Title

correlate - Correlations (covariances) of variables or coefficients

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Syntax

Display correlation matrix or covariance matrix

<u>cor</u>relate [varlist] [if] [in] [weight] [, correlate_options]

Display all pairwise correlation coefficients

pwcorr [varlist] [if] [in] [weight] [, pwcorr_options]

correlate_options	Description
Options	
means	display means, standard deviations, minimums, and maximums with matrix
<u>nof</u> ormat	ignore display format associated with variables
<u>c</u> ovariance	display covariances
wrap	allow wide matrices to wrap
pwcorr_options	Description
Main	
obs	print number of observations for each entry
sig	print significance level for each entry
<u>list</u> wise	use listwise deletion to handle missing values
<u>case</u> wise	synonym for listwise
<pre>print(#)</pre>	significance level for displaying coefficients
	significance level for displaying with a star
<u>b</u> onferroni	use Bonferroni-adjusted significance level
<u>sid</u> ak	use Šidák-adjusted significance level

varlist may contain time-series operators; see [U] **11.4.4 Time-series varlists**. by is allowed with correlate and pwcorr; see [D] by. aweights and fweights are allowed; see [U] **11.1.6 weight**.

Menu

correlate

Statistics > Summaries, tables, and tests > Summary and descriptive statistics > Correlations and covariances

pwcorr

Statistics > Summaries, tables, and tests > Summary and descriptive statistics > Pairwise correlations

Description

The correlate command displays the correlation matrix or covariance matrix for a group of variables. If *varlist* is not specified, the matrix is displayed for all variables in the dataset. Also see the estat vce command in [R] estat vce.

pwcorr displays all the pairwise correlation coefficients between the variables in *varlist* or, if *varlist* is not specified, all the variables in the dataset.

Options for correlate

Options

means displays summary statistics (means, standard deviations, minimums, and maximums) with the matrix.

noformat displays the summary statistics requested by the means option in g format, regardless of the display formats associated with the variables.

covariance displays the covariances rather than the correlation coefficients.

wrap requests that no action be taken on wide correlation matrices to make them readable. It prevents Stata from breaking wide matrices into pieces to enhance readability. You might want to specify this option if you are displaying results in a window wider than 80 characters. Then you may need to set linesize to however many characters you can display across a line; see [R] log.

Options for pwcorr

Main

obs adds a line to each row of the matrix reporting the number of observations used to calculate the correlation coefficient.

sig adds a line to each row of the matrix reporting the significance level of each correlation coefficient.

listwise handles missing values through listwise deletion, meaning that the entire observation is omitted from the estimation sample if any of the variables in *varlist* is missing for that observation. By default, pwcorr handles missing values by pairwise deletion; all available observations are used to calculate each pairwise correlation without regard to whether variables outside that pair are missing.

correlate uses listwise deletion. Thus listwise allows users of pwcorr to mimic correlate's treatment of missing values while retaining access to pwcorr's features.

casewise is a synonym for listwise.

- print(#) specifies the significance level of correlation coefficients to be printed. Correlation coefficients with larger significance levels are left blank in the matrix. Typing pwcorr, print(.10)
 would list only correlation coefficients significant at the 10% level or better.
- star(#) specifies the significance level of correlation coefficients to be starred. Typing pwcorr, star(.05) would star all correlation coefficients significant at the 5% level or better.
- bonferroni makes the Bonferroni adjustment to calculated significance levels. This option affects
 printed significance levels and the print() and star() options. Thus pwcorr, print(.05)
 bonferroni prints coefficients with Bonferroni-adjusted significance levels of 0.05 or less.
- sidak makes the Šidák adjustment to calculated significance levels. This option affects printed significance levels and the print() and star() options. Thus pwcorr, print(.05) sidak prints coefficients with Šidák-adjusted significance levels of 0.05 or less.

Remarks and examples

stata.com

Remarks are presented under the following headings:

correlate pwcorr Video example

correlate

Typing correlate by itself produces a correlation matrix for all variables in the dataset. If you specify the *varlist*, a correlation matrix for just those variables is displayed.

Example 1

We have state data on demographic characteristics of the population. To obtain a correlation matrix, we type

```
. use http://www.stata-press.com/data/r13/census13
(1980 Census data by state)
. correlate
(obs=50)
                  state
                           brate
                                      pop
                                             medage division
                                                               region mrgrate
       state
                 1.0000
       brate
                 0.0208
                         1.0000
                -0.0540 -0.2830
                                   1.0000
         pop
     medage
                -0.0624
                        -0.8800
                                   0.3294
                                             1.0000
   division
                -0.1345
                          0.6356
                                  -0.1081
                                           -0.5207
                                                      1.0000
                                  -0.1515
                -0.1339
                          0.6086
                                           -0.5292
                                                      0.9688
                                                               1.0000
     region
                                                     0.2280
                 0.0509
                          0.0677
                                  -0.1502 -0.0177
                                                               0.2490
                                                                        1.0000
    mrgrate
                -0.0655
                          0.3508
                                  -0.2064 -0.2229
                                                      0.5522
                                                               0.5682
                                                                        0.7700
    dvcrate
   medagesq
                -0.0621
                        -0.8609
                                   0.3324
                                            0.9984 -0.5162 -0.5239 -0.0202
                dvcrate medagesq
    dvcrate
                 1.0000
                -0.2192
                          1.0000
   medagesq
```

Because we did not specify the wrap option, Stata did its best to make the result readable by breaking the table into two parts.

To obtain the correlations between mrgrate, dvcrate, and medage, we type

correlate mi (obs=50)	rgrate dvcr	ate medag	e
	mrgrate	dvcrate	medage
mrgrate	1.0000		
dvcrate	0.7700	1.0000	
medage	-0.0177	-0.2229	1.0000

Example 2

The pop variable in example 1 represents the total population of the state. Thus, to obtain population-weighted correlations among mrgrate, dvcrate, and medage, we type

```
. correlate mrgrate dvcrate medage [w=pop]
(analytic weights assumed)
(sum of wgt is 2.2591e+08)
(obs=50)
mrgrate dvcrate medage
mrgrate 1.0000
dvcrate 0.5854 1.0000
medage -0.1316 -0.2833 1.0000
```

With the covariance option, correlate can be used to obtain covariance matrices, as well as correlation matrices, for both weighted and unweighted data.

▶ Example 3

To obtain the matrix of covariances between mrgrate, dvcrate, and medage, we type correlate mrgrate dvcrate medage, covariance:

. correlate mrgrate dvcrate medage, covariance (obs=50) mrgrate dvcrate medage mrgrate .000662 dvcrate .000063 1.0e-05 medage -.000769 -.001191 2.86775

We could have obtained the pop-weighted covariance matrix by typing correlate mrgrate dvcrate medage [w=pop], covariance.

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pwcorr

correlate calculates correlation coefficients by using casewise deletion; when you request correlations of variables x_1, x_2, \ldots, x_k , any observation for which any of x_1, x_2, \ldots, x_k is missing is not used. Thus if x_3 and x_4 have no missing values, but x_2 is missing for half the data, the correlation between x_3 and x_4 is calculated using only the half of the data for which x_2 is not missing. Of course, you can obtain the correlation between x_3 and x_4 .

pwcorr makes obtaining such pairwise correlation coefficients easier.

Example 4

Using auto.dta, we investigate the correlation between several of the variables.

```
. use http://www.stata-press.com/data/r13/auto1
(Automobile Models)
. pwcorr mpg price rep78 foreign, obs sig
                    mpg
                            price
                                     rep78 foreign
                 1.0000
         mpg
                     74
                -0.4594
                           1.0000
       price
                 0.0000
                     74
                               74
                 0.3739
                           0.0066
                                    1.0000
       rep78
                 0.0016
                           0.9574
                                        69
                     69
                               69
     foreign
                 0.3613
                           0.0487
                                    0.5922
                                              1.0000
                 0.0016
                           0.6802
                                    0.0000
                     74
                               74
                                        69
                                                  74
. pwcorr mpg price headroom rear_seat trunk rep78 foreign, print(.05) star(.01)
                    mpg
                            price headroom rear_s~t
                                                        trunk
                                                                  rep78 foreign
                 1.0000
         mpg
                -0.4594*
                           1.0000
       price
   headroom
                -0.4220*
                                    1.0000
                           0.4194*
                                    0.5238*
  rear_seat
                -0.5213*
                                             1.0000
                -0.5703*
                           0.3143*
                                    0.6620*
                                            0.6480*
                                                       1.0000
       trunk
                 0.3739*
                                                                 1.0000
       rep78
                 0.3613*
                                   -0.2939
                                            -0.2409 -0.3594*
                                                                 0.5922*
     foreign
                                                                          1.0000
. pwcorr mpg price headroom rear_seat trunk rep78 foreign, print(.05) bon
                    mpg
                            price headroom rear_s~t
                                                        trunk
                                                                  rep78
                                                                         foreign
                 1.0000
         mpg
       price
                -0.4594
                           1.0000
   headroom
                -0.4220
                                    1.0000
                -0.5213
                                    0.5238
                                              1.0000
                           0.4194
  rear_seat
                -0.5703
                                    0.6620
                                              0.6480
       trunk
                                                       1.0000
                 0.3739
                                                                 1.0000
       rep78
                 0.3613
                                                      -0.3594
                                                                 0.5922
                                                                          1.0000
     foreign
```

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Technical note

The correlate command will report the correlation matrix of the data, but there are occasions when you need the matrix stored as a Stata matrix so that you can further manipulate it. You can obtain the matrix by typing

```
. matrix accum R = varlist, noconstant deviations
. matrix R = corr(R)
```

The first line places the cross-product matrix of the data in matrix R. The second line converts that to a correlation matrix. Also see [P] matrix define and [P] matrix accum.

Video example

Pearson's correlation coefficient in Stata

Stored results

correlate stores the following in r():

Scalars	
r(N)	number of observations
r(rho)	ρ (first and second variables)
r(cov_12)	covariance (covariance only)
r(Var_1)	variance of first variable (covariance only)
r(Var_2)	variance of second variable (covariance only)
Matrices	
r(C)	correlation or covariance matrix

pwcorr will leave in its wake only the results of the last call that it makes internally to correlate for the correlation between the last variable and itself. Only rarely is this feature useful.

Methods and formulas

For a discussion of correlation, see, for instance, Snedecor and Cochran (1989, 177–195); for an introductory explanation using Stata examples, see Acock (2014, 200–206).

According to Snedecor and Cochran (1989, 180), the term "co-relation" was first proposed by Galton (1888). The product-moment correlation coefficient is often called the Pearson product-moment correlation coefficient because Pearson (1896) and Pearson and Filon (1898) were partially responsible for popularizing its use. See Stigler (1986) for information on the history of correlation.

The estimate of the product-moment correlation coefficient, ρ , is

$$\widehat{\rho} = \frac{\sum_{i=1}^{n} w_i(x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum_{i=1}^{n} w_i(x_i - \overline{x})^2} \sqrt{\sum_{i=1}^{n} w_i(y_i - \overline{y})^2}}$$

where w_i are the weights, if specified, or $w_i = 1$ if weights are not specified. $\overline{x} = (\sum w_i x_i)/(\sum w_i)$ is the mean of x, and \overline{y} is similarly defined.

The unadjusted significance level is calculated by pwcorr as

$$p=2* ttail(n-2,|\widehat{
ho}|\sqrt{n-2}\,/\sqrt{1-\widehat{
ho}^2}$$
)

Let v be the number of variables specified so that k = v(v-1)/2 correlation coefficients are to be estimated. If bonferroni is specified, the adjusted significance level is $p' = \min(1, kp)$. If sidak is specified, $p' = \min\{1, 1 - (1-p)^k\}$. In both cases, see *Methods and formulas* in [R] **oneway** for a more complete description of the logic behind these adjustments.

Carlo Emilio Bonferroni (1892–1960) studied in Turin and taught there and in Bari and Florence. He published on actuarial mathematics, probability, statistics, analysis, geometry, and mechanics. His work on probability inequalities has been applied to simultaneous statistical inference, although the method known as Bonferroni adjustment usually relies only on an inequality established earlier by Boole.

Florence Nightingale David (1909–1993) was born in Ivington, England, to parents who were friends with Florence Nightingale, David's namesake. She began her studies in statistics under the direction of Karl Pearson at University College London and continued her studies under the direction of Jerzy Neyman. After receiving her doctorate in statistics in 1938, David became a senior statistician for various departments within the British military. She developed statistical models to forecast the toll on life and infrastructure that would occur if a large city were bombed. In 1938, she also published her book Tables of the Correlation Coefficient, dealing with the distributions of correlation coefficients. After the war, she returned to University College London, serving as a lecturer until her promotion to professor in 1962. In 1967, David joined the University of California-Riverside, eventually becoming chair of the Department of Statistics. One of her most well-known works is the book Games, Gods and Gambling: The Origins and History of Probability and Statistical Ideas from the Earliest Times to the Newtonian Era, a history of statistics. David published over 100 papers on topics including combinatorics, symmetric functions, the history of statistics, and applications of statistics, including ecological diversity. She published under the name F. N. David to avoid revealing her gender in a male-dominated profession.

Karl Pearson (1857–1936) studied mathematics at Cambridge. He was professor of applied mathematics (1884–1911) and eugenics (1911–1933) at University College London. His publications include literary, historical, philosophical, and religious topics. Statistics became his main interest in the early 1890s after he learned about its application to biological problems. His work centered on distribution theory, the method of moments, correlation, and regression. Pearson introduced the chi-squared test and the terms coefficient of variation, contingency table, heteroskedastic, histogram, homoskedastic, kurtosis, mode, random sampling, random walk, skewness, standard deviation, and truncation. Despite many strong qualities, he also fell into prolonged disagreements with others, most notably, William Bateson and R. A. Fisher.

Zbyněk Šidák (1933–1999) was a notable Czech statistician and probabilist. He worked on Markov chains, rank tests, multivariate distribution theory and multiple-comparison methods, and he served as the chief editor of *Applications of Mathematics*.

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Also see

- [R] esize Effect size based on mean comparison
- [R] **icc** Intraclass correlation coefficients
- [R] **pcorr** Partial and semipartial correlation coefficients
- [R] spearman Spearman's and Kendall's correlations
- [R] summarize Summary statistics
- [R] **tetrachoric** Tetrachoric correlations for binary variables