### xtdpd — Linear dynamic panel-data estimation

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# Description

xtdpd fits a linear dynamic panel-data model where the unobserved panel-level effects are correlated with the lags of the dependent variable. The command can fit Arellano–Bond and Arellano–Bover/Blundell–Bond models like those fit by xtabond and xtdpdsys. However, it also allows models with low-order moving-average correlation in the idiosyncratic errors or predetermined variables with a more complicated structure than allowed for xtabond or xtdpdsys.

# **Quick start**

Arellano–Bond model of y on L.y and x with the first difference of x as an instrument for the difference equation using xtset data

xtdpd y L.y x, div(x) dgmmiv(y)

Add the first difference of the lag of x as an instrument for the level equation

xtdpd y L.y x, div(x) dgmmiv(y) lgmmiv(x)

Use lags 3 to 5 of x as instruments for the difference equation

xtdpd y L.y x, div(x) dgmmiv(y, lagrange(35))

## Menu

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# Syntax

xtdpd depvar [indepvars] [if] [in], dgmmiv(varlist [...]) [options]

options	Description
Model	
* dgmmiv(varlist[])	GMM-type instruments for the difference equation; can be specified more than once
lgmmiv(varlist[])	GMM-type instruments for the level equation; can be specified more than once
iv( <i>varlist</i> [])	standard instruments for the difference and level equations; can be specified more than once
div( <i>varlist</i> [])	standard instruments for the difference equation only; can be specified more than once
liv(varlist)	standard instruments for the level equation only; can be specified more than once
<u>nocons</u> tant	suppress constant term
<u>two</u> step	compute the two-step estimator instead of the one-step estimator
<u>h</u> ascons	check for collinearity only among levels of independent variables; by default checks occur among levels and differences
<u>fod</u> eviation	use forward-orthogonal deviations instead of first differences
SE/Robust	
vce( <i>vcetype</i> )	vcetype may be gmm or robust
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
<u>ar</u> tests(#)	use # as maximum order for AR tests; default is artests(2)
display_options	control spacing and line width
<u>coefl</u> egend	display legend instead of statistics
*1 · () · · 1	

\*dgmmiv() is required.

A panel variable and a time variable must be specified; use xtset; see [XT] xtset. *depvar*, *indepvars*, and all *varlists* may contain time-series operators; see [U] 11.4.4 Time-series varlists. by, collect, statsby, and xi are allowed; see [U] 11.1.10 Prefix commands.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

## Options

Model

dgmmiv(varlist [, lagrange(flag [llag])]) specifies GMM-type instruments for the difference equation. Levels of the variables are used to form GMM-type instruments for the difference equation. All possible lags are used, unless lagrange(flag llag) restricts the lags to begin with flag and end with llag. You may specify as many sets of GMM-type instruments for the difference equation as you need within the standard Stata limits on matrix size. Each set may have its own flag and llag. dgmmiv() is required.

- lgmmiv(varlist [, lag(#)]) specifies GMM-type instruments for the level equation. Differences of the variables are used to form GMM-type instruments for the level equation. The first lag of the differences is used unless lag(#) is specified, indicating that #th lag of the differences be used. You may specify as many sets of GMM-type instruments for the level equation as you need within the standard Stata limits on matrix size. Each set may have its own lag.
- iv (varlist [, nodifference]) specifies standard instruments for both the differenced and level equations. Differences of the variables are used as instruments for the differenced equations, unless nodifference is specified, which requests that levels be used. Levels of the variables are used as instruments for the level equations. You may specify as many sets of standard instruments for both the differenced and level equations as you need within the standard Stata limits on matrix size.
- div(varlist [, nodifference]) specifies additional standard instruments for the difference equation. Specified variables may not be included in iv() or in liv(). Differences of the variables are used, unless nodifference is specified, which requests that levels of the variables be used as instruments for the difference equation. You may specify as many additional sets of standard instruments for the difference equation as you need within the standard Stata limits on matrix size.
- liv(varlist) specifies additional standard instruments for the level equation. Specified variables may not be included in iv() or in div(). Levels of the variables are used as instruments for the level equation. You may specify as many additional sets of standard instruments for the level equation as you need within the standard Stata limits on matrix size.

noconstant; see [R] Estimation options.

twostep specifies that the two-step estimator be calculated.

- hascons specifies that xtdpd check for collinearity only among levels of independent variables; by default checks occur among levels and differences. This option should typically be specified when time-invariant covariates or time-indicator variables are included in the level equation.
- fodeviation specifies that forward-orthogonal deviations be used instead of first differences. fodeviation is not allowed when there are gaps in the data or when lgmmiv() is specified.

SE/Robust

vce(*vcetype*) specifies the type of standard error reported, which includes types that are derived from asymptotic theory and that are robust to some kinds of misspecification; see *Methods and formulas*.

vce(gmm), the default, uses the conventionally derived variance estimator for generalized method of moments estimation.

vce(robust) uses the robust estimator. For the one-step estimator, this is the Arellano-Bond robust VCE estimator. For the two-step estimator, this is the Windmeijer (2005) WC-robust estimator.

Reporting

level(#); see [R] Estimation options.

artests(#) specifies the maximum order of the autocorrelation test to be calculated. The tests are reported by estat abond; see [XT] **xtdpd postestimation**. Specifying the order of the highest test at estimation time is more efficient than specifying it to estat abond, because estat abond must refit the model to obtain the test statistics. The maximum order must be less than or equal to the number of periods in the longest panel. The default is artests(2).

*display\_options*: vsquish and nolstretch; see [R] Estimation options.

The following option is available with xtdpd but is not shown in the dialog box:

coeflegend; see [R] Estimation options.

## **Remarks and examples**

If you have not read [XT] xtabond and [XT] xtdpdsys, you should do so before continuing.

Linear dynamic panel-data models include p lags of the dependent variable as covariates and contain unobserved panel-level effects, fixed or random. By construction, the unobserved panel-level effects are correlated with the lagged dependent variables, making standard estimators inconsistent. xtdpd fits a dynamic panel-data model by using the Arellano–Bond (1991) or the Arellano–Bover/Blundell–Bond (1995, 1998) estimator.

Consider the dynamic panel-data model

$$y_{it} = \sum_{j=1}^{p} \alpha_j y_{i,t-j} + \mathbf{x}_{it} \boldsymbol{\beta}_1 + \mathbf{w}_{it} \boldsymbol{\beta}_2 + \nu_i + \epsilon_{it} \qquad i = \{1, \dots, N\}; \ t = \{1, \dots, T_i\}$$
(1)

where

the  $\alpha_1, \ldots, \alpha_p$  are p parameters to be estimated,

 $\mathbf{x}_{it}$  is a 1 imes  $k_1$  vector of strictly exogenous covariates,

 $\boldsymbol{\beta}_{_1}$  is a  $k_1 \times 1$  vector of parameters to be estimated,

 $\mathbf{w}_{it}$  is a  $1 imes k_2$  vector of predetermined covariates,

 $\pmb{\beta}_{\scriptscriptstyle 2}$  is a  $k_2\times 1$  vector of parameters to be estimated,

 $\nu_i$  are the panel-level effects (which may be correlated with  $x_{it}$  or  $w_{it}$ ), and

and  $\epsilon_{it}$  are i.i.d. or come from a low-order moving-average process, with variance  $\sigma_{\epsilon}^2.$ 

Building on the work of Anderson and Hsiao (1981, 1982) and Holtz-Eakin, Newey, and Rosen (1988), Arellano and Bond (1991) derived one-step and two-step GMM estimators using moment conditions in which lagged levels of the dependent and predetermined variables were instruments for the difference equation. Blundell and Bond (1998) show that the lagged-level instruments in the Arellano–Bond estimator become weak as the autoregressive process becomes too persistent or the ratio of the variance of the panel-level effect  $\nu_i$  to the variance of the idiosyncratic error  $\epsilon_{it}$  becomes too large. Building on the work of Arellano and Bover (1995), Blundell and Bond (1998) proposed a system estimator that uses moment conditions in which lagged levels as instruments for the level equation in addition to the moment conditions of lagged levels as instruments for the difference equation. The additional moment conditions are valid only if the initial condition  $E[\nu_i \Delta y_{i2}] = 0$  holds for all *i*; see Blundell and Bond (1998) and Blundell, Bond, and Windmeijer (2000).

xtdpd fits dynamic panel-data models by using the Arellano-Bond or the Arellano-Bover/Blundell-Bond system estimator. The parameters of many standard models can be more easily estimated using the Arellano-Bond estimator implemented in xtabond or using the Arellano-Bover/Blundell-Bond system estimator implemented in xtdpdsys; see [XT] **xtabond** and [XT] **xtdpdsys**. xtdpd can fit more complex models at the cost of a more complicated syntax. That the idiosyncratic errors follow a low-order MA process and that the predetermined variables have a more complicated structure than accommodated by xtabond and xtdpdsys are two common reasons for using xtdpd instead of xtabond or xtdpdsys. The standard GMM robust two-step estimator of the VCE is known to be seriously biased. Windmeijer (2005) derived a bias-corrected robust estimator for two-step VCEs from GMM estimators known as the WC-robust estimator, which is implemented in xtdpd.

The Arellano-Bond test of autocorrelation of order m and the Sargan test of overidentifying restrictions derived by Arellano and Bond (1991) are computed by xtdpd but reported by estat abond and estat sargan, respectively; see [XT] **xtdpd postestimation**.

Because xtdpd extends xtabond and xtdpdsys, [XT] **xtabond** and [XT] **xtdpdsys** provide useful background.

### Example 1: An Arellano–Bond estimator

Arellano and Bond (1991) apply their new estimators and test statistics to a model of dynamic labor demand that had previously been considered by Layard and Nickell (1986), using data from an unbalanced panel of firms from the United Kingdom. All variables are indexed over the firm *i* and time *t*. In this dataset,  $n_{it}$  is the log of employment in firm *i* inside the United Kingdom at time *t*,  $w_{it}$  is the natural log of the real product wage,  $k_{it}$  is the natural log of the gross capital stock, and  $ys_{it}$  is the natural log of industry output. The model also includes time dummies yr1980, yr1981, yr1982, yr1983, and yr1984. To gain some insight into the syntax for xtdpd, we reproduce the first example from [XT] **xtabond** using xtdpd:

=

=

Wald chi2(16)

Prob > chi2

611

140

Δ

6

1757.07

0.0000

. use https://www.stata-press.com/data/r19/abdata . xtdpd L(0/2).n L(0/1).w L(0/2).(k ys) yr1980-yr1984 year, noconstant > div(L(0/1).w L(0/2).(k ys) yr1980-yr1984 year) dgmmiv(n) Dynamic panel-data estimation Number of obs = Number of groups = Group variable: id Time variable: year Obs per group: min = 4.364286 avg = max =

41

Number of instruments =

n	Coefficient	Std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.6862261	.1486163	4.62	0.000	.3949435	.9775088
L2.	0853582	.0444365	-1.92	0.055	1724523	.0017358
w						
	6078208	.0657694	-9.24	0.000	7367265	4789151
L1.	. 3926237	.1092374	3.59	0.000	.1785222	.6067251
k						
	.3568456	.0370314	9.64	0.000	.2842653	.4294259
L1.	0580012	.0583051	-0.99	0.320	172277	.0562747
L2.	0199475	.0416274	-0.48	0.632	1015357	.0616408
ys						
	.6085073	.1345412	4.52	0.000	.3448115	.8722031
L1.	7111651	.1844599	-3.86	0.000	-1.0727	3496304
L2.	.1057969	.1428568	0.74	0.459	1741974	.3857912
yr1980	.0029062	.0212705	0.14	0.891	0387832	.0445957
yr1981	0404378	.0354707	-1.14	0.254	1099591	.0290836
yr1982	0652767	.048209	-1.35	0.176	1597646	.0292111
yr1983	0690928	.0627354	-1.10	0.271	1920521	.0538664
yr1984	0650302	.0781322	-0.83	0.405	2181665	.0881061
year	.0095545	.0142073	0.67	0.501	0182912	.0374002

Instruments for differenced equation

```
GMM-type: L(2/.).n
```

Standard: D.w LD.w D.k LD.k L2D.k D.ys LD.ys L2D.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

Unlike most instrumental-variables estimation commands, the independent variables in the varlist are not automatically used as instruments. In this example, all the independent variables are strictly exogenous, so we include them in div(), a list of variables whose first differences will be instruments for the difference equation. We include the dependent variable in dgmmiv(), a list of variables whose lagged levels will be used to create GMM-type instruments for the difference equation. (GMM-type instruments are discussed in a technical note below.)

The footer in the output reports the instruments used. The first line indicates that xtdpd used lags from 2 on back to create the GMM-type instruments described in Arellano and Bond (1991) and Holtz-Eakin, Newey, and Rosen (1988). The second line says that the first difference of all the variables included in the div() varlist were used as standard instruments for the difference equation.

### Technical note

GMM-type instruments are built from lags of one variable. Ignoring the strictly exogenous variables for simplicity, our model is

$$n_{it} = \alpha_1 n_{it-1} + \alpha_2 n_{it-2} + \nu_i + \epsilon_{it} \tag{2}$$

After differencing we have

$$\Delta n_{it} = \Delta \alpha_1 n_{it-1} + \Delta \alpha_2 n_{it-2} + \Delta \epsilon_{it} \tag{3}$$

Equation (3) implies that we need instruments that are not correlated with either  $\epsilon_{it}$  or  $\epsilon_{it-1}$ . Equation (2) shows that L2.n is the first lag of n that is not correlated with  $\epsilon_{it}$  or  $\epsilon_{it-1}$ , so it is the first lag of n that can be used to instrument the difference equation.

Consider the following data from one of the complete panels in the previous example:

```
. list id year n L2.n dl2.n if id==140
```

				L2.	L2D.
	id	year	n	n	n
1023.	140	1976	.4324315		
1024.	140	1977	.3694925		
1025.	140	1978	.3541718	.4324315	
1026.	140	1979	.3632532	.3694925	0629391
1027.	140	1980	.3371863	.3541718	0153207
1028.	140	1981	.285179	.3632532	.0090815
1029.	140	1982	.1756326	.3371863	026067
1030.	140	1983	.1275133	.285179	0520073
1031.	140	1984	.0889263	.1756326	1095464

The missing values in L2D.n show that we lose 3 observations because of lags and the difference that removes the panel-level effects. The first nonmissing observation occurs in 1979 and observations on n from 1976 and 1977 are available to instrument the 1979 difference equation. The table below gives the observations available to instrument the differenced equation for the data above.

Year of	Years of	Number of
difference errors	instruments	instruments
1979	1976-1977	2
1980	1976-1978	3
1981	1976-1979	4
1982	1976-1980	5
1983	1976-1981	6
1984	1976-1982	7

The table shows that there are a total of 27 GMM-type instruments.

The output in the example above informs us that there were a total of 41 instruments applied to the difference equation. Because there are 14 standard instruments, there must have been 27 GMM-type instruments, which matches our above calculation.

#### Example 2: An Arellano–Bond estimator with predetermined variables

Sometimes we cannot assume strict exogeneity. Recall that a variable  $x_{it}$  is said to be strictly exogenous if  $E[x_{it}\epsilon_{is}] = 0$  for all t and s. If  $E[x_{it}\epsilon_{is}] \neq 0$  for s < t but  $E[x_{it}\epsilon_{is}] = 0$  for all  $s \ge t$ , the variable is said to be predetermined. Intuitively, if the error term at time t has some feedback on the subsequent realizations of  $x_{it}$ ,  $x_{it}$  is a predetermined variable. In the output below, we use xtdpd to reproduce example 6 in [XT] **xtabond**.

```
. xtdpd L(0/2).n L(0/1).(w ys) L(0/2).k yr1980-yr1984 year,
> div(L(0/1).(ys) yr1980-yr1984 year) dgmmiv(n) dgmmiv(L.w L2.k, lag(1 .))
> twostep noconstant vce(robust)
Dynamic panel-data estimation
                                                Number of obs
                                                                            611
                                                Number of groups =
                                                                            140
Group variable: id
Time variable: year
                                                Obs per group:
                                                               min =
                                                                              4
                                                                       4.364286
                                                               avg =
                                                               max =
                                                                              6
Number of instruments =
                            83
                                                Wald chi2(15)
                                                                  =
                                                                         958.30
                                                Prob > chi2
                                                                   =
                                                                         0.0000
Two-step results
```

(Std. err. adjusted for clustering on id)

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.8580958	.1265515	6.78	0.000	.6100594	1.106132
L2.	081207	.0760703	-1.07	0.286	2303022	.0678881
			1.01	0.200	12000022	
w						
	6910855	.1387684	-4.98	0.000	9630666	4191044
L1.	.5961712	.1497338	3.98	0.000	.3026982	.8896441
ys						
	.6936392	.1728623	4.01	0.000	.3548354	1.032443
L1.	8773678	.2183085	-4.02	0.000	-1.305245	449491
k						
	.4140654	.1382788	2.99	0.003	.1430439	.6850868
L1.	1537048	.1220244	-1.26	0.208	3928681	.0854586
L2.	1025833	.0710886	-1.44	0.149	2419143	.0367477
yr1980	0072451	.017163	-0.42	0.673	0408839	.0263938
yr1981	0609608	.030207	-2.02	0.044	1201655	0017561
yr1982	1130369	.0454826	-2.49	0.013	2021812	0238926
yr1983	1335249	.0600213	-2.22	0.026	2511645	0158853
yr1984	1623177	.0725434	-2.24	0.025	3045001	0201352
year	.0264501	.0119329	2.22	0.027	.003062	.0498381
	I					
Instruments fo	or differenced	equation				

Instruments for differenced equation GMM-type: L(2/.).n L(1/.).L.w L(1/.).L2.k Standard: D.ys LD.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

The footer informs us that we are now including GMM-type instruments from the first lag of L.w on back and from the first lag of L2.k on back.

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#### Example 3: A weaker definition of predetermined variables

As discussed in [XT] **xtabond** and [XT] **xtdpdsys**, xtabond and xtdpdsys both use a strict definition of predetermined variables with lags. In the strict definition, the most recent lag of the variable in pre() is considered predetermined. (Here specifying pre(w, lag(1, .)) to xtabond means that L.w is a predetermined variable and pre(k, lag(2, .)) means that L2.k is a predetermined variable.) In a weaker definition, the current observation is considered predetermined, but subsequent lags are included in the model. Here w and k would be predetermined instead of L.w and L2.w. The output below implements this weaker definition for the previous example.

```
. xtdpd L(0/2).n L(0/1).(w ys) L(0/2).k yr1980-yr1984 year,
> div(L(0/1).(ys) yr1980-yr1984 year) dgmmiv(n) dgmmiv(w k, lag(1 .))
> twostep noconstant vce(robust)
Dynamic panel-data estimation
                                                Number of obs
                                                                  =
                                                                           611
                                                Number of groups =
Group variable: id
                                                                           140
Time variable: year
                                                Obs per group:
                                                              min =
                                                                      4.364286
                                                              avg =
                                                              max =
Number of instruments =
                           101
                                                Wald chi2(15)
                                                                        879.53
                                                                 =
                                                Prob > chi2
                                                                        0.0000
                                                                 =
```

```
Two-step results
```

(Std. err. adjusted for clustering on id)

n	Coefficient	WC-robust std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.6343155	.1221058	5.19	0.000	.3949925	.8736384
L2.	0871247	.0704816	-1.24	0.216	2252661	.0510168
			1.21	0.210	.2202001	
w						
	720063	.1133359	-6.35	0.000	9421973	4979287
L1.	.238069	.1223186	1.95	0.052	0016712	.4778091
ys						
	.5999718	.1653036	3.63	0.000	.2759827	.923961
L1.	5674808	.1656411	-3.43	0.001	8921314	2428303
k						
	.3931997	.0986673	3.99	0.000	.1998153	.5865842
L1.	0019641	.0772814	-0.03	0.980	1534329	.1495047
L2.	0231165	.0487317	-0.47	0.635	1186288	.0723958
yr1980	006209	.0162138	-0.38	0.702	0379875	.0255694
yr1981	0398491	.0313794	-1.27	0.204	1013516	.0216535
yr1982	0525715	.0397346	-1.32	0.186	1304498	.0253068
yr1983	0451175	.051418	-0.88	0.380	145895	.05566
yr1984	0437772	.0614391	-0.71	0.476	1641955	.0766412
year	.0173374	.0108665	1.60	0.111	0039605	.0386352

Instruments for differenced equation

GMM-type: L(2/.).n L(1/.).w L(1/.).k

Standard: D.ys LD.ys D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year

As expected, the output shows that the additional 18 instruments available under the weaker definition can affect the magnitudes of the estimates. Applying the stricter definition when the true model was generated by the weaker definition yielded consistent but inefficient results; there were some additional moment conditions that could have been included but were not. In contrast, applying the weaker definition when the true model was generated by the stricter definition yields inconsistent estimates.

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### Example 4: A system estimator of a dynamic panel-data model

Here we use xtdpd to reproduce example 2 from [XT] **xtdpdsys** in which we used the system estimator to fit a model with predetermined variables.

<pre>. xtdpd L(0/1).n L(0/2).(w k) yr1980-yr1984 year, div(yr1980-yr1984 year) &gt; dgmmiv(n) dgmmiv(L2.(w k), lag(1 .)) lgmmiv(n L1.(w k)) vce(robust) hascons</pre>						
Dynamic panel-	Dynamic panel-data estimation			Number	of obs =	751
Group variable				Number	of groups =	140
Time variable:	year					
				Obs per	• •	F
					min =	5
					avg = max =	5.364286 7
						•
Number of inst	ruments =	95		Wald ch		7562.80
0	h			Prob >	chi2 =	0.0000
One-step resul	ts	(	(Std. err.	adjuste	d for cluster	ring on id)
		Robust				
n	Coefficient	std. err.	Z	P> z	[95% conf.	interval]
n						
L1.	.913278	.0460602	19.83	0.000	.8230017	1.003554
	.010210	.0100002	10.00	0.000	.0200011	1.000001
w						
	728159	.1019044	-7.15	0.000	927888	5284301
L1.	.5602737	.1939617	2.89	0.004	.1801156	.9404317
L2.	0523028	.1487653	-0.35	0.725	3438774	.2392718
k						
	.4820097	.0760787	6.34	0.000	.3328983	.6311212
L1.	2846944	.0831902	-3.42	0.001	4477442	1216446
L2.	1394181	.0405709	-3.44	0.001	2189356	0599006
yr1980	0325146	.0216371	-1.50	0.133	0749226	.0098935
yr1981	0726116	.0346482	-2.10	0.036	1405207	0047024
yr1982	0477038	.0451914	-1.06	0.291	1362772	.0408696
yr1983	0396264	.0558734	-0.71	0.478	1491362	.0698835
yr1984	0810383	.0736648	-1.10	0.271	2254186	.063342
year	.0192741	.0145326	1.33	0.185	0092092	.0477574
year _cons	.0192741 -37.34972	.0145326 28.77747	1.33 -1.30	0.185 0.194	0092092 -93.75252	.0477574 19.05308

GMM-type: L(2/.).n L(1/.).L2.w L(1/.).L2.k Standard: D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year Instruments for level equation GMM-type: LD.n L2D.w L2D.k Standard: \_cons The first lags of the variables included in lgmmiv() are used to create GMM-type instruments for the level equation. Only the first lags of the variables in lgmmiv() are used because the moment conditions using higher lags are redundant; see Blundell and Bond (1998) and Blundell, Bond, and Windmeijer (2000).

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### Example 5: Allowing for MA(1) errors

All the previous examples have used moment conditions that are valid only if the idiosyncratic errors are i.i.d. This example shows how to use xtdpd to estimate the parameters of a model with first-order moving-average [MA(1)] errors using the Arellano–Bond estimator, the Arellano–Bover/Blundell–Bond system estimator, or any other consistent GMM estimator you want to specify. For simplicity, we assume that the independent variables are strictly exogenous. Also, to highlight the fact that we can specify the instrument list flexibly, we only include the levels and first lags of the exogenous variables in the instrument list. An Arellano–Bond estimator, for instance, would have included levels and first and second lags of the exogenous variables.

We begin by noting that the Sargan test rejects the null hypothesis that the overidentifying restrictions are valid in the model with i.i.d. errors.

Assuming that the idiosyncratic errors are MA(1) implies that only lags three or higher are valid instruments for the difference equation. (See the technical note below.)

. xtdpd L(0/1).n L(0/2).(w k) yr1980-yr1984 year, > div(L(0/1).(w k) yr1980-yr1984 year) dgmmiv(n, lag(3 .)) hascons						
Dynamic panel-data estimation Group variable: id Time variable: year			Number		751 140	
	<i>J</i>			Obs per	group:	
				F	min =	5
					avg =	5.364286
					max =	7
Number of inst	trumonte =	32		Wald ch	i2(13) =	1195.04
Number of The		52		Prob >		0.0000
One-step resul	lts			1100 /	CIII2	
n	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
n L1.	.8696303	.2014473	4.32	0.000	.4748008	1.26446
ш.	.0090303	.2014473	4.52	0.000	.4740000	1.20440
w						
	5802971	.0762659	-7.61	0.000	7297756	4308187
L1.	.2918658	.1543883	1.89	0.059	0107296	.5944613
L2.	5903459	.2995123	-1.97	0.049	-1.177379	0033126
k						
	.3428139	.0447916	7.65	0.000	.2550239	.4306039
L1.	1383918	.0825823	-1.68	0.094	3002502	.0234665
L2.	0260956	.1535855	-0.17	0.865	3271177	.2749265
yr1980	0036873	.0301587	-0.12	0.903	0627973	.0554226
yr1981	.00218	.0592014	0.04	0.971	1138526	.1182125
yr1982	.0782939	.0897622	0.87	0.383	0976367	.2542246
yr1983	.1734231	.1308914	1.32	0.185	0831193	.4299655
yr1984	.2400685	.1734456	1.38	0.166	0998787	.5800157
year	0354681	.0309963	-1.14	0.253	0962198	.0252836
_cons	73.13706	62.61443	1.17	0.243	-49.58496	195.8591
Instruments for differenced equation GMM-type: L(3/.).n Standard: D.w LD.w D.k LD.k D.yr1980 D.yr1981 D.yr1982 D.yr1983						

```
GMM-type: L(3/.).n
Standard: D.w LD.w D.k LD.k D.yr1980 D.yr1981 D.yr1982 D.yr1983
D.yr1984 D.year
Instruments for level equation
Standard: _cons
```

The results from estat sargan no longer reject the null hypothesis that the overidentifying restrictions are valid.

Moving on to the system estimator, we note that the Sargan test rejects the null hypothesis after fitting the model with i.i.d. errors.

Now we fit the model using the additional moment conditions constructed from the second lag of n as an instrument for the level equation.

. xtdpd L(0/1) > div(L(0/1).( > hascons					.)) lgmmiv(n,	lag(2))
Dynamic panel-data estimation Group variable: id Time variable: year			Number Number	of obs = of groups =	751 140	
	·			Obs per	group:	
					min =	5
					avg = max =	5.364286 7
Number of inst	ruments =	38		Wald ch Prob >		3680.01 0.0000
One-step resul	lts					
n	Coefficient	Std. err.	z	P> z	[95% conf.	interval]
n						
L1.	.9603675	.095608	10.04	0.000	.7729794	1.147756
w						
	5433987	.068835	-7.89	0.000	6783128	4084845
L1.	.4356183	.0881727	4.94	0.000	.262803	.6084336
L2.	2785721	.1115061	-2.50	0.012	4971201	0600241
k						
	.3139331	.0419054	7.49	0.000	.2317999	.3960662
L1.	160103	.0546915	-2.93	0.003	2672963	0529096
L2.	1295766	.0507752	-2.55	0.011	2290943	030059
yr1980	0200704	.0248954	-0.81	0.420	0688644	.0287236
yr1981	0425838	.0422155	-1.01	0.313	1253246	.040157
yr1982	.0048723	.0600938	0.08	0.935	1129093	.122654
yr1983	.0458978	.0785687	0.58	0.559	1080941	.1998897
yr1984	.0633219	.1026188	0.62	0.537	1378074	.2644511
year	0075599	.019059	-0.40	0.692	0449148	.029795
_cons	16.20856	38.00619	0.43	0.670	-58.28221	90.69932
<pre>Instruments for differenced equation GMM-type: L(3/.).n Standard: D.w LD.w D.k LD.k D.yr1980 D.yr1981 D.yr1982 D.yr1983 D.yr1984 D.year Instruments for level equation GMM-type: L2D.n Standard: _cons</pre>						

The estimate of the coefficient on L.n is now 0.96. Blundell, Bond, and Windmeijer (2000, 63–65) show that the moment conditions in the system estimator remain informative as the true coefficient on L.n approaches unity. Holtz-Eakin, Newey, and Rosen (1988) show that because the large-sample distribution of the estimator is derived for fixed number of periods and a growing number of individuals there is no "unit-root" problem.

The results from estat sargan no longer reject the null hypothesis that the overidentifying restrictions are valid.

Technical note

To find the valid moment conditions for the model with MA(1) errors, we begin by writing the model

$$n_{it} = \alpha n_{it-1} + \beta x_{it} + \nu_i + \epsilon_{it} + \gamma \epsilon_{it-1}$$

where the  $\epsilon_{it}$  are assumed to be i.i.d.

Because the composite error,  $\epsilon_{it} + \gamma \epsilon_{it-1}$ , is MA(1), only lags two or higher are valid instruments for the level equation, assuming the initial condition that  $E[\nu_i \Delta n_{i2}] = 0$ . The key to this point is that lagging the above equation two periods shows that  $\epsilon_{it-2}$  and  $\epsilon_{it-3}$  appear in the equation for  $n_{it-2}$ . Because the  $\epsilon_{it}$  are i.i.d.,  $n_{it-2}$  is a valid instrument for the level equation with errors  $\nu_i + \epsilon_{it} + \gamma \epsilon_{it-1}$ . ( $n_{it-2}$  will be correlated with  $n_{it-1}$  but uncorrelated with the errors  $\nu_i + \epsilon_{it} + \gamma \epsilon_{it-1}$ .) An analogous argument works for higher lags.

First-differencing the above equation yields

$$\Delta n_{it} = \alpha \Delta n_{it-1} + \beta \Delta x_{it} + \Delta \epsilon_{it} + \gamma \Delta \epsilon_{it-1}$$

Because  $\epsilon_{it-2}$  is the farthest lag of  $\epsilon_{it}$  that appears in the difference equation, lags three or higher are valid instruments for the differenced composite errors. (Lagging the level equation three periods shows that only  $\epsilon_{it-3}$  and  $\epsilon_{it-4}$  appear in the equation for  $n_{it-3}$ , which implies that  $n_{it-3}$  is a valid instrument for the current difference equation. An analogous argument works for higher lags.)

1

# **Stored results**

xtdpd stores the following in e():

S	cal	ars

	e(N)	number of observations
	e(N_g)	number of groups
	e(df_m)	model degrees of freedom
	e(g_min)	smallest group size
	e(g_avg)	average group size
	e(g_max)	largest group size
	e(t_min)	minimum time in sample
	e(t_max)	maximum time in sample
	e(chi2)	$\chi^2$
	e(arm#)	test for autocorrelation of order #
	e(artests)	number of AR tests computed
	e(sig2)	estimate of $\sigma_{\epsilon}^2$
	e(rss)	sum of squared differenced residuals
	e(sargan)	Sargan test statistic
	e(rank)	rank of e(V)
	e(zrank)	rank of instrument matrix
Mac	ros	
	e(cmd)	xtdpd
	e(cmdline)	command as typed
	e(depvar)	name of dependent variable
	e(twostep)	twostep, if specified
	e(ivar)	variable denoting groups
	e(tvar)	variable denoting time within groups
	e(vce)	vcetype specified in vce()
	e(vcetype)	title used to label Std. err.
	e(system)	system, if system estimator
	e(transform)	specified transform
	e(datasignature)	checksum from datasignature
	e(datasignaturevars)	variables used in calculation of checksum
	e(properties)	b V
	e(estat_cmd)	program used to implement estat
	e(predict)	program used to implement predict
	e(marginsok)	predictions allowed by margins
Mat	rices	
	e(b)	coefficient vector
	e(V)	variance-covariance matrix of the estimators
Fun	ctions	
	e(sample)	marks estimation sample
	*	1

In addition to the above, the following is stored in r():

Matrices

r(table)

matrix containing the coefficients with their standard errors, test statistics, p-values, and confidence intervals

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

# Methods and formulas

Consider dynamic panel-data models of the form

$$y_{it} = \sum_{j=1}^{p} \alpha_{j} y_{i,t-j} + \mathbf{x}_{it} \boldsymbol{\beta}_{1} + \mathbf{w}_{it} \boldsymbol{\beta}_{2} + \nu_{i} + \epsilon_{it}$$

where the variables are as defined as in (1).

x and w may contain lagged independent variables and time dummies.

Let  $\mathbf{X}_{it}^{L} = (y_{i,t-1}, y_{i,t-2}, \dots, y_{i,t-p}, \mathbf{x}_{it}, \mathbf{w}_{it})$  be the  $1 \times K$  vector of covariates for i at time t, where  $K = p + k_1 + k_2$ , p is the number of included lags,  $k_1$  is the number of strictly exogenous variables in  $x_{it}$ , and  $k_2$  is the number of predetermined variables in  $w_{it}$ . (The superscript L stands for levels.)

Now rewrite this relationship as a set of  $T_i$  equations for each individual,

$$\mathbf{y}_i^L = \mathbf{X}_i^L \boldsymbol{\delta} + 
u_i \boldsymbol{\iota}_i + \boldsymbol{\epsilon}_i$$

where  $T_i$  is the number of observations available for individual i;  $\mathbf{y}_i$ ,  $\boldsymbol{\iota}_i$ , and  $\boldsymbol{\epsilon}_i$  are  $T_i \times 1$ , whereas  $\mathbf{X}_i$  is  $T_i \times K$ .

The estimators use both the levels and a transform of the variables in the above equation. Denote the transformed variables by an \*, so that  $\mathbf{y}_i^*$  is the transformed  $\mathbf{y}_i^L$  and  $\mathbf{X}_i^*$  is the transformed  $\mathbf{X}_i^L$ . The transform may be either the first difference or the forward-orthogonal deviations (FOD) transform. The (i, t)th observation of the FOD transform of a variable x is given by

$$x_{it}^* = c_t \left\{ x_{it} - \frac{1}{T - t} (x_{it+1} + x_{it+2} + \dots + x_{iT}) \right\}$$

where  $c_t^2 = (T - t)/(T - t + 1)$  and T is the number of observations on x; see Arellano and Bover (1995) and Arellano (2003).

Here we present the formulas for the Arellano–Bover/Blundell–Bond system estimator. The formulas for the Arellano–Bond estimator are obtained by setting the additional level matrices in the system estimator to null matrices.

Stacking the transformed and untransformed vectors of the dependent variable for a given i yields

$$\mathbf{y}_i = \begin{pmatrix} \mathbf{y}_i^* \ \mathbf{y}_i^L \end{pmatrix}$$

Similarly, stacking the transformed and untransformed matrices of the covariates for a given i yields

$$\mathbf{X}_i = egin{pmatrix} \mathbf{X}_i^* \ \mathbf{X}_i^L \end{pmatrix}$$

 $\mathbf{Z}_i$  is a matrix of instruments,

$$\mathbf{Z}_i = \begin{pmatrix} \mathbf{Z}_{di} & \mathbf{0} & \mathbf{D}_i & \mathbf{0} & \mathbf{I}_i^d \\ \mathbf{0} & \mathbf{Z}_{Li} & \mathbf{0} & \mathbf{L}_i & \mathbf{I}_i^L \end{pmatrix}$$

where  $\mathbf{Z}_{di}$  is the matrix of GMM-type instruments created from the dgmmiv() options,  $\mathbf{Z}_{Li}$  is the matrix of GMM-type instruments created from the lgmmiv() options,  $\mathbf{D}_i$  is the matrix of standard instruments created from the div() options,  $\mathbf{L}_i$  is the matrix of standard instruments created from the liv() options,  $\mathbf{I}_i^d$  is the matrix of standard instruments created from the iv() options for the differenced errors, and  $\mathbf{I}_i^L$  is the matrix of standard instruments created from the iv() options for the level errors.

div(), liv(), and iv() simply add columns to instrument matrix. The GMM-type instruments are more involved. Begin by considering a simple balanced-panel example in which our model is

$$y_{it} = \alpha_1 y_{i,t-1} + \alpha_2 y_{i,t-2} + \nu_i + \epsilon_{it}$$

We do not need to consider covariates because strictly exogenous variables are handled using div(), iv(), or liv(), and predetermined or endogenous variables are handled analogous to the dependent variable.

Assume that the data come from a balanced panel in which there are no missing values. After firstdifferencing the equation, we have

$$\Delta y_{it} = \alpha_1 \Delta y_{i,t-1} + \alpha_2 \Delta y_{i,t-2} + \Delta \epsilon_{it}$$

The first 3 observations are lost to lags and differencing. If we assume that the  $\epsilon_{it}$  are not autocorrelated, for each *i* at t = 4,  $y_{i1}$  and  $y_{i2}$  are valid instruments for the differenced equation. Similarly, at t = 5,  $y_{i1}$ ,  $y_{i2}$ , and  $y_{i3}$  are valid instruments. We specify dgmmiv(y) to obtain an instrument matrix with one row for each period that we are instrumenting:

$$\mathbf{Z}_{di} = \begin{pmatrix} y_{i1} & y_{i2} & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & y_{i1} & y_{i2} & y_{i3} & \dots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \dots & 0 & y_{i1} & \dots & y_{i,T-2} \end{pmatrix}$$

Because p = 2,  $\mathbf{Z}_{di}$  has T - p - 1 rows and  $\sum_{m=p}^{T-2} m$  columns.

Specifying lgmmiv(y) creates the instrument matrix

$$\mathbf{Z}_{Li} = \begin{pmatrix} \Delta.y_{i2} & 0 & 0 & \dots & 0 \\ 0 & \Delta.y_{i3} & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \dots & \Delta.y_{i(T_i-1)} \end{pmatrix}$$

This extends to other lag structures with complete data. Unbalanced data and missing observations are handled by dropping the rows for which there are no data and filling in zeros in columns where missing data are required.

After defining

$$\mathbf{Q}_{xz} = \sum_{i} \mathbf{X}'_{i} \mathbf{Z}_{i}$$
$$\mathbf{Q}_{zy} = \sum_{i} \mathbf{Z}'_{i} \mathbf{y}_{i}$$
$$\mathbf{W}_{1} = \mathbf{Q}_{xz} \mathbf{A}_{1} \mathbf{Q}'_{xz}$$
$$\mathbf{A}_{1} = \left(\sum_{i} \mathbf{Z}'_{i} \mathbf{H}_{1i} \mathbf{Z}_{i}\right)^{-1}$$

and

$$\mathbf{H}_{1i} = \begin{pmatrix} \mathbf{H}_{di} & \mathbf{0} \\ \mathbf{0} & \mathbf{H}_{Li} \end{pmatrix}$$

the one-step estimates are given by

$$\widehat{\boldsymbol{\beta}}_1 = \mathbf{W}_1^{-1} \mathbf{Q}_{xz} \mathbf{A}_1 \mathbf{Q}_{zy}$$

When using the first-difference transform  $\mathbf{H}_{di}$ , is given by

$$\mathbf{H}_{di} = \begin{pmatrix} 1 & -.5 & 0 & \dots & 0 & 0 \\ -.5 & 1 & -.5 & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & 1 & -.5 \\ 0 & 0 & 0 & \dots & -.5 & 1 \end{pmatrix}$$

and  $\mathbf{H}_{Li}$  is given by 0.5 times the identity matrix. When using the FOD transform, both  $\mathbf{H}_{di}$  and  $\mathbf{H}_{Li}$  are equal to the identity matrix.

The transformed one-step residuals are given by

$$\hat{\boldsymbol{\epsilon}}_{1i}^* = \mathbf{y}_i^* - \hat{\boldsymbol{\beta}}_1 \mathbf{X}_i^*$$

which are used to compute

$$\hat{\sigma}_1^2 = \left\{1/(N-K)\right\} \sum_i^N \hat{\boldsymbol{\epsilon}}_{1i}^{*\prime} \hat{\boldsymbol{\epsilon}}_{1i}^*$$

The GMM one-step VCE is then given by

$$\hat{V}_{\mathrm{GMM}}[\widehat{\boldsymbol{\beta}}_1] = \hat{\sigma}_1^2 \mathbf{W}_1^{-1}$$

The one-step level residuals are given by

$$\widehat{\pmb{\epsilon}}_{1i}^L = \mathbf{y}_i^L - \widehat{\pmb{\beta}}_1 \mathbf{X}_i^L$$

Stacking the residual vectors yields

$$\hat{oldsymbol{\epsilon}}_{1i} = \begin{pmatrix} \hat{oldsymbol{\epsilon}}_{1i}^{*} \\ \hat{oldsymbol{\epsilon}}_{1i}^{L} \end{pmatrix}$$

which is used to compute  $\mathbf{H}_{2i} = \hat{\boldsymbol{\epsilon}}_{1i}' \hat{\boldsymbol{\epsilon}}_{1i}$ , which is used in

$$\mathbf{A}_2 = \left(\sum_i \mathbf{Z}_i' \mathbf{H}_{2i} \mathbf{Z}_i\right)^{-1}$$

and the robust one-step VCE is given by

$$\hat{V}_{\text{robust}}[\widehat{\boldsymbol{\beta}}_1] = \mathbf{W}_1^{-1} \mathbf{Q}_{xz} \mathbf{A}_1 \mathbf{A}_2^{-1} \mathbf{A}_1 \mathbf{Q}_{xz}' \mathbf{W}_1^{-1}$$

 $\hat{V}_{\rm robust}[\widehat{\pmb{\beta}}_1]$  is robust to heteroskedasticity in the errors. After defining

$$\mathbf{W}_2 = \mathbf{Q}_{xz} \mathbf{A}_2 \mathbf{Q}_{xz}'$$

the two-step estimates are given by

$$\widehat{\boldsymbol{\beta}}_2 = \mathbf{W}_2^{-1} \mathbf{Q}_{xz} \mathbf{A}_2 \mathbf{Q}_{zy}$$

The GMM two-step VCE is then given by

$$\widehat{V}_{\mathrm{GMM}}[\widehat{\boldsymbol{eta}}_2] = \mathbf{W}_2^{-1}$$

The GMM two-step VCE is known to be severely biased. Windmeijer (2005) derived the Windmeijer bias-corrected (WC) estimator for the robust VCE of two-step GMM estimators. xtdpd implements this WC-robust estimator of the VCE. The formulas for this method are involved; see Windmeijer (2005). The WC-robust estimator of the VCE is robust to heteroskedasticity in the errors.

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### Also see

- [XT] xtdpd postestimation Postestimation tools for xtdpd
- [XT] xtabond Arellano-Bond linear dynamic panel-data estimation
- [XT] xtdpdsys Arellano-Bover/Blundell-Bond linear dynamic panel-data estimation
- [XT] xtivreg Instrumental variables and two-stage least squares for panel-data models
- [XT] **xtreg** Linear models for panel data
- [XT] xtregar Fixed- and random-effects linear models with an AR(1) disturbance
- [XT] **xtset** Declare data to be panel data
- [R] gmm Generalized method of moments estimation
- [U] 20 Estimation and postestimation commands

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