arfima postestimation — Postestimation tools for arfima

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Description

The following postestimation commands are of special interest after arfima:

Command	Description
estat acplot	estimate autocorrelations and autocovariances
irf	create and analyze IRFs
psdensity	estimate the spectral density

The following standard postestimation commands are also available:

Command	Description					
contrast	contrasts and ANOVA-style joint tests of estimates					
*estat ic	Akaike's and Schwarz's Bayesian information criteria (AIC and BIC)					
estat summarize	summary statistics for the estimation sample					
estat vce	variance-covariance matrix of the estimators (VCE)					
estimates	cataloging estimation results					
forecast	dynamic forecasts and simulations					
lincom	point estimates, standard errors, testing, and inference for linear combinations of coefficients					
lrtest	likelihood-ratio test					
*margins	marginal means, predictive margins, marginal effects, and average marginal effects					
*marginsplot	graph the results from margins (profile plots, interaction plots, etc.)					
*nlcom	point estimates, standard errors, testing, and inference for nonlinear combinations of coefficients					
predict	predictions, residuals, influence statistics, and other diagnostic measures					
*predictnl	point estimates, standard errors, testing, and inference for generalized predictions					
pwcompare	pairwise comparisons of estimates					
test	Wald tests of simple and composite linear hypotheses					
testnl	Wald tests of nonlinear hypotheses					

 * estat ic, margins, marginsplot, nlcom, and predictnl are not appropriate after arfima, mpl.

Syntax for predict

statistic	Description						
 1ain							
xb	predicted values; the default						
<u>r</u> esiduals	predicted innovations						
<u>rsta</u> ndard	standardized innovations						
<u>fdif</u> ference	fractionally differenced series						
These statistics are the estimation sar	available both in and out of sample; type predict if e(sample) if wanted only for nple.						
options	Description						

<pre>rmse([type] newvar)</pre>	put the estimated root mean squared error of the predicted statistic in a new variable; only permitted with options xb and residuals
dynamic(<i>datetime</i>)	forecast the time series starting at <i>datetime</i> ; only permitted with option xb

datetime is a # or a time literal, such as td(1jan1995) or tq(1995q1); see [D] datetime.

Menu for predict

Statistics > Postestimation > Predictions, residuals, etc.

Options for predict

Main

xb, the default, calculates the predictions for the level of *depvar*.

residuals calculates the predicted innovations.

rstandard calculates the standardized innovations.

fdifference calculates the fractionally differenced predictions of *depvar*.

Options

rmse([type] newvar) puts the root mean squared errors of the predicted statistics into the specified new variables. The root mean squared errors measure the variances due to the disturbances but do not account for estimation error. rmse() is only permitted with the xb and residuals options.

dynamic (datetime) specifies when predict starts producing dynamic forecasts. The specified datetime must be in the scale of the time variable specified in tsset, and the datetime must be inside a sample for which observations on the dependent variables are available. For example, dynamic(tq(2008q4)) causes dynamic predictions to begin in the fourth quarter of 2008, assuming that your time variable is quarterly; see [D] datetime. If the model contains exogenous variables, they must be present for the whole predicted sample. dynamic() may only be specified with xb.

Remarks and examples

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Remarks are presented under the following headings:

Forecasting after ARFIMA IRF results for ARFIMA

Forecasting after ARFIMA

We assume that you have already read [TS] **arfima**. In this section, we illustrate some of the features of predict after fitting an ARFIMA model using arfima.

Example 1

We have monthly data on the one-year Treasury bill secondary market rate imported from the Federal Reserve Bank (FRED) database using freduse; see Drukker (2006) and Stata YouTube video: Using freduse to download time-series data from the Federal Reserve for an introduction to freduse. Below we fit an ARFIMA model with two autoregressive terms and one moving-average term to the data.

	www.stata-pres r treasury bil				onthly 195	9-20	01)
. arfima tbly Iteration 0: Iteration 1: Iteration 2: Iteration 3: Iteration 4: Iteration 5: Iteration 6: Iteration 6: Iteration 7: Iteration 9: Refining estiv Iteration 0: Iteration 1: ARFIMA regres	log likelind log likelind log likelind log likelind log likelind log likelind log likelind log likelind mates: log likelind log likelind	(1) dd = -235.3 dd = -235.2 dd = -235.2 dd = -235.1 dd = -235.1	6104 (b. 5974 (b. 2544 (b. 3353 3063 2108 1917 1869 1868	acked up) acked up) acked up)			
Sample: 1959m				Numbe	er of obs	=	506
bumpio: itootm	2001m0				chi2(4)	=	1864.15
Log likelihoo	d = -235.11868	3		Prob	> chi2	=	0.0000
tb1yr	Coef.	OIM Std. Err.	Z	P> z	[95% C	onf.	Interval]
tb1yr cons	5.496709	2.920357	1.88	0.060	22708	64	11.2205
ARFIMA							
ar L1. L2.	.2326107 .3885212	.1136655 .0835665	2.05 4.65	0.041 0.000	.00983		.4553911 .5523086
ma L1.	.7755848	.0669562	11.58	0.000	.64435	31	.9068166
d	.4606489	.0646542	7.12	0.000	.3339	29	.5873688
/sigma2	. 1466495	.009232	15.88	0.000	.12855	51	.1647439

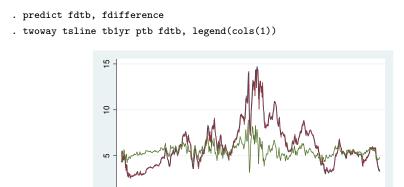
Note: The test of the variance against zero is one sided, and the two-sided confidence interval is truncated at zero.

All the parameters are statistically significant at the 5% level, and they indicate a high degree of dependence in the series. In fact, the confidence interval for the fractional-difference parameter d indicates that the series may be nonstationary. We will proceed as if the series is stationary and suppose that it is fractionally integrated of order 0.46.

We begin our postestimation analysis by predicting the series in sample:

. predict ptb (option xb assumed)

We continue by using the estimated fractional-difference parameter to fractionally difference the original series and by plotting the original series, the predicted series, and the fractionally differenced series. See [TS] **arfima** for a definition of the fractional-difference operator.



1970m1

xb prediction

The above graph shows that the in-sample predictions appear to track the original series well and that the fractionally differenced series looks much more like a stationary series than does the original. \triangleleft

tb1yr fractionally differenced

1980m1

month
1-Year Treasury Bill: Secondary Market Rate

1990m1

2000m1

Example 2

In this example, we use the above estimates to produce a dynamic forecast and a confidence interval for the forecast for the one-year treasury bill rate and plot them.

We begin by extending the dataset and using predict to put the dynamic forecast in the new ftb variable and the root mean squared error of the forecast in the new rtb variable. (As discussed in *Methods and formulas*, the root mean squared error of the forecast accounts for the idiosyncratic error but not for the estimation error.)

```
. tsappend, add(12)
```

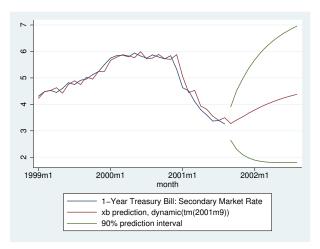
0 -1960m1

```
. predict ftb, xb dynamic(tm(2001m9)) rmse(rtb)
```

Now we compute a 90% confidence interval around the dynamic forecast and plot the original series, the in-sample forecast, the dynamic forecast, and the confidence interval of the dynamic forecast.

```
. scalar z = invnormal(0.95)
. generate lb = ftb - z*rtb if month>=tm(2001m9)
(506 missing values generated)
. generate ub = ftb + z*rtb if month>=tm(2001m9)
(506 missing values generated)
. twoway tsline tb1yr ftb if month>tm(1998m12) ||
> tsrline lb ub if month>=tm(2001m9),
> legend(cols(1) label(3 "90% prediction interval"))
```

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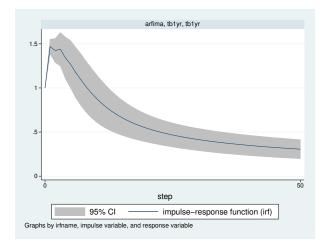
IRF results for ARFIMA

We assume that you have already read [TS] **irf** and [TS] **irf create**. In this section, we illustrate how to calculate the implulse–response function (IRF) of an ARFIMA model.

Example 3

Here we use the estimates obtained in example 1 to calculate the IRF of the ARFIMA model; see [TS] **irf** and [TS] **irf** create for more details about IRFs.

```
. irf create arfima, step(50) set(myirf)
(file myirf.irf created)
(file myirf.irf now active)
(file myirf.irf updated)
. irf graph irf
```



The figure shows that a shock to tb1yr causes an initial spike in tb1yr, after which the impact of the shock starts decaying slowly. This behavior is characteristic of long-memory processes.

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Methods and formulas

Denote γ_h , h = 1, ..., t, to be the autocovariance function of the ARFIMA(p, d, q) process for two observations, y_t and y_{t-h} , h time periods apart. The covariance matrix V of the process of length T has a Toeplitz structure of

$$\mathbf{V} = \begin{pmatrix} \gamma_0 & \gamma_1 & \gamma_2 & \cdots & \gamma_{T-1} \\ \gamma_1 & \gamma_0 & \gamma_1 & \cdots & \gamma_{T-2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \gamma_{T-1} & \gamma_{T-2} & \gamma_{T-3} & \cdots & \gamma_0 \end{pmatrix}$$

where the process variance is $\gamma_0 = \text{Var}(y_t)$. We factor $\mathbf{V} = \mathbf{LDL}'$, where \mathbf{L} is lower triangular and $\mathbf{D} = \text{Diag}(\nu_t)$. The structure of \mathbf{L}^{-1} is of importance.

$$\mathbf{L}^{-1} = \begin{pmatrix} 1 & 0 & 0 & \dots & 0 & 0 \\ -\tau_{1,1} & 1 & 0 & \dots & 0 & 0 \\ -\tau_{2,2} & -\tau_{2,1} & 1 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ -\tau_{T-1,T-1} & -\tau_{T-1,T-2} & -\tau_{T-1,T-2} & \dots & -\tau_{T-1,1} & 1 \end{pmatrix}$$

Let $z_t = y_t - \mathbf{x}_t \beta$. The best linear predictor of z_{t+1} based on z_1, z_2, \ldots, z_t is $\hat{z}_{t+1} = \sum_{k=1}^t \tau_{t,k} z_{t-k+1}$. Define $-\tau_t = (-\tau_{t,t}, -\tau_{t,t-1}, \ldots, -\tau_{t-1,1})$ to be the *t*th row of \mathbf{L}^{-1} up to, but not including, the diagonal. Then $\tau_t = \mathbf{V}_t^{-1} \gamma_t$, where \mathbf{V}_t is the $t \times t$ upper left submatrix of \mathbf{V} and $\gamma_t = (\gamma_1, \gamma_2, \ldots, \gamma_t)'$. Hence, the best linear predictor of the innovations is computed as $\hat{\boldsymbol{\epsilon}} = \mathbf{L}^{-1} \mathbf{z}$, and the one-step predictions are $\hat{\mathbf{y}} = \hat{\boldsymbol{\epsilon}} + \mathbf{X} \hat{\boldsymbol{\beta}}$. In practice, the computation is

$$\widehat{\mathbf{y}} = \widehat{\mathbf{L}}^{-1} \left(\mathbf{y} - \mathbf{X} \widehat{\boldsymbol{eta}} \right) + \mathbf{X} \widehat{\boldsymbol{eta}}$$

where $\hat{\mathbf{L}}$ and $\hat{\mathbf{V}}$ are computed from the maximum likelihood estimates. We use the Durbin–Levinson algorithm (Palma 2007; Golub and Van Loan 1996) to factor $\hat{\mathbf{V}}$, invert $\hat{\mathbf{L}}$, and scale $\mathbf{y} - \mathbf{X}\hat{\boldsymbol{\beta}}$ using only the vector of estimated autocovariances $\hat{\boldsymbol{\gamma}}$.

The prediction error variances of the one-step predictions are computed recursively in the Durbin–Levinson algorithm. They are the ν_t elements in the diagonal matrix **D** computed from the Cholesky factorization of **V**. The recursive formula is $\nu_0 = \gamma_0$, and $\nu_t = \nu_{t-1}(1 - \tau_{t,t}^2)$.

Forecasting is carried out as described by Beran (1994, sec. 8.7), $\hat{\mathbf{z}}_{T+k} = \tilde{\gamma}'_k \hat{\mathbf{V}}^{-1} \hat{\mathbf{z}}$, where $\tilde{\gamma}'_k = (\hat{\gamma}_{T+k-1}, \hat{\gamma}_{T+k-2}, \dots, \hat{\gamma}_k)$. The forecast mean squared error is computed as $MSE(\hat{\mathbf{z}}_{T+k}) = \hat{\gamma}_0 - \tilde{\gamma}'_k \hat{\mathbf{V}}^{-1} \tilde{\boldsymbol{\gamma}}_k$. Computation of $\hat{\mathbf{V}}^{-1} \tilde{\boldsymbol{\gamma}}_k$ is carried out efficiently using algorithm 4.7.2 of Golub and Van Loan (1996).

References

Beran, J. 1994. Statistics for Long-Memory Processes. Boca Raton: Chapman & Hall/CRC.
Drukker, D. M. 2006. Importing Federal Reserve economic data. Stata Journal 6: 384–386.
Golub, G. H., and C. F. Van Loan. 1996. Matrix Computations. 3rd ed. Baltimore: Johns Hopkins University Press.
Palma, W. 2007. Long-Memory Time Series: Theory and Methods. Hoboken, NJ: Wiley.

Also see

- [TS] arfima Autoregressive fractionally integrated moving-average models
- [TS] estat acplot Plot parametric autocorrelation and autocovariance functions
- [TS] irf Create and analyze IRFs, dynamic-multiplier functions, and FEVDs
- [TS] psdensity Parametric spectral density estimation after arima, arfima, and ucm
- [U] 20 Estimation and postestimation commands