stata’s iweight rule is that

1. the weights are not normalized and
2. they are generally inserted into calculation formulas in the same way as fweights. There are exceptions; see the Methods and formulas for the particular command.

iweights are used mostly by programmers who are often on the way to implementing one of the other kinds of weights.

### 20.24 A list of postestimation commands

The following commands can be used after estimation:

- **[R] contrast** contrasts and ANOVA-style joint tests of estimates
- **[R] estat ic** Akaike’s and Schwarz’s Bayesian information criteria (AIC and BIC)
- **[R] estat summarize** summary statistics for the estimation sample
- **[R] estat vce** variance–covariance matrix of the estimators (VCE)
- **[R] estat summarize** cataloging estimation results
- **[TS] forecast** dynamic forecasts and simulations
- **[R] hausman** Hausman specification test
- **[R] lincom** point estimates, standard errors, testing, and inference for linear combinations of coefficients
- **[R] linktest** specification link test for single-equation models
- **[R] lrtest** likelihood-ratio test
- **[R] margins** marginal means, predictive margins, and marginal effects
- **[R] marginsplot** graph the results from margins (profile plots, interaction plots, etc.)
- **[R] nlcom** point estimates, standard errors, testing, and inference for generalized predictions
- **[R] predict** predictions, residuals, influence statistics, and other diagnostic measures
- **[R] predictnl** point estimates, standard errors, testing, and inference for generalized predictions
- **[R] pwcompare** pairwise comparisons of estimates
- **[R] suest** seemingly unrelated estimation
- **[R] test** Wald tests of simple and composite linear hypotheses
- **[R] testnl** Wald tests of nonlinear hypotheses

Also see [U] 13.5 Accessing coefficients and standard errors for accessing coefficients and standard errors.

The commands above are general-purpose postestimation commands that can be used after almost all estimation commands. Many estimation commands provide other estimator-specific postestimation commands. The full list of postestimation commands available for an estimator can be found in an entry titled estimator postestimation that immediately follows each estimator’s entry in the reference manuals.
20.25 References


Baum, C. F. 2009. *An Introduction to Stata Programming*. College Station, TX: Stata Press.


