Title

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Irtest - Likelihood-ratio test after estimation

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Syntax

lrtest $modelspec_1 \ [modelspec_2] \ [, options]$

where modelspec is

name | . | (namelist)

where *name* is the name under which estimation results were stored using estimates store (see [R] estimates store), and "." refers to the last estimation results, whether or not these were already stored.

options	Description
<u>st</u> ats	display statistical information about the two models
<u>di</u> r	display descriptive information about the two models
<u>d</u> f(#)	override the automatic degrees-of-freedom calculation; seldom used
force	force testing even when apparently invalid

Menu

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Description

lrtest performs a likelihood-ratio test of the null hypothesis that the parameter vector of a statistical model satisfies some smooth constraint. To conduct the test, both the unrestricted and the restricted models must be fit using the maximum likelihood method (or some equivalent method), and the results of at least one must be stored using estimates store; see [R] estimates store.

 $modelspec_1$ and $modelspec_2$ specify the restricted and unrestricted model in any order. $modelspec_1$ and $modelspec_2$ cannot have names in common; for example, lrtest (A B C) (C D E) is not allowed because both model specifications include C. If $modelspec_2$ is not specified, the last estimation result is used; this is equivalent to specifying $modelspec_2$ as a period (.).

lrtest supports composite models specified by a parenthesized list of model names. In a composite model, we assume that the log likelihood and dimension (number of free parameters) of the full model are obtained as the sum of the log-likelihood values and dimensions of the constituting models.

lrtest provides an important alternative to test (see [R] test) for models fit via maximum likelihood or equivalent methods.

Options

- stats displays statistical information about the unrestricted and restricted models, including the information indices of Akaike and Schwarz.
- dir displays descriptive information about the unrestricted and restricted models; see estimates dir in [R] estimates store.
- df(#) is seldom specified; it overrides the automatic degrees-of-freedom calculation.
- force forces the likelihood-ratio test calculations to take place in situations where lrtest would normally refuse to do so and issue an error. Such situations arise when one or more assumptions of the test are violated, for example, if the models were fit with vce(robust), vce(cluster *clustvar*), or pweights; when the dependent variables in the two models differ; when the null log likelihoods differ; when the samples differ; or when the estimation commands differ. If you use the force option, there is no guarantee as to the validity or interpretability of the resulting test.

Remarks and examples

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The standard way to use lrtest is to do the following:

- 1. Fit either the restricted model or the unrestricted model by using one of Stata's estimation commands and then store the results using estimates store *name*.
- 2. Fit the alternative model (the unrestricted or restricted model) and then type 'lrtest *name* .'. lrtest determines for itself which of the two models is the restricted model by comparing the degrees of freedom.

Often you may want to store the alternative model with estimates store $name_2$, for instance, if you plan additional tests against models yet to be fit. The likelihood-ratio test is then obtained as lrtest name name₂.

Remarks are presented under the following headings:

Nested models Composite models

Nested models

lrtest may be used with any estimation command that reports a log likelihood, including heckman, logit, poisson, stcox, and streg. You must check that one of the model specifications implies a statistical model that is *nested within* the model implied by the other specification. Usually, this means that both models are fit with the same estimation command (for example, both are fit by logit, with the same dependent variables) and that the set of covariates of one model is a subset of the covariates of the other model. Second, lrtest is valid only for models that are fit by maximum likelihood or by some equivalent method, so it does not apply to models that were fit with probability weights or clusters. Specifying the vce(robust) option similarly would indicate that you are worried about the valid specification of the model, so you would not use lrtest. Third, lrtest assumes that under the null hypothesis, the test statistic is (approximately) distributed as chi-squared. This assumption is not true for likelihood-ratio tests of "boundary conditions", such as tests for the presence of overdispersion or random effects (Gutierrez, Carter, and Drukker 2001).

Example 1

We have data on infants born with low birthweights along with the characteristics of the mother (Hosmer, Lemeshow, and Sturdivant 2013; see also [R] **logistic**). We fit the following model:

. use http://w (Hosmer & Leme	-	ss.com/data/	r13/lbw			
. logistic lou	v age lwt i.ra	ace smoke pt	l ht ui			
Logistic regre	ession			Number	r of obs =	189
					i2(8) =	33.22
					> chi2 =	0.0001
Log likelihood	d = -100.724	1		Pseudo	o R2 =	0.1416
low	Odds Ratio	Std. Err.	Z	P> z	[95% Conf.	Interval]
age	.9732636	.0354759	-0.74	0.457	.9061578	1.045339
lwt	.9849634	.0068217	-2.19	0.029	.9716834	.9984249
race						
black	3.534767	1.860737	2.40	0.016	1.259736	9.918406
other	2.368079	1.039949	1.96	0.050	1.001356	5.600207
smoke	2.517698	1.00916	2.30	0.021	1.147676	5.523162
ptl	1.719161	.5952579	1.56	0.118	.8721455	3.388787
ht	6.249602	4.322408	2.65	0.008	1.611152	24.24199
ui	2.1351	.9808153	1.65	0.099	.8677528	5.2534
_cons	1.586014	1.910496	0.38	0.702	.1496092	16.8134

We now wish to test the constraint that the coefficients on age, lwt, ptl, and ht are all zero or, equivalently here, that the odds ratios are all 1. One solution is to type

. test age lwt ptl ht
(1) [low]age = 0
(2) [low]lwt = 0
(3) [low]ptl = 0
(4) [low]ht = 0
chi2(4) = 12.38
Prob > chi2 = 0.0147

This test is based on the inverse of the information matrix and is therefore based on a quadratic approximation to the likelihood function; see [R] test. A more precise test would be to refit the model, applying the proposed constraints, and then calculate the likelihood-ratio test.

We first save the current model:

. estimates store full

We then fit the constrained model, which here is the model omitting age, lwt, ptl, and ht:

. logistic lou	w i.race smoke	e ui					
Logistic regre	ession			Number	r of obs	=	189
				LR chi	i2(4)	=	18.80
				Prob >	> chi2	=	0.0009
Log likelihood	d = -107.93404	4		Pseudo	5 R2	=	0.0801
low	Odds Ratio	Std. Err.	z	P> z	[95% C	Conf.	Interval]
race							
black	3.052746	1.498087	2.27	0.023	1.1667	747	7.987382
other	2.922593	1.189229	2.64	0.008	1.3164	157	6.488285
smoke	2.945742	1.101838	2.89	0.004	1.4151		6.131715
ui	2.419131	1.047359	2.04	0.041	1.0354	159	5.651788
_cons	.1402209	.0512295	-5.38	0.000	.06852	216	.2869447

That done, lrtest compares this model with the model we previously stored:

. lrtest full .		
Likelihood-ratio test	LR chi2(4) =	14.42
(Assumption: . nested in full)	Prob > chi2 =	0.0061

Let's compare results. test reported that age, lwt, ptl, and ht were jointly significant at the 1.5% level; lrtest reports that they are significant at the 0.6% level. Given the quadratic approximation made by test, we could argue that lrtest's results are more accurate.

lrtest explicates the assumption that, from a comparison of the degrees of freedom, it has assessed that the last fit model (.) is nested within the model stored as full. In other words, full is the unconstrained model and . is the constrained model.

The names in "(Assumption: . nested in full)" are actually links. Click on a name, and the results for that model are replayed.

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Aside: The nestreg command provides a simple syntax for performing likelihood-ratio tests for nested model specifications; see [R] **nestreg**. In the previous example, we fit a full logistic model, used estimates store to store the full model, fit a constrained logistic model, and used lrtest to report a likelihood-ratio test between two models. To do this with one call to nestreg, use the lrtable option.

Technical note

lrtest determines the degrees of freedom of a model as the rank of the (co)variance matrix e(V). There are two issues here. First, the *numerical* determination of the rank of a matrix is a subtle problem that can, for instance, be affected by the scaling of the variables in the model. The rank of a matrix depends on the number of (independent) linear combinations of coefficients that sum exactly to zero. In the world of numerical mathematics, it is hard to tell whether a very small number is really nonzero or is a real zero that happens to be slightly off because of roundoff error from the finite precision with which computers make floating-point calculations. Whether a small number is being classified as one or the other, typically on the basis of a threshold, affects the determined degrees of freedom. Although Stata generally makes sensible choices, it is bound to make mistakes occasionally. The moral of this story is to make sure that the calculated degrees of freedom is as you expect before interpreting the results.

Technical note

A second issue involves regress and related commands such as anova. Mainly for historical reasons, regress does not treat the residual variance, σ^2 , the same way that it treats the regression coefficients. Type estat vce after regress, and you will see the regression coefficients, not $\hat{\sigma}^2$. Most estimation commands for models with ancillary parameters (for example, streg and heckman) treat all parameters as equals. There is nothing technically wrong with regress here; we are usually focused on the regression coefficients, and their estimators are uncorrelated with $\hat{\sigma}^2$. But, formally, σ^2 adds a degree of freedom to the model, which does not matter if you are comparing two regression models by a likelihood-ratio test. This test depends on the difference in the degrees of freedom, and hence being "off by 1" in each does not matter. But, if you are comparing a regression model with a larger model—for example, a heteroskedastic regression model fit by arch—the automatic determination of the degrees of freedom is incorrect, and you must specify the df (#) option.

Example 2

Returning to the low-birthweight data in the example 1, we now wish to test that the coefficient on 2.race (black) is equal to that on 3.race (other). The base model is still stored under the name full, so we need only fit the constrained model and perform the test. With z as the index of the logit model, the base model is

```
z = \beta_0 + \beta_1 \text{age} + \beta_2 \text{lwt} + \beta_3 2.\text{race} + \beta_4 3.\text{race} + \cdots
```

If $\beta_3 = \beta_4$, this can be written as

```
z = \beta_0 + \beta_1 \text{age} + \beta_2 \text{lwt} + \beta_3 (2.\text{race} + 3.\text{race}) + \cdots
```

We can fit the constrained model as follows:

```
. constraint 1 2.race = 3.race
```

. logistic low age lwt i.race smoke ptl ht ui,	constraints(1)		
Logistic regression	Number of obs	=	189
	Wald chi2(7)	=	25.17
Log likelihood = -100.9997	Prob > chi2	=	0.0007
(1) [low]2.race - [low]3.race = 0			

low	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
age	.9716799	.0352638	-0.79	0.429	.9049649	1.043313
lwt	.9864971	.0064627	-2.08	0.038	.9739114	.9992453
race						
black	2.728186	1.080207	2.53	0.011	1.255586	5.927907
other	2.728186	1.080207	2.53	0.011	1.255586	5.927907
smoke	2.664498	1.052379	2.48	0.013	1.228633	5.778414
ptl	1.709129	.5924776	1.55	0.122	.8663666	3.371691
ht	6.116391	4.215585	2.63	0.009	1.58425	23.61385
ui	2.09936	.9699702	1.61	0.108	.8487997	5.192407
_cons	1.309371	1.527398	0.23	0.817	.1330839	12.8825

Comparing this model with our original model, we obtain

. lrtest full .		
Likelihood-ratio test	LR chi2(1) =	0.55
(Assumption: . nested in full)	Prob > chi2 =	0.4577

By comparison, typing test 2.race=3.race after fitting our base model results in a significance level of 0.4572. Alternatively, we can first store the restricted model, here using the name equal. Next lrtest is invoked specifying the names of the restricted and unrestricted models (we do not care about the order). This time, we also add the option stats requesting a table of model statistics, including the model selection indices AIC and BIC.

. estimates st	tore equal					
. lrtest equal	l full, st	ats				
Likelihood-rat	tio test				LR chi2(1) =	0.55
(Assumption: e	equal nest	ed in full)			Prob > chi2 =	0.4577
Model	Obs	ll(null)	ll(model)	df	AIC	BIC
equal	189	•	-100.9997	8	217.9994	243.9334
full	189	-117.336	-100.724	9	219.448	248.6237

N=Obs used in calculating BIC; see [R] BIC note Note:

Composite models

Irtest supports composite models; that is, models that can be fit by fitting a series of simpler models or by fitting models on subsets of the data. Theoretically, a composite model is one in which the likelihood function, $L(\theta)$, of the parameter vector, θ , can be written as the product

$$L(\theta) = L_1(\theta_1) \times L_2(\theta_2) \times \cdots \times L_k(\theta_k)$$

of likelihood terms with $\theta = (\theta_1, \dots, \theta_k)$ a partitioning of the full parameter vector. In such a case, the full-model likelihood $L(\theta)$ is maximized by maximizing the likelihood terms $L_j(\theta_j)$ in turn. Obviously, $\log L(\hat{\theta}) = \sum_{j=1}^k \log L_j(\hat{\theta}_j)$. The degrees of freedom for the composite model is obtained as the sum of the degrees of freedom of the constituting models.

Example 3

As an example of the application of composite models, we consider a test of the hypothesis that the coefficients of a statistical model do not differ between different portions ("regimes") of the covariate space. Economists call a test for such a hypothesis a *Chow test*.

We continue the analysis of the data on children of low birthweight by using logistic regression modeling and study whether the regression coefficients are the same among the three races: white, black, and other. A likelihood-ratio Chow test can be obtained by fitting the logistic regression model for each of the races and then comparing the combined results with those of the model previously stored as full. Because the full model included dummies for the three races, this version of the Chow test allows the intercept of the logistic regression model to vary between the regimes (races).

```
. logistic low age lwt smoke ptl ht ui if 1.race, nolog
```

Logistic regree		1		Number LR chi Prob > Pseudo	chi2	= = =	96 13.86 0.0312 0.1311
low	Odds Ratio	Std. Err.	z	P> z	[95%	Conf.	Interval]
age lwt	.9869674 .9900874	.0527757	-0.25 -0.93	0.806	.8887	089	1.096021 1.011103
smoke ptl ht ui _cons	4.208697 1.592145 2.900166 1.229523 .4891008	2.680133 .7474264 3.193537 .9474768 .993785	2.26 0.99 0.97 0.27 -0.35	0.024 0.322 0.334 0.789 0.725	1.20 .6344 .3350 .2715 .0091	379 554 165	14.66222 3.995544 25.1032 5.567715 26.23746

. estimates store white

. logistic lo Logistic regr	ession			LR ch	r of obs = i2(6) = > chi2 =	26 10.12 0.1198
Log likelihoo	d = -12.65415	7		Pseudo		0.2856
low	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	[Interval]
age	.8735313	.1377846	-0.86	0.391	.6412332	1.189983
lwt	.9747736	.016689	-1.49	0.136	.9426065	1.008038
smoke	16.50373	24.37044	1.90	0.058	.9133647	298.2083
ptl	4.866916	9.33151	0.83	0.409	.1135573	208.5895
ht	85.05605	214.6382	1.76	0.078	.6049308	11959.27
ui	67.61338	133.3313	2.14	0.033	1.417399	3225.322
_cons	48.7249	169.9216	1.11	0.265	.0523961	45310.94
. estimates s		ka ntl ht vi	if 2 mo.	no nolog		
	w age iwt smol	ke pui nu ui	11 J.14	ce, norog		
Logistic regr	•	ke pti nt ui	11 3.14		r of obs =	67
•	•	ke pri nt ui	11 5.14			
Logistic regr	ession	-	11 5.14	Number LR ch: Prob	i2(6) = > chi2 =	67 14.06 0.0289
Logistic regr	ession	-	11 5.14	Number LR ch	i2(6) = > chi2 =	14.06
Logistic regr	ession	-	z	Number LR ch: Prob	i2(6) = > chi2 =	14.00 0.0289 0.1589
Logistic regr	ession d = -37.228444	4		Number LR ch: Prob 2 Pseude	i2(6) = > chi2 = o R2 =	14.06 0.0289 0.1589 Interval]
Logistic regr	ession d = -37.228444 Odds Ratio	4 Std. Err.	Z	Number LR ch Prob 7 Pseudo P> z	i2(6) = > chi2 = o R2 = [95% Conf.	14.06 0.0285 0.1585 Interval
Logistic regr	ession d = -37.228444 Odds Ratio .9263905 .9724499 .7979034	4 Std. Err. .0665386	z -1.06 -1.72 -0.28	Number LR ch: Prob Pseudo 0.287 0.085 0.776	i2(6) = > chi2 = o R2 = [95% Conf. .8047407	14.06 0.0289 0.1589 Interval 1.06643 1.003839 3.787586
Logistic regr Log likelihoo low age lwt	ession d = -37.228444 Odds Ratio .9263905 .9724499	4 Std. Err. .0665386 .015762	z -1.06 -1.72 -0.28 1.67	Number LR ch: Prob 3 Pseudo P> z 0.287 0.085	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053	14.06 0.0289 0.1589 Interval 1.06643 1.003839 3.787586
Log likelihoo low age lwt smoke ptl ht	ession d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537	z -1.06 -1.72 -0.28 1.67 1.59	Number LR ch: Prob : Pseudo P> z 0.287 0.085 0.776 0.094 0.112	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764	14.00 0.028 0.1585 Interval 1.06643 1.00383 3.78758 9.682908 96.98826
Logistic regr Log likelihoo low age lwt smoke ptl ht ui	d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503 2.925006	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537 2.046473	z -1.06 -1.72 -0.28 1.67 1.59 1.53	Number LR ch: Prob 3 Pseudo P> z 0.287 0.085 0.776 0.094 0.112 0.125	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764 .7423107	14.00 0.028 0.158 1.06642 1.00383 3.78758 9.682900 96.98820 11.5257
Log likelihoo Log likelihoo low age lwt smoke ptl ht	ession d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537	z -1.06 -1.72 -0.28 1.67 1.59	Number LR ch: Prob : Pseudo P> z 0.287 0.085 0.776 0.094 0.112	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764	14.00 0.028 0.158 Interval 1.0664 1.00383 3.78758 9.68290 96.9882 11.5257
Logistic regr Log likelihoo low age lwt smoke ptl ht ui	d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503 2.925006 49.09444	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537 2.046473	z -1.06 -1.72 -0.28 1.67 1.59 1.53	Number LR ch: Prob 3 Pseudo P> z 0.287 0.085 0.776 0.094 0.112 0.125	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764 .7423107	14.0 0.028 0.158 Interval 1.0664 1.00383 3.78758 9.68290 96.9882 11.5257
Logistic regr Log likelihood low age lwt smoke ptl ht ui _cons	d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503 2.925006 49.09444 tore other	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537 2.046473 113.9165	z -1.06 -1.72 -0.28 1.67 1.59 1.53 1.68	Numbe: LR ch: Prob 3 Pseudo P> z 0.287 0.085 0.776 0.094 0.112 0.125 0.093	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764 .7423107	14.00 0.028 0.158 Interval 1.0664 1.00383 3.78758 9.68290 96.9882 11.5257
Logistic regr Log likelihood low age lwt smoke ptl ht ui _cons . estimates s	d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503 2.925006 49.09444 tore other	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537 2.046473 113.9165 he likelihood	z -1.06 -1.72 -0.28 1.67 1.59 1.53 1.68	Numbe: LR ch: Prob 3 Pseudo P> z 0.287 0.085 0.776 0.094 0.112 0.125 0.093	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764 .7423107	14.00 0.028 0.158 1.06642 1.00383 3.78758 9.682900 96.98820 11.5257
Logistic regr Log likelihood low age lwt smoke ptl ht ui _cons . estimates s	ession d = -37.228444 Odds Ratio .9263905 .9724499 .7979034 2.845675 7.767503 2.925006 49.09444 tore other y to perform t 1) (white black	4 Std. Err. .0665386 .015762 .6340585 1.777944 10.00537 2.046473 113.9165 he likelihood	z -1.06 -1.72 -0.28 1.67 1.59 1.53 1.68	Number LR ch: Prob : Pseudo P> z 0.287 0.085 0.776 0.094 0.112 0.125 0.093	i2(6) = > chi2 = o R2 = [95% Conf. .8047407 .9420424 .1680885 .8363053 .6220764 .7423107	14.06 0.0289 0.1589

Assumption: (full) nested in (white, black, other)

Obs	ll(null)	ll(model)	df	AIC	BIC
189 96	-117.336	-100.724 -45.92706	9 7	219.448	248.6237
26	-17.71291	-12.65416	7 7	39.30831	48.11499
	189 96	189 -117.336 96 -52.85752 26 -17.71291	189 -117.336 -100.724 96 -52.85752 -45.92706 26 -17.71291 -12.65416	189 -117.336 -100.724 9 96 -52.85752 -45.92706 7 26 -17.71291 -12.65416 7	189 -117.336 -100.724 9 219.448 96 -52.85752 -45.92706 7 105.8541 26 -17.71291 -12.65416 7 39.30831

Note: N=Obs used in calculating BIC; see [R] BIC note

We cannot reject the hypothesis that the logistic regression model applies to each of the races at any reasonable significance level. By specifying the stats option, we can verify the degrees of freedom of the test: 12 = 7 + 7 + 7 - 9. We can obtain the same test by fitting an expanded model with interactions between all covariates and race.

. logistic low race##c.(age lwt smoke ptl ht ui)						
Logistic regre	ession			LR	ber of obs = chi2(20) = b > chi2 =	189 43.05 0.0020
Log likelihood	l = −95.809661	1			udo $R2 =$	0.1835
low	Odds Ratio	Std. Err.	z	P> z	[95% Conf.	Interval]
race						
black	99.62137	402.0829	1.14	0.254	.0365434	271578.9
other	100.3769	309.586	1.49	0.135	.2378638	42358.38
age	.9869674	.0527757	-0.25	0.806	.8887649	1.096021
lwt	.9900874	.0106101	-0.93	0.353	.9695089	1.011103
smoke	4.208697	2.680133	2.26	0.024	1.20808	14.66222
ptl	1.592145	.7474264	0.99	0.322	.6344379	3.995544
ht	2.900166	3.193537	0.97	0.334	.3350554	25.1032
ui	1.229523	.9474768	0.27	0.789	.2715165	5.567715
race#c.age						
black	.885066	.1474079	-0.73	0.464	.638569	1.226714
other	.9386232	.0840486	-0.71	0.479	.7875366	1.118695
race#c.lwt						
black	.9845329	.0198857	-0.77	0.440	.9463191	1.02429
other	.9821859	.0190847	-0.93	0.355	.9454839	1.020313
race#c.smoke						
black	3.921338	6.305992	0.85	0.395	.167725	91.67917
other	.1895844	.1930601	-1.63	0.102	.025763	1.395113
race#c.ptl						
black	3.05683	6.034089	0.57	0.571	.0638301	146.3918
other	1.787322	1.396789	0.74	0.457	.3863582	8.268285
race#c.ht						
black	29.328	80.7482	1.23	0.220	.1329492	6469.623
other	2.678295	4.538712	0.58	0.561	.0966916	74.18702
race#c.ui						
black	54.99155	116.4274	1.89	0.058	.8672471	3486.977
other	2.378976	2.476124	0.83	0.405	.309335	18.29579
_cons	.4891008	.993785	-0.35	0.725	.0091175	26.23746
. lrtest full						
Likelihood-rat	io test				LR chi2(12) =	9.83
(Assumption: full nested in .)					Prob > chi2 =	0.6310

Applying lrtest for the full model against the model with all interactions yields the same test statistic and *p*-value as for the full model against the composite model for the three regimes. Here the specification of the model with interactions was convenient, and logistic had no problem computing the estimates for the expanded model. In models with more complicated likelihoods, such as Heckman's selection model (see [R] heckman) or complicated survival-time models (see [ST] streg), fitting the models with all interactions may be numerically demanding and may be much more time consuming than fitting a series of models separately for each regime.

Given the model with all interactions, we could also test the hypothesis of no differences among the regions (races) by a Wald version of the Chow test by using the testparm command; see [R] test.

```
. testparm race#c.(age lwt smoke ptl ht ui)
(1)
      [low]2.race#c.age = 0
(2)
      [low]3.race#c.age = 0
(3)
      [low]2.race#c.lwt = 0
(4)
      [low]3.race#c.lwt = 0
(5)
      [low]2.race#c.smoke = 0
(6)
      [low]3.race#c.smoke = 0
(7)
      [low]2.race#c.ptl = 0
( 8) [low]3.race#c.ptl = 0
(9) [low]2.race#c.ht = 0
(10) [low]3.race#c.ht = 0
(11)
      [low]2.race#c.ui = 0
(12) [low]3.race#c.ui = 0
          chi2(12) =
                         8.24
        Prob > chi2 =
                         0.7663
```

We conclude that, here, the Wald version of the Chow test is similar to the likelihood-ratio version of the Chow test.

Stored results

lrtest stores the following in r():

Scalars

r(p)	level of significance
r(df)	degrees of freedom
r(chi2)	LR test statistic

Programmers wishing their estimation commands to be compatible with lrtest should note that lrtest requires that the following results be returned:

e(cmd)	name of estimation command
e(11)	log likelihood
e(V)	variance-covariance matrix of the estimators
e(N)	number of observations

lrtest also verifies that e(N), $e(11_0)$, and e(depvar) are consistent between two noncomposite models.

Methods and formulas

Let L_0 and L_1 be the log-likelihood values associated with the full and constrained models, respectively. The test statistic of the likelihood-ratio test is $LR = -2(L_1 - L_0)$. If the constrained model is true, LR is approximately χ^2 distributed with $d_0 - d_1$ degrees of freedom, where d_0 and d_1 are the model degrees of freedom associated with the full and constrained models, respectively (Greene 2012, 526–527).

lrtest determines the degrees of freedom of a model as the rank of e(V), computed as the number of nonzero diagonal elements of invsym(e(V)).

1

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Also see

- [R] test Test linear hypotheses after estimation
- [R] **testnl** Test nonlinear hypotheses after estimation
- [R] nestreg Nested model statistics