**xtreg** fits regression models to panel data. In particular, **xtreg** with the `be` option fits random-effects models by using the between regression estimator; with the `fe` option, it fits fixed-effects models (by using the within regression estimator); and with the `re` option, it fits random-effects models by using the GLS estimator (producing a matrix-weighted average of the between and within results). See [XT] **xtdata** for a faster way to fit fixed- and random-effects models.

### Quick start

Random-effects linear regression by GLS of $y$ on $x_1$ and $x_2$ using **xtset** data

```
xtreg y x1 x2
```

As above, but estimate by maximum likelihood

```
xtreg y x1 x2, mle
```

Fixed-effects model with cluster–robust standard errors for panels nested within `cvar`

```
xtreg y x1 x2, fe vce(cluster cvar)
```

Population-averaged model with an exchangeable within-panel correlation structure

```
xtrreg y x1 x2, pa
```

As above, but specify an autoregressive correlation structure of order 1

```
xtrreg y x1 x2, pa corr(ar 1)
```

Between-effects model

```
xtrreg y x1 x2, be
```

### Menu

Statistics > Longitudinal/panel data > Linear models > Linear regression (FE, RE, PA, BE)
Syntax

GLS random-effects (RE) model

```
xtreg depvar [indepvars] [if] [in] [, re RE_options]
```

Between-effects (BE) model

```
xtreg depvar [indepvars] [if] [in], be [BE_options]
```

Fixed-effects (FE) model

```
xtreg depvar [indepvars] [if] [in] [weight], fe [FE_options]
```

ML random-effects (MLE) model

```
xtreg depvar [indepvars] [if] [in] [weight], mle [MLE_options]
```

Population-averaged (PA) model

```
xtreg depvar [indepvars] [if] [in] [weight], pa [PA_options]
```

<table>
<thead>
<tr>
<th>RE_options</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Model</strong></td>
<td></td>
</tr>
<tr>
<td>re</td>
<td>use random-effects estimator; the default</td>
</tr>
<tr>
<td>sa</td>
<td>use Swamy–Arora estimator of the variance components</td>
</tr>
<tr>
<td><strong>SE/Robust</strong></td>
<td></td>
</tr>
<tr>
<td>vce(vcetype)</td>
<td>vcetype may be conventional, robust, cluster clustvar, bootstrap, or jackknife</td>
</tr>
<tr>
<td><strong>Reporting</strong></td>
<td></td>
</tr>
<tr>
<td>level(#)</td>
<td>set confidence level; default is level(95)</td>
</tr>
<tr>
<td>theta</td>
<td>reportθ</td>
</tr>
<tr>
<td>display_options</td>
<td>control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling</td>
</tr>
<tr>
<td>coeflegend</td>
<td>display legend instead of statistics</td>
</tr>
</tbody>
</table>
### BE_options

<table>
<thead>
<tr>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Model</strong></td>
</tr>
<tr>
<td><strong>be</strong> use between-effects estimator</td>
</tr>
<tr>
<td><strong>wls</strong> use weighted least squares</td>
</tr>
<tr>
<td><strong>SE</strong></td>
</tr>
<tr>
<td><strong>vce(vcetype)</strong> vcetype may be conventional, bootstrap, or jackknife</td>
</tr>
<tr>
<td><strong>Reporting</strong></td>
</tr>
<tr>
<td><strong>_level(#)</strong> set confidence level; default is _level(95)</td>
</tr>
<tr>
<td><strong>display_options</strong> control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling</td>
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</tbody>
</table>

### FE_options

<table>
<thead>
<tr>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Model</strong></td>
</tr>
<tr>
<td><strong>fe</strong> use fixed-effects estimator</td>
</tr>
<tr>
<td><strong>SE/Robust</strong></td>
</tr>
<tr>
<td><strong>vce(vcetype)</strong> vcetype may be conventional, robust, cluster clustvar, bootstrap, or jackknife</td>
</tr>
<tr>
<td><strong>Reporting</strong></td>
</tr>
<tr>
<td><strong>_level(#)</strong> set confidence level; default is _level(95)</td>
</tr>
<tr>
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</tr>
</tbody>
</table>

### MLE_options

<table>
<thead>
<tr>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Model</strong></td>
</tr>
<tr>
<td><strong>noconstant</strong> suppress constant term</td>
</tr>
<tr>
<td><strong>mle</strong> use ML random-effects estimator</td>
</tr>
<tr>
<td><strong>SE/Robust</strong></td>
</tr>
<tr>
<td><strong>vce(vcetype)</strong> vcetype may be oim, robust, cluster clustvar, bootstrap, or jackknife</td>
</tr>
<tr>
<td><strong>Reporting</strong></td>
</tr>
<tr>
<td><strong>_level(#)</strong> set confidence level; default is _level(95)</td>
</tr>
<tr>
<td><strong>display_options</strong> control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling</td>
</tr>
<tr>
<td><strong>Maximization</strong></td>
</tr>
<tr>
<td><strong>maximize_options</strong> control the maximization process; seldom used</td>
</tr>
<tr>
<td><strong>coeflegend</strong> display legend instead of statistics</td>
</tr>
</tbody>
</table>

### Maximization

- **maximize_options** control the maximization process; seldom used
- **coeflegend** display legend instead of statistics
### Model Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>noconstant</code></td>
<td>suppress constant term</td>
</tr>
<tr>
<td><code>pa</code></td>
<td>use population-averaged estimator</td>
</tr>
<tr>
<td><code>offset()</code></td>
<td>include <code>varname</code> in model with coefficient constrained to 1</td>
</tr>
</tbody>
</table>

### Correlation Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>corr()</code></td>
<td>within-panel correlation structure</td>
</tr>
<tr>
<td><code>force</code></td>
<td>estimate even if observations unequally spaced in time</td>
</tr>
</tbody>
</table>

### SE/Robust Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>vce()</code></td>
<td><code>vcetype</code> may be <code>conventional</code>, <code>robust</code>, <code>bootstrap</code>, or <code>jackknife</code></td>
</tr>
<tr>
<td><code>nmp</code></td>
<td>use divisor $N - P$ instead of the default $N$</td>
</tr>
<tr>
<td><code>rgf</code></td>
<td>multiply the robust variance estimate by $(N - 1)/(N - P)$</td>
</tr>
<tr>
<td><code>scale()</code></td>
<td>overrides the default scale parameter; <code>parm</code> may be x2, dev, phi, or #</td>
</tr>
</tbody>
</table>

### Reporting Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>level()</code></td>
<td>set confidence level; default is <code>level(95)</code></td>
</tr>
<tr>
<td><code>display_options</code></td>
<td>control columns and column formats, row spacing, line width,</td>
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<tr>
<td></td>
<td>display of omitted variables and base and empty cells, and</td>
</tr>
<tr>
<td></td>
<td>factor-variable labeling</td>
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</tbody>
</table>

### Optimization Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>optimize_options</code></td>
<td>control the optimization process; seldom used</td>
</tr>
<tr>
<td><code>coeflegend</code></td>
<td>display legend instead of statistics</td>
</tr>
</tbody>
</table>

### Correlation Types

<table>
<thead>
<tr>
<th>Option</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>exchangeable</code></td>
<td>exchangeable</td>
</tr>
<tr>
<td><code>independent</code></td>
<td>independent</td>
</tr>
<tr>
<td><code>unstructured</code></td>
<td>unstructured</td>
</tr>
<tr>
<td><code>fixed matname</code></td>
<td>user-specified</td>
</tr>
<tr>
<td><code>ar</code></td>
<td>autoregressive of order #</td>
</tr>
<tr>
<td><code>stationary</code></td>
<td>stationary of order #</td>
</tr>
<tr>
<td><code>nonstationary</code></td>
<td>nonstationary of order #</td>
</tr>
</tbody>
</table>

A panel variable must be specified. For `xtreg`, `pa`, correlation structures other than `exchangeable` and `independent` require that a time variable also be specified. Use `xtset`; see [XT] `xtset`.

`indevars` may contain factor variables; see [U] 11.4.3 Factor variables.

`depar` and `indevars` may contain time-series operators; see [U] 11.4.4 Time-series varlists.

`by`, `mi estimate`, and `statsby` are allowed; see [U] 11.1.10 Prefix commands. `fp` is allowed for the between-effects, fixed-effects, and maximum-likelihood random-effects models.

`vce(bootstrap)` and `vce(jackknife)` are not allowed with the `mi estimate` prefix; see [MI] `mi estimate`.

`aweights`, `fweights`, and `pweights` are allowed for the fixed-effects model. `iweights`, `fweights`, and `pweights` are allowed for the population-averaged model. `iweights` are allowed for the maximum-likelihood random-effects (MLE) model. See [U] 11.1.6 weight. Weights must be constant within panel.

`coeflegend` does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.
Options for RE model

re, the default, requests the GLS random-effects estimator.

sa specifies that the small-sample Swamy–Arora estimator individual-level variance component be used instead of the default consistent estimator. See xtreg, re in Methods and formulas for details.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (conventional), that are robust to some kinds of misspecification (robust), that allow for intragroup correlation (cluster clustvar), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [XT] vce_options.

vce(conventional), the default, uses the conventionally derived variance estimator for generalized least-squares regression.

Specifying vce(robust) is equivalent to specifying vce(cluster panelvar); see xtreg, re in Methods and formulas.

level(#); see [R] Estimation options.

theta specifies that the output include the estimated value of \( \theta \) used in combining the between and fixed estimators. For balanced data, this is a constant, and for unbalanced data, a summary of the values is presented in the header of the output.

display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%,fmt), pformat(%,fmt), sformat(%fmt), and nolstretch; see [R] Estimation options.

The following option is available with xtreg but is not shown in the dialog box:

coeflegend; see [R] Estimation options.

Options for BE model

be requests the between regression estimator.

wls specifies that, for unbalanced data, weighted least squares be used rather than the default OLS. Both methods produce consistent estimates. The true variance of the between-effects residual is \( \sigma^2_\nu + T_i \sigma^2_\epsilon \) (see xtreg, be in Methods and formulas below). WLS produces a “stabilized” variance of \( \sigma^2_\nu/T_i + \sigma^2_\epsilon \), which is also not constant. Thus the choice between OLS and WLS amounts to which is more stable.

Comment: xtreg, be is rarely used anyway, but between estimates are an ingredient in the random-effects estimate. Our implementation of xtreg, re uses the OLS estimates for this ingredient, based on our judgment that \( \sigma^2_\nu \) is large relative to \( \sigma^2_\epsilon \) in most models. Formally, only a consistent estimate of the between estimates is required.
vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (conventional) and that use bootstrap or jackknife methods (bootstrap, jackknife); see [XT] vce_options.

vce(conventional), the default, uses the conventionally derived variance estimator for generalized least-squares regression.

Options for FE model

fe requests the fixed-effects (within) regression estimator.

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (conventional), that are robust to some kinds of misspecification (robust), that allow for intragroup correlation (cluster clustvar), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [XT] vce_options.

vce(conventional), the default, uses the conventionally derived variance estimator for generalized least-squares regression.

Specifying vce(robust) is equivalent to specifying vce(cluster panelvar); see xtreg, fe in Methods and formulas.

level(#) and display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt), sformat(%fmt), and nolstretch; see [R] Estimation options.

The following option is available with xtreg but is not shown in the dialog box: coeflegend; see [R] Estimation options.
Options for MLE model

- **Model**
  - `noconstant`; see [R] Estimation options.
  
  `mle` requests the maximum-likelihood random-effects estimator.

- **SE/Robust**
  - `vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [XT] `vce_options`.

- **Reporting**
  - `level(#)`; see [R] Estimation options.

  `display_options`: `noci`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fwrap(#)`, `fwrapon(style)`, `cformat(\%fmt)`, `pformat(\%fmt)`, `sformat(\%fmt)`, and `nolstretch`; see [R] Estimation options.

- **Maximization**
  - `maximize_options`: `iterate(#)`, `[no]log, trace, tolerance(#)`, `ltolerance(#)`, and `from(init_specs)`; see [R] Maximize. These options are seldom used.

The following option is available with `xtreg` but is not shown in the dialog box:

- `coeflegend`; see [R] Estimation options.

Options for PA model

- **Model**
  - `noconstant`; see [R] Estimation options.

  `pa` requests the population-averaged estimator. For linear regression, this is the same as a random-effects estimator (both interpretations hold).

  `xtreg, pa` is equivalent to `xtgee, family(gaussian) link(id) corr(exchangeable)`, which are the defaults for the `xtgee` command. `xtreg, pa` allows all the relevant `xtgee` options such as `vce(robust)`. Whether you use `xtreg, pa` or `xtgee` makes no difference. See [XT] `xtgee`.

- **offset(varname)”; see [R] Estimation options.

- **Correlation**
  - `corr(correlation)` specifies the within-panel correlation structure; the default corresponds to the equal-correlation model, `corr(exchangeable)`.

  When you specify a correlation structure that requires a lag, you indicate the lag after the structure’s name with or without a blank; for example, `corr(ar 1)` or `corr(ar1)`.

  If you specify the fixed correlation structure, you specify the name of the matrix containing the assumed correlations following the word fixed, for example, `corr(fixed myr)`. 
force specifies that estimation be forced even though the time variable is not equally spaced. This is relevant only for correlation structures that require knowledge of the time variable. These correlation structures require that observations be equally spaced so that calculations based on lags correspond to a constant time change. If you specify a time variable indicating that observations are not equally spaced, the (time dependent) model will not be fit. If you also specify force, the model will be fit, and it will be assumed that the lags based on the data ordered by the time variable are appropriate.

\textit{SE/Robust}

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (conventional), that are robust to some kinds of misspecification (robust), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [XT] \textit{vce options}.

vce(conventional), the default, uses the conventionally derived variance estimator for generalized least-squares regression.

nmp; see [XT] \textit{vce options}.

rgf specifies that the robust variance estimate is multiplied by $\frac{(N - 1)}{(N - P)}$, where $N$ is the total number of observations and $P$ is the number of coefficients estimated. This option can be used with family(gaussian) only when vce(robust) is either specified or implied by the use of pweights. Using this option implies that the robust variance estimate is not invariant to the scale of any weights used.

scale(x2|dev|phi|#); see [XT] \textit{vce options}.

\textit{Reporting}

level(#); see [R] \textit{Estimation options}.

display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(\%fmt), pformat(\%fmt), sformat(\%fmt), and nolstretch; see [R] \textit{Estimation options}.

\textit{Optimization}

optimize_options control the iterative optimization process. These options are seldom used.

iterate(#) specifies the maximum number of iterations. When the number of iterations equals #, the optimization stops and presents the current results, even if convergence has not been reached. The default is iterate(100).

tolerance(#) specifies the tolerance for the coefficient vector. When the relative change in the coefficient vector from one iteration to the next is less than or equal to #, the optimization process is stopped. tolerance(1e-6) is the default.

log and nolog specify whether to display the iteration log. The iteration log is displayed by default unless you used set iterlog off to suppress it; see set iterlog in [R] \textit{set iter}.

trace specifies that the current estimates be printed at each iteration.

The following option is available with xtreg but is not shown in the dialog box: coeflegend; see [R] \textit{Estimation options}. 
Remarks and examples

If you have not read [XT] xt, please do so.

See Baltagi (2013, chap. 2) and Wooldridge (2020, chap. 14) for good overviews of fixed-effects and random-effects models. Allison (2009) provides perspective on the use of fixed- versus random-effects estimators and provides many examples using Stata.

Consider fitting models of the form

$$y_{it} = \alpha + x_{it}\beta + \nu_i + \epsilon_{it} \quad (1)$$

In this model, $\nu_i + \epsilon_{it}$ is the error term that we have little interest in; we want estimates of $\beta$. $\nu_i$ is the unit-specific error term; it differs between units, but for any particular unit, its value is constant.

In the pulmonary data of [XT] xt, a person who exercises less would presumably have a lower forced expiratory volume (FEV) year after year and so would have a negative $\nu_i$.

$\epsilon_{it}$ is the “usual” error term with the usual properties (mean 0, uncorrelated with itself, uncorrelated with $x$, uncorrelated with $\nu$, and homoskedastic), although in a more thorough development, we could decompose $\epsilon_{it} = \nu_i + \omega_{it}$, assume that $\omega_{it}$ is a conventional error term, and better describe $\nu_i$.

Before making the assumptions necessary for estimation, let’s perform some useful algebra on (1). Whatever the properties of $\nu_i$ and $\epsilon_{it}$, if (1) is true, it must also be true that

$$\bar{y}_i = \alpha + \bar{x}_i\beta + \nu_i + \bar{\epsilon}_i \quad (2)$$

where $\bar{y}_i = \sum_t y_{it}/T_i$, $\bar{x}_i = \sum_t x_{it}/T_i$, and $\bar{\epsilon}_i = \sum_t \epsilon_{it}/T_i$. Subtracting (2) from (1), it must be equally true that

$$(y_{it} - \bar{y}_i) = (x_{it} - \bar{x}_i)\beta + (\epsilon_{it} - \bar{\epsilon}_i) \quad (3)$$

These three equations provide the basis for estimating $\beta$. In particular, xtreg, fe provides what is known as the fixed-effects estimator—also known as the within estimator—and amounts to using OLS to perform the estimation of (3). xtreg, be provides what is known as the between estimator and amounts to using OLS to perform the estimation of (2). xtreg, re provides the random-effects estimator and is a (matrix) weighted average of the estimates produced by the between and within estimators. In particular, the random-effects estimator turns out to be equivalent to estimation of

$$(y_{it} - \theta\bar{y}_i) = (1 - \theta)\alpha + (x_{it} - \theta\bar{x}_i)\beta + \{(1 - \theta)\nu_i + (\epsilon_{it} - \theta\bar{\epsilon}_i)\} \quad (4)$$

where $\theta$ is a function of $\sigma^2_\nu$ and $\sigma^2_\epsilon$. If $\sigma^2_\nu = 0$, meaning that $\nu_i$ is always 0, $\theta = 0$ and (1) can be estimated by OLS directly. Alternatively, if $\sigma^2_\epsilon = 0$, meaning that $\epsilon_{it}$ is 0, $\theta = 1$ and the within estimator returns all the information available (which will, in fact, be a regression with an $R^2$ of 1).

For more reasonable cases, few assumptions are required to justify the fixed-effects estimator of (3). The estimates are, however, conditional on the sample in that the $\nu_i$ are not assumed to have a distribution but are instead treated as fixed and estimable. This statistical fine point can lead to difficulty when making out-of-sample predictions, but that aside, the fixed-effects estimator has much to recommend it.

More is required to justify the between estimator of (2), but the conditioning on the sample is not assumed because $\nu_i + \bar{\epsilon}_i$ is treated as an error term. Newly required is that we assume that $\nu_i$ and $\bar{x}_i$ are uncorrelated. This follows from the assumptions of the OLS estimator but is also transparent: were $\nu_i$ and $\bar{x}_i$ correlated, the estimator could not determine how much of the change in $\bar{y}_i$, associated with an increase in $\bar{x}_i$, to assign to $\beta$ versus how much to attribute to the unknown correlation. (This, of course, suggests the use of an instrumental-variable estimator, $\bar{z}_i$, which is correlated with $\bar{x}_i$ but uncorrelated with $\nu_i$, though that approach is not implemented here.)
The random-effects estimator of (4) requires the same no-correlation assumption. In comparison with the between estimator, the random-effects estimator produces more efficient results, albeit ones with unknown small-sample properties. The between estimator is less efficient because it discards the over-time information in the data in favor of simple means; the random-effects estimator uses both the within and the between information.

All of this would seem to leave the between estimator of (2) with no role (except for a minor, technical part it plays in helping to estimate \( \sigma^2_\nu \) and \( \sigma^2_\epsilon \), which are used in the calculation of \( \theta \), on which the random-effects estimates depend). Let’s, however, consider a variation on (1):

\[
y_{it} = \alpha + \bar{x}_i \beta_1 + (x_{it} - \bar{x}_i) \beta_2 + \nu_i + \epsilon_{it} \tag{1'}
\]

In this model, we postulate that changes in the average value of \( x \) for an individual have a different effect from temporary departures from the average. In an economic situation, \( y \) might be purchases of some item and \( x \) income; a change in average income should have more effect than a transitory change. In a clinical situation, \( y \) might be a physical response and \( x \) the level of a chemical in the brain; the model allows a different response to permanent rather than transitory changes.

The variations of (2) and (3) corresponding to (1') are

\[
\bar{y}_i = \alpha + \bar{x}_i \beta_1 + \nu_i + \bar{\epsilon}_i \tag{2'}
\]

\[
(y_{it} - \bar{y}_i) = (x_{it} - \bar{x}_i) \beta_2 + (\epsilon_{it} - \bar{\epsilon}_i) \tag{3'}
\]

That is, the between estimator estimates \( \beta_1 \) and the within \( \beta_2 \), and neither estimates the other. Thus even when estimating equations like (1), it is worth comparing the within and between estimators. Differences in results can suggest models like (1'), or at the least some other specification error.

Finally, it is worth understanding the role of the between and within estimators with regressors that are constant over time or constant over units. Consider the model

\[
y_{it} = \alpha + x_{it} \beta_1 + s_i \beta_2 + z_t \beta_3 + \nu_i + \epsilon_{it} \tag{1''}
\]

This model is the same as (1), except that we explicitly identify the variables that vary over both time and \( i \) (\( x_{it} \), such as output or FEV); variables that are constant over time (\( s_i \), such as race or sex); and variables that vary solely over time (\( z_t \), such as the consumer price index or age in a cohort study). The corresponding between and within equations are

\[
\bar{y}_i = \alpha + \bar{x}_i \beta_1 + s_i \beta_2 + \bar{z} \beta_3 + \nu_i + \bar{\epsilon}_i \tag{2''}
\]

\[
(y_{it} - \bar{y}_i) = (x_{it} - \bar{x}_i) \beta_1 + (z_t - \bar{z}) \beta_3 + (\epsilon_{it} - \bar{\epsilon}_i) \tag{3''}
\]

In the between estimator of (2''), no estimate of \( \beta_3 \) is possible because \( \bar{z} \) is a constant across the \( i \) observations; the regression-estimated intercept will be an estimate of \( \alpha + \bar{z} \beta_3 \). On the other hand, it can provide estimates of \( \beta_1 \) and \( \beta_2 \). It can estimate effects of factors that are constant over time, such as race and sex, but to do so it must assume that \( \nu_i \) is uncorrelated with those factors.
Assessing goodness of fit

Assessing goodness of fit

xtreg reports “R-squares” corresponding to these three equations. R-squares is in quotes because the R-squares reported do not have all the properties of the OLS $R^2$.

The ordinary properties of $R^2$ include being equal to the squared correlation between $\hat{y}$ and $y$ and being equal to the fraction of the variation in $y$ explained by $\hat{y}$—formally defined as $\text{Var}(\hat{y})/\text{Var}(y)$.

Remarks are presented under the following headings:

Assessing goodness of fit

xtreg and associated commands

The within estimator of (3′′′), like the between estimator, provides an estimate of $\beta_1$ but provides no estimate of $\beta_2$ for time-invariant factors. Instead, it provides an estimate of $\beta_3$, the effects of the time-varying factors. The within estimator can also provide estimates $u_i$ for $\nu_i$. More correctly, the estimator $u_i$ is an estimator of $\nu_i + s_i\beta_3$. Thus $u_i$ is an estimator of $\nu_i$ only if there are no time-invariant variables in the model. If there are time-invariant variables, $u_i$ is an estimate of $\nu_i$ plus the effects of the time-invariant variables.

The within estimator of (3′′′) is a popular measure of goodness of fit in ordinary regression. In our case, given $\hat{\alpha}$ and $\hat{\beta}$ estimates of $\alpha$ and $\beta$, we can assess the goodness of fit with respect to (1), (2), or (3). The prediction equations are, respectively,

\[
\hat{y}_{it} = \hat{\alpha} + x_{it}\hat{\beta} \\
\hat{\nu}_{it} = \hat{\alpha} + \bar{x}_i\hat{\beta} \\
\hat{\gamma}_{it} = (\hat{y}_{it} - \hat{\nu}_{it}) = (x_{it} - \bar{x}_i)\hat{\beta}
\]

In particular, xtreg, be obtains its estimates by performing OLS on (2), and therefore its reported $R^2$ between is an ordinary $R^2$. The other two reported $R^2$’s are merely correlations squared, or, if you prefer, $R^2$’s from the second-round regressions $y_{it} = \gamma_{11}\hat{y}_{it}$ and $y_{it} = \gamma_{13}\hat{y}_{it}$.

xtreg, fe obtains its estimates by performing OLS on (3), so its reported $R^2$ within is an ordinary $R^2$. As with be, the other $R^2$’s are correlations squared, or, if you prefer, $R^2$’s from the second-round regressions $\bar{y}_i = \gamma_{22}\hat{\nu}_i$ and, as with be, $\hat{y}_{it} = \gamma_{23}\hat{\gamma}_{it}$.

xtreg, re obtains its estimates by performing OLS on (4); none of the $R^2$’s corresponding to (1′′′), (2′′′), or (3′′′) correspond directly to this estimator (the “relevant” $R^2$ is the one corresponding to (4)). All three reported $R^2$’s are correlations squared, or, if you prefer, from second-round regressions.
Example 1: Between-effects model

Using nlswork.dta described in [XT] xt, we will model ln_wage in terms of completed years of schooling (grade), current age and age squared, current years worked (experience) and experience squared, current years of tenure on the current job and tenure squared, whether black (race = 2), whether residing in an area not designated a standard metropolitan statistical area (SMSA), and whether residing in the South.

To obtain the between-effects estimates, we use xtreg, be. nlswork.dta has previously been xtset idcode year because that is what is true of the data, but for running xtreg, it would have been sufficient to have xtset idcode by itself.

```
. use https://www.stata-press.com/data/r16/nlswork
   (National Longitudinal Survey. Young Women 14-26 years of age in 1968)
```

The between-effects regression is estimated on person-averages, so the “n = 4697” result is relevant.

| Variable   | Coef. | Std. Err. | t     | P>|t| | [95% Conf. Interval] |
|------------|-------|-----------|-------|-----|---------------------|
| grade      | 0.0607602 | 0.0020006 | 30.37 | 0.000 | 0.0568382 0.0646822 |
| age        | 0.0323158 | 0.0087251 | 3.70  | 0.000 | 0.0152105 0.0494211 |
| c.age#c.age | -0.0005997 | 0.0001429 | -4.20 | 0.000 | -0.0008799 -0.0003194 |
| ttl_exp    | 0.0138853 | 0.0056749 | 2.45  | 0.014 | 0.0027598 0.0250108 |
| c.ttl_exp#c.ttl_exp | 0.0007342 | 0.0003267 | 2.25  | 0.025 | 0.0000936 0.0013747 |
| tenure     | 0.0698419 | 0.0060729 | 11.50 | 0.000 | 0.0579361 0.0817476 |
| c.tenure#c.tenure | -0.0028756 | 0.0004098 | -7.02 | 0.000 | -0.0036789 -0.0020722 |
| race black | -0.0564167 | 0.0105131 | -5.37 | 0.000 | -0.0770272 -0.0358061 |
| not_smsa   | -0.1860406 | 0.0112495 | -16.54 | 0.000 | -0.2080949 -0.1639862 |
| south      | -0.0993378 | 0.010136  | -9.80 | 0.000 | -0.1192091 -0.0794665 |
| _cons      | 0.3339113  | 0.1210434 | 2.76  | 0.006 | 0.0966093 0.5712133 |
For goodness of fit, the $R^2$ between is directly relevant; our $R^2$ is 0.4900. If, however, we use these estimates to predict the within model, we have an $R^2$ of 0.1591. If we use these estimates to fit the overall data, our $R^2$ is 0.3695.

The $F$ statistic tests that the coefficients on the regressors grade, age, . . . , south are all jointly zero. Our model is significant.

The root mean squared error of the fitted regression, which is an estimate of the standard deviation of $\nu_i + \epsilon_i$, is 0.3036.

For our coefficients, each year of schooling increases hourly wages by 6.1%; age increases wages up to age 26.9 and thereafter decreases them (because the quadratic $ax^2 + bx + c$ turns over at $x = -b/2a$, which for our age and c.age#c.age coefficients is $0.0323158/(2 \times 0.0005997) \approx 26.9$); total experience increases wages at an increasing rate (which is surprising and bothersome); tenure on the current job increases wages up to a tenure of 12.1 years and thereafter decreases them; wages of blacks are, these things held constant, (approximately) 5.6% below that of nonblacks (approximately because 2.race is an indicator variable); residing in a non-SMSA (rural area) reduces wages by 18.6%; and residing in the South reduces wages by 9.9%.
Example 2: Fixed-effects model

To fit the same model with the fixed-effects estimator, we specify the *fe* option.

```
. xtreg ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp tenure
> c.tenure#c.tenure 2.race not_smsa south, fe
```

Note: grade omitted because of collinearity
Note: 2.race omitted because of collinearity

Fixed-effects (within) regression

<table>
<thead>
<tr>
<th></th>
<th>Number of obs = 28,091</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Group variable: idcode</td>
<td>Number of groups = 4,697</td>
<td></td>
</tr>
<tr>
<td>R-sq:</td>
<td>Obs per group:</td>
<td></td>
</tr>
<tr>
<td>within = 0.1727</td>
<td>min = 1</td>
<td></td>
</tr>
<tr>
<td>between = 0.3505</td>
<td>avg = 6.0</td>
<td></td>
</tr>
<tr>
<td>overall = 0.2625</td>
<td>max = 15</td>
<td></td>
</tr>
<tr>
<td>corr(u_i, Xb) = 0.1936</td>
<td>F(8,23386) = 610.12</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Prob &gt; F = 0.0000</td>
<td></td>
</tr>
</tbody>
</table>

| ln_wage       | Coef.  | Std. Err. | t     | P>|t|  | [95% Conf. Interval] |
|---------------|--------|-----------|-------|------|----------------------|
| grade         | 0 (omitted) | 0.0359987 | .0033864 | 10.63 | 0.000 | .0293611 .0426362 |
| age           | .0359987 | .0033864 | 10.63 | 0.000 | .0293611 .0426362 |
| c.age#c.age   | -.000723 | .0000533 | -13.58 | 0.000 | -.0008274 -.0006186 |
| ttl_exp       | .0334668 | .0029653 | 11.29 | 0.000 | .0276545 .039279 |
| c.ttl_exp#c.ttl_exp | .0002163 | .0001277 | 1.69 | 0.090 | -.0000341 .0004666 |
| tenure        | .0357539 | .0018487 | 19.34 | 0.000 | .0321303 .0393775 |
| c.tenure#c.tenure | -.0019701 | .000125 | -15.76 | 0.000 | -.0022151 -.0017251 |
| race           |          |          |       |      |          |
| black          | 0 (omitted) |          |          |       |          |
| not_smsa       | -.0890108 | .0095316 | -9.34 | 0.000 | -.1076933 -.0703282 |
| south          | -.0606309 | .0109319 | -5.55 | 0.000 | -.0820582 -.0392036 |
| _cons          | 1.03732   | .0485546 | 21.36 | 0.000 | .9421496 1.13249 |
| sigma_u        | .35562203 |          |       |      |          |
| sigma_e        | .29068923 |          |       |      |          |
| rho            | .59946283 (fraction of variance due to u_i) |   |

F test that all u_i=0: F(4696, 23386) = 6.65  Prob > F = 0.0000

The observation summary at the top is the same as for the between-effects model, although this time it is the “Number of obs” that is relevant.

Our three $R^2$'s are not too different from those reported previously; the $R^2$ within is slightly higher (0.1727 versus 0.1591), and the $R^2$ between is a little lower (0.3505 versus 0.4900), as expected, because the between estimator maximizes $R^2$ between and the within estimator $R^2$ within. In terms of overall fit, these estimates are somewhat worse (0.2625 versus 0.3695).

If the unobserved time-invariant component $\nu$ is not correlated with the regressors, estimates from the fixed-effects model are consistent but inefficient relative to estimates from the random-effects model. In this case, the interpretation of $\text{sigma}_u$ in the coefficient table is the same for the fixed-effects and random-effects models. However, $\text{sigma}_u$ is a nuisance parameter when $\nu$ is correlated with the covariates.
Here both grade and 2.race were omitted from the model because they do not vary over time. Because grade and 2.race are time invariant, our estimate $u_i$ is an estimate of $\nu_i$ plus the effects of grade and 2.race, so our estimate of the standard deviation is based on the variation in $\nu_i$, grade, and 2.race. On the other hand, had 2.race and grade been omitted merely because they were collinear with the other regressors in our model, $u_i$ would be an estimate of $\nu_i$, and 0.355622 would be an estimate of $\sigma_{\nu}$. (xtsum and xttab allow you to determine whether a variable is time invariant; see [XT] xtsum and [XT] xttab.)

Regardless of the status of $u_i$, our estimate of the standard deviation of $\epsilon_{it}$ is valid (and, in fact, is the estimate that would be used by the random-effects estimator to produce its results).

Our estimate of the correlation of $u_i$ with $x_{it}$ suffers from the problem of what $u_i$ measures. We find correlation but cannot say whether this is correlation of $\nu_i$ with $x_{it}$ or merely correlation of grade and 2.race with $x_{it}$. In any case, the fixed-effects estimator is robust to such a correlation, and the other estimates it produces are unbiased.

So, although this estimator produces no estimates of the effects of grade and 2.race, it does predict that age has a positive effect on wages up to age 24.9 years (compared with 26.9 years estimated by the between estimator); that total experience still increases wages at an increasing rate (which is still bothersome); that tenure increases wages up to 9.1 years (compared with 12.1); that living in a non-SMSA reduces wages by 8.9% (compared with a more drastic 18.6%); and that living in the South reduces wages by 6.1% (as compared with 9.9%).
Example 3: Fixed-effects models with robust standard errors

If we suspect that there is heteroskedasticity or within-panel serial correlation in the idiosyncratic error term $\epsilon_{it}$, we could specify the `vce(robust)` option:

```
. xtreg ln_w grade c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp tenure
c.tenure#c.tenure 2.race not_smsa south, fe vce(robust)
```

```
Fixed-effects (within) regression

<table>
<thead>
<tr>
<th>ln_wage</th>
<th>Robust</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Coef. Std. Err.</td>
</tr>
<tr>
<td>grade</td>
<td>0 (omitted)</td>
</tr>
<tr>
<td>age</td>
<td>.0359987 .0052407</td>
</tr>
<tr>
<td>c.age#c.age</td>
<td>-.000723 .0000845</td>
</tr>
<tr>
<td>ttl_exp</td>
<td>.0334668 .004069</td>
</tr>
<tr>
<td>c.ttl_exp#c.ttl_exp</td>
<td>.0002163 .0001763</td>
</tr>
<tr>
<td>tenure</td>
<td>.0357539 .0024683</td>
</tr>
<tr>
<td>c.tenure#c.tenure</td>
<td>-.0019701 .0001696</td>
</tr>
<tr>
<td>race black</td>
<td>0 (omitted)</td>
</tr>
<tr>
<td>not_smsa</td>
<td>-.0606309 .0163366</td>
</tr>
<tr>
<td>south _cons</td>
<td>1.03732 .0739644</td>
</tr>
</tbody>
</table>

Although the estimated coefficients are the same with and without the `vce(robust)` option, the robust estimator produced larger standard errors and a $p$-value for `c.ttl_exp#c.ttl_exp` above the conventional 10%. The $F$ test of $\nu_i = 0$ is suppressed because it is too difficult to compute the robust form of the statistic when there are more than a few panels.
The robust standard errors reported above are identical to those obtained by clustering on the panel variable `idcode`. Clustering on the panel variable produces an estimator of the VCE that is robust to cross-sectional heteroskedasticity and within-panel (serial) correlation that is asymptotically equivalent to that proposed by Arellano (1987). Although the example above applies the fixed-effects estimator, the robust and cluster-robust VCE estimators are also available for the random-effects estimator. Wooldridge (2020) and Arellano (2003) discuss these robust and cluster-robust VCE estimators for the fixed-effects and random-effects estimators. More details are available in Methods and formulas.

Example 4: Random-effects model

Refitting our log-wage model with the random-effects estimator, we obtain:

```
  . xtreg ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp tenure
    > c.tenure#c.tenure 2.race not_smsa south, re theta
```

Random-effects GLS regression

<table>
<thead>
<tr>
<th>Group variable: idcode</th>
<th>Number of obs = 28,091</th>
</tr>
</thead>
<tbody>
<tr>
<td>R-sq:</td>
<td>Number of groups = 4,697</td>
</tr>
<tr>
<td>within = 0.1715</td>
<td>Obs per group:</td>
</tr>
<tr>
<td>between = 0.4784</td>
<td>min = 1</td>
</tr>
<tr>
<td>overall = 0.3708</td>
<td>avg = 6.0</td>
</tr>
<tr>
<td>corr(u_i, X) = 0 (assumed)</td>
<td>max = 15</td>
</tr>
<tr>
<td>Wald chi2(10) = 9244.74</td>
<td></td>
</tr>
<tr>
<td>Prob &gt; chi2 = 0.0000</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>theta</th>
</tr>
</thead>
<tbody>
<tr>
<td>min 5% median 95% max</td>
</tr>
<tr>
<td>0.2520 0.2520 0.5499 0.7016 0.7206</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>ln_wage</th>
<th>Coef. Std. Err. z P&gt;</th>
<th>z</th>
<th>[95% Conf. Interval]</th>
</tr>
</thead>
<tbody>
<tr>
<td>grade</td>
<td>.0646499 .0017812 36.30 0.000 .0611589 .0681409</td>
<td></td>
<td></td>
</tr>
<tr>
<td>age</td>
<td>.0368059 .0031195 11.80 0.000 .0306918 .0429201</td>
<td></td>
<td></td>
</tr>
<tr>
<td>c.age#c.age</td>
<td>-.0007133 .00005 -14.27 0.000 -.0008113 -.0006153</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ttl_exp</td>
<td>.0290208 .002422 11.98 0.000 .0242739 .0337678</td>
<td></td>
<td></td>
</tr>
<tr>
<td>c.ttl_exp#c.ttl_exp</td>
<td>.0003049 .0001162 2.62 0.009 .000077 .0005327</td>
<td></td>
<td></td>
</tr>
<tr>
<td>tenure</td>
<td>.0392519 .0017554 22.36 0.000 .0358113 .0426925</td>
<td></td>
<td></td>
</tr>
<tr>
<td>c.tenure#c.tenure</td>
<td>-.0020035 .0001193 -16.80 0.000 -.0022373 -.0017697</td>
<td></td>
<td></td>
</tr>
<tr>
<td>race</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>black</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>not_smsa</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>south</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>_cons</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

| sigma_u | .2572072 |
| sigma_e | .29068923 |
| rho     | .44045273 (fraction of variance due to u_i) |

According to the $R^2$'s, this estimator performs worse within than the within fixed-effects estimator and worse between than the between estimator, as it must, and slightly better overall.
We estimate that $\sigma_\nu$ is 0.2579 and $\sigma_\epsilon$ is 0.2907 and, by assertion, assume that the correlation of $\nu$ and $x$ is zero.

All that is known about the random-effects estimator is its asymptotic properties, so rather than reporting an $F$ statistic for overall significance, `xtreg, re` reports a $\chi^2$. Taken jointly, our coefficients are significant.

`xtreg, re` also reports a summary of the distribution of $\theta_i$, an ingredient in the estimation of (4). $\theta$ is not a constant here because we observe women for unequal periods.

We estimate that schooling has a rate of return of 6.5% (compared with 6.1% between and no estimate within); that the increase of wages with age turns around at 25.8 years (compared with 26.9 between and 24.9 within); that total experience yet again increases wages increasingly; that the effect of job tenure turns around at 9.8 years (compared with 12.1 between and 9.1 within); that being black reduces wages by 5.3% (compared with 5.6% between and no estimate within); that living in a non-SMSA reduces wages 13.1% (compared with 18.6% between and 8.9% within); and that living in the South reduces wages 8.7% (compared with 9.9% between and 6.1% within).
Example 5: Random-effects model fit using ML

We could also have fit this random-effects model with the maximum likelihood estimator:

```
xtreg ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp tenure
>  c.tenure#c.tenure 2.race not_smsa south, mle
```

Fitting constant-only model:
Iteration 0: log likelihood = -12663.954
Iteration 1: log likelihood = -12649.756
Iteration 2: log likelihood = -12649.614
Iteration 3: log likelihood = -12649.614

Fitting full model:
Iteration 0: log likelihood = -8922.145
Iteration 1: log likelihood = -8853.6409
Iteration 2: log likelihood = -8853.4255
Iteration 3: log likelihood = -8853.4254

Random-effects ML regression
Number of obs = 28,091
Number of groups = 4,697
Random effects u_i ~ Gaussian
Obs per group:
  min = 1
  avg = 6.0
  max = 15
LR chi2(10) = 7592.38
Log likelihood = -8853.4254
Prob > chi2 = 0.0000

| ln_wage       | Coef. | Std. Err. | z     | P>|z|  | [95% Conf. Interval] |
|---------------|-------|-----------|-------|------|---------------------|
| grade         | 0.06461093 | 0.0017372 | 37.19 | 0.000 | 0.0612044 - 0.0680142 |
| age           | 0.0368531  | 0.0031226 | 11.80 | 0.000 | 0.0307330 - 0.0429732 |
| c.age#c.age   | -0.0007132 | 0.0000501 | -14.24 | 0.000 | -0.0008113 - 0.000615 |
| ttl_exp       | 0.0288196  | 0.0024143 | 11.94 | 0.000 | 0.0240877 - 0.0335515 |
| c.ttl_exp#c.ttl_exp | 0.000309  | 0.0001163 | 2.66  | 0.008 | 0.0000811 - 0.0005369 |
| tenure        | 0.0394371  | 0.0017604 | 22.40 | 0.000 | 0.0359868 - 0.0428875 |
| c.tenure#c.tenure | -0.0020052 | 0.0001195 | -16.77 | 0.000 | -0.0022395 - 0.0017709 |
| race          |         |           |      |      |                     |
| black         | -0.0533394 | 0.0097338 | -5.48 | 0.000 | -0.0724172 - -0.0342615 |
| not_smsa      | -0.1323433 | 0.0071322 | -18.56 | 0.000 | -0.1463221 - -0.1183644 |
| south         | -0.0875599 | 0.0072143 | -12.14 | 0.000 | -0.1016998 - -0.0734201 |
| _cons         | 0.2390837  | 0.0491902 | 4.86  | 0.000 | 0.1426727 - 0.3354947 |
| /sigma_u      | 0.2485556  | 0.0035017 | 2.24  | 0.000 | 0.2417863 - 0.2555144 |
| /sigma_e      | 0.2918458  | 0.001352  | 22.40 | 0.000 | 0.289208 - 0.2945076  |
| rho           | 0.4204033  | 0.0074828 | 5.58  | 0.000 | 0.4057959 - 0.4351212 |

LR test of sigma_u=0: chibar2(01) = 7339.84
Prob >= chibar2 = 0.000

```
The estimates are nearly the same as those produced by `xtreg, re`—the GLS estimator. For instance, `xtreg, re` estimated the coefficient on `grade` to be 0.0646499, `xtreg, mle` estimated 0.0646093, and the ratio is $0.0646499/0.0646093 = 1.001$ to three decimal places. Similarly, the standard errors are nearly equal: $0.0017811/0.0017372 = 1.025$. Below we compare all 11 coefficients:

<table>
<thead>
<tr>
<th>Estimator</th>
<th>Coefficient ratio</th>
<th>SE ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>min.</td>
</tr>
<tr>
<td><code>xtreg, mle</code> (ML)</td>
<td>1.</td>
<td>1.</td>
</tr>
<tr>
<td><code>xtreg, re</code> (GLS)</td>
<td>.997</td>
<td>.987</td>
</tr>
</tbody>
</table>

Example 6: Population-averaged model

We could also have fit this model with the population-averaged estimator:

```stata
. xtreg ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp tenure > c.tenure#c.tenure 2.race not_smsa south, pa
```

```
Iteration 1: tolerance = .0310561
Iteration 2: tolerance = .00074898
Iteration 3: tolerance = .0000147
Iteration 4: tolerance = 2.880e-07
GEE population-averaged model Number of obs = 28,091
Group variable: idcode Number of groups = 4,697
Link: identity Obs per group:
Family: Gaussian min = 1
Correlation: exchangeable avg = 6.0
max = 15 Wald chi2(10) = 9598.89
Scale parameter: .1436709 Prob > chi2 = 0.0000
```

```
ln_wage          Coef. Std. Err.    z     P>|z|      [95% Conf. Interval]
----------------- ------------- -------- -------- --------- --------------
grade            .0645427 .0016829  38.35  0.000     .0612442   .0678412
age             .0369320 .0031509   11.72  0.000     .0307508   .0431076
c.age#c.age     -.0007129 .0000506  -14.10  0.000    -.0008121  -.0006138
ttl_exp         .0284878 .0024169   11.79  0.000     .0237508   .0332248
c.ttl_exp#c.ttl_exp -.0003158 .0001172  -2.69  0.007     -.0005456  -.000086
tenure          .0397468 .0017779   22.36  0.000     .0362621   .0432315
c.tenure#c.tenure -.002008  .0001209  -16.61  0.000    -.0022449  -.0017711
race            -black  -.0538314 .0094086  -5.72  0.000    -.072272   -.0353909
                 not_smsa -.1347788 .0070543  -19.11  0.000   -.1486049  -.1209526
                 south  -.0885969 .0071132  -12.46  0.000    -.1025386  -.0746552
                 _cons   .2396286 .0491465   4.88   0.000     .1433034   .3359539
```
These results differ from those produced by `xtreg, re` and `xtreg, mle`. Coefficients are larger and standard errors smaller. `xtreg, pa` is simply another way to run the `xtgee` command. That is, we would have obtained the same output had we typed

```
. xtgee ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp
tenure c.tenure#c.tenure 2.race not_smsa south
(output omitted because it is the same as above)
```

See [XT] `xtgee`. In the language of `xtgee`, the random-effects model corresponds to an exchangeable correlation structure and identity link, and `xtgee` also allows other correlation structures. Let’s stay with the random-effects model, however. `xtgee` will also produce robust estimates of variance, and we refit this model that way by typing

```
. xtgee ln_w grade age c.age#c.age ttl_exp c.ttl_exp#c.ttl_exp
tenure c.tenure#c.tenure 2.race not_smsa south, vce(robust)
(output omitted, coefficients the same, standard errors different)
```

In the previous example, we presented a table comparing `xtreg, re` with `xtreg, mle`. Below we add the results from the estimates shown and the ones we did with `xtgee, vce(robust)`:  

<table>
<thead>
<tr>
<th>Estimator</th>
<th>Coefficient ratio</th>
<th>SE ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>min.</td>
</tr>
<tr>
<td><code>xtreg, mle</code> (ML)</td>
<td>1.</td>
<td>1.</td>
</tr>
<tr>
<td><code>xtreg, re</code> (GLS)</td>
<td>.997</td>
<td>.987</td>
</tr>
<tr>
<td><code>xtreg, pa</code> (PA)</td>
<td>1.060</td>
<td>.847</td>
</tr>
<tr>
<td><code>xtgee, vce(robust)</code> (PA)</td>
<td>1.060</td>
<td>.847</td>
</tr>
</tbody>
</table>

So, which are right? This is a real dataset, and we do not know. However, in example 2 in [XT] `xtreg postestimation`, we will present evidence that the assumptions underlying the `xtreg, re` and `xtreg, mle` results are not met.
Stored results

_xtreg, re_ stores the following in _e():_

**Scalars**
- _e(N)_  number of observations
- _e(N_g)_  number of groups
- _e(df_m)_  model degrees of freedom
- _e(g_min)_  smallest group size
- _e(g_avg)_  average group size
- _e(g_max)_  largest group size
- _e(Tcon)_  1 if _T_ is constant
- _e(sigma)_  ancillary parameter (_gamma, lnormal_)
- _e(sigma_u)_  panel-level standard deviation
- _e(sigma_e)_  standard deviation of _e_ \(_it\)
- _e(r2_w)_  _R-squared_ for within model
- _e(r2_o)_  _R-squared_ for overall model
- _e(r2_b)_  _R-squared_ for between model
- _e(N_clust)_  number of clusters
- _e(chi2)_  _\chi^2_
- _e(p)_  _p_-value for model test
- _e(rho)_  _\rho_
- _e(theta_min)_  minimum _\theta_
- _e(theta_5)_  _\theta_ , 5th percentile
- _e(theta_50)_  _\theta_ , 50th percentile
- _e(theta_95)_  _\theta_ , 95th percentile
- _e(theta_max)_  maximum _\theta_
- _e(rmse)_  root mean squared error of GLS regression
- _e(Tbar)_  harmonic mean of group sizes
- _e(rank)_  rank of _e(V)_

**Macros**
- _e(cmd)_  _xtreg_
- _e(cmdline)_  command as typed
- _e(depvar)_  name of dependent variable
- _e(ivar)_  variable denoting groups
- _e(model)_  _re_
- _e(clustvar)_  name of cluster variable
- _e(chi2type)_  _Wald_; type of model _\chi^2_ test
- _e(vce)_  _vcetype_ specified in _vce()_
- _e(vcetype)_  title used to label Std. Err.
- _e(sa)_  _sa_, if specified
- _e(properties)_  _b V_
- _e(predict)_  program used to implement _predict_
- _e(marginsnotok)_  predictions disallowed by _margins_
- _e(asbalanced)_  factor variables _fvset_ as _asbalanced_
- _e(asobserved)_  factor variables _fvset_ as _asobserved_

**Matrices**
- _e(b)_  coefficient vector
- _e(bf)_  coefficient vector for fixed-effects model
- _e(theta)_  _\theta_
- _e(V)_  variance–covariance matrix of the estimators
- _e(VCEf)_  VCE for fixed-effects model

**Functions**
- _e(sample)_  marks estimation sample
xtreg, be stores the following in e():

Scalars
- e(N) number of observations
- e(N_g) number of groups
- e(mss) model sum of squares
- e(df_m) model degrees of freedom
- e(rss) residual sum of squares
- e(df_r) residual degrees of freedom
- e(ll) log likelihood
- e(ll_0) log likelihood, constant-only model
- e(g_min) smallest group size
- e(g_avg) average group size
- e(g_max) largest group size
- e(Tcon) 1 if \( T \) is constant
- e(r2) \( R^2 \) statistic
- e(r2_a) adjusted \( R^2 \)-squared
- e(r2_w) \( R^2 \)-squared for within model
- e(r2_o) \( R^2 \)-squared for overall model
- e(r2_b) \( R^2 \)-squared for between model
- e(F) \( F \) statistic
- e(p) \( p \)-value for model test
- e(rmse) root mean squared error
- e(Tbar) harmonic mean of group sizes
- e(rank) rank of e(V)

Macros
- e(cmd) xtreg
- e(cmdline) command as typed
- e(depvar) name of dependent variable
- e(ivar) variable denoting groups
- e(model) be
- e(typ) WLS, if wls specified
- e(title) title in estimation output
- e(vce) vcetype specified in vce()
- e(properties) b V
- e(predict) program used to implement predict
- e(marginsok) predictions allowed by margins
- e(marginsnotok) predictions disallowed by margins
- e(asbalanced) factor variables fvset as asbalanced
- e(asobserved) factor variables fvset as asobserved

Matrices
- e(b) coefficient vector
- e(V) variance–covariance matrix of the estimators

Functions
- e(sample) marks estimation sample
xtreg, fe stores the following in e():

Scalars
- **e(N)**: number of observations
- **e(N_g)**: number of groups
- **e(mss)**: model sum of squares
- **e(df_m)**: model degrees of freedom
- **e(rss)**: residual sum of squares
- **e(df_r)**: residual degrees of freedom
- **e(tss)**: total sum of squares
- **e(g_min)**: smallest group size
- **e(g_avg)**: average group size
- **e(g_max)**: largest group size
- **e(Tcon)**: 1 if $T$ is constant
- **e(sigma)**: ancillary parameter (gamma, lnormal)
- **e(corr)**: $corr(u_i, Xb)$
- **e(sigma_u)**: panel-level standard deviation
- **e(sigma_e)**: standard deviation of $\epsilon_{it}$
- **e(r2)**: $R$-squared
- **e(r2_a)**: adjusted $R$-squared
- **e(r2_w)**: $R$-squared for within model
- **e(r2_o)**: $R$-squared for overall model
- **e(r2_b)**: $R$-squared for between model
- **e(ll)**: log likelihood
- **e(ll_0)**: log likelihood, constant-only model
- **e(N_clust)**: number of clusters
- **e(rho)**: $\rho$
- **e(F)**: $F$ statistic
- **e(F_f)**: $F$ statistic for test of $u_i=0$
- **e(p)**: $p$-value for model test
- **e(p_f)**: $p$-value for test of $u_i=0$
- **e(df_a)**: degrees of freedom for absorbed effect
- **e(df_b)**: numerator degrees of freedom for $F$ statistic
- **e(rmse)**: root mean squared error
- **e(Tbar)**: harmonic mean of group sizes
- **e(rank)**: rank of $e(V)$

Macros
- **e(cmd)**: xtreg
- **e(cmdline)**: command as typed
- **e(depvar)**: name of dependent variable
- **e(ivar)**: variable denoting groups
- **e(model)**: fe
- **e(wtype)**: weight type
- **e(wexp)**: weight expression
- **e(clustvar)**: name of cluster variable
- **e(vce)**: vcetype specified in vce()
- **e(vcetype)**: title used to label Std. Err.
- **e(properties)**: b V
- **e(predict)**: program used to implement predict
- **e(marginsnotok)**: predictions disallowed by margins
- **e(asbalanced)**: factor variables fvset as asbalanced
- **e(asobserved)**: factor variables fvset as aasobserved

Matrices
- **e(b)**: coefficient vector
- **e(V)**: variance–covariance matrix of the estimators
- **e(V_modelbased)**: model-based variance

Functions
- **e(sample)**: marks estimation sample
xtreg, mle stores the following in e():

Scalars
- e(N) number of observations
- e(N_g) number of groups
- e(df_m) model degrees of freedom
- e(g_min) smallest group size
- e(g_avg) average group size
- e(g_max) largest group size
- e(sigma_u) panel-level standard deviation
- e(sigma_e) standard deviation of $\epsilon_{it}$
- e(ll) log likelihood
- e(ll_0) log likelihood, constant-only model
- e(ll_c) log likelihood, comparison model
- e(N_clust) number of clusters
- e(chi2) $\chi^2$
- e(chi2_c) $\chi^2$ for comparison test
- e(p) $p$-value for model test
- e(rho) $\rho$
- e(rank) rank of e(V)

Macros
- e(cmd) xtreg
- e(cmdline) command as typed
- e(depvar) name of dependent variable
- e(ivar) variable denoting groups
- e(model) ml
- e(wtype) weight type
- e(wexp) weight expression
- e(title) title in estimation output
- e(clustvar) name of cluster variable
- e(vce) vcetype specified in vce()
- e(vcetype) title used to label Std. Err.
- e(chi2type) Wald or LR; type of model $\chi^2$ test
- e(chi2_ct) Wald or LR; type of model $\chi^2$ test corresponding to e(chi2_c)
- e(distrib) Gaussian; the distribution of the RE
- e(properties) b V
- e(predict) program used to implement predict
- e(marginsnotok) predictions disallowed by margins
- e(asbalanced) factor variables fvset as asbalanced
- e(asobserved) factor variables fvset as asobserved

Matrices
- e(b) coefficient vector
- e(V) variance–covariance matrix of the estimators

Functions
- e(sample) marks estimation sample
xtreg, pa stores the following in e():

Scalars
- e(N) number of observations
- e(N_g) number of groups
- e(df_m) model degrees of freedom
- e(chi2) \( \chi^2 \)
- e(p) \( p \)-value for model test
- e(df_pear) degrees of freedom for Pearson \( \chi^2 \)
- e(chi2_dev) \( \chi^2 \) test of deviance
- e(chi2_dis) \( \chi^2 \) test of deviance dispersion
- e(deviance) deviance
- e(dispers) deviance dispersion
- e(phi) scale parameter
- e(g_min) smallest group size
- e(g_avg) average group size
- e(g_max) largest group size
- e(rank) rank of e(V)
- e(tol) target tolerance
- e(dif) achieved tolerance
- e(rc) return code

Macros
- e(cmd) xtgee
- e(cmd2) xtreg
- e(cmdline) command as typed
- e(depvar) name of dependent variable
- e(ivar) variable denoting groups
- e(tvar) variable denoting time within groups
- e(model) pa
- e(family) Gaussian
- e(link) identity; link function
- e(corr) correlation structure
- e(scale) x2, dev, phi, or #; scale parameter
- e(wtype) weight type
- e(wexp) weight expression
- e(offset) linear offset variable
- e(chi2type) Wald; type of model \( \chi^2 \) test
- e(vce) vcetype specified in vce()
- e(vcetype) title used to label Std. Err.
- e(rgf) rgf, if rgf specified
- e(nmp) nmp, if specified
- e(properties) b V
- e(predict) program used to implement predict
- e(marginsnotok) predictions disallowed by margins
- e(asbalanced) factor variables fvset as asbalanced
- e(asobserved) factor variables fvset as asobserved

Matrices
- e(b) coefficient vector
- e(R) estimated working correlation matrix
- e(V) variance–covariance matrix of the estimators
- e(V_modelbased) model-based variance

Functions
- e(sample) marks estimation sample

Methods and formulas

The model to be fit is

\[ y_{it} = \alpha + x_{it}\beta + \nu_i + \epsilon_{it} \]

for \( i = 1, \ldots, n \) and, for each \( i, t = 1, \ldots, T \), of which \( T_i \) periods are actually observed.
Methods and formulas are presented under the following headings:

xtreg, fe  
xtreg, be  
xtreg, re  
xtreg, mle  
xtreg, pa

xtreg, fe

xtreg, fe produces estimates by running OLS on

\[
(y_{it} - \bar{y}_i + \bar{y}) = \alpha + (x_{it} - \bar{x}_i + \bar{x})\beta + (\epsilon_{it} - \bar{\epsilon}_i + \bar{\epsilon}) + \bar{\epsilon}
\]

where \(\bar{y}_i = \sum_{t=1}^{T_i} y_{it} / T_i\), and similarly, \(\bar{y} = \sum_i \sum_t y_{it} / (nT_i)\). The conventional covariance matrix of the estimators is adjusted for the extra \(n - 1\) estimated means, so results are the same as using OLS on (1) to estimate \(\nu_i\) directly. Specifying vce(robust) or vce(cluster clustvar) causes the Huber/White/sandwich VCE estimator to be calculated for the coefficients estimated in this regression. See [P] _robust, particularly Introduction and Methods and formulas. Wooldridge (2020) and Arellano (2003) discuss this application of the Huber/White/sandwich VCE estimator. As discussed by Wooldridge (2020), Stock and Watson (2008), and Arellano (2003), specifying vce(robust) is equivalent to specifying vce(cluster panelvar), where panelvar is the variable that identifies the panels.

Clustering on the panel variable produces a consistent VCE estimator when the disturbances are not identically distributed over the panels or there is serial correlation in \(\epsilon_{it}\).

The cluster–robust VCE estimator requires that there are many clusters and the disturbances are uncorrelated across the clusters. The panel variable must be nested within the cluster variable because of the within-panel correlation induced by the within transform.

From the estimates \(\hat{\alpha}\) and \(\hat{\beta}\), estimates \(u_i\) of \(\nu_i\) are obtained as \(u_i = \bar{y}_i - \alpha - \bar{x}_i\hat{\beta}\). Reported from the calculated \(u_i\) are its standard deviation and its correlation with \(\bar{x}_i\hat{\beta}\). Reported as the standard deviation of \(e_{it}\) is the regression’s estimated root mean squared error, \(s\), which is adjusted (as previously stated) for the \(n - 1\) estimated means.

Reported as \(R^2\) within is the \(R^2\) from the mean-deviated regression.

Reported as \(R^2\) between is corr(\(\bar{x}_i\hat{\beta}, \bar{y}_i\))^2.

Reported as \(R^2\) overall is corr(\(x_{it}\hat{\beta}, y_{it}\))^2.

xtreg, be

xtreg, be fits the following model:

\[
\bar{y}_i = \alpha + \bar{x}_i\beta + \nu_i + \bar{\epsilon}_i
\]

Estimation is via OLS unless \(T_i\) is not constant and the wls option is specified. Otherwise, the estimation is performed via WLS. The estimates and conventional VCE are obtained from regress for both cases, but for WLS, [aweight=T_i] is specified.

Reported as \(R^2\) between is the \(R^2\) from the fitted regression.

Reported as \(R^2\) within is corr\{(\(x_{it} - \bar{x}_i\)\(\hat{\beta}, y_{it} - \bar{y}_i\))^2.

Reported as \(R^2\) overall is corr(\(x_{it}\hat{\beta}, y_{it}\))^2.
28 xtreg — Fixed-, between-, and random-effects and population-averaged linear models

xtreg, re

The key to the random-effects estimator is the GLS transform. Given estimates of the idiosyncratic component, \( \hat{\sigma}_e^2 \), and the individual component, \( \hat{\sigma}_u^2 \), the GLS transform of a variable \( z \) for the random-effects model is

\[
z_{it}^* = z_{it} - \hat{\theta}_i z_i
\]

where \( z_i = 1/T_i \sum_{t=1}^{T_i} z_{it} \) and

\[
\hat{\theta}_i = 1 - \sqrt{\frac{\hat{\sigma}_e^2}{T_i \hat{\sigma}_u^2 + \hat{\sigma}_e^2}}
\]

Given an estimate of \( \hat{\theta}_i \), one transforms the dependent and independent variables, and then the coefficient estimates and the conventional variance–covariance matrix come from an OLS regression of \( y_{it}^* \) on \( x_{it}^* \) and the transformed constant \( 1 - \hat{\theta}_i \). Specifying vce(robust) or vce(cluster clustvar) causes the Huber/White/sandwich VCE estimator to be calculated for the coefficients estimated in this regression. See \[p\] _robust; in particular, see Introduction and Methods and formulas. Wooldridge (2020) and Arellano (2003) discuss this application of the Huber/White/sandwich VCE estimator. As discussed by Wooldridge (2020), Stock and Watson (2008), and Arellano (2003), specifying vce(robust) is equivalent to specifying vce(cluster panelvar), where panelvar is the variable that identifies the panels.

Clustering on the panel variable produces a consistent VCE estimator when the disturbances are not identically distributed over the panels or there is serial correlation in \( \epsilon_{it} \).

The cluster–robust VCE estimator requires that there are many clusters and the disturbances are uncorrelated across the clusters. The panel variable must be nested within the cluster variable because of the within-panel correlation that is generally induced by the random-effects transform when there is heteroskedasticity or within-panel serial correlation in the idiosyncratic errors.

Stata has two implementations of the Swamy–Arora method for estimating the variance components. They produce the same results in balanced panels and share the same estimator of \( \sigma_e^2 \). However, the two methods differ in their estimator of \( \sigma_u^2 \) in unbalanced panels. We call the first \( \hat{\sigma}_{uT}^2 \) and the second \( \hat{\sigma}_{uSA}^2 \). Both estimators are consistent; however, \( \hat{\sigma}_{uSA}^2 \) has a more elaborate adjustment for small samples than \( \hat{\sigma}_{uT}^2 \). (See Baltagi [2013], Baltagi and Chang [1994], and Swamy and Arora [1972] for derivations of these methods.)

Both methods use the same function of within residuals to estimate the idiosyncratic error component \( \sigma_e \). Specifically,

\[
\hat{\sigma}_e^2 = \frac{\sum_{i=1}^{n} \sum_{t=1}^{T_i} e_{it}^2}{N - n - K + 1}
\]

where

\[
e_{it} = (y_{it} - \bar{y}_i + \bar{y}) - \hat{\alpha}_w - (x_{it} - \bar{x}_i + \bar{x}) \hat{\beta}_w
\]

and \( \hat{\alpha}_w \) and \( \hat{\beta}_w \) are the within estimates of the coefficients and \( N = \sum_{i=1}^{n} T_i \). After passing the within residuals through the within transform, only the idiosyncratic errors are left.
The default method for estimating $\sigma_u^2$ is

$$
\hat{\sigma}_{uT}^2 = \max \left\{ 0, \frac{SSR_b}{n - K} - \frac{\hat{\sigma}_e^2}{T} \right\}
$$

where

$$
SSR_b = \sum_{i=1}^{n} \left( \bar{y}_i - \hat{\alpha}_b - \bar{x}_i \hat{\beta}_b \right)^2
$$

$\hat{\alpha}_b$ and $\hat{\beta}_b$ are coefficient estimates from the between regression and $T$ is the harmonic mean of $T_i$:

$$
T = \frac{n}{\sum_{i=1}^{n} \frac{1}{T_i}}
$$

This estimator is consistent for $\sigma_u^2$ and is computationally less expensive than the second method. The sum of squared residuals from the between model estimate a function of both the idiosyncratic component and the individual component. Using our estimator of $\sigma_e^2$, we can remove the idiosyncratic component, leaving only the desired individual component.

The second method is the Swamy–Arora method for unbalanced panels derived by Baltagi and Chang (1994), which has a more precise small-sample adjustment. Using this method,

$$
\hat{\sigma}_{uSA}^2 = \max \left\{ 0, \frac{SSR_b^* - (n - K)\hat{\sigma}_e^2}{N - c_{tr}} \right\}
$$

where

$$
SSR_b^* = \sum_{i=1}^{n} T_i \left( \bar{y}_i - \hat{\alpha}_b - \bar{x}_i \hat{\beta}_b \right)^2
$$

$$
c_{tr} = \text{trace} \left\{ (X'PX)^{-1}X'ZZ'X \right\}
$$

$$
P = \text{diag} \left\{ \left( \frac{1}{T_i} \right) \nu_{T_i}, \nu_{T_i}' \right\}
$$

$$
Z = \text{diag} [\nu_{T_i}]
$$

$X$ is the $N \times K$ matrix of covariates, including the constant, and $\nu_{T_i}$ is a $T_i \times 1$ vector of ones.

The estimated coefficients $(\hat{\alpha}, \hat{\beta})$ and their estimated covariance matrix $\hat{V}$ are reported together with the previously calculated quantities $\hat{\sigma}_e$ and $\hat{\sigma}_u$. The standard deviation of $\nu_i + e_{it}$ is calculated as $\sqrt{\hat{\sigma}_e^2 + \hat{\sigma}_u^2}$.

Reported as $R^2$ between is $\text{corr}(\bar{x}_i \hat{\beta}, \bar{y}_i)^2$.

Reported as $R^2$ within is $\text{corr}\left\{ (x_{it} - \bar{x}_i) \hat{\beta}, y_{it} - \bar{y}_i \right\}^2$.

Reported as $R^2$ overall is $\text{corr}(x_{it} \hat{\beta}, y_{it})^2$. 
xtreg, mle

The log likelihood for the $i$th unit is

$$
l_i = -\frac{1}{2} \left( \frac{1}{\sigma_e^2} \left[ \sum_{t=1}^{T_i} (y_{it} - x_{it}\beta)^2 - \frac{\sigma_u^2}{T_i\sigma_u^2 + \sigma_e^2} \left\{ \sum_{t=1}^{T_i} (y_{it} - x_{it}\beta) \right\}^2 \right] + \ln \left( T_i \sigma_u^2 + \sigma_e^2 + 1 \right) + T_i \ln(2\pi\sigma_e^2) \right)
$$

The `mle` and `re` options yield essentially the same results, except when total $N = \sum_i T_i$ is small (200 or less) and the data are unbalanced.

Similarly to `xtreg, fe` and `xtreg, re`, specifying `vce(robust)` or `vce(cluster clustvar)` causes the Huber/White/sandwich VCE estimator to be calculated for the estimated parameters in this regression.

Specifying `vce(robust)` is equivalent to specifying `vce(cluster panelvar)`, where `panelvar` is the variable that identifies the panels.

Clustering on the panel variable produces a consistent VCE estimator when the disturbances are not identically distributed over the panels or there is serial correlation in it.

The cluster–robust VCE estimator requires that there are many clusters and the disturbances are uncorrelated across the clusters. The panel variable must be nested within the cluster variable because of the within-panel correlation that is generally induced by the random-effects transform when there is heteroskedasticity or within-panel serial correlation in the idiosyncratic errors.

xtreg, pa

See [XT] `xtgee` for details on the methods and formulas used to calculate the population-averaged model using a generalized estimating equations approach.

Acknowledgments

We thank Richard Goldstein, who wrote the first draft of the routine that fits random-effects regressions, Badi Baltagi of the Department of Economics at Syracuse University, and Manuelita Ureta of the Department of Economics at Texas A&M University, who assisted us in working our way through the literature.

References


Also see

[XT] **xtreg postestimation** — Postestimation tools for xtreg

[XT] **xtregress** — Extended random-effects linear regression

[XT] **xtgee** — Fit population-averaged panel-data models by using GEE

[XT] **xtgls** — Fit panel-data models by using GLS

[XT] **xtheckman** — Random-effects regression with sample selection

[XT] **xtivreg** — Instrumental variables and two-stage least squares for panel-data models

[XT] **xtregar** — Fixed- and random-effects linear models with an AR(1) disturbance

[XT] **xtset** — Declare data to be panel data

[ME] **mixed** — Multilevel mixed-effects linear regression

[MI] **Estimation** — Estimation commands for use with mi estimate

[R] **areg** — Linear regression with a large dummy-variable set

[R] **regress** — Linear regression

[SP] **spxtregress** — Spatial autoregressive models for panel data

[TS] **forecast** — Econometric model forecasting

[TS] **prais** — Prais–Winsten and Cochrane–Orcutt regression

[U] **20 Estimation and postestimation commands**