example 31g — Two-factor measurement model (generalized response)

Description Remarks and examples Also see

## Description

We demonstrate a two-factor generalized linear measurement model with the same data used in [SEM] example 29g:

```
. use http://www.stata-press.com/data/r13/gsem_cfa
(Fictional math abilities data)
. describe
Contains data from http://www.stata-press.com/data/r13/gsem_cfa.dta
  obs:
                  500
                                                Fictional math abilities data
 vars:
                   19
                                                21 Mar 2013 10:38
 size:
               18,500
                                                (_dta has notes)
               storage
                         display
                                     value
variable name
                         format
                                     label
                                                variable label
                type
school
                byte
                         %9.0g
                                                School id
                                                Student id
id
                long
                         %9.0g
q1
                byte
                         %9.0g
                                    result
                                                al correct
q2
                byte
                         %9.0g
                                    result
                                                q2 correct
                                                q3 correct
q3
                byte
                         %9.0g
                                    result
q4
                byte
                         %9.0g
                                    result
                                                q4 correct
                         %9.0g
q5
                byte
                                    result
                                                q5 correct
q6
                byte
                         %9.0g
                                    result
                                                q6 correct
                byte
                         %9.0g
                                    result
                                                q7 correct
q7
8p
                byte
                         %9.0g
                                    result
                                                q8 correct
att1
                float
                         %26.0g
                                     agree
                                                Skills taught in math class will
                                                  help me get a better job.
att2
                float
                         %26.0g
                                     agree
                                                Math is important in everyday
                                                  life
att3
                float
                         %26.0g
                                                Working math problems makes me
                                     agree
                                                  anxious.
att4
                float
                         %26.0g
                                                Math has always been my worst
                                     agree
                                                  subject.
att5
                float
                         %26.0g
                                                I am able to learn new math
                                     agree
                                                  concepts easily.
test1
                byte
                         %9.0g
                                                Score, math test 1
test2
                 byte
                         %9.0g
                                                Score, math test 2
test3
                 byte
                         %9.0g
                                                Score, math test 3
test4
                         %9.0g
                                                Score, math test 4
                byte
```

Sorted by:

. notes

\_dta:

- 1. Fictional data on math ability and attitudes of 500 students from 20 schools.
- 2. Variables q1-q8 are incorrect/correct (0/1) on individual math questions.
- Variables att1-att5 are items from a Likert scale measuring each student's attitude toward math.
- 4. Variables test1-test4 are test scores from tests of four different aspects of mathematical abilities. Range of scores: 0-100.

These data record results from a fictional instrument measuring mathematical ability. Variables q1 through q8 are the items from the instrument.

In this example, we will also be using variables att1 through att5. These are five Likert-scale questions measuring each student's attitude toward math.

See Multiple-factor measurement models in [SEM] intro 5 for background.

## **Remarks and examples**

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Remarks are presented under the following headings:

Fitting the two-factor model Fitting the model with the Builder

#### Fitting the two-factor model

We extend the measurement model fit in [SEM] example 29g from one factor, math ability, to two factors, math ability and attitude. The model we wish to fit is



In this model, mathematical ability affects the correctness of the answers to the items just as previously. The new component, attitude toward mathematics, is correlated with math ability. We expect this correlation to be positive, but that is yet to be determined.

What is important about the attitudinal questions is that the responses are ordinal, that is, the ordering of the possible answers is significant. In other cases, we might have a categorical variable taking on, say, five values; even if the values are 1, 2, 3, 4, and 5, there is no case in which answer 5 is greater than answer 4, answer 4 is greater than answer 3, and so on.

For our attitude measures, however, response 5 signifies strong agreement with a statement and 1 signifies strong disagreement. We handle the ordinal property by specifying that the attitudinal responses are family ordinal, link logit, also known as ordered logit or ordinal logistic regression, and also known in Stata circles as ologit.

In the command language, to fit a one-factor measurement model with math ability, we would type

```
gsem (MathAb -> q1-q8), logit
```

To include the second factor, attitude correlated with math ability, we would type

The covariance between MathAtt and MathAb does not even appear in the command! That is because latent exogenous variables are assumed to be correlated in the command language unless you specify otherwise; in path diagrams, such variables are correlated only if a curved path is drawn between them.

There is another, minor difference in syntax between the one-factor and two-factor models that is worth your attention. Notice that the logit was outside the parentheses in the command to fit the one-factor model, but it is inside the parentheses in the command to fit the two-factor model. Actually, logit could have appeared inside the parentheses to fit the one-factor model. When options appear inside parentheses, they affect only what is specified inside the parentheses. When they appear outside parentheses, they affect all parenthetical specifications.

To obtain the estimates of the two-factor model, we type

```
. gsem (MathAb -> q1-q8, logit)
       (MathAtt -> att1-att5, ologit)
Fitting fixed-effects model:
Iteration 0:
               \log likelihood = -6629.7253
Iteration 1:
               log likelihood = -6628.7848
Iteration 2:
               log likelihood = -6628.7848
Refining starting values:
Grid node 0:
               \log likelihood = -6457.4584
Fitting full model:
Iteration 0:
               \log likelihood = -6457.4584
Iteration 1:
               \log likelihood = -6437.9594
Iteration 2:
               log likelihood = -6400.2731
Iteration 3:
               log likelihood = -6396.3795
               \log likelihood = -6394.5787
Iteration 4:
Iteration 5:
               \log likelihood = -6394.4019
Iteration 6:
               \log likelihood = -6394.3923
Iteration 7:
               \log likelihood = -6394.3923
Generalized structural equation model
                                                                             500
                                                   Number of obs
                                                                    _
Log likelihood = -6394.3923
 (1)
       [q1]MathAb = 1
 (2)
       [att1]MathAtt = 1
                    Coef.
                             Std. Err.
                                                 P>|z|
                                                            [95% Conf. Interval]
                                            z
q1 <-
      MathAb
                            (constrained)
                        1
                  .0446118
                             .1272964
                                          0.35
                                                 0.726
                                                           -.2048845
                                                                        .2941082
       _cons
q2 <-
      MathAb
                 .3446081
                             .1050264
                                          3.28
                                                 0.001
                                                            .1387601
                                                                        .5504562
       _cons
                -.4572215
                             .0979965
                                         -4.67
                                                 0.000
                                                           -.6492911
                                                                        -.265152
```

~2 <	_									
42 V	- MathAb	.5445245	1386993	3.93	0.000	.272679	.8163701			
	_cons	.1591406	.1033116	1.54	0.123	0433464	.3616276			
	_									
91 .	MathAb	.2858874	.0948553	3.01	0.003	.0999743	.4718004			
	_cons	3196648	.0947684	-3.37	0.001	5054075	1339222			
a5 <	_									
40	MathAb	.8174803	.1867024	4.38	0.000	.4515504	1.18341			
	_cons	04543	.116575	-0.39	0.697	2739127	.1830527			
q6 <	_									
•	MathAb	.6030448	.1471951	4.10	0.000	.3145478	.8915419			
	_cons	309992	.1070853	-2.89	0.004	5198753	1001086			
q7 <-	_									
•	MathAb	.72084	.1713095	4.21	0.000	.3850796	1.056601			
	_cons	.1047265	.1116494	0.94	0.348	1141023	.3235552			
q8 <	_									
•	MathAb	.5814761	.1426727	4.08	0.000	.3018428	.8611094			
	_cons	0250442	.1045134	-0.24	0.811	2298868	.1797983			
att1	<-									
	MathAtt	1 (constrained)								
att2	<-									
	MathAtt	.3788714	.0971223	3.90	0.000	.1885152	.5692276			
att3	<-									
	MathAtt	-1.592717	.3614859	-4.41	0.000	-2.301216	8842173			
att4	<-									
	MathAtt	8100107	.153064	-5.29	0.000	-1.11001	5100108			
att5	<-									
	MathAtt	.5225423	.1170141	4.47	0.000	.2931988	.7518858			
att1										
	/cut1	-1.10254	.1312272	-8.40	0.000	-1.359741	8453396			
	/cut2	2495339	.1160385	-2.15	0.032	4769651	0221027			
	/cut3	.2983261	.1164414	2.56	0.010	.0701052	.5265471			
	/cut4	1.333053	.1391907	9.58	0.000	1.060244	1.605861			
att2										
	/cut1	-1.055791	.1062977	-9.93	0.000	-1.264131	8474513			
	/cut2	1941211	.0941435	-2.06	0.039	378639	0096032			
	/cut3	.3598488	.0952038	3.78	0.000	.1732528	.5464448			
	/cut4	1.132624	.1082204	10.47	0.000	.9205156	1.344732			
att3										
	/cut1	-1.053519	.1733999	-6.08	0.000	-1.393377	7136614			
	/cut2	0491073	.1442846	-0.34	0.734	3318999	.2336853			
	/cut3	.5570671	.1538702	3.62	0.000	.2554871	.8586471			
	/cut4	1.666859	.2135554	7.81	0.000	1.248298	2.08542			

att4						
/cut1	-1.07378	.1214071	-8.84	0.000	-1.311734	8358264
/cut2	2112462	.1076501	-1.96	0.050	4222366	0002559
/cut3	.406347	.1094847	3.71	0.000	.191761	.620933
/cut4	1.398185	.1313327	10.65	0.000	1.140778	1.655593
att5						
/cut1	-1.244051	.1148443	-10.83	0.000	-1.469142	-1.018961
/cut2	336135	.0986678	-3.41	0.001	5295203	1427498
/cut3	.2137776	.0978943	2.18	0.029	.0219084	.4056468
/cut4	.9286849	.107172	8.67	0.000	.7186316	1.138738
var(MathAb)	2.300652	.7479513			1.216527	4.350909
var(MathAtt)	1.520854	.4077674			.8992196	2.572228
cov(MathAtt,						
MathAb)	.8837681	.2204606	4.01	0.000	.4516733	1.315863

Notes:

- 1. The estimated covariance between math attitude and ability is 0.88.
- 2. We can calculate the correlation from the estimated covariance; the formula is  $\hat{\rho}_{xy} = \hat{\sigma}_{xy}/(\hat{\sigma}_x \hat{\sigma}_y)$ . The estimated values are  $\hat{\sigma}_{xy} = 0.8838$ ,  $\hat{\sigma}_x^2 = 2.301$ , and  $\hat{\sigma}_y^2 = 1.521$ . Thus the estimated correlation between attitude and ability is 0.4724.
- 3. There is something new in the output, namely, things labeled /cut1, ..., /cut4. These appear for each of the five attitudinal measures. These are the ordered logit's cutpoints, the values on the logit's distribution that separate attitude 1 from attitude 2, attitude 2 from attitude 3, and so on. The four cutpoints map the continuous distribution into five ordered, categorical groups.
- 4. There's something interesting hiding in the MathAtt coefficients: the coefficients for two of the paths, att3 att4 <- MathAtt, are negative! If you look back to the description of the data, you will find that the sense of these two questions was reversed from those of the other questions. Strong agreement on these two questions was agreement with a negative feeling about mathematics.

### Fitting the model with the Builder

Use the diagram in Fitting the two-factor model above for reference.

1. Open the dataset.

In the Command window, type

- . use http://www.stata-press.com/data/r13/gsem\_cfa
- 2. Open a new Builder diagram.

Select menu item Statistics > SEM (structural equation modeling) > Model building and estimation.

- 3. Put the Builder in gsem mode by clicking on the <sup>G</sup> button.
- 4. Create the measurement component for MathAb.

Select the Add Measurement Component tool, <sup>39</sup>, and then click in the diagram about one-third of the way up from the bottom and slightly left of the center.

In the resulting dialog box,

- a. change the Latent variable name to MathAb;
- b. select q1, q2, q3, q4, q5, q6, q7, and q8 by using the Measurement variables control;
- c. check Make measurements generalized;
- d. select Bernoulli, Logit in the Family/Link control;
- e. select Down in the Measurement direction control;
- f. click on OK.

If you wish, move the component by clicking on any variable and dragging it.

5. Create the measurement component for MathAtt.

Select the Add Measurement Component tool, <sup>30</sup>, and then click in the diagram about one-third of the way down from the top and slightly left of the center.

In the resulting dialog box,

- a. change the Latent variable name to MathAtt;
- b. select att1, att2, att3, att4, and att5 by using the Measurement variables control;
- c. check Make measurements generalized;
- d. select Ordinal, Logit in the Family/Link control;
- e. select Up in the Measurement direction control;
- f. click on OK.

If you wish, move the component by clicking on any variable and dragging it.

- 6. Create the covariance between MathAtt and MathAb.

  - b. Click in the top-left quadrant of the MathAb oval, and drag a covariance to the bottom left of the MathAtt oval.
- 7. Clean up.

If you do not like where a covariance has been connected to its variable, use the Select tool,

**N**, to simply click on the covariance, and then click on where it connects to an oval and drag the endpoint. You can also change the bow of the covariance by dragging the control point that extends from one end of the selected covariance.

8. Estimate.

Click on the **Estimate** button, **(D)**, in the Standard Toolbar, and then click on **OK** in the resulting *GSEM estimation options* dialog box.

You can open a completed diagram in the Builder by typing

. webgetsem gsem\_2fmm

# Also see

- [SEM] example 27g Single-factor measurement model (generalized response)
- [SEM] example 29g Two-parameter logistic IRT model
- [SEM] example 32g Full structural equation model (generalized response)
- [SEM] gsem Generalized structural equation model estimation command
- [SEM] intro 5 Tour of models