Title

contrast - Contrasts and linear hypothesis tests after estimation

Syntax	Menu	Description	Options
Remarks and examples	Stored results	Methods and formulas	References
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Syntax

contrast termlist [, options]

where *termlist* is a list of factor variables or interactions that appear in the current estimation results. The variables may be typed with or without contrast operators, and you may use any factor-variable syntax:

See the operators (op.) table below for the list of contrast operators.

options	Description
Main	
<u>over</u> all	add a joint hypothesis test for all specified contrasts
<u>asobs</u> erved	treat all factor variables as observed
lincom	treat user-defined contrasts as linear combinations
Equations	
equation(<i>eqspec</i>)	perform contrasts in termlist for equation eqspec
atequations	perform contrasts in termlist within each equation
Advanced	
<pre>emptycells(empspec)</pre>	treatment of empty cells for balanced factors
noestimcheck	suppress estimability checks
Reporting	
<u>l</u> evel(#)	confidence level; default is level(95)
<pre>mcompare(method)</pre>	adjust for multiple comparisons; default is mcompare(noadjust)
noeffects	suppress table of individual contrasts
<u>ci</u> effects	show effects table with confidence intervals
pveffects	show effects table with <i>p</i> -values
effects	show effects table with confidence intervals and <i>p</i> -values
nowald	suppress table of Wald tests
<u>noatlev</u> els	report only the overall Wald test for terms that use the within @ or nested operator
nosvyadjust	compute unadjusted Wald tests for survey results
sort	sort the individual contrast values in each term
post	post contrasts and their VCEs as estimation results
display_options	control column formats, row spacing, line width, and factor-variable labeling
eform_option	report exponentiated contrasts
df(#)	use t distribution with # degrees of freedom for computing p -values and confidence intervals

df(#) does not appear in the dialog box.

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Term	Description
Main effects	
А	joint test of the main effects of A
r.A	individual contrasts that decompose A using r.
Interaction effects	
A#B	joint test of the two-way interaction effects of A and B
A#B#C	joint test of the three-way interaction effects of A, B, and C
<i>r</i> . A # <i>g</i> .B	individual contrasts for each interaction of A and B defined by r . and g .
Partial interaction effe	ects
r.A#B	joint tests of interactions of A and B within each contrast defined by $r.A$
A#r.B	joint tests of interactions of A and B within each contrast defined by $r.B$
Simple effects	
A@B	joint tests of the effects of A within each level of B
A@B#C	joint tests of the effects of A within each combination of the levels of B and C
r.A@B	individual contrasts of A that decompose A@B using r .
r.A@B#C	individual contrasts of A that decompose A@B#C using r .
Other conditional effe	octs
A#B@C	joint tests of the interaction effects of A and B within each level of C
A#B@C#D	joint tests of the interaction effects of A and B within each combination of the levels of C and D
r.A#g.B@C	individual contrasts for each interaction of A and B that decompose A#B@C using r . and g .
Nested effects	
A B	joint tests of the effects of A nested in each level of B
A B#C	joint tests of the effects of A nested in each combination of the levels of B and C
A#B C	joint tests of the interaction effects of A and B nested in each level of C
A#B C#D	joint tests of the interaction effects of A and B nested in each combination of the levels of C and D
r.A B	individual contrasts of A that decompose $A B$ using r .
r.A B#C	individual contrasts of A that decompose $A B#C$ using r .
r.A#g.B C	individual contrasts for each interaction of A and B defined by r . and g . nested in each level of C
Slope effects	
A#c.x	joint test of the effects of A on the slopes of x
A#c.x#c.y	joint test of the effects of A on the slopes of the product (interaction) of x and y
A#B#c.x	joint test of the interaction effects of A and B on the slopes of x
A#B#c.x#c.y	joint test of the interaction effects of A and B on the slopes of the product (interaction) of x and y
r.A#c.x	individual contrasts of A 's effects on the slopes of x using r .
Denominators	
/ term2	use $term2$ as the denominator in the F tests of the preceding terms
/	use the residual as the denominator in the F tests of the preceding terms (the default if no other /s are specified)

A, B, C, and D represent any factor variable in the current estimation results.

x and y represent any continuous variable in the current estimation results.

r. and g. represent any contrast operator. See the table below.

c. specifies that a variable be treated as continuous; see [U] 11.4.3 Factor variables.

Operators are allowed on any factor variable that does not appear to the right of @ or |. Operators decompose the effects of the associated factor variable into one-degree-of-freedom effects (contrasts).

Higher-level interactions are allowed anywhere an interaction operator (#) appears in the table.

Time-series operators are allowed if they were used in the estimation.

_eqns designates the equations in manova, mlogit, mprobit, and mvreg and can be specified anywhere a factor variable appears.

/ is allowed only after anova, cnsreg, manova, mvreg, or regress.

operators (op.)	Description
r.	differences from the reference (base) level; the default
a.	differences from the next level (adjacent contrasts)
ar.	differences from the previous level (reverse adjacent contrasts)
As-balanced operators	
g.	differences from the balanced grand mean
h.	differences from the balanced mean of subsequent levels (Helmert contrasts)
j.	differences from the balanced mean of previous levels (reverse Helmert contrasts)
р.	orthogonal polynomial in the level values
q.	orthogonal polynomial in the level sequence
As-observed operators	
gw.	differences from the observation-weighted grand mean
hw.	differences from the observation-weighted mean of subsequent levels
jw.	differences from the observation-weighted mean of previous levels
pw.	observation-weighted orthogonal polynomial in the level values
qw.	observation-weighted orthogonal polynomial in the level sequence
	vidual contrasts may be selected by using the $op#$. or $op(numlist)$. syntax. For selects the adjacent contrast for level 3 of A, and $p(1/2)$. B selects the linear and

quadratic effects of B. Also see Orthogonal polynomial contrasts and Beyond linear models.

Custom contrasts	Description
{A numlist}	user-defined contrast on the levels of factor A
{A#B numlist}	user-defined contrast on the levels of the interaction between ${\tt A}$ and ${\tt B}$

Custom contrasts may be part of a term, such as {A numlist}#B, {A numlist}@B, {A numlist}|B, {A#B numlist}, and {A numlist}#{B numlist}. The same is true of higher-order custom contrasts, such as {A#B numlist}@C, {A#B numlist}#r.C, and {A#B numlist}#c.x.

Higher-order interactions with at most eight factor variables are allowed with custom contrasts.

method	Description
	do not adjust for multiple comparisons; the default Bonferroni's method; adjust across all terms
<u>sid</u> ak [adjustall] <u>sch</u> effe	Šidák's method; adjust across all terms Scheffé's method

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Menu

Statistics > Postestimation > Contrasts

Description

contrast tests linear hypotheses and forms contrasts involving factor variables and their interactions from the most recently fit model. The tests include ANOVA-style tests of main effects, simple effects, interactions, and nested effects. contrast can use named contrasts to decompose these effects into comparisons against reference categories, comparisons of adjacent levels, comparisons against the grand mean, orthogonal polynomials, and such. Custom contrasts may also be specified.

contrast can be used with svy estimation results; see [SVY] svy postestimation.

Contrasts can also be computed for margins of linear and nonlinear responses; see [R] margins, contrast.

Options

Main

overall specifies that a joint hypothesis test over all terms be performed.

- asobserved specifies that factor covariates be evaluated using the cell frequencies observed in the estimation sample. The default is to treat all factor covariates as though there were an equal number of observations in each level.
- lincom specifies that user-defined contrasts be treated as linear combinations. The default is to require that all user-defined contrasts sum to zero. (Summing to zero is part of the definition of a contrast.)

Equations

equation(*eqspec*) specifies the equation from which contrasts are to be computed. The default is to compute contrasts from the first equation.

atequations specifies that the contrasts be computed within each equation.

Advanced

- emptycells (*empspec*) specifies how empty cells are handled in interactions involving factor variables that are being treated as balanced.
 - emptycells(strict) is the default; it specifies that contrasts involving empty cells be treated as not estimable.
 - emptycells(reweight) specifies that the effects of the observed cells be increased to accommodate any missing cells. This makes the contrast estimable but changes its interpretation.

noestimcheck specifies that contrast not check for estimability. By default, the requested contrasts are checked and those found not estimable are reported as such. Nonestimability is usually caused by empty cells. If noestimcheck is specified, estimates are computed in the usual way and reported even though the resulting estimates are manipulable, which is to say they can differ across equivalent models having different parameterizations.

Reporting

- level(#) specifies the confidence level, as a percentage, for confidence intervals. The default is level(95) or as set by set level; see [U] 20.7 Specifying the width of confidence intervals.
- mcompare(*method*) specifies the method for computing *p*-values and confidence intervals that account for multiple comparisons within a factor-variable term.

Most methods adjust the comparisonwise error rate, α_c , to achieve a prespecified experimentwise error rate, α_e .

mcompare(noadjust) is the default; it specifies no adjustment.

$$\alpha_c = \alpha_e$$

mcompare(bonferroni) adjusts the comparisonwise error rate based on the upper limit of the Bonferroni inequality

$$\alpha_e \leq m \alpha_c$$

where m is the number of comparisons within the term.

The adjusted comparisonwise error rate is

$$\alpha_c = \alpha_e/m$$

mcompare(sidak) adjusts the comparisonwise error rate based on the upper limit of the probability
inequality

$$\alpha_e \leq 1 - (1 - \alpha_c)^m$$

where m is the number of comparisons within the term.

The adjusted comparisonwise error rate is

$$\alpha_c = 1 - (1 - \alpha_e)^{1/m}$$

This adjustment is exact when the m comparisons are independent.

- mcompare(scheffe) controls the experimentwise error rate using the F or χ^2 distribution with degrees of freedom equal to the rank of the term.
- mcompare(*method* adjustall) specifies that the multiple-comparison adjustments count all comparisons across all terms rather than performing multiple comparisons term by term. This leads to more conservative adjustments when multiple variables or terms are specified in *marginslist*. This option is compatible only with the bonferroni and sidak methods.
- noeffects suppresses the table of individual contrasts with confidence intervals. This table is produced by default when the mcompare() option is specified or when a term in *termlist* implies all individual contrasts.
- cieffects specifies that a table containing a confidence interval for each individual contrast be reported.
- pveffects specifies that a table containing a *p*-value for each individual contrast be reported.
- effects specifies that a single table containing a confidence interval and *p*-value for each individual contrast be reported.

nowald suppresses the table of Wald tests.

- noatlevels indicates that only the overall Wald test be reported for each term containing within or nested (@ or |) operators.
- nosvyadjust is for use with svy estimation commands. It specifies that the Wald test be carried out without the default adjustment for the design degrees of freedom. That is to say the test is carried out as $W/k \sim F(k, d)$ rather than as $(d k + 1)W/(kd) \sim F(k, d k + 1)$, where k is the dimension of the test and d is the total number of sampled PSUs minus the total number of strata.
- sort specifies that the table of individual contrasts be sorted by the contrast values within each term.
- post causes contrast to behave like a Stata estimation (e-class) command. contrast posts the vector of estimated contrasts along with the estimated variance-covariance matrix to e(), so you can treat the estimated contrasts just as you would results from any other estimation command. For example, you could use test to perform simultaneous tests of hypotheses on the contrasts, or you could use lincom to create linear combinations.
- display_options: vsquish, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt), sformat(%fmt), and nolstretch.
 - vsquish specifies that the blank space separating factor-variable terms or time-series-operated variables from other variables in the model be suppressed.
 - nofvlabel displays factor-variable level values rather than attached value labels. This option overrides the fvlabel setting; see [R] set showbaselevels.
 - fvwrap(#) specifies how many lines to allow when long value labels must be wrapped. Labels
 requiring more than # lines are truncated. This option overrides the fvwrap setting; see [R] set
 showbaselevels.
 - fvwrapon(*style*) specifies whether value labels that wrap will break at word boundaries or break based on available space.

fvwrapon(word), the default, specifies that value labels break at word boundaries.

fvwrapon(width) specifies that value labels break based on available space.

This option overrides the fvwrapon setting; see [R] set showbaselevels.

- cformat(% fint) specifies how to format contrasts, standard errors, and confidence limits in the table of estimated contrasts.
- pformat (% fmt) specifies how to format p-values in the table of estimated contrasts.
- sformat (% fmt) specifies how to format test statistics in the table of estimated contrasts.
- nolstretch specifies that the width of the table of estimated contrasts not be automatically widened to accommodate longer variable names. The default, lstretch, is to automatically widen the table of estimated contrasts up to the width of the Results window. To change the default, use set lstretch off. nolstretch is not shown in the dialog box.
- *eform_option* specifies that the contrasts table be displayed in exponentiated form. e^{contrast} is displayed rather than contrast. Standard errors and confidence intervals are also transformed. See [R] *eform_option* for the list of available options.

The following option is available with contrast but is not shown in the dialog box:

df(#) specifies that the t distribution with # degrees of freedom be used for computing p-values and confidence intervals. The default is to use e(df_r) degrees of freedom or the standard normal distribution if e(df_r) is missing.

Remarks and examples

stata.com

Remarks are presented under the following headings:

Introduction One-way models Estimated cell means Testing equality of cell means Reference category contrasts Reverse adjacent contrasts Orthogonal polynomial contrasts Two-way models Estimated interaction cell means Simple effects Interaction effects Main effects Partial interaction effects Three-way and higher-order models Contrast operators Differences from a reference level (r.) Differences from the next level (a.) Differences from the previous level (ar.) Differences from the grand mean (g.) Differences from the mean of subsequent levels (h.) Differences from the mean of previous levels (j.) Orthogonal polynomials (p. and q.) User-defined contrasts Empty cells Empty cells, ANOVA style Nested effects Multiple comparisons Unbalanced data Using observed cell frequencies Weighted contrast operators Testing factor effects on slopes Chow tests Beyond linear models Multiple equations Video example

Introduction

contrast performs ANOVA-style tests of main effects, interactions, simple effects, and nested effects. It can easily decompose these tests into constituent contrasts using either named contrasts (codings) or user-specified contrasts. Comparing levels of factor variables—whether as main effects, interactions, or simple effects—is as easy as adding a contrast operator to the variable. The operators can compare each level with the previous level, each level with a reference level, each level with the mean of previous levels, and more.

contrast tests and estimates contrasts. A contrast of the parameters $\mu_1, \mu_2, \ldots, \mu_p$ is a linear combination $\sum_i c_i \mu_i$ whose c_i sum to zero. A difference of population means that $\mu_1 - \mu_2$ is a contrast, as are most other comparisons of population or model quantities (Coster 2005). Some contrasts may be estimated with lincom, but contrast is much more powerful. contrast can handle multiple contrasts simultaneously, and the command's contrast operators make it easy to specify complicated linear combinations.

Both the contrast operation and the creation of the margins for comparison can be performed as though the data were balanced (typical for experimental designs) or using the observed frequencies in the estimation sample (typical for observational studies). contrast can perform these analyses on the results of almost all of Stata's estimators, not just the linear-models estimators.

Most of contrast's computations can be considered comparisons of estimated cell means from a model fit. Tests of interactions are tests of whether the cell means for the interaction are all equal. Tests of main effects are tests of whether the marginal cell means for the factor are all equal. More focused comparisons of cell means (for example, is level 2 equal to level 1) are specified using contrast operators. More formally, all of contrast's computations are comparisons of conditional expectations; cell means are one type of conditional expectation.

All contrasts can also easily be graphed; see [R] marginsplot.

For a discussion of contrasts and testing for linear models, see Searle (1971) and Searle (1997). For discussions specifically related to experimental design, see Kuehl (2000), Winer, Brown, and Michels (1991), and Milliken and Johnson (2009). Rosenthal, Rosnow, and Rubin (2000) focus on contrasts with applications in behavioral sciences. Mitchell (2012) focuses on contrasts in Stata.

contrast is a flexible tool for understanding the effects of categorical covariates. If your model contains categorical covariates, and especially if it contains interactions, you will want to use contrast.

One-way models

Suppose we have collected data on cholesterol levels for individuals from five age groups. To study the effect of age group on cholesterol, we can begin by fitting a one-way model using regress:

```
. use http://www.stata-press.com/data/r13/cholesterol
(Artificial cholesterol data)
. label list ages
ages:
           1 10-19
           2 20-29
           3 30-39
           4 40-59
           5 60-79
 regress chol i.agegrp
                                                          Number of obs =
      Source
                      SS
                               df
                                         MS
                                                                                75
                                                          F( 4,
                                                                    70) =
                                                                             35.02
       Model
                14943.3997
                                   3735.84993
                                                          Prob > F
                                                                            0.0000
                                4
                                                                        =
                               70
   Residual
                7468.21971
                                   106.688853
                                                          R-squared
                                                                        =
                                                                            0.6668
                                                          Adj R-squared =
                                                                            0.6477
                22411.6194
                               74
                                   302.859722
                                                          Root MSE
       Total
                                                                            10.329
                                                                         =
                     Coef.
                             Std. Err.
                                                  P>|t|
                                                             [95% Conf. Interval]
        chol
                                             t.
      agegrp
      20-29
                 8.203575
                             3.771628
                                           2.18
                                                  0.033
                                                             .6812991
                                                                          15.72585
      30-39
                             3.771628
                                           5.71
                                                                          29.06333
                 21.54105
                                                  0.000
                                                             14.01878
      40-59
                  30.15067
                             3.771628
                                           7.99
                                                  0.000
                                                              22.6284
                                                                          37.67295
      60-79
                 38.76221
                             3.771628
                                                  0.000
                                                             31.23993
                                                                          46.28448
                                          10.28
                  180.5198
                             2.666944
                                          67.69
                                                  0.000
                                                             175.2007
                                                                          185.8388
       _cons
```

Estimated cell means

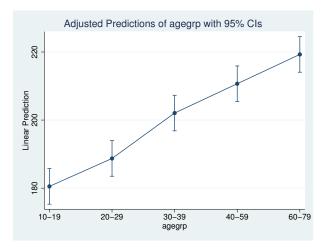
margins will show us the estimated cell means for each age group based on our fitted model:

. margins ageg	grp					
Adjusted predi	ictions			Numbe	r of obs =	75
Model VCE	: OLS					
Expression : Linear prediction, predict()						
	I	Delta-method				
	Margin	Std. Err.	t	P> t	[95% Conf.	Interval]
agegrp						
10-19	180.5198	2.666944	67.69	0.000	175.2007	185.8388
20-29	188.7233	2.666944	70.76	0.000	183.4043	194.0424
30-39	202.0608	2.666944	75.76	0.000	196.7418	207.3799
40-59	210.6704	2.666944	78.99	0.000	205.3514	215.9895
60-79	219.282	2.666944	82.22	0.000	213.9629	224.601

We can graph those means with marginsplot:

. marginsplot

Variables that uniquely identify margins: agegrp



Testing equality of cell means

Are all the means equal? That is to say is there an effect of age group on cholesterol level? We can answer that by asking contrast to test whether the means of the age groups are identical.

. contrast agegrp					
Contrasts of marginal linear predictions					
Margins : asbalanced					
	df	F	P>F		
agegrp	4	35.02	0.0000		
Denominator	70				

The means are clearly different. We could have obtained this same test directly had we fit our model using anova rather than regress.

. anova chol agegrp

		Number of obs Root MSE			squared j R-squared	
	Source	Partial SS	df	MS	F	Prob > F
-	Model	14943.3997	4	3735.84993	35.02	0.0000
	agegrp	14943.3997	4	3735.84993	35.02	0.0000
	Residual	7468.21971	70	106.688853		
-	Total	22411.6194	74	302.859722		

Achieving a more direct test result is why we recommend using anova instead of regress for models where our focus is on the categorical covariates. The models fit by anova and regress are identical; they merely parameterize the effects differently. The results of contrast will be identical regardless of which command is used to fit the model. If, however, we were fitting models whose responses are nonlinear functions of the covariates, such as logistic regression, then there would be no analogue to anova, and we would appreciate contrast's ability to quickly test main effects and interactions.

Reference category contrasts

Now that we know that the overall effect of age group is statistically significant, we can explore the effects of each age group. One way to do that is to use the reference category operator, r.:

```
. contrast r.agegrp
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F	
agegrp	1	4 70		
(20-29 vs 10-19) (30-39 vs 10-19)	1	4.73 32.62	0.0330 0.0000	
(40-59 vs 10-19)	1	63.91	0.0000	
(60-79 vs 10-19)	1	105.62	0.0000	
Joint	4	35.02	0.0000	
Denominator	70			
	Contrast	Std. Err.	[95% Conf	. Interval]
agegrp				
(20-29 vs 10-19)	8.203575	3.771628	.6812991	15.72585
(30-39 vs 10-19)	21.54105	3.771628	14.01878	29.06333
(40-59 vs 10-19)	30.15067	3.771628	22.6284	37.67295
(60-79 vs 10-19)	38.76221	3.771628	31.23993	46.28448

The cell mean of each age group is compared against the base age group (ages 10–19). The first table shows that each difference is significant. The second table gives an estimate and confidence interval for each contrast. These are the comparisons that linear regression gives with a factor covariate and no interactions. The contrasts are identical to the coefficients from our linear regression.

Reverse adjacent contrasts

We have far more flexibility with contrast. Age group is ordinal, so it is interesting to compare each age group with the preceding age group (rather than against one reference group). We specify that analysis by using the reverse adjacent operator, ar.:

. contrast ar.agegrp					
Contrasts of marginal linear predictions					
Margins : asba	Margins : asbalanced				
	df	F	P>F		
agegrp					
(20-29 vs 10-19)	1	4.73	0.0330		
(30-39 vs 20-29)	1	12.51	0.0007		
(40-59 vs 30-39)	1	5.21	0.0255		
(60-79 vs 40-59)	1	5.21	0.0255		
Joint	4	35.02	0.0000		
Denominator 70					

	Contrast	Std. Err.	[95% Conf. Interval]
agegrp (20-29 vs 10-19) (30-39 vs 20-29) (40-59 vs 30-39) (60-79 vs 40-59)	8.203575 13.33748 8.60962 8.611533	3.771628 3.771628 3.771628 3.771628	.6812991 15.72585 5.815204 20.85976 1.087345 16.1319 1.089257 16.13381

The 20–29 age group's cholesterol level is 8.2 points higher than the 10–19 age group's cholesterol level; the 30–39 age group's level is 13.3 points higher than the 20–29 age group's level; and so on. Each age group is statistically different from the preceding age group at the 5% level.

Orthogonal polynomial contrasts

The relationship between age group and cholesterol level looked almost linear in our graph. We can examine that relationship further by using the orthogonal polynomial operator, p.:

. contrast p.a	agegrp, noeffec	ts	
Contrasts of m	marginal linear	predictions	3
Margins	: asbalanced		
	df	F	P>F
agegrp			
(linear)	1	139.11	0.0000
(quadratic)	1	0.15	0.6962
(cubic)	1	0.37	0.5448
(quartic)	1	0.43	0.5153
Joint	4	35.02	0.0000
Denominator	70		

Only the linear effect is statistically significant.

We can even perform the joint test that all effects beyond linear are zero. We do that by selecting all polynomial contrasts above linear—that is, polynomial contrasts 2, 3, and 4.

-	2 3 4).agegrp, no marginal linear j		5
Margins	asbalanced		
	df	F	P>F
agegrp			
(quadratic)	1	0.15	0.6962
(cubic)	1	0.37	0.5448
(quartic)	1	0.43	0.5153
Joint	3	0.32	0.8129
Denominator	70		

The joint test has three degrees of freedom and is clearly insignificant. A linear effect of age group seems adequate for this model.

Two-way models

Suppose we are investigating the effects of different dosages of a blood pressure medication and believe that the effects may be different for men and women. We can fit the following ANOVA model for bpchange, the change in diastolic blood pressure. Change is defined as the after measurement minus the before measurement, so that negative values of bpchange correspond to decreases in blood pressure.

. anova bpchange dose##gender

	Number of obs Root MSE			-squared lj R-squared	= 0.9647 = 0.9573
Source	Partial SS	df	MS	F	Prob > F
Model	1411.9087	5	282.381741	131.09	0.0000
dose	963.481795	2	481.740897	223.64	0.0000
gender	355.118817	1	355.118817	164.85	0.0000
dose#gender	93.3080926	2	46.6540463	21.66	0.0000
Residual	51.699253	24	2.15413554		
Total	1463.60796	29	50.4692399		

Estimated interaction cell means

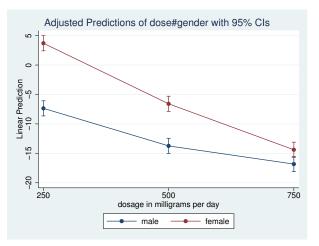
Everything is significant, including the interaction. So increasing dosage is effective and differs by gender. Let's explore the effects. First, let's look at the estimated cell mean of blood pressure change for each combination of gender and dosage.

. margins dose	e#gender					
Adjusted predi	ictions			Numbe	er of obs =	30
Expression :	: Linear pred	iction, pred	ict()			
	·····					
]]]	Delta-method	l			
	Margin	Std. Err.	t	P> t	[95% Conf.	Interval]
dose#gender						
250#male	-7.35384	.6563742	-11.20	0.000	-8.708529	-5.99915
250#female	3.706567	.6563742	5.65	0.000	2.351877	5.061257
500#male	-13.73386	.6563742	-20.92	0.000	-15.08855	-12.37917
500#female	-6.584167	.6563742	-10.03	0.000	-7.938857	-5.229477
750#male	-16.82108	.6563742	-25.63	0.000	-18.17576	-15.46639
750#female	-14.38795	.6563742	-21.92	0.000	-15.74264	-13.03326

Our data are balanced, so these results will not be affected by the many different ways that margins can compute cell means. Moreover, because our model consists of only dose and gender, these are also the point estimates for each combination.

We can graph the results:

```
. marginsplot
Variables that uniquely identify margins: dose gender
```



The lines are not parallel, which we expected because the interaction term is significant. Males experience a greater decline in blood pressure at every dosage level, but the effect of increasing dosage is greater for females. In fact, it is not clear if we can tell the difference between male and female response at the maximum dosage.

Simple effects

We can contrast the male and female responses within dosage to see the simple effects of gender. Because there are only two levels in gender, the choice of contrast operator is largely irrelevant. Aside from orthogonal polynomials, all operators produce the same estimates, although the effects can change signs.

```
. contrast r.gender@dose
Contrasts of marginal linear predictions
Margins
              : asbalanced
                                  df
                                                F
                                                         P>F
          gender@dose
(female vs male) 250
                                   1
                                           141.97
                                                      0.0000
(female vs male) 500
                                            59.33
                                                      0.0000
                                   1
(female vs male) 750
                                            6.87
                                                      0.0150
                                   1
                Joint
                                   3
                                            69.39
                                                      0.0000
          Denominator
                                  24
                                                       [95% Conf. Interval]
                           Contrast
                                       Std. Err.
          gender@dose
(female vs male) 250
                           11.06041
                                        .9282533
                                                      9.144586
                                                                   12.97623
(female vs male) 500
                           7.149691
                                       .9282533
                                                       5.23387
                                                                   9.065512
(female vs male) 750
                           2.433124
                                       .9282533
                                                      .5173031
                                                                   4.348944
```

The effect for males is about 11 points higher than for females at a dosage of 250, and that shrinks to 2.4 points higher at the maximum dosage of 750.

We can form the simple effects the other way by contrasting the effect of dose at each level of gender:

```
. contrast ar.dose@gender
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F
dose@gender			
(500 vs 250) male	1	47.24	0.0000
(500 vs 250) female	1	122.90	0.0000
(750 vs 500) male	1	11.06	0.0028
(750 vs 500) female	1	70.68	0.0000
Joint	4	122.65	0.0000
Denominator	24		

	Contrast	Std. Err.	[95% Conf. Interval]
dose@gender (500 vs 250) male (500 vs 250) female (750 vs 500) male (750 vs 500) female	-6.380018 -10.29073 -3.087217 -7.803784	.9282533 .9282533 .9282533 .9282533	-8.295839 -4.464198 -12.20655 -8.374914 -5.003038 -1.171396 -9.719605 -5.887963

Here we use the ar. reverse adjacent contrast operator so that first we are comparing a dosage of 500 with a dosage of 250, and then we are comparing 750 with 500. We see that increasing the dosage has a larger effect on females—10.3 points when going from 250 to 500 compared with 6.4 points for males, and 7.8 points when going from 500 to 750 versus 3.1 points for males.

Interaction effects

By specifying contrast operators on both factors, we can decompose the interaction effect into separate interaction contrasts.

. contrast ar.dose#r.gender Contrasts of marginal linear predictions Margins : asbalanced

	df	F	P>F
dose#gender (500 vs 250) (female vs male) (750 vs 500) (female vs male) Joint	1 1 2	8.87 12.91 21.66	0.0065 0.0015 0.0000
Denominator	24		

	Contrast	Std. Err.	[95% Conf	. Interval]
dose#gender (500 vs 250)				
(female vs male) (750 vs 500)	-3.910716	1.312748	-6.620095	-1.201336
(female vs male)	-4.716567	1.312748	-7.425947	-2.007187

Look for departures from zero to indicate an interaction effect between dose and gender. Both contrasts are significantly different from zero. Of course, we already knew the overall interaction was significant from our ANOVA results. The effect of increasing dose from 250 to 500 is 3.9 points greater in females than in males, and the effect of increasing dose from 500 to 750 is 4.7 points greater in females than in males. The confidence intervals for both estimates easily exclude zero, meaning that there is an interaction effect.

The joint test of these two interaction effects reproduces the test of interaction effects in the anova output. We can see that the F statistic of 21.66 matches the statistic from our original ANOVA results.

Main effects

We can perform tests of the main effects by listing each variable individually in contrast.

. contrast dose gender Contrasts of marginal linear predictions					
Margins : asbalanced					
	df	F	P>F		
dose	2	223.64	0.0000		
gender	1	164.85	0.0000		
Denominator	24				

The F tests are equivalent to the tests of main effects in the anova output. This is true only for linear models. contrast provides an easy way to obtain main effects and other ANOVA-style tests for models whose responses are not linear in the parameters—logistic, probit, glm, etc.

If we include contrast operators on the variables, we can also decompose the main effects into individual contrasts:

. contrast ar.c Contrasts of ma	0	predictions	
	asbalanced	predictions	
	df	F	P>F
dose			
(500 vs 250)	1	161.27	0.0000
(750 vs 500)	1	68.83	0.0000
Joint	2	223.64	0.0000
gender	1	164.85	0.0000
Denominator	24		

	Contrast	Std. Err.	[95% Conf.	Interval]
dose (500 vs 250) (750 vs 500)	-8.335376 -5.4455	.6563742 .6563742	-9.690066 -6.80019	-6.980687 -4.090811
gender (female vs male)	6.881074	.5359273	5.774974	7.987173

By specifying the ar. operator on dose, we decompose the main effect for dose into two one-degreeof-freedom contrasts, comparing the marginal mean of blood pressure change for each dosage level with that of the previous level. Because gender has only two levels, we cannot decompose this main effect any further. However, specifying a contrast operator on gender allowed us to calculate the difference in the marginal means for women and men.

Partial interaction effects

At this point, we have looked at the total interaction effects and at the main effects of each variable. The partial interaction effects are a midpoint between these two types of effects where we collect the individual interaction effects along the levels of one of the variables and perform a joint test of those interactions. If we think of the interaction effects as forming a table, with the levels of one factor variable forming the rows and the levels of the other forming the columns, partial interaction effects are joint tests of the interactions in a row or a column. To perform these tests, we specify a contrast operator on only one of the variables in our interaction. For this particular model, these are not very interesting because our variables have only two and three levels. Therefore, the tests of the partial interaction effects reproduce the tests that we obtained for the total interaction effects. We specify a contrast operator only on dose to decompose the overall test for interaction effects into joint tests for each ar.dose contrast:

. contrast ar.dose#gender Contrasts of marginal linear predictions Margins : asbalanced

	df	F	P>F
dose#gender (500 vs 250) (joint) (750 vs 500) (joint) Joint	1 1 2	8.87 12.91 21.66	0.0065 0.0015 0.0000
Denominator	24		

The first row is a joint test of all the interaction effects involving the (500 vs 250) comparison of dosages. The second row is a joint test of all the interaction effects involving the (750 vs 500) comparison. If we look back at our output in *Interaction effects*, we can see that there was only one of each of these interaction effects. Therefore, each test labeled (joint) has only one degree-of-freedom.

We could have instead included a contrast operator on gender to compute the partial interaction effects along the other dimension:

. contrast dose#r.gender						
Contrasts of marginal linear predictions						
Margins : asbalanced						
	·					
	df	F	P>F			
dose#gender	2	21.66	0.0000			
Denominator	24					

Here we obtain a joint test of all the interaction effects involving the (female vs male) comparison for gender. Because gender has only two levels, the (female vs male) contrast is the only reference category contrast possible. Therefore, we obtain a single joint test of all the interaction effects.

Clearly, the partial interaction effects are not interesting for this particular model. However, if our factors had more levels, the partial interaction effects would produce tests that are not available in the total interaction effects. For example, if our model included factors for four dosage levels and three races, then typing

. contrast ar.dose#race

would produce three joint tests, one for each of the reverse adjacent contrasts for dosage. Each of these tests would be a two-degree-of-freedom test because race has three levels.

Three-way and higher-order models

All the contrasts and tests that we reviewed above for two-way models can be used with models that have more terms. For instance, we could fit a three-way full factorial model by using the anova command:

```
. use http://www.stata-press.com/data/r13/cont3way
```

. anova y race##sex##group

We could then test the simple effects of race within each level of the interaction between sex and group:

. contrast race@sex#group

To see the reference category contrasts that decompose these simple effects, type

. contrast r.race@sex#group

We could test the three-way interaction effects by typing

. contrast race#sex#group

or the interaction effects for the interaction of race and sex by typing

. contrast race#sex

To see the individual reference category contrasts that decompose this interaction effect, type

. contrast r.race#r.sex

We could even obtain joint tests for the interaction of race and sex within each level of group by typing

. contrast race#sex@group

For tests of the main effects of each factor, we can type

. contrast race sex group

We can calculate the individual reference category contrasts that decompose these main effects:

. contrast r.race r.sex r.group

For the partial interaction effects, we could type

. contrast r.race#group

to obtain a joint test of the two-way interaction effects of race and group for each of the individual r.race contrasts.

We could type

. contrast r.race#sex#group

to obtain a joint test of all the three-way interaction terms for each of the individual r.race contrasts.

Contrast operators

contrast recognizes a set of contrast operators that are used to specify commonly used contrasts. When these operators are used, contrast will report a test for each individual contrast in addition to the joint test for the term. We have already seen a few of these, like r. and ar., in the previous examples. Here we will take a closer look at each of the unweighted operators.

Here we use the cholesterol dataset and the one-way ANOVA model from the example in *One-way* models:

```
. use http://www.stata-press.com/data/r13/cholesterol
(Artificial cholesterol data)
. anova chol agegrp
  (output omitted)
```

The margins command reports the estimated cell means, $\hat{\mu}_1, \ldots, \hat{\mu}_5$, for each of the five age groups.

	Margin	Delta-method Std. Err.	t	P> t	[95% Conf.	Interval]
agegrp						
10-19	180.5198	2.666944	67.69	0.000	175.2007	185.8388
20-29	188.7233	2.666944	70.76	0.000	183.4043	194.0424
30-39	202.0608	2.666944	75.76	0.000	196.7418	207.3799
40-59	210.6704	2.666944	78.99	0.000	205.3514	215.9895
60-79	219.282	2.666944	82.22	0.000	213.9629	224.601

Contrast operators provide an easy way to make certain types of comparisons of these cell means. We use the ordinal factor agegrp to demonstrate these operators because some types of contrasts are only meaningful when the levels of the factor have a natural ordering. We demonstrate these contrast operators using a one-way model; however, they are equally applicable to main effects, simple effects, and interactions for more complicated models.

Differences from a reference level (r.)

The r. operator specifies that each level of the attached factor variable be compared with a reference level. These are referred to as reference-level or reference-category contrasts (or effects), and r. is the reference-level operator.

In the following, we use the **r**. operator to test the effect of each category of age group when that category is compared with a reference category.

. contrast r.agegr	þ			
Contrasts of margin	al linear pro	edictions		
Margins : asba	alanced			
	df	F	P>F	
agegrp				
(20-29 vs 10-19) (30-39 vs 10-19)	1	4.73 32.62	0.0330	
(40-59 vs 10-19)	1	63.91	0.0000	
(60-79 vs 10-19)	1	105.62	0.0000	
Joint	4	35.02	0.0000	
Denominator	70			
	Contrast	Std. Err.	[95% Conf	. Interval]
agegrp	0 000575	0.774000		
(20-29 vs 10-19)	8.203575 21.54105		.6812991 14.01878	15.72585 29.06333
(30-39 vs 10-19) (40-59 vs 10-19)	21.54105 30.15067		22.6284	
(40 05 VS 10 15) (60-79 vs 10-19)	38.76221		31.23993	
	L			

In the first table, the row labeled (20-29 vs 10-19) is a test of $\mu_2 = \mu_1$, a test that the mean cholesterol levels for the 10-19 age group and the 20-29 age group are equal. The tests in the next three rows are defined similarly. The row labeled Joint provides the joint test for these four hypotheses, which is just the test of the main effects of age group.

The second table provides the contrasts of each category with the reference category along with confidence intervals. The contrast in the row labeled (20-29 vs 10-19) is the difference in the cell means of the second age group and the first age group, $\hat{\mu}_2 - \hat{\mu}_1$.

The first level of a factor is the default reference level, but we can specify a different reference level by using the b. operator; see [U] **11.4.3.2 Base levels**. Here we use the last age group, (60-79), instead of the first as the reference category. We also include the nowald option so that only the table of contrasts and their confidence intervals is produced.

Margins : asbalanced							
		Contrast	Std. Err.	[95% Conf.	Interval]		
(10-19 vs (20-29 vs (30-39 vs (40-59 vs	60-79) 60-79)	-38.76221 -30.55863 -17.22115 -8.611533	3.771628 3.771628 3.771628 3.771628	-46.28448 -38.08091 -24.74343 -16.13381	-31.23993 -23.03636 -9.698877 -1.089257		

. contrast rb5.agegrp, nowald Contrasts of marginal linear predictions Margins : asbalanced

Now the first row is labeled (10-19 vs 60-79) and is the difference in the cell means of the first and fifth age groups.

Differences from the next level (a.)

The a. operator specifies that each level of the attached factor variable be compared with the next level. These are referred to as adjacent contrasts (or effects), and a. is the adjacent operator. This operator is only meaningful with factor variables that have a natural ordering in the levels.

We can use the a. operator to perform tests that each level of age group differs from the next adjacent level.

. contrast a.agegrp							
Contrasts of margin	nal linear pro	edictions					
Margins : asba	alanced						
	df	F	P>F				
agegrp		4 70	0.0000				
(10-19 vs 20-29) (20-29 vs 30-39)	1	4.73 12.51	0.0330 0.0007				
(30-39 vs 40-59)	1	5.21	0.0255				
(40-59 vs 60-79)	1	5.21	0.0255				
Joint	4	35.02	0.0000				
Denominator	70						
	Contrast	Std. Err.	[95% Conf.	[Interval]			
agegrp (10-19 vs 20-29) (20-29 vs 30-39) (30-39 vs 40-59) (40-59 vs 60-79)	-8.203575 -13.33748 -8.60962 -8.611533	3.771628 3.771628	-15.72585 -20.85976 -16.1319 -16.13381	-1.087345			

In the first table, the row labeled (10-19 vs 20-29) tests the effect of belonging to the 10-19 age group instead of the 20-29 age group. Likewise, the rows labeled (20-29 vs 30-39), (30-39 vs 40-59), and (40-59 vs 60-79) are tests for the effects of being in the younger of the two age groups instead of the older one.

In the second table, the contrast in the row labeled (10-19 vs 20-29) is the difference in the cell means of the first and second age groups, $\hat{\mu}_1 - \hat{\mu}_2$. The contrasts in the other rows are defined similarly.

Differences from the previous level (ar.)

The ar. operator specifies that each level of the attached factor variable be compared with the previous level. These are referred to as reverse adjacent contrasts (or effects), and ar. is the reverse adjacent operator. As with the a. operator, this operator is only meaningful with factor variables that have a natural ordering in the levels.

In the following, we use the ar. operator to report tests for the individual reverse adjacent effects of agegrp.

. contrast ar.ageg	rp			
Contrasts of margin	nal linear pro	edictions		
Margins : asba	alanced			
	df	F	P>F	
agegrp				
(20-29 vs 10-19) (30-39 vs 20-29)	1	4.73 12.51	0.0330 0.0007	
(40-59 vs 30-39)	1	5.21	0.0255	
(60-79 vs 40-59) Joint	1 4	5.21 35.02	0.0255 0.0000	
501110	4	35.02	0.0000	
Denominator	70			
	Contrast	Std. Err.	[95% Conf	. Interval
agegrp (20-29 vs 10-19)	9 002575	3.771628	.6812991	15.7258
(20-29 VS 10-19) (30-39 VS 20-29)	13.33748		5.815204	20.8597
(40-59 vs 20-39)	8.60962		1.087345	
(40 05 VS 00 05) (60-79 vs 40-59)	8.611533		1.089257	16.1338

Here the Wald tests in the first table for the individual reverse adjacent effects are equivalent to the tests for the adjacent effects in the previous example. However, if we compare values of the contrasts in the bottom tables, we see the difference between the **r**. and the **ar**. operators. This time, the contrast in the first row is labeled (20-29 vs 10-19) and is the difference in the cell means of the second and first age groups, $\hat{\mu}_2 - \hat{\mu}_1$. This is the estimated effect of belonging to the 20-29 age group instead of the 10-19 age group. The remaining rows make similar comparisons to the previous level.

Differences from the grand mean (g.)

The g. operator specifies that each level of a factor variable be compared with the grand mean of all levels. For this operator, the grand mean is computed using a simple average of the cell means.

Here are the grand mean effects of agegrp:

. contrast g.agegrp Contrasts of marginal linear predictions Margins : asbalanced							
	df	F	P>F				
agegrp							
(10-19 vs mean)	1	68.42	0.0000				
(20-29 vs mean)	1	23.36	0.0000				
(30-39 vs mean)	1	0.58	0.4506				
(40-59 vs mean)	1	19.08	0.0000				
(60-79 vs mean)	1	63.65	0.0000				
Joint	4	35.02	0.0000				
Denominator	70						
	Contrast	Std. Err.	[95% Conf.	Interval]			
agegrp (10-19 vs mean) (20-29 vs mean) (30-39 vs mean) (40-59 vs mean) (60-79 vs mean)	-19.7315 -11.52793 1.809552 10.41917 19.0307	2.385387 2.385387	-24.48901 -16.28543 -2.947953 5.661668 14.2732				

There are five age groups in our estimation sample. Thus the row labeled (10-19 vs mean) tests $\mu_1 = (\mu_1 + \mu_2 + \mu_3 + \mu_4 + \mu_5)/5$. The row labeled (20-29 vs mean) tests $\mu_2 = (\mu_1 + \mu_2 + \mu_3 + \mu_4 + \mu_5)/5$. The remaining rows perform similar tests for the third, fourth, and fifth age groups. In our example, the means for all age groups except the 30-39 age group are statistically different from the grand mean.

Differences from the mean of subsequent levels (h.)

The h. operator specifies that each level of the attached factor variable be compared with the mean of subsequent levels. These are referred to as Helmert contrasts (or effects), and h. is the Helmert operator. For this operator, the mean is computed using a simple average of the cell means. This operator is only meaningful with factor variables that have a natural ordering in the levels.

Here are the Helmert contrasts for agegrp:

```
. contrast h.agegrp
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F
agegrp (10-19 vs >10-19) (20-29 vs >20-29) (30-39 vs >30-39) (40-59 vs 60-79) Joint	1 1 1 1 4	68.42 50.79 15.63 5.21 35.02	0.0000 0.0000 0.0002 0.0255 0.0000
Denominator	70		

	Contrast	Std. Err.	[95% Conf. Interval]
agegrp (10-19 vs >10-19) (20-29 vs >20-29) (30-39 vs >30-39) (40-59 vs 60-79)	-24.66438 -21.94774 -12.91539 -8.611533	2.981734 3.079522 3.266326 3.771628	-30.61126 -18.7175 -28.08965 -15.80583 -19.42987 -6.400905 -16.13381 -1.089257

The row labeled (10-19 vs >10-19) tests $\mu_1 = (\mu_2 + \mu_3 + \mu_4 + \mu_5)/4$, that is, that the cell mean for the youngest age group is equal to the average of the cell means for the older age groups. The row labeled (20-29 vs >20-29) tests $\mu_2 = (\mu_3 + \mu_4 + \mu_5)/3$. The tests in the other rows are defined similarly.

Differences from the mean of previous levels (j.)

The j. operator specifies that each level of the attached factor variable be compared with the mean of the previous levels. These are referred to as reverse Helmert contrasts (or effects), and j. is the reverse Helmert operator. For this operator, the mean is computed using a simple average of the cell means. This operator is only meaningful with factor variables that have a natural ordering in the levels.

Here are the reverse Helmert contrasts of agegrp:

. contrast j.agegrp						
Contrasts of margina	al linear pred	dictions				
Margins : asbal	lanced					
	df	F	P>F			
agegrp (20-29 vs 10-19)	1	4.73	0.0330			
(30-39 vs <30-39)	1	28.51	0.0000			
(40-59 vs <40-59)	1	43.18	0.0000			
(60-79 vs <60-79)	1	63.65	0.0000			
Joint	4	35.02	0.0000			
Denominator	70					
	Contrast	Std. Err.	[95% Conf.	Interval]		
agegrp (20-29 vs 10-19) (30-39 vs <30-39) (40-59 vs <40-59)	8.203575 17.43927 20.2358	3.771628 3.266326 3.079522	.6812991 10.92479 14.09389	15.72585 23.95375 26.37771		
(40-39 Vs (40-39) (60-79 vs (60-79)	23.78838	2.981734	17.8415	29.73526		

The row labeled (20-29 vs 10-19) tests $\mu_2 = \mu_1$, that is, that the cell means for the 20-29 and the 10-19 age groups are equal. The row labeled (30-39 vs <30-29) tests $\mu_3 = (\mu_1 + \mu_2)/2$, that is, that the cell mean for the 30-39 age group is equal to the average of the cell means for the 10-19 and 20-29 age groups. The tests in the remaining rows are defined similarly.

Orthogonal polynomials (p. and q.)

The p. and q. operators specify that orthogonal polynomials be applied to the attached factor variable. Orthogonal polynomial contrasts allow us to partition the effects of a factor variable into linear, quadratic, cubic, and higher-order polynomial components. The p. operator applies orthogonal polynomials using the values of the factor variable. The q. operator applies orthogonal polynomials using the level indices. If the level values of the factor variable are equally spaced, as with our agegrp variable, then the p. and q. operators yield the same result. These operators are only meaningful with factor variables that have a natural ordering in the levels.

Because agegrp has five levels, contrast can test the linear, quadratic, cubic, and quartic effects of agegrp.

. contrast p.agegrp, noeffects							
Contrasts of marginal linear predictions							
Margins : asbalanced							
df F P>F							
agegrp							
(linear)	1	139.11	0.0000				
(quadratic)	1	0.15	0.6962				
(cubic)	1	0.37	0.5448				
(quartic)	1	0.43	0.5153				
Joint 4 35.02 0.000							
Denominator	70						

The row labeled (linear) tests the linear effect of agegrp, the only effect that appears to be significant in this case.

The labels for our agegrp variable show the age ranges that correspond to each level.

. label list ages ages: 1 10-19 2 20-29 3 30-39 4 40-59 5 60-79

Notice that these groups do not have equal widths. Now let's refit our model using the agemidpt variable. The values of agemidpt indicate the midpoint of each age group that was defined by the agegrp variable and are, therefore, not equally spaced.

. anova chol agemidpt

		Number of obs Root MSE			-squared lj R-squared		0.6668 0.6477
_	Source	Partial SS	df	MS	F	P	rob > F
	Model	14943.3997	4	3735.84993	35.02		0.0000
	agemidpt	14943.3997	4	3735.84993	35.02		0.0000
	Residual	7468.21971	70	106.688853			
	Total	22411.6194	74	302.859722			

Now if we use the q. operator, we will obtain the same results as above because the level indices of agemidpt are equivalent to the values of agegrp.

. contrast q.agemidpt, noeffects					
marginal linear	predictions	5			
: asbalanced					
T					
df	F	P>F			
1	139.11	0.0000			
1	0.15	0.6962			
1	0.37	0.5448			
1	0.43	0.5153			
4	35.02	0.0000			
70					
	df 1 1 1 1 4	arginal linear predictions : asbalanced df F 1 139.11 1 0.15 1 0.37 1 0.43 4 35.02			

However, if we use the p. operator, we will instead fit an orthogonal polynomial to the midpoint values.

. contrast p.agemidpt, noeffects						
Contrasts of marginal linear predictions						
Margins	: asbalanced					
	df	F	P>F			
agemidpt						
(linear)	1	133.45	0.0000			
(quadratic)	1	5.40	0.0230			
(cubic)	1	0.05	0.8198			
(quartic)	1	1.16	0.2850			
Joint	4	35.02	0.0000			
Denominator	70					

Using the values of the midpoints, the quadratic effect is also significant at the 5% level.

Technical note

We used the noeffects option when working with orthogonal polynomial contrasts. Apart from perhaps the sign of the contrast, the values of the individual contrasts are not meaningful for orthogonal polynomial contrasts. In addition, many textbooks provide tables with contrast coefficients that can be used to compute orthogonal polynomial contrasts where the levels of a factor are equally spaced. If we use these coefficients and calculate the contrasts manually with user-defined contrasts, as described below, the Wald tests for the polynomial terms will be equivalent, but the values of the individual contrasts will not necessarily match those that we obtain when using the polynomial contrast operator. When we use one of these contrast operators, an algorithm is used to calculate the coefficients of the polynomial contrast that will allow for unequal spacing in the levels of the factor as well as in the weights for the cell frequencies (when using pw. or qw.), as described in *Methods and formulas*.

User-defined contrasts

In the previous examples, we performed tests using contrast operators. When there is not a contrast operator available to calculate the contrast in which we are interested, we can specify custom contrasts.

Here we fit a one-way model for cholesterol on the factor race, which has three levels:

```
. label list race
race:
1 black
2 white
3 other
. anova chol race
```

-						
		Number of obs Root MSE			squared j R-squared	
	Source	Partial SS	df	MS	F	Prob > F
	Model	669.278235	2	334.639117	1.11	0.3357
	race	669.278235	2	334.639117	1.11	0.3357
	Residual	21742.3412	72	301.976961		
	Total	22411.6194	74	302.859722		

margins calculates the estimated cell mean cholesterol level for each race:

. margins race Adjusted pred:				Numbe	er of obs =	75
Expression : Linear prediction, predict()						
	Margin	Delta-method Std. Err.	t	P> t	[95% Conf.	Interval]
race black white other	204.4279 197.6132 198.7127	3.475497 3.475497 3.475497	58.82 56.86 57.18	0.000 0.000 0.000	197.4996 190.6849 191.7844	211.3562 204.5415 205.6409

Suppose we want to test the following linear combination:

$$\sum_{i=1}^{3} c_i \mu_i$$

where μ_i is the cell mean of chol when race is equal to its *i*th level (the means estimated using margins above). Assuming the c_i elements sum to zero, this linear combination is a contrast. We can specify this type of custom contrast by using the following syntax:

$$\{ race \ c_1 \ c_2 \ c_3 \}$$

The null hypothesis for the test of the main effects of race is

$$H_{0_{\text{race}}}: \mu_1 = \mu_2 = \mu_3$$

Although $H_{0_{race}}$ can be tested using any of several different contrasts on the cell means, we will test it by comparing the second and third cell means with the first. To test that the cell means for blacks and whites are equal, $\mu_1 = \mu_2$, we can specify the contrast

{race -1 1 0}

To test that the cell means for blacks and other races are equal, $\mu_1 = \mu_3$, we can specify the contrast

{race -1 0 1}

We can use both in a single call to contrast.

. contrast {ra Contrasts of m Margins		-	S	
	df	F	P>F	
race				
(1) (2)	1	1.92 1.35	0.1699 0.2488	
Joint	2	1.11	0.3357	
Denominator	72			
	Contrast	Std. Err.	[95% Conf	. Interval]
race (1) (2)	-6.814717 -5.715261	4.915095 4.915095	-16.61278 -15.51332	2.983345 4.082801

The row labeled (1) is the test for $\mu_1 = \mu_2$, the first specified contrast. The row labeled (2) is the test for $\mu_1 = \mu_3$, the second specified contrast. The row labeled Joint is the overall test for the main effects of race.

Now let's fit a model with two factors, race and age group:

. anova chol race##agegrp

	Number of obs Root MSE			squared j R-squared	= 0.7524 = 0.6946
Source	Partial SS	df	MS	F	Prob > F
Model	16861.438	14	1204.38843	13.02	0.0000
race agegrp race#agegrp	669.278235 14943.3997 1248.76005	2 4 8	334.639117 3735.84993 156.095006	3.62 40.39 1.69	0.0329 0.0000 0.1201
Residual	5550.18143	60	92.5030238		
Total	22411.6194	74	302.859722		

The null hypothesis for the test of the main effects of race is now

$$H_{0_{\text{race}}}: \mu_{1} = \mu_{2} = \mu_{3}$$

where μ_i is the marginal mean of chol when race is equal to its *i*th level.

We can use the same syntax as above to perform this test by specifying contrasts on the marginal means of race:

. contrast {ra	ace -1 1 0} {1	race -1 0 1}		
Contrasts of m	narginal linea	ar prediction	IS	
Margins	asbalanced			
	df	F	P>F	
race (1)	1	6.28	0.0150	
(2)	1	4.41		
Joint	2	3.62	0.0329	
Denominator	60			
	Contrast	Std. Err.	[95% Conf	. Interval]
race (1) (2)	-6.814717 -5.715261		-12.2562 -11.15675	

Custom contrasts may be specified on the cell means of interactions, too. Here we use margins to calculate the mean of chol for each cell in the interaction of race and agegrp:

```
. margins race#agegrp
```

. margins race	e#agegrp					
Adjusted predi	ictions			Numbe	r of obs =	75
Expression	: Linear pred:	iction, pred	ict()			
	I	Delta-method				
	Margin	Std. Err.	t	P> t	[95% Conf.	Interval]
race#agegrp						
black#10-19	179.2309	4.301233	41.67	0.000	170.6271	187.8346
black#20-29	196.4777	4.301233	45.68	0.000	187.874	205.0814
black#30-39	210.6694	4.301233	48.98	0.000	202.0656	219.2731
black#40-59	214.097	4.301233	49.78	0.000	205.4933	222.7008
black#60-79	221.6646	4.301233	51.54	0.000	213.0609	230.2684
white#10-19	186.0727	4.301233	43.26	0.000	177.469	194.6765
white#20-29	184.6714	4.301233	42.93	0.000	176.0676	193.2751
white#30-39	196.2633	4.301233	45.63	0.000	187.6595	204.867
white#40-59	209.9953	4.301233	48.82	0.000	201.3916	218.5991
white#60-79	211.0633	4.301233	49.07	0.000	202.4595	219.667
other#10-19	176.2556	4.301233	40.98	0.000	167.6519	184.8594
other#20-29	185.0209	4.301233	43.02	0.000	176.4172	193.6247
other#30-39	199.2498	4.301233	46.32	0.000	190.646	207.8535
other#40-59	207.9189	4.301233	48.34	0.000	199.3152	216.5227
other#60-79	225.118	4.301233	52.34	0.000	216.5143	233.7218

Now we are interested in testing the following linear combination of these cell means:

$$\sum_{i=1}^{3} \sum_{j=1}^{5} c_{ij} \mu_{ij}$$

We can specify this type of custom contrast using the following syntax:

{race#agegrp $c_{11} c_{12} \ldots c_{15} c_{21} c_{22} \ldots c_{25} c_{31} c_{32} \ldots c_{35}$ }

Because the marginal means of chol for each level of race are linear combinations of the cell means, we can compose the test for the main effects of race in terms of the cell means directly. The constraint that the marginal means for blacks and whites are equal, $\mu_{1.} = \mu_{2.}$, translates to the following constraint on the cell means:

$$\frac{1}{5}(\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15}) = \frac{1}{5}(\mu_{21} + \mu_{22} + \mu_{23} + \mu_{24} + \mu_{25})$$

Ignoring the common factor, we can specify this contrast as

contrast will fill in the trailing zeros for us if we neglect to specify them, so

is also allowed. The other constraint, $\mu_{1.} = \mu_{3.}$, translates to

$$\frac{1}{5}(\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15}) = \frac{1}{5}(\mu_{31} + \mu_{32} + \mu_{33} + \mu_{34} + \mu_{35})$$

This can be specified to contrast as

The following call to contrast yields the same test results as above.

. contrast {ra > {ra	ace#agegrp -1 ace#agegrp -1			1 1	1},	noeffects
Contrasts of m	narginal line	ar predictio	ons			
Margins	asbalanced					
	r					
	df	F	P>F			
race#agegrp						
(1) (1)	1	6.28	0.0150			
(2) (2)	1	4.41	0.0399			
Joint	2	3.62	0.0329			
Denominator	60					

The row labeled (1) (1) is the test for

$$\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15} = \mu_{21} + \mu_{22} + \mu_{23} + \mu_{24} + \mu_{25}$$

It was the first specified contrast. The row labeled (2) (2) is the test for

$$\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15} = \mu_{31} + \mu_{32} + \mu_{33} + \mu_{34} + \mu_{35}$$

It was the second specified contrast. The row labeled Joint tests (1) (1) and (2) (2) simultaneously.

We used the noeffects option above to suppress the table of contrasts. We can omit the 1/5 from the equations for $\mu_{1.} = \mu_{2.}$ and $\mu_{1.} = \mu_{3.}$ and still obtain the appropriate tests. However, if we want to calculate the differences in the marginal means, we must include the 1/5 = 0.2 on each of the contrast coefficients as follows:

```
. contrast {race#agegrp -0.2 -0.2 -0.2 -0.2 -0.2
0.2 0.2 0.2 0.2 0.2 0.2}
{race#agegrp -0.2 -0.2 -0.2 -0.2 -0.2
0 0 0 0 0
0.2 0.2 0.2 0.2 0.2 0.2}
```

So far, we have reproduced the reference category contrasts by specifying user-defined contrasts on the marginal means and then on the cell means. For this test, it would have been easier to use the r. contrast operator:

. contrast r.race, noeffects							
Contrasts of margin	Contrasts of marginal linear predictions						
Margins : asbalanced							
	df	F	P>F				
race							
(white vs black)	1	6.28	0.0150				
(other vs black)	1	4.41	0.0399				
Joint	2	3.62	0.0329				
Denominator	60						

In most cases, we can use contrast operators to perform tests. However, if we want to compare, for instance, the second and third age groups with the fourth and fifth age groups with the test

$$\frac{1}{2}(\mu_{\cdot 2} + \mu_{\cdot 3}) = \frac{1}{2}(\mu_{\cdot 4} + \mu_{\cdot 5})$$

there is not a contrast operator that corresponds to this particular contrast. A custom contrast is necessary.

. contrast {agegrp 0 -0.5 -0.5 0.5 0.5} Contrasts of marginal linear predictions Margins : asbalanced

	abbaranooa			
	df	F	P>F	
agegrp	1	62.19	0.0000	
Denominator	60			
	Contrast	Std. Err.	[95% Conf	. Interval]
agegrp (1)	19.58413	2.483318	14.61675	24.5515

Empty cells

An empty cell is a combination of the levels of factor variables that is not observed in the estimation sample. In the previous examples, we have seen data with three levels of race, five levels of agegrp, and all level combinations of race and agegrp present. Suppose there are no observations for white individuals in the second age group (ages 20-29).

70

13.51

0.0000

0.7582

0.7021

9.4706

11.83119

16.28928

15.39084

183.7153

```
use http://www.stata-press.com/data/r13/cholesterol2
(Artificial cholesterol data, empty cells)
. label list
ages:
            1 10-19
            2 20-29
            3 30-39
            4 40-59
            5 60-79
race:
            1 black
           2 white
           3 other
. regress chol race##agegrp
note: 2.race#2.agegrp identifies no observations in the sample
      Source
                      SS
                                df
                                          MS
                                                           Number of obs =
                                                           F( 13,
                                                                      56) =
       Model
                 15751.6113
                                13
                                    1211.66241
                                                           Prob > F
                                                                          =
    Residual
                 5022.71559
                                56
                                    89.6913498
                                                           R-squared
                                                                          =
                                                           Adj R-squared =
                                                           Root MSE
       Total
                 20774.3269
                                69
                                    301.077201
                                                                          =
        chol
                     Coef.
                              Std. Err.
                                              t.
                                                   P>|t|
                                                               [95% Conf. Interval]
        race
      white
                  12.84185
                              5.989703
                                            2.14
                                                   0.036
                                                              .8430383
                                                                           24.84067
                                           -0.03
      other
                  -.167627
                              5.989703
                                                   0.978
                                                             -12.16644
      agegrp
      20-29
                  17.24681
                              5.989703
                                            2.88
                                                   0.006
                                                              5.247991
                                                                           29.24562
      30-39
                  31.43847
                              5.989703
                                            5.25
                                                   0.000
                                                              19.43966
                                                                           43.43729
      40-59
                  34.86613
                              5.989703
                                            5.82
                                                   0.000
                                                              22.86732
                                                                           46.86495
      60-79
                  44.43374
                              5.989703
                                            7.42
                                                   0.000
                                                              32.43492
                                                                           56.43256
 race#agegrp
white#20-29
                             (empty)
                         0
white#30-39
                 -22.83983
                              8.470719
                                           -2.70
                                                   0.009
                                                             -39.80872
                                                                          -5.870939
white#40-59
                 -14.67558
                              8.470719
                                           -1.73
                                                   0.089
                                                             -31.64447
                                                                           2.293306
white#60-79
                 -10.51115
                              8.470719
                                           -1.24
                                                   0.220
                                                             -27.48004
                                                                           6.457735
other#20-29
                 -6.054425
                              8.470719
                                           -0.71
                                                   0.478
                                                             -23.02331
                                                                           10.91446
other#30-39
                 -11.48083
                              8.470719
                                           -1.36
                                                   0.181
                                                             -28.44971
                                                                           5.488063
other#40-59
                              8.470719
                                           -0.08
                                                   0.936
                                                              -17.6485
                 -.6796112
other#60-79
                 -1.578052
                              8.470719
                                           -0.19
                                                   0.853
                                                             -18.54694
                                                   0.000
                  175.2309
                              4.235359
                                           41.37
                                                              166.7464
       _cons
```

Now let's use contrast to test the main effects of race:

. contrast race						
Contrasts of marginal linear predictions						
Margins : asbalanced						
	df	F	P>F			
race	(not testable)					
Denominator	56					

By "not testable", contrast means that it cannot form a test for the main effects of race based on estimable functions of the model coefficients. agegrp has five levels, so contrast constructs an estimate of the *i*th margin for race as

$$\widehat{\mu}_{i\cdot} = \frac{1}{5} \sum_{j=1}^{5} \widehat{\mu}_{ij} = \widehat{\mu}_0 + \widehat{\alpha}_i + \frac{1}{5} \sum_{j=1}^{5} \left\{ \widehat{\beta}_j + (\widehat{\alpha}\widehat{\beta})_{ij} \right\}$$

but $(\widehat{\alpha\beta})_{22}$ was constrained to zero because of the empty cell, so $\widehat{\mu}_{2}$ is not an estimable function of the model coefficients.

See *Estimable functions* in *Methods and formulas* of [R] **margins** for a technical description of estimable functions. The emptycells(reweight) option causes contrast to estimate μ_2 . by

$$\widehat{\mu}_{2.} = \frac{\widehat{\mu}_{21} + \widehat{\mu}_{23} + \widehat{\mu}_{24} + \widehat{\mu}_{25}}{4}$$

which is an estimable function of the model coefficients.

. contrast race, emptycells(reweight)								
Contrasts of marginal linear predictions								
Margins : asbalanced Empty cells : reweight								
	P>F							
race 2 3.17 0.049								
Denominator	56							

We can reconstruct the effect of the emptycells(reweight) option by using custom contrasts.

	ace#agegrp -4 - ace#agegrp -1 -			1 1}, noeffects
Contrasts of m	narginal linear	prediction	ıs	
Margins	: asbalanced			
	I			
	df	F	P>F	
race#agegrp				
(1) (1)	1	1.06	0.3080	
(2) (2)	1	2.37	0.1291	
Joint	2	3.17	0.0498	
Denominator	56			

The row labeled (1) (1) is the test for

$$\frac{1}{5}(\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15}) = \frac{1}{4}(\mu_{21} + \mu_{23} + \mu_{24} + \mu_{25})$$

It was the first specified contrast. The row labeled (2) (2) is the test for

$$\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15} = \mu_{31} + \mu_{32} + \mu_{33} + \mu_{34} + \mu_{35}$$

It was the second specified contrast. The row labeled Joint is the overall test of the main effects of race.

Empty cells, ANOVA style

. anova chol race##agegrp

Let's refit the linear model from the previous example with anova to compare with contrast's test for the main effects of race.

	Number of obs Root MSE			quared R-squared	= 0.7582 = 0.7021
Source	Partial SS	df	MS	F	Prob > F
Model	15751.6113	13	1211.66241	13.51	0.0000
race agegrp race#agegrp	305.49046 14387.8559 795.807574	2 4 7	152.74523 3596.96397 113.686796	1.70 40.10 1.27	0.1914 0.0000 0.2831
Residual	5022.71559	56	89.6913498		
Total	20774.3269	69	301.077201		

contrast and anova handled the empty cell differently; the F statistic reported by contrast was 3.17, but anova reported 1.70. To see how they differ, consider the following table of the cell means and margins for our situation.

		1	2	agegrp 3	4	5	
race	$\frac{1}{2}$	$\mu_{11} \ \mu_{21}$	μ_{12}	μ_{13}	μ_{14}	μ_{15}	μ_{1} .
Tace	3	μ_{21} μ_{31}	μ_{32}	$\mu_{23} \ \mu_{33}$	$\mu_{24} \ \mu_{34}$	$\mu_{25} \ \mu_{35}$	μ_{3} .
		$\mu_{\cdot 1}$		$\mu_{\cdot 3}$	$\mu_{\cdot 4}$	$\mu_{.5}$	

For testing the main effects of race, we know that we will be testing the equality of the marginal means for rows 1 and 3, that is, $\mu_{1.} = \mu_{3.}$. This translates into the following constraint:

$$\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15} = \mu_{31} + \mu_{32} + \mu_{33} + \mu_{34} + \mu_{35}$$

Because row 2 contains an empty cell in column 2, anova dropped column 2 and tested the equality of the marginal mean for row 2 with the average of the marginal means from rows 1 and 3, using only the remaining cell means. This translates into the following constraint:

$$2(\mu_{21} + \mu_{23} + \mu_{24} + \mu_{25}) = \mu_{11} + \mu_{13} + \mu_{14} + \mu_{15} + \mu_{31} + \mu_{33} + \mu_{34} + \mu_{35}$$
(1)

Now that we know the constraints that anova used to test for the main effects of race, we can use custom contrasts to reproduce the anova test result.

	ace#agegrp -1 -1 ace#agegrp 1 0				noeffects
Contrasts of m	marginal linear p	predictions	3		
Margins	: asbalanced				
	df	F	P>F		
race#agegrp					
(1) (1)	1	2.37	0.1291		
(2) (2)	1	1.03	0.3138		
Joint	2	1.70	0.1914		
Denominator	56				

The row labeled (1) (1) is the test for $\mu_{1.} = \mu_{3.}$; it was the first specified contrast. The row labeled (2) (2) is the test for the constraint in (1); it was the second specified contrast. The row labeled Joint is an overall test for the main effects of race.

Nested effects

contrast has the | operator for computing simple effects when the levels of one factor are nested within the levels of another. Here is a fictional example where we are interested in the effect of five methods of teaching algebra on students' scores for the math portion of the SAT. Suppose three algebra classes are randomly sampled from classes using each of the five methods so that class is nested in method as demonstrated in the following tabulation.

. use http://www.stata-press.com/data/r13/sat
(Artificial SAT data)

. tabulate class method

	method							
class	1	2	3	4	5	Total		
1	5	0	0	0	0	5		
2	5	0	0	0	0	5		
3	5	0	0	0	0	5		
4	0	5	0	0	0	5		
5	0	5	0	0	0	5		
6	0	5	0	0	0	5		
7	0	0	5	0	0	5		
8	0	0	5	0	0	5		
9	0	0	5	0	0	5		
10	0	0	0	5	0	5		
11	0	0	0	5	0	5		
12	0	0	0	5	0	5		
13	0	0	0	0	5	5		
14	0	0	0	0	5	5		
15	0	0	0	0	5	5		
Total	15	15	15	15	15	75		

We will consider method as fixed and class nested in method as random. To use class nested in method as the error term for method, we can specify the following anova model:

. anova score method / class|method /

	Number of obs Root MSE			quared R-squared	= 0.7599 = 0.7039
Source	Partial SS	df	MS	F	Prob > F
Model	980312	14	70022.2857	13.56	0.0000
method class method	905872 74440	4 10	226468 7444	30.42	0.0000
class method	74440	10	7444	1.44	0.1845
Residual	309760	60	5162.66667		
Total	1290072	74	17433.4054		

Like anova, contrast allows the | operator, which specifies that one variable is nested in the levels of another. We can use contrast to test the main effects of method and the simple effects of class within method.

Contrasts of marginal linear predictions Margins : asbalanced					
	df	F	P>F		
method	(not testable)				
class method					
1	2	2.80	0.0687		
2	2	0.91	0.4089		
3	2	1.10	0.3390		
4	2	0.22	0.8025		
5	2	2.18	0.1221		
Joint	10	1.44	0.1845		
Denominator	60				

. contrast method class method

Although contrast was able to perform the individual tests for the simple effects of class within method, empty cells in the interaction between method and class prevented contrast from testing for a main effect of method. Here we add the emptycells(reweight) option so that contrast can take the empty cells into account when computing the marginal means for method.

. contrast method class | method, emptycells (reweight) Contrasts of marginal linear predictions : asbalanced Margins Empty cells : reweight F df P>F method 4 43.87 0.0000 class | method 2 2.80 0.0687 1 2 2 0.91 0.4089 3 0.3390 2 1.10 4 2 0.22 0.8025 5 2 2.18 0.1221 Joint 10 1.44 0.1845 Denominator 60

Now contrast does report a test for the main effects of method. However, if we compare this with the anova results, we will see that the results are different. They are different because contrast uses the residual error term to compute the F test by default. Using notation similar to anova, we can use the / operator to specify a different error term for the test. Therefore, we can reproduce the test of main effects from our anova command by typing

. contrast method / class|method /, emptycells(reweight) Contrasts of marginal linear predictions Margins : asbalanced Empty cells : reweight F df P>F method 4 30.42 0.0000 class | method 10 (denominator) class | method 2.80 2 0.0687 1 2 2 0.91 0.4089 З 2 1.10 0.3390 4 2 0.22 0.8025 2 5 2.18 0.1221 Joint 10 1.44 0.1845 Denominator 60

Multiple comparisons

We have seen that contrast can report the individual linear combinations that make up the requested effects. Depending upon the specified option, contrast will report confidence intervals, *p*-values, or both in the effects table. By default, the reported confidence intervals and *p*-values are not adjusted for multiple comparisons. Use the mcompare() option to adjust the confidence intervals and *p*-values for multiple comparisons of the individual effects.

Let's compute the grand mean effects of race using the g. operator. We also specify the mcompare(bonferroni) option to compute *p*-values and confidence intervals using Bonferroni's adjustment.

```
. use http://www.stata-press.com/data/r13/cholesterol
(Artificial cholesterol data)
. anova chol race##agegrp
  (output omitted)
. contrast g.race, mcompare(bonferroni)
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F	Bonferroni P>F
race				
(black vs mean)	1	7.07	0.0100	0.0301
(white vs mean)	1	2.82	0.0982	0.2947
(other vs mean)	1	0.96	0.3312	0.9936
Joint	2	3.62	0.0329	
Denominator	60			

Note: Bonferroni-adjusted p-values are reported for tests on individual contrasts only.

	Number of Comparisons			
race	3			
	Contrast	Std. Err.	Bonfe [95% Conf.	
race (black vs mean) (white vs mean) (other vs mean)	4.17666 -2.638058 -1.538602	1.570588 1.570588 1.570588	.3083743 -6.506343 -5.406887	8.044945 1.230227 2.329684

The last table reports a Bonferroni-adjusted confidence interval for each individual contrast. (Use the effects option to add p-values to the last table.) The first table includes a Bonferroni-adjusted p-value for each test that is not a joint test.

Joint tests are never adjusted for multiple comparisons. For example,

. contrast race@agegrp, mcompare(bonferroni)						
Contrasts of marginal linear predictions						
Margins : asbalanced						
	df	F	P>F			
race@agegrp						
10-19	2	1.37	0.2620			
20-29	2	2.44	0.0958			
30-39	2	3.12	0.0512			
40-59	2	0.53	0.5889			
60-79	2	2.90	0.0628			
Joint	10	2.07	0.0409			
Denominator	60					

Note: Bonferroni-adjusted p-values are reported for tests on individual contrasts only.

	Number of Comparisons
race@agegrp	10

	Bonferroni Contrast Std. Err. [95% Conf. Interval]			
	Contrast	Sta. Err.	[95% Conf. Interval]	
race@agegrp				
(white vs base) 10-19	6.841855	6.082862	-10.88697 24.57068	
(white vs base) 20-29	-11.80631	6.082862	-29.53513 5.922513	
(white vs base) 30-39	-14.40607	6.082862	-32.13489 3.322751	
(white vs base) 40-59	-4.101691	6.082862	-21.83051 13.62713	
(white vs base) 60-79	-10.60137	6.082862	-28.33019 7.127448	
(other vs base) 10-19	-2.975244	6.082862	-20.70407 14.75358	
(other vs base) 20-29	-11.45679	6.082862	-29.18561 6.272031	
(other vs base) 30-39	-11.41958	6.082862	-29.1484 6.309244	
(other vs base) 40-59	-6.17807	6.082862	-23.90689 11.55075	
(other vs base) 60-79	3.453375	6.082862	-14.27545 21.1822	

Here we have five tests of simple effects with two degrees of freedom each. No Bonferroni-adjusted *p*-values are available for these tests, but the confidence intervals for the individual contrasts are adjusted.

Unbalanced data

By default, contrast treats all factors as balanced when computing marginal means. By balanced, we mean that contrast assumes an equal number of observations in each level of each factor and an equal number of observations in each cell of each interaction. If our data are balanced, there is no issue. If, however, our data are not balanced, we might prefer that contrast use the actual cell frequencies from our data in computing marginal means. We instruct contrast to use observed frequencies by adding the asobserved option.

Even if our data are unbalanced, we might still want contrast to compute balanced marginal means. It depends on what we want to test and what our data represent. If we have data from a designed experiment that started with an equal number of males and females but the data became unbalanced because the data from a few males were unusable, we might still want our margins computed as though the data were balanced. If, however, we have a representative sample of individuals from Los Angeles with 40% of European descent, 34% African-American, 25% Hispanic, and 1% Australian, we probably want our margins computed using these representative frequencies. We do not want Australians receiving the same weight as Europeans.

The following examples will use an unbalanced version of our dataset.

-	//www.stata-p cholesterol o			lesterol3		
. tab race a	agegrp					
			agegrp			
race	10-19	20-29	30-39	40-59	60-79	Total
black	1	5	5	4	3	18
white	4	5	7	4	4	24
other	3	7	6	5	4	25
Total	8	17	18	13	11	67

The row labeled Total gives observed cell frequencies for age group. These can be obtained by summing frequencies from the cells in the corresponding column. In this respect, we can also refer to them as marginal frequencies. We use the terms marginal frequencies and cell frequencies interchangeably below. We begin by fitting the two-factor model with an interaction.

. anova chol race##agegrp

		Number of obs Root MSE			-squared 1j R-squared	=	0.8179 0.7689
_	Source	Partial SS	df	MS	F	Р	rob > F
	Model	16379.9926	14	1169.99947	16.68		0.0000
	race	230.754396	2	115.377198	1.64		0.2029
	agegrp	13857.9877	4	3464.49693	49.39		0.0000
r	ace#agegrp	857.815209	8	107.226901	1.53		0.1701
_	Residual	3647.2774	52	70.13995			
	Total	20027.27	66	303.443485			

Using observed cell frequencies

Recall that the marginal means are computed from the cell means. Treating the factors as balanced yields the following marginal means for race:

$$\eta_{1.} = \frac{1}{5}(\mu_{11} + \mu_{12} + \mu_{13} + \mu_{14} + \mu_{15})$$
$$\eta_{2.} = \frac{1}{5}(\mu_{21} + \mu_{22} + \mu_{23} + \mu_{24} + \mu_{25})$$
$$\eta_{3.} = \frac{1}{5}(\mu_{31} + \mu_{32} + \mu_{33} + \mu_{34} + \mu_{35})$$

If we have a fixed population and unbalanced cells, then the η_i do not represent population means. If, however, our data are representative of the population, we can use the frequencies from our estimation sample to estimate the population marginal means, denoted μ_i .

Here are the results of testing for a main effect of race, treating all the factors as balanced.

```
. contrast r.race
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F	
race				
(white vs black)	1	3.28	0.0757	
(other vs black)	1	1.50	0.2263	
Joint	2	1.64	0.2029	
Denominator	52			
	Contrast	Std. Err.	[95% Conf.	Interval]
race				
(white vs black)	-5.324254	2.93778	-11.21934	.5708338
(other vs black)	-3.596867	2.93778	-9.491955	2.298221

The row labeled (white vs black) is the test for $\eta_{2.} = \eta_{1.}$. The row labeled (other vs black) is the test for $\eta_{3.} = \eta_{1.}$.

If the observed marginal frequencies are representative of the distribution of the levels of agegrp, we can use them to form the marginal means of chol for each of the levels of race from the cell means.

$$\mu_{1.} = \frac{1}{67} (8\mu_{11} + 17\mu_{12} + 18\mu_{13} + 13\mu_{14} + 11\mu_{15})$$

$$\mu_{2.} = \frac{1}{67} (8\mu_{21} + 17\mu_{22} + 18\mu_{23} + 13\mu_{24} + 11\mu_{25})$$

$$\mu_{3.} = \frac{1}{67} (8\mu_{31} + 17\mu_{32} + 18\mu_{33} + 13\mu_{34} + 11\mu_{35})$$

Here are the results of testing for the main effects of race, using the observed marginal frequencies:

. contrast r.race, asobserved

```
Contrasts of marginal linear predictions
```

	df	F	P>F	
race				
(white vs black)	1	7.25	0.0095	
(other vs black)	1	3.89	0.0538	
Joint	2	3.74	0.0304	
Denominator	52			
	Contrast	Std. Err.	[95% Conf	. Interval]
race				
(white vs black)	-7.232433	2.686089	-12.62246	-1.842402
(other vs black)	-5.231198	2.651203	-10.55123	.0888295

The row labeled (white vs black) is the test for $\mu_{2.} = \mu_{1.}$. The row labeled (other vs black) is the test for $\mu_{3.} = \mu_{1.}$. Both tests were insignificant when we tested the cell means resulting from balanced frequencies; however, when we tested the cell means from observed frequencies, the first test is significant beyond the 5% level (and the second test is nearly so).

Here we reproduce the results of the asobserved option with custom contrasts. Because we are modifying the way that the marginal means are constructed from the cell means, we will specify the contrasts on the predicted cell means. We use macro expansion, =exp, to evaluate the fractions instead of approximating them with decimals. Macro expansion guarantees that the contrast coefficients sum to zero. For more information, see *Macro expansion operators and function* in [P] macro.

>	ace#agegrp -'' ((marginal linea	=8/67' '=17, =8/67' -'=17, 0 0 =8/67' '=17,	/67', -'=18/67', /67', '=18/67', /67', -'=18/67', 0 /67', '=18/67', 18	'=13/67' -'=13/67' 0	<pre>'=11/67'} -'=11/67' 0</pre>
	df	F	P>F		
race#agegrp					
(1) (1)	1	7.25	0.0095		
(2) (2)	1	3.89	0.0538		
Joint	2	3.74	0.0304		
Denominator	52				
	r				
	Contrast	Std. Err.	[95% Conf.	Interval]	
race#agegrp					
(1) (1)	-7.232433	2.686089	-12.62246	-1.842402	
(2) (2)	-5.231198	2.651203	-10.55123	.0888295	

Weighted contrast operators

contrast provides observation-weighted versions of five of the contrast operators—gw., hw., jw., pw., and qw.. The first three of these operators perform comparisons of means across cells, and like the marginal means just discussed, these means can be computed in two ways: 1) as though the cell frequencies were equal or 2) using the observed cell frequencies from the estimation sample. The weighted operators provide versions of the standard (as balanced) operators that weight these means by their cell frequencies. The two orthogonal polynomial operators involve similar adjustments for weighting.

Let's examine what this means by using the gw. operator. The gw. operator is a weighted version of the g. operator. The gw. operator computes the grand mean using the cell frequencies for race obtained from the model fit.

Here we test the effects of race, comparing each level with the weighted grand mean but otherwise treating the factors as balanced in the marginal mean calculations.

. contrast gw.race Contrasts of marg Margins : asl		ictions	
	df	F	P>F
race (black vs mean) (white vs mean) (other vs mean) Joint	1 1 1 2	2.78 2.06 0.06 1.64	0.1014 0.1573 0.8068 0.2029
Denominator	52		

	Contrast	Std. Err.	[95% Conf.	Interval]
race (black vs mean) (white vs mean) (other vs mean)	3.24931 -2.074944 347557	1.948468 1.44618 1.414182	6605779 -4.976915 -3.18532	7.159198 .8270276 2.490206

The observed marginal frequencies of race are 18, 24, and 25. Thus the row labeled (black vs mean) tests $\eta_1 = (18\eta_1 + 24\eta_2 + 25\eta_3)/67$; the row labeled (white vs mean) tests $\eta_2 = (18\eta_1 + 24\eta_2 + 25\eta_3)/67$; and the row labeled (other vs mean) tests $\eta_3 = (18\eta_1 + 24\eta_2 + 25\eta_3)/67$.

Now we reproduce the above results using custom contrasts. We are weighting the calculation of the grand mean from the marginal means for each of the races, but we are not weighting the calculation of the marginal means themselves. Therefore, we can specify the custom contrast on the marginal means for race instead of on the cell means.

	ace '=49/67' ace -'=18/67' ace -'=18/67'	ʻ=43/67'-ʻ	=25/67;}	
Contrasts of m	narginal linea	ar prediction	S	
Margins	asbalanced	-		
	df	F	P>F	
race				
(1) (2)	1		0.1014 0.1573	
(3)	1		0.8068	
Joint	2	1.64	0.2029	
Denominator	52			
	Contrast	Std. Err.	[95% Conf.	Interval]
race				
(1)	3.24931	1.948468	6605779	7.159198
(2)			-4.976915	
(3)	347557	1.414182	-3.18532	2.490206

Now we will test for each race the difference between the marginal mean and the weighted grand mean, treating the factors as observed in the marginal mean calculations.

. contrast	; gi	J.race,	a	sobserve	ed wald ci	i
Contrasts	of	margina	1	linear	predictio	ons
Margins		: asobs	sei	rved		

	df	F	P>F	
race (black vs mean)	1	6.81	0.0118	
(white vs mean)		3.74	0.0587	
(other vs mean)	1	0.26	0.6099	
Joint	2	3.74	0.0304	
Denominator	52			
	Contrast	Std. Err.	[95% Conf.	Interval]
race	4 5 40 8 20	4 740004	4 050400	0.004004
(black vs mean) (white vs mean)	4.542662 -2.689771	1.740331 1.39142	1.050432 -5.481859	8.034891
(other vs mean)	6885363	1.341261	-3.379973	2.002901

The row labeled (black vs mean) tests $\mu_{1.} = (18\mu_{1.} + 24\mu_{2.} + 25\mu_{3.})/67$; the row labeled (white vs mean) tests $\mu_{2.} = (18\mu_{1.} + 24\mu_{2.} + 25\mu_{3.})/67$; and the row labeled (other vs mean) tests $\mu_{3.} = (18\mu_{1.} + 24\mu_{2.} + 25\mu_{3.})/67$.

Here we use a custom contrast to reproduce the above result testing $\mu_{1.} = (18\mu_{1.} + 24\mu_{2.} + 25\mu_{3.})/67$. Because both the calculation of the marginal means and the calculation of the grand mean are adjusted, we specify the custom contrast on the cell means.

. contrast {ra	ace#agegrp '	=49/67*8/67,	'=49/67*17/6	7' '=49/67	′*18/67'
>	(=49/67*13/67'	'=49/67*11/	67'	
>	_ '	=24/67*8/67'	-'=24/67*17/6	7' -'=24/67	′*18/67'
>	_ '	=24/67*13/67;	-'=24/67*11/	67'	
>	_ '	=25/67*8/67,	-'=25/67*17/6	7' -'=25/67	′*18/67'
>	_ '	=25/67*13/67;	-'=25/67*11/	67'}, nowal	.d
Contrasts of m	marginal line	ar prediction	S		
Margins	: asbalanced				
	I				
	Contrast	Std. Err.	[95% Conf.	Interval]	
race#agegrp					
(1) (1)	4.542662	1.740331	1.050432	8.034891	

The Helmert and reverse Helmert contrasts also involve calculating averages of the marginal means; therefore, weighted versions of these parameters are available as well. The hw. operator is a weighted version of the h. operator that computes the mean of the subsequent levels using the cell frequencies obtained from the model fit. The jw. operator is a weighted version of the j. operator that computes the mean of the previous levels using the cell frequencies obtained from the model fit.

For orthogonal polynomials, we can use the pw. and qw. operators, which are the weighted versions of the p. and q. operators. In this case, the cell frequencies from the model fit are used in the calculation of the orthogonal polynomial contrast coefficients.

Testing factor effects on slopes

For linear models where the independent variables are all factor variables, the linear prediction at fixed levels of the factor variables turns out to be a cell mean. With these models, contrast computes and tests the effects of the factor variables on the expected mean of the dependent variable. When factor variables are interacted with continuous variables, contrast distinguishes factor effects on the intercept from factor effects on the slope.

Here we have 1980 census data including information on the birth rate (brate), the median age (medage), and the region of the country (region) for each of the 50 states. We can fit an ANCOVA model for brate using main effects of the factor variable region and the continuous variable medage.

		Number of obs Root MSE			quared R-squared	= 0.8264 = 0.8110
_	Source	Partial SS	df	MS	F	Prob > F
	Model	34872.8589	4	8718.21473	53.57	0.0000
	region	2197.75453	3	732.584844	4.50	0.0076
	medage	15327.423	1	15327.423	94.18	0.0000
_	Residual	7323.96108	45	162.754691		
	Total	42196.82	49	861.159592		

For those more comfortable with linear regression, this is equivalent to the regression model

. regress brate i.region c.medage

You may use either.

We can use contrast to compute reference category effects for region. These contrasts compare the adjusted means of NCentral, South, and West regions with the adjusted mean of the NE region.

. contrast r.region Contrasts of marginal linear predictions Margins : asbalanced

	df	F	P>F
region (NCentral vs NE) (South vs NE) (West vs NE) Joint	1 1 1 3	2.24 0.78 10.33 4.50	0.1417 0.3805 0.0024 0.0076
Denominator	45		

	Contrast	Std. Err.	[95% Conf.	Interval]
region (NCentral vs NE) (South vs NE) (West vs NE)	9.061063 5.06991 21.71328	6.057484 5.72396 6.755616	-3.139337 -6.458738 8.106774	21.26146 16.59856 35.31979

Let's add the interaction between region and medage to the model.

. anova brate region##c.medage

	Number of obs Root MSE			quared R-squared	= 0.9000 = 0.8833
Source	Partial SS	df	MS	F	Prob > F
Model	37976.3149	7	5425.18784	53.99	0.0000
region	3405.07044	3	1135.02348	11.30	0.0000
medage	5279.71448	1	5279.71448	52.54	0.0000
region#medage	3103.45597	3	1034.48532	10.29	0.0000
Residual	4220.5051	42	100.488217		
Total	42196.82	49	861.159592		

The parameterization for the expected value of brate as a function of region and medage is given by

$$E(\texttt{brate}|\texttt{region}=i,\texttt{medage})=lpha_0+lpha_i+eta_0\texttt{medage}+eta_i\texttt{medage}$$

where α_0 is the intercept and β_0 is the slope of medage. We are modeling the effects of region in two different ways. The α_i parameters measure the effect of region on the intercept, and the β_i parameters measure the effect of region on the slope of medage.

contrast computes and tests effects on slopes separately from effects on intercepts. First, we will compute the reference category effects of region on the intercept:

. contrast r.region Contrasts of margin Margins : asba		edictions		
	df	F	P>F	
region				
(NCentral vs NE)	1	0.09	0.7691	
(South vs NE)	1	0.01		
(West vs NE)	1	8.50	0.0057	
Joint	3	11.30	0.0000	
Denominator	42			
	Contrast	Std. Err.	[95% Conf.	Interval]
region (NCentral vs NE) (South vs NE) (West vs NE)	-49.38396 -9.058983 343.0024	117.424	-386.6622 -246.0302 105.5656	287.8942 227.9123 580.4393

Now we will compute the reference category effects of region on the slope of medage:

. contrast r.region Contrasts of margin	•	edictions		
Margins : asba	alanced			
	df	F	P>F	
region#c.medage				
(NCentral vs NE)	1	0.16	0.6917	
(South vs NE)	1	0.03	0.8558	
(West vs NE)	1	8.18	0.0066	
Joint	3	10.29	0.0000	
Denominator	42			
	Contrast	Std. Err.	[95% Conf.	Interval]
region#c.medage				
(NCentral vs NE)	2.208539	5.530981	-8.953432	13.37051
(South vs NE)	.6928008	3.788735	-6.953175	8.338777
(West vs NE)	-10.94649	3.827357	-18.67041	-3.22257

At the 5% level, the slope of medage for the West region differs from that of the NE region, but at that level of significance, we cannot say that the slope for the NCentral or the South region differs from that of the NE region.

This model is simple enough that the reference category contrasts reproduce the coefficients for region and for the interactions in an equivalent model fit by regress.

. regress brat	ce region##c.m	edage				
Source	SS	df	MS		Number of obs F(7, 42)	
Model Residual	37976.3149 4220.5051		5.18784 .488217		Prob > F R-squared	= 0.0000 = 0.9000
Total	42196.82	49 861	.159592		Adj R-squared Root MSE	= 0.8833 = 10.024
brate	Coef.	Std. Err.	t	P> t	[95% Conf.	Interval]
region						
NCentral	-49.38396	167.1281	-0.30	0.769	-386.6622	287.8942
South	-9.058983	117.424	-0.08	0.939	-246.0302	227.9123
West	343.0024	117.6547	2.92	0.006	105.5656	580.4393
medage	-8.802707	3.462865	-2.54	0.015	-15.79105	-1.814362
region# c.medage						
NCentral	2.208539	5.530981	0.40	0.692	-8.953432	13.37051
South	.6928008	3.788735	0.18	0.856	-6.953175	8.338777
West	-10.94649	3.827357	-2.86	0.007	-18.67041	-3.22257
_cons	411.8268	108.2084	3.81	0.000	193.4533	630.2002

This will not be the case for models that are more complicated.

Chow tests

Now let's suppose we are fitting a model for birth rates on median age and marriage rate. We are also interested in whether the regression coefficients differ for states in the east versus states in the west. We use census divisions to create a new variable, west, that indicates which states are in the western half of the United States.

. generate west = inlist(division, 4, 7, 8, 9)

We fit a model that includes a separate intercept for west as well as an interaction between west and each of the other variables in our model.

. regress brate i.west##c.medage i.west##c.mrgrate df Source SS MS Number of obs = 50 F(5, 44) = 92.09 Model 38516.2172 5 7703.24344 Prob > F 0.0000 = Residual 3680.60281 44 83.6500639 R-squared 0.9128 Adj R-squared = 0.9029 42196.82 Root MSE Total 49 861.159592 9.146 brate Coef. Std. Err. t P>|t| [95% Conf. Interval] 1.west 327.8733 58.71793 5.58 0.000 209.5351 446.2115 medage -7.532304 1.387624 -5.43 0.000 -10.32888 -4.735731west# c.medage -10.114431.849103 -5.470.000 -13.84105-6.387808 1 1.29 0.204 mrgrate 828.6813 643.3443 -467.8939 2125.257 west# c.mrgrate 1 -800.8036 645.488 -1.240.221 -2101.699500.092 366.5325 47.08904 7.78 0.000 271.6308 461.4343 _cons

We can test the effects of west on the intercept and on the slopes of medage and mrgrate. We will specify all of these effects in a single contrast command and include the overall option to obtain a joint test of effects, that is, a test that the coefficients for eastern states and for western states are equal.

<pre>. contrast west west#c.medage west#c.mrgrate, overal Contrasts of marginal linear predictions Margins : asbalanced</pre>					
	df	F	P>F		
west	1	31.18	0.0000		
west#c.medage	1	29.92	0.0000		
west#c.mrgrate	1	1.54	0.2213		
Overall	3	22.82	0.0000		
Denominator	44				

This overall test is referred to as a Chow test in econometrics (Chow 1960).

Beyond linear models

contrast may be used after almost any estimation command, with the added benefit that contrast provides direct support for testing main and interaction effects that is not available in most estimation commands. To illustrate, we will use contrast with results from a logistic regression. Stata's logit command fits logistic regression models, reporting the fitted regression coefficients. The logistic command fits the same models but reports odds ratios. Although contrast can report odds ratios for the computed effects, the tests are all computed from linear combinations of the model coefficients regardless of which estimation command we used.

Suppose we have data on patient satisfaction for three hospitals in a city. Let's begin by fitting a model for satisfied, whether the patient was satisfied with his or her treatment, using the main effects of hospital:

```
. use http://www.stata-press.com/data/r13/hospital, clear
(Artificial hospital satisfaction data)
. logit satisfied i.hospital
Iteration 0:
              \log likelihood = -393.72216
Iteration 1: log likelihood = -387.55736
Iteration 2: log likelihood = -387.4768
Iteration 3: log likelihood = -387.47679
Logistic regression
                                                  Number of obs
                                                                           802
                                                                  =
                                                  LR chi2(2)
                                                                  =
                                                                         12.49
                                                  Prob > chi2
                                                                  =
                                                                        0.0019
Log likelihood = -387.47679
                                                  Pseudo R2
                                                                  =
                                                                        0.0159
   satisfied
                            Std. Err.
                                                          [95% Conf. Interval]
                    Coef.
                                           7.
                                                P>|z|
   hospital
                 .5348129
                            .2136021
                                         2.50
                                                0.012
                                                          .1161604
                                                                      .9534654
          2
          3
                 .7354519
                            .2221929
                                         3.31
                                                0.001
                                                          .2999618
                                                                      1.170942
       _cons
                 1.034708
                            .1391469
                                         7.44
                                                0.000
                                                          .7619855
                                                                      1.307431
```

Because there are no other independent variables in this model, the reference category effects of hospital computed by contrast will match the fitted model coefficients, assuming a common reference level.

```
. contrast r.hospital
```

```
Contrasts of marginal linear predictions
```

```
Margins : asbalanced
```

	df	chi2	P>chi2	
hospital				
(2 vs 1)	1	6.27	0.0123	
(3 vs 1)	1	10.96	0.0009	
Joint	2	12.55	0.0019	
	Contrast	Std. Err.	[95% Conf.	 Interval]
hospital (2 vs 1)	.5348129	.2136021	.1161604	.9534654
(3 vs 1)	.7354519	.2221929	.2999618	1.17094

We see that the reference category effects are equal to the fitted coefficients. They also have the same interpretation, the difference in log odds from the reference category. The top table also provides a joint test of these effects, a test of the main effects of hospital.

We also have information on the condition for which each patient is being treated in the variable illness. Here we fit a logistic regression using a two-way crossed model of hospital and illness.

```
. label list illness
illness:
            1 heart attack
           2 stroke
           3 pneumonia
            4 lung disease
            5 kidney failure
. logistic satisfied hospital##illness
Logistic regression
                                                     Number of obs
                                                                      =
                                                                                802
                                                     LR chi2(14)
                                                                      =
                                                                             38.51
                                                     Prob > chi2
                                                                      =
                                                                             0.0004
Log likelihood = -374.46865
                                                     Pseudo R2
                                                                      =
                                                                             0.0489
   satisfied
                Odds Ratio
                              Std. Err.
                                                   P>|z|
                                                              [95% Conf. Interval]
                                              z
    hospital
          2
                  1.226496
                              .5492177
                                           0.46
                                                   0.648
                                                               .509921
                                                                          2.950049
          3
                                                   0.254
                                                                          4.308021
                  1.711111
                              .8061016
                                           1.14
                                                              .6796395
     illness
     stroke
                  1.328704
                              .6044214
                                           0.62
                                                   0.532
                                                               .544779
                                                                          3.240678
                  .7993827
                              .3408305
                                          -0.53
                                                   0.599
                                                                          1.843653
  pneumonia
                                                              .3466015
lung dise..
                  1.231481
                              .5627958
                                           0.46
                                                   0.649
                                                              .5028318
                                                                          3.016012
                                           0.51
kidney fa..
                      1.25
                              .5489438
                                                   0.611
                                                              .5285676
                                                                          2.956102
    hospital#
     illness
   2#stroke
                  2.434061
                              1.768427
                                           1.22
                                                   0.221
                                                              .5860099
                                                                          10.11016
2#pneumonia
                  4.045805
                              2.868559
                                           1.97
                                                   0.049
                                                              1.008058
                                                                          16.23769
          2 #
lung dise ...
                    .54713
                              .3469342
                                          -0.95
                                                   0.342
                                                              .1578866
                                                                            1.89599
          2 #
kidney fa..
                  1.594425
                              1.081104
                                           0.69
                                                   0.491
                                                              .4221288
                                                                          6.022312
                  .5416535
                              .3590089
                                          -0.93
                                                   0.355
                                                              .1477555
                                                                          1.985635
   3#stroke
                  1.579502
                                                                          5.758783
3#pneumonia
                              1.042504
                                           0.69
                                                   0.489
                                                              .4332209
          3 #
lung dise..
                  3.137388
                             2.595748
                                           1.38
                                                   0.167
                                                              .6198955
                                                                          15.87881
          3 #
kidney fa..
                  1.672727
                              1.226149
                                           0.70
                                                   0.483
                                                              .3976256
                                                                          7.036812
                  2.571429
                              .8099239
                                           3.00
                                                   0.003
                                                              1.386983
                                                                          4.767358
       _cons
```

Using contrast, we can obtain an ANOVA-style table of tests for the main effects and interaction effects of hospital and illness.

. contrast hospital##illness Contrasts of marginal linear predictions Margins : asbalanced					
df chi2 P>chi					
hospital	2	14.92	0.0006		
illness	4	4.09	0.3937		
hospital#illness 8 20.45 0.0088					

Our interaction effect is significant, so we decide to evaluate the simple reference category effects of hospital within illness. We are particularly interested in patient satisfaction when being treated for a heart attack or stroke, so we will use the i. operator to limit our output to simple effects within the first two illnesses.

```
. contrast r.hospital@i(1 2).illness, nowald
Contrasts of marginal linear predictions
Margins : asbalanced
```

	Contrast	Std. Err.	[95% Conf.	Interval]
hospital@illness (2 vs 1) heart attack (2 vs 1) stroke (3 vs 1) heart attack (3 vs 1) stroke	.2041611 1.093722 .5371429 0759859	.4477942 .5721288 .4710983 .4662325	6734995 0276296 3861928 9897847	1.081822 2.215074 1.460479 .8378129

The row labeled (2 vs 1) heart attack estimates simple effects on the log odds when comparing hospital 2 with hospital 1 for patients having heart attacks. These effects are differences in the cell means of the linear predictions.

We can add the or option to report an odds ratio for each of these simple effects:

. contrast r.hospital@i(1 2).illness, nowald or Contrasts of marginal linear predictions Margins : asbalanced

	Odds Ratio	Std. Err.	[95% Conf. Interval]
hospital@illness (2 vs 1) heart attack (2 vs 1) stroke (3 vs 1) heart attack (3 vs 1) stroke	1.226496 2.985366 1.711111 .9268293	.5492177 1.708014 .8061016 .4321179	.509921 2.950049 .9727486 9.162089 .6796395 4.308021 .3716567 2.311306

These odds ratios are just the exponentiated version of the contrasts in the previous table.

For contrasts of the margins of nonlinear predictions, such as predicted probabilities, see [R] margins, contrast.

Multiple equations

contrast works with models containing multiple equations. Commands such as intreg and gnbreg allow their ancillary parameters to be modeled as functions of independent variables, and contrast can compute and test effects within these equations. In addition, contrast allows a special pseudofactor for equation—called _eqns—when working with results from manova, mvreg, mlogit, and mprobit.

In example 4 of [MV] **manova**, we fit a two-way MANOVA model using data from Woodard (1931). Here we will fit this model using mvreg. The data represent patients with jaw fractures. y1 is the patient's age, y2 is blood lymphocytes, and y3 is blood polymorphonuclears. Two factor variables, gender and fracture, are used as independent variables.

(Ta	ble 4.6 Two	www.stata-pre o-Way Unbalan	ced Data for	Fracture			Rench	er (1998))
. m	vreg y1 y2	y3 = gender#	#fracture, vs	squish no	ofvlabe	1		
Equ	ation	Obs Par	ms RMS	SE "R	-sq"	F		Р
y1		27	6 10.2177	77 0 4	4086	2.902124	0.03	
y2		27	6 5.26876		4743	3.78967	0.01	
y3		27	6 4.99364	17 0.4	4518	3.460938	0.01	95
		Coef.	Std. Err.	t	P> t	[95%	Conf.	Interval]
y1								
-	2.gender	-17.5	11.03645	-1.59	0.128	-40.45	5156	5.451555
	fracture							
	2	-12.625	5.518225	-2.29	0.033	-24.10		-1.149222
	3	5.666667	5.899231	0.96	0.348	-6.601	456	17.93479
	gender#							
	fracture	o				=		
	22	21.375	12.68678	1.68	0.107	-5.008		47.75859
	23	8.833333	13.83492	0.64	0.530	-19.93		37.60463
	_cons	39.5	4.171386	9.47	0.000	30.82	2513	48.17487
y2								
0	2.gender	20.5	5.69092	3.60	0.002	8.665	5083	32.33492
	fracture							
	2	-3.125	2.84546	-1.10	0.285	-9.042	2458	2.792458
	3	.6666667	3.041925	0.22	0.829	-5.659	9362	6.992696
	gender#							
	fracture							
	22	-19.625	6.541907	-3.00	0.007	-33.22		-6.02036
	23	-23.66667	7.133946	-3.32	0.003	-38.50		-8.830813
	_cons	35.5	2.150966	16.50	0.000	31.02	2682	39.97318
yЗ								
50	2.gender	-18.16667	5.393755	-3.37	0.003	-29.38	3359	-6.949739
	fracture							
	2	1.083333	2.696877	0.40	0.692	-4.52	2513	6.691797
	3	-3	2.883083	-1.04	0.310	-8.9		2.9957
	gender#							
	fracture							
	2 2	19.91667	6.200305	3.21	0.004	7.022	2426	32.81091
	23	23.5	6.76143	3.48	0.002	9.438	3837	37.56116
	_cons	61.16667	2.038648	30.00	0.000	56.92	2707	65.40627
	<u> </u>							

contrast computes Wald tests using the coefficients from the first equation by default.

. contrast gender##fracture						
Contrasts of marginal linear predictions						
Margi	Margins : asbalanced					
		r				
		df	F	P>F		
y1						
-	gender	1	2.16	0.1569		
	fracture	2	2.74	0.0880		
gende	r#fracture	2	1.69	0.2085		
Denominator 21						

Here we use the equation() option to compute the Wald tests in the y2 equation:

```
. contrast gender##fracture, equation(y2)
Contrasts of marginal linear predictions
Margins : asbalanced
```

	df	F	P>F
y2			
gender	1	5.41	0.0301
fracture	2	7.97	0.0027
gender#fracture	2	5.97	0.0088
Denominator	21		

Here we use the equation index to compute the Wald tests in the third equation:

```
. contrast gender##fracture, equation(#3)
Contrasts of marginal linear predictions
Margins
              : asbalanced
                           df
                                         F
                                                  P>F
yЗ
                                      2.23
                                               0.1502
         gender
                            1
       fracture
                            2
                                      6.36
                                               0.0069
                                      6.66
                                               0.0058
gender#fracture
                            2
    Denominator
                           21
```

Here we use the atequations option to compute Wald tests for each equation in the model. We also use the vsquish option to suppress the extra blank lines between terms.

. contrast gender##fracture, atequations vsquish Contrasts of marginal linear predictions Margins : asbalanced

	df	F	P>F
y1			
gender	1	2.16	0.1569
fracture	2	2.74	0.0880
gender#fracture	2	1.69	0.2085
y2			
gender	1	5.41	0.0301
fracture	2	7.97	0.0027
gender#fracture	2	5.97	0.0088
y3			
gender	1	2.23	0.1502
fracture	2	6.36	0.0069
gender#fracture	2	6.66	0.0058
Denominator	21		

Because we are investigating the results from mvreg, we can use the special _eqns factor to test for a marginal effect on the means among the dependent variables:

. contrast _eqns					
Contrasts of marginal linear predictions					
Margins : asbalanced					
	df	F	P>F		
_eqns	2	49.19	0.0000		
Denominator 21					

Here we test whether the main effects of gender differ among the dependent variables:

. contrast gender#_eqns				
Contrasts of marginal linear predictions				
Margins : asbalanced				
	16			
	df	F	P>F	
gender#_eqns	2	3.61	0.0448	
Denominator	21			

Although it is not terribly interesting in this case, we can even calculate contrasts across equations:

. contrast gender#reqns				
Contrasts of marginal linear predictions				
Margins : asba	alanced			
	df	F	P>F	
gender#_eqns (joint) (2 vs 1)	1	5.82	0.0251	
(joint) (3 vs 1)	1	0.40	0.5352	
Joint	2	3.61	0.0448	
Denominator 21				

Video example

Introduction to contrasts in Stata: One-way ANOVA

Stored results

contrast stores the following in r():

```
Scalars
    r(df_r)
                                variance degrees of freedom
                                number of terms in termlist
    r(k_terms)
                                confidence level of confidence intervals
    r(level)
Macros
    r(cmd)
                                contrast
    r(cmdline)
                                command as typed
    r(est_cmd)
                                e(cmd) from original estimation results
    r(est_cmdline)
                                e(cmdline) from original estimation results
    r(title)
                                title in output
    r(overall)
                                overall or empty
    r(emptycells)
                                empspec from emptycells()
                                method from mcompare()
    r(mcmethod)
    r(mctitle)
                                title for method from mcompare()
    r(mcadjustall)
                                adjustall or empty
    r(margin_method)
                                asbalanced or asobserved
Matrices
    r(b)
                                contrast estimates
    r(V)
                                variance-covariance matrix of the contrast estimates
    r(error)
                                contrast estimability codes;
                                  0 means estimable,
                                  8 means not estimable
                                matrix of contrasts applied to the model coefficients
    r(L)
    r(table)
                                matrix containing the contrasts with their standard errors,
                                test statistics, p-values, and confidence intervals
    r(F)
                                vector of F statistics; r(df_r) present
    r(chi2)
                                vector of \chi^2 statistics; r(df_r) not present
                                vector of p-values corresponding to r(F) or r(chi2)
    r(p)
                                vector of degrees of freedom corresponding to r(p)
    r(df)
    r(df2)
                                vector of denominator degrees of freedom corresponding to r(F)
```

contrast with the post option stores the following in e():

Scalars	
e(df_r)	variance degrees of freedom
e(k_terms)	number of terms in termlist
Macros	
e(cmd)	contrast
e(cmdline)	command as typed
e(est_cmd)	e(cmd) from original estimation results
e(est_cmdline)	e(cmdline) from original estimation results
e(title)	title in output
e(overall)	overall or empty
e(emptycells)	<pre>empspec from emptycells()</pre>
e(margin_method)	asbalanced or asobserved
e(properties)	b V
Matrices	
e(b)	contrast estimates
e(V)	variance-covariance matrix of the contrast estimates
e(error)	contrast estimability codes;
	0 means estimable,
	8 means not estimable
e(L)	matrix of contrasts applied to the model coefficients
e(F)	vector of unadjusted F statistics; $e(df_r)$ present
e(chi2)	vector of χ^2 statistics; e(df_r) not present
e(p)	vector of unadjusted <i>p</i> -values corresponding to e(F) or e(chi2)
e(df)	vector of degrees of freedom corresponding to e(p)
e(df2)	vector of denominator degrees of freedom corresponding to $e(F)$

Methods and formulas

Methods and formulas are presented under the following headings:

Marginal linear predictions Contrast operators Reference level contrasts Adjacent contrasts Grand mean contrasts Helmert contrasts Reverse Helmert contrasts Orthogonal polynomial contrasts Contrasts within interactions Multiple comparisons

Marginal linear predictions

contrast treats intercept effects separately from slope effects. To illustrate, consider the following parameterization for a quadratic regression of y on x that also models the effects of two factor variables A and B, where the levels of A are indexed by $i = 1, \ldots, k_a$ and the levels of B are indexed by $j = 1, \ldots, k_b$.

$$E(y|A = i, B = j, x) = \eta_{0ij} + \eta_{1ij}x + \eta_{2ij}x^2$$

$$\eta_{0ij} = \eta_0 + \alpha_{0i} + \beta_{0j} + (\alpha\beta)_{0ij}$$

$$\eta_{1ij} = \eta_1 + \alpha_{1i} + \beta_{1j} + (\alpha\beta)_{1ij}$$
$$\eta_{2ij} = \eta_2 + \alpha_{2i} + \beta_{2j} + (\alpha\beta)_{2ij}$$

We have partitioned the coefficients into three groups of parameters: η_{0ij} is a cell prediction for the intercept, η_{1ij} is a cell prediction for the slope on x, and η_{2ij} is a cell prediction for the slope on x^2 . For the intercept parameters, η_0 is the intercept, α_{0i} represents a main effect for factor A at its *i*th level, β_{0j} represents a main effect for factor B at its *j*th level, and $(\alpha\beta)_{0ij}$ represents an effect for the intercept of A and B at the *ij*th level. The individual coefficients in η_{1ij} and η_{2ij} have similar interpretations, but the effects are on the slopes of x and x^2 , respectively.

The marginal intercepts for A are given by

$$\eta_{0i.} = \sum_{j=1}^{k_b} f_{ij} \eta_{0ij}$$

where f_{ij} is a marginal relative frequency of the *j*th level of *B* and is controlled by the asobserved and emptycells(reweight) options according to

$$f_{ij} = \begin{cases} 1/k_b, & \text{default} \\ w_{.j}/w_{..}, & \text{asobserved} \\ 1/(k_b - e_{i.}), & \text{emptycells(reweight)} \\ w_{ij}/w_{i.}, & \text{emptycells(reweight) and asobserved} \end{cases}$$

Above, w_{ij} is the number of individuals with A at its *i*th level and B at its *j*th,

$$w_{i.} = \sum_{j=1}^{k_b} w_{ij}$$
$$w_{.j} = \sum_{i=1}^{k_a} w_{ij}$$
$$w_{..} = \sum_{i=1}^{k_a} \sum_{j=1}^{k_b} w_{ij}$$

and e_i is the number of empty cells where A is at its *i*th level. The marginal intercepts for B and marginal slopes on x and x^2 are similarly defined.

Estimates for the cell intercepts and slopes are computed using the corresponding linear combination of the coefficients from the fitted model. For example, the estimated cell intercepts are computed using

$$\widehat{\eta}_{0ij} = \widehat{\eta}_0 + \widehat{\alpha}_{0i} + \widehat{\beta}_{0j} + (\widehat{\alpha}\widehat{\beta})_{0ij}$$

and the estimated marginal intercepts for A are computed as

$$\widehat{\eta}_{0i.} = \sum_{j=1}^{k_b} f_{ij} \widehat{\eta}_{0ij}$$

Contrast operators

contrast performs Wald tests using linear combinations of marginal linear predictions. For example, the following linear combination can be used to test for a specific effect of factor A on the marginal intercepts.

$$\sum_{i=1}^{k_a} c_i \eta_{0i}.$$

If the c_i elements sum to zero, the linear combination is called a contrast. If the factor A is represented by a variable named A, then we specify this contrast using the following syntax:

$$\{A \ c_1 \ c_2 \ \dots \ c_{k_a}\}$$

Similarly, the following linear combination can be used to test for a specific interaction effect of factors A and B on the marginal slope of x.

$$\sum_{i=1}^{k_a} \sum_{j=1}^{k_b} c_{ij} \eta_{1ij}$$

If the factor B is represented by a variable named B, then we specify this contrast using the following syntax:

$$\{A\#B \ c_{11} \ c_{12} \ \dots \ c_{1k_b} \ c_{21} \ \dots \ c_{k_ak_b} \}$$

contrast has variable operators for several commonly used contrasts. Each contrast operator specifies a matrix of linear combinations that yield the requested set of contrasts to be applied to the marginal linear predictions associated with the attached factor variable.

Reference level contrasts

The **r**. operator compares each level with a reference level. Let **R** be the corresponding contrast matrix for factor A, and then **R** is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{R}_{ij} = \begin{cases} -1, & \text{if } j \text{ is the reference level} \\ 1, & \text{if } i = j \text{ and } j \text{ is less than the reference level} \\ 1, & \text{if } i + 1 = j \text{ and } j \text{ is greater than the reference level} \\ 0, & \text{otherwise} \end{cases}$$

$$k_a$$
 k_b

If $k_a = 5$ and the reference level is the third level of A (specified as rb(#3).A), then

$$\mathbf{R} = \begin{pmatrix} 1 & 0 & -1 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 & 0 \\ 0 & 0 & -1 & 0 & 1 \end{pmatrix}$$

Adjacent contrasts

The a. operator compares each level with the next level. Let A be the corresponding contrast matrix for factor A, and then A is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{A}_{ij} = \begin{cases} 1, & \text{if } i = j \\ -1, & \text{if } i + 1 = j \\ 0, & \text{otherwise} \end{cases}$$

If $k_a = 5$, then

$$\mathbf{A} = \begin{pmatrix} 1 & -1 & 0 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & 1 & -1 & 0 \\ 0 & 0 & 0 & 1 & -1 \end{pmatrix}$$

The ar. operator compares each level with the previous level. If A is the contrast matrix for the a. operator, then -A is the corresponding contrast matrix for the ar. operator.

Grand mean contrasts

The g. operator compares each level with the mean of all the levels. Let G be the corresponding contrast matrix for factor A, and then G is a $k_a \times k_a$ matrix with elements

$$\mathbf{G}_{ij} = \begin{cases} 1 - 1/k_a, & \text{if } i = j \\ -1/k_a, & \text{if } i \neq j \end{cases}$$

If $k_a = 5$, then

$$\mathbf{G} = \begin{pmatrix} 4/5 & -1/5 & -1/5 & -1/5 & -1/5 \\ -1/5 & 4/5 & -1/5 & -1/5 & -1/5 \\ -1/5 & -1/5 & 4/5 & -1/5 & -1/5 \\ -1/5 & -1/5 & -1/5 & 4/5 & -1/5 \\ -1/5 & -1/5 & -1/5 & -1/5 & 4/5 \end{pmatrix}$$

The gw. operator compares each level with the weighted mean of all the levels. The weights are taken from the observed weighted cell frequencies in the estimation sample of the fitted model. Let \mathbf{G}_w be the corresponding contrast matrix for factor A, and then \mathbf{G}_w is a $k_a \times k_a$ matrix with elements

$$\mathbf{G}_{ij} = \begin{cases} 1 - w_i/w_{\cdot}, & \text{if } i = j \\ -w_j/w_{\cdot}, & \text{if } i \neq j \end{cases}$$

where w_i is a marginal weight representing the number of individuals with A at its *i*th level and $w_i = \sum_i w_i$.

Helmert contrasts

The h. operator compares each level with the mean of the subsequent levels. Let H be the corresponding contrast matrix for factor A, and then H is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{H}_{ij} = \begin{cases} 1, & \text{if } i = j \\ -1/(k_a - i), & \text{if } i < j \\ 0, & \text{otherwise} \end{cases}$$

If $k_a = 5$, then

$$\mathbf{H} = \begin{pmatrix} 1 & -1/4 & -1/4 & -1/4 & -1/4 \\ 0 & 1 & -1/3 & -1/3 & -1/3 \\ 0 & 0 & 1 & -1/2 & -1/2 \\ 0 & 0 & 0 & 1 & -1 \end{pmatrix}$$

The hw. operator compares each level with the weighted mean of the subsequent levels. Let \mathbf{H}_w be the corresponding contrast matrix for factor A, and then \mathbf{H}_w is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{H}_{wij} = \begin{cases} 1, & \text{if } i = j \\ -w_j / \sum_{l=j}^{k_a} w_l, & \text{if } i < j \\ 0, & \text{otherwise} \end{cases}$$

Reverse Helmert contrasts

The j. operator compares each level with the mean of the previous levels. Let J be the corresponding contrast matrix for factor A, and then J is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{J}_{ij} = \begin{cases} 1, & \text{if } i+1=j\\ -1/i, & \text{if } j \leq i\\ 0, & \text{otherwise} \end{cases}$$

If $k_a = 5$, then

$$\mathbf{H} = \begin{pmatrix} -1 & 1 & 0 & 0 & 0 \\ -1/2 & -1/2 & 1 & 0 & 0 \\ -1/3 & -1/3 & -1/3 & 1 & 0 \\ -1/4 & -1/4 & -1/4 & -1/4 & 1 \end{pmatrix}$$

The jw. operator compares each level with the weighted mean of the previous levels. Let \mathbf{J}_w be the corresponding contrast matrix for factor A, and then \mathbf{J}_w is a $(k_a - 1) \times k_a$ matrix with elements

$$\mathbf{J}_{wij} = \begin{cases} 1, & \text{if } i+1=j\\ -w_j / \sum_{l=1}^i w_l, & \text{if } i \leq j\\ 0, & \text{otherwise} \end{cases}$$

Orthogonal polynomial contrasts

The p. operator applies orthogonal polynomial contrasts using the level values of the attached factor variable. The q. operator applies orthogonal polynomial contrasts using the level indices of the attached factor variable. These two operators are equivalent when the level values of the attached factor are equally spaced. The pw. and qw. operators are weighted versions of p. and q., where the weights are taken from the observed weighted cell frequencies in the estimation sample of the fitted model. contrast uses the Christoffel–Darboux recurrence formula for computing orthogonal polynomial contrasts (Abramowitz and Stegun 1972). The elements of the contrasts are normalized such that

$$\mathbf{Q}'\mathbf{W}\mathbf{Q} = \frac{1}{w}\mathbf{I}$$

where **W** is a diagonal matrix of the marginal cell weights w_1, w_2, \ldots, w_k of the attached factor variable (all 1 for p. and q.), and w. is the sum of the weights (the number of levels k for p. and q.).

Contrasts within interactions

Contrast operators are allowed to be specified on factor variables participating in interactions. In such cases, contrast applies the proper matrix product of the contrast matrices to the cell margins of the interacted factor variables.

For example, consider the contrasts implied by specifying r.A#h.B. Let M be the matrix of estimated cell margins for the levels of A and B, where the rows of M are indexed by the levels of A and the columns are indexed by the levels of B. contrast puts the estimated cell margins in the following vector form:

$$\mathbf{v} = \mathrm{vec}(\mathbf{M}') = egin{pmatrix} \mathbf{M}_{11} & \mathbf{M}_{12} & dots & dots$$

The individual contrasts are then given by the elements of

 $(\mathbf{R} \otimes \mathbf{H})\mathbf{v}$

where \otimes denotes the Kronecker direct product.

Multiple comparisons

See [R] **pwcompare** for details on the methods and formulas used to adjust *p*-values and confidence intervals for multiple comparisons. The formulas for Bonferroni's method and Šidák's method are presented with m = k(k - 1)/2, the number of pairwise comparisons for a factor term with k levels. For contrasts, *m* is instead the number of contrasts being performed on the factor term; often, m = k - 1 for a term with k levels.

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Also see

- [R] contrast postestimation Postestimation tools for contrast
- [R] **lincom** Linear combinations of estimators
- [R] margins Marginal means, predictive margins, and marginal effects
- [R] margins, contrast Contrasts of margins
- [R] **pwcompare** Pairwise comparisons
- [R] test Test linear hypotheses after estimation
- [U] 20 Estimation and postestimation commands