

ranksum — Equality tests on unmatched data
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Syntax

Wilcoxon rank-sum test

```
ranksum varname [if] [in], by(groupvar) [porder]
```

Nonparametric equality-of-medians test

```
median varname [if] [in] [weight], by(groupvar) [median_options]
```

ranksum_options

Description

Main

* *by*(*groupvar*)

grouping variable

porder

probability that variable for first group is larger than variable for second group

median_options

Description

Main

* *by*(*groupvar*)

grouping variable

exact

perform Fisher's exact test

medianties(below)

assign values equal to the median to below group

medianties(above)

assign values equal to the median to above group

medianties(drop)

drop values equal to the median from the analysis

medianties(split)

split values equal to the median equally between the two groups

* *by*(*groupvar*) is required.*by* is allowed with *ranksum* and *median*; see [D] *by*.*fweights* are allowed with *median*; see [U] 11.1.6 *weight*.

Menu

ranksum

Statistics > Nonparametric analysis > Tests of hypotheses > Wilcoxon rank-sum test

median

Statistics > Nonparametric analysis > Tests of hypotheses > K-sample equality-of-medians test

Description

`ranksum` tests the hypothesis that two independent samples (that is, *unmatched* data) are from populations with the same distribution by using the Wilcoxon rank-sum test, which is also known as the Mann–Whitney two-sample statistic (Wilcoxon 1945; Mann and Whitney 1947).

`median` performs a nonparametric k -sample test on the equality of medians. It tests the null hypothesis that the k samples were drawn from populations with the same median. For two samples, the chi-squared test statistic is computed both with and without a continuity correction.

`ranksum` and `median` are for use with *unmatched* data. For equality tests on matched data, see [R] [signrank](#).

Options for ranksum

Main

`by`(*groupvar*) is required. It specifies the name of the grouping variable.

`porder` displays an estimate of the probability that a random draw from the first population is larger than a random draw from the second population.

Options for median

Main

`by`(*groupvar*) is required. It specifies the name of the grouping variable.

`exact` displays the significance calculated by Fisher's exact test. For two samples, both one- and two-sided probabilities are displayed.

`medianties`(*below* | *above* | *drop* | *split*) specifies how values equal to the overall median are to be handled. The median test computes the median for *varname* by using all observations and then divides the observations into those falling above the median and those falling below the median. When values for an observation are equal to the sample median, they can be dropped from the analysis by specifying `medianties(drop)`; added to the group above or below the median by specifying `medianties(above)` or `medianties(below)`, respectively; or if there is more than 1 observation with values equal to the median, they can be equally divided into the two groups by specifying `medianties(split)`. If this option is not specified, `medianties(below)` is assumed.

Remarks and examples

[stata.com](https://www.stata.com)

► Example 1

We are testing the effectiveness of a new fuel additive. We run an experiment with 24 cars: 12 cars with the fuel treatment and 12 cars without. We input these data by creating a dataset with 24 observations. `mpg` records the mileage rating, and `treat` records 0 if the mileage corresponds to untreated fuel and 1 if it corresponds to treated fuel.

```

. use http://www.stata-press.com/data/r13/fuel12
. ranksum mpg, by(treat)
Two-sample Wilcoxon rank-sum (Mann-Whitney) test

```

treat	obs	rank sum	expected
untreated	12	128	150
treated	12	172	150
combined	24	300	300

```

unadjusted variance      300.00
adjustment for ties      -4.04
-----
adjusted variance        295.96
Ho: mpg(treat==untreated) = mpg(treat==treated)
      z = -1.279
      Prob > |z| = 0.2010

```

These results indicate that the medians are not statistically different at any level smaller than 20.1%. Similarly, the median test,

```

. median mpg, by(treat) exact
Median test

```

Greater than the median	whether car received fuel additive		Total
	untreated	treated	
no	7	5	12
yes	5	7	12
Total	12	12	24

```

      Pearson chi2(1) = 0.6667   Pr = 0.414
      Fisher's exact = 0.684
1-sided Fisher's exact = 0.342
Continuity corrected:
      Pearson chi2(1) = 0.1667   Pr = 0.683

```

fails to reject the null hypothesis that there is no difference between the fuel with the additive and the fuel without the additive.

Compare these results from these two tests with those obtained from the `signrank` and `signtest` where we found significant differences; see [R] [signrank](#). An experiment run on 24 different cars is not as powerful as a before-and-after comparison using the same 12 cars.

◀

Stored results

`ranksum` stores the following in `r()`:

Scalars

<code>r(N_1)</code>	sample size n_1
<code>r(N_2)</code>	sample size n_2
<code>r(z)</code>	z statistic
<code>r(Var_a)</code>	adjusted variance
<code>r(group1)</code>	value of variable for first group
<code>r(sum_obs)</code>	actual sum of ranks for first group
<code>r(sum_exp)</code>	expected sum of ranks for first group
<code>r(porder)</code>	probability that draw from first population is larger than draw from second population

`median` stores the following in `r()`:

Scalars

<code>r(N)</code>	sample size
<code>r(chi2)</code>	Pearson's χ^2
<code>r(p)</code>	significance of Pearson's χ^2
<code>r(p_exact)</code>	Fisher's exact p
<code>r(groups)</code>	number of groups compared
<code>r(chi2_cc)</code>	continuity-corrected Pearson's χ^2
<code>r(p_cc)</code>	continuity-corrected significance
<code>r(p1_exact)</code>	one-sided Fisher's exact p

Methods and formulas

For a practical introduction to these techniques with an emphasis on examples rather than theory, see [Acock \(2014\)](#), [Bland \(2000\)](#), or [Sprent and Smeeton \(2007\)](#). For a summary of these tests, see [Snedecor and Cochran \(1989\)](#).

Methods and formulas are presented under the following headings:

ranksum
median

ranksum

For the Wilcoxon rank-sum test, there are two independent random variables, X_1 and X_2 , and we test the null hypothesis that $X_1 \sim X_2$. We have a sample of size n_1 from X_1 and another of size n_2 from X_2 .

The data are then ranked without regard to the sample to which they belong. If the data are tied, averaged ranks are used. Wilcoxon's test statistic (1945) is the sum of the ranks for the observations in the first sample:

$$T = \sum_{i=1}^{n_1} R_{1i}$$

Mann and Whitney's U statistic (1947) is the number of pairs (X_{1i}, X_{2j}) such that $X_{1i} > X_{2j}$. These statistics differ only by a constant:

$$U = T - \frac{n_1(n_1 + 1)}{2}$$

Again Fisher's principle of randomization provides a method for calculating the distribution of the test statistic, ties or not. The randomization distribution consists of the $\binom{n}{n_1}$ ways to choose n_1 ranks from the set of all $n = n_1 + n_2$ ranks and assign them to the first sample.

It is a straightforward exercise to verify that

$$E(T) = \frac{n_1(n+1)}{2} \quad \text{and} \quad \text{Var}(T) = \frac{n_1 n_2 s^2}{n}$$

where s is the standard deviation of the combined ranks, r_i , for both groups:

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (r_i - \bar{r})^2$$

This formula for the variance is exact and holds both when there are no ties and when there are ties and we use averaged ranks. (Indeed, the variance formula holds for the randomization distribution of choosing n_1 numbers from any set of n numbers.)

Using a normal approximation, we calculate

$$z = \frac{T - E(T)}{\sqrt{\text{Var}(T)}}$$

When the `porder` option is specified, the probability

$$p = \frac{U}{n_1 n_2}$$

is computed.

□ Technical note

We follow the great majority of the literature in naming these tests for Wilcoxon, Mann, and Whitney. However, they were independently developed by several other researchers in the late 1940s and early 1950s. In addition to Wilcoxon, Mann, and Whitney, credit is due to [Festinger \(1946\)](#), [Whitfield \(1947\)](#), [Haldane and Smith \(1947\)](#), and [Van der Reyden \(1952\)](#). Leon Festinger (1919–1989), John Burdon Sanderson Haldane (1892–1964), and Cedric Austen Bardell Smith (1917–2002) are well known for other work, but little seems to be known about Whitfield or van der Reyden. For a detailed study, including information on these researchers, see [Berry, Mielke, and Johnston \(2012\)](#). □

median

The median test examines whether it is likely that two or more samples came from populations with the same median. The null hypothesis is that the samples were drawn from populations with the same median. The alternative hypothesis is that at least one sample was drawn from a population with a different median. The test should be used only with ordinal or interval data.

Assume that there are score values for k independent samples to be compared. The median test is performed by first computing the median score for all observations combined, regardless of the sample group. Each score is compared with this computed grand median and is classified as being above the grand median, below the grand median, or equal to the grand median. Observations with scores equal to the grand median can be dropped, added to the “above” group, added to the “below” group, or split between the two groups.

Once all observations are classified, the data are cast into a $2 \times k$ contingency table, and a Pearson’s chi-squared test or Fisher’s exact test is performed.

Henry Berthold Mann (1905–2000) was born in Vienna, Austria, where he completed a doctorate in algebraic number theory. He moved to the United States in 1938 and for several years made his livelihood by tutoring in New York. During this time, he proved a celebrated conjecture in number theory and studied statistics at Columbia with Abraham Wald, with whom he wrote three papers. After the war, he taught at Ohio State and the Universities of Wisconsin and Arizona. In addition to his work in number theory and statistics, he made major contributions to algebra and combinatorics.

Donald Ransom Whitney (1915–2007) studied at Oberlin, Princeton, and Ohio State Universities and worked at the latter throughout his career. His PhD thesis under Henry Mann was on nonparametric statistics. It was this work that produced the test that bears their names.

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Also see

- [R] [signrank](#) — Equality tests on matched data
- [R] [ttest](#) — t tests (mean-comparison tests)