sts test — Test equality of survivor functions

| Description | Quick start |
|-------------|----------------------|
| Options | Remarks and examples |
| References | Also see |

Menu Stored results Syntax Methods and formulas

Description

sts test tests the equality of survivor functions across two or more groups. The log-rank, Cox, Wilcoxon–Breslow–Gehan, Tarone–Ware, Peto–Peto–Prentice, and Fleming–Harrington tests are provided, in both unstratified and stratified forms.

sts test also provides a test for trend.

sts test can be used with single- or multiple-record or single- or multiple-failure st data.

Quick start

Log-rank test for the equality of survivor functions across levels of v1 using stset data sts test v1

Stratified log-rank test for equality of survivor functions across v1 with strata svar sts test v1, strata(svar)

- Same as above, and show tests for each stratum sts test v1, strata(svar) detail
- Log-rank test for equality, and test for a trend in survivor functions for v1 sts test v1, trend
- Test equality of survivor functions using the Wilcoxon-Breslow-Gehan test sts test v1, wilcoxon
- Likelihood-ratio test for the equality of survivor functions based on the Cox model sts test v1, cox
- Stratified Cox test of equality of survivor functions with strata svar sts test v1, cox strata(svar)
- Test equality of survivor functions using the Tarone–Ware test sts test v1, tware
- Same as above, and test for a trend using the same weights as used in the Tarone–Ware test sts test v1, tware trend

Menu

Statistics > Survival analysis > Summary statistics, tests, and tables > Test equality of survivor functions

Syntax

| options | Description |
|----------------------------|---|
| Main | |
| <u>l</u> ogrank | perform log-rank test of equality; the default |
| cox | perform Cox test of equality |
| wilcoxon | perform Wilcoxon-Breslow-Gehan test of equality |
| <u>tw</u> are | perform Tarone–Ware test of equality |
| peto | perform Peto-Peto-Prentice test of equality |
| $\frac{1}{\text{fh}}(p q)$ | perform generalized Fleming-Harrington test of equality |
| trend | test trend of the survivor function across three or more ordered groups |
| strata(varlist) | perform stratified test on <i>varlist</i> , displaying overall test results |
| detail | display individual test results; modifies strata() |
| Options | |
| $mat(mname_1 mname_2)$ | store vector u in $mname_1$ and matrix V in $mname_2$ |
| noshow | do not show st setting information |
| <u>not</u> itle | suppress title |

sts test varlist [if] [in] [, options]

You must stset your data before using sts test; see [ST] stset. collect is allowed; see [U] 11.1.10 Prefix commands.

Note that fweights, iweights, and pweights may be specified using stset; see [ST] stset.

Options

Main

logrank, cox, wilcoxon, tware, peto, and fh(pq) specify the test of equality desired. logrank is the default, unless the data are pweighted, in which case cox is the default and is the only possibility.

wilcoxon specifies the Wilcoxon-Breslow-Gehan test; tware, the Tarone-Ware test; peto, the Peto-Peto-Prentice test; and fh(), the generalized Fleming-Harrington test. The Fleming-Harrington test requires two arguments, p and q. When p = 0 and q = 0, the Fleming-Harrington test reduces to the log-rank test; when p = 1 and q = 0, the test reduces to the Mann-Whitney-Wilcoxon test.

trend specifies that a test for trend of the survivor function across three or more ordered groups be performed.

strata(varlist) requests that a stratified test be performed.

detail modifies strata(); it requests that, in addition to the overall stratified test, the tests for the individual strata be reported. detail is not allowed with cox.

Options

 $mat(mname_1 mname_2)$ requests that the vector **u** be stored in $mname_1$ and that matrix **V** be stored in $mname_2$. The other tests are rank tests of the form $\mathbf{u}'\mathbf{V}^{-1}\mathbf{u}$. This option may not be used with cox.

noshow prevents sts test from showing the key st variables. This option is seldom used because most people type stset, show or stset, noshow to set whether they want to see these variables mentioned at the top of the output of every st command; see [ST] **stset**.

notitle requests that the title printed above the test be suppressed.

Remarks and examples

Remarks are presented under the following headings:

The log-rank test The Wilcoxon (Breslow–Gehan) test The Tarone–Ware test The Peto–Peto–Prentice test The generalized Fleming–Harrington tests The "Cox" test The trend test Video example

sts test tests the equality of the survivor function across groups. With the exception of the Cox test, these tests are members of a family of statistical tests that are extensions to censored data of traditional nonparametric rank tests for comparing two or more distributions. A technical description of these tests can be found in the *Methods and formulas* section of this entry. Simply, at each distinct failure time in the data, the contribution to the test statistic is obtained as a weighted standardized sum of the difference between the observed and expected number of deaths in each of the *k* groups. The expected number of deaths is obtained under the null hypothesis of no differences between the survival experience of the *k* groups.

The weights or weight function used determines the test statistic. For example, when the weight is 1 at all failure times, the log-rank test is computed, and when the weight is the number of subjects at risk of failure at each distinct failure time, the Wilcoxon–Breslow–Gehan test is computed.

The following table summarizes the weights used for each statistical test.

| Test | Weight at each distinct failure time (t_i) |
|------------------------|---|
| Log-rank | 1 |
| Wilcoxon-Breslow-Gehan | n_i |
| Tarone–Ware | $\sqrt{n_i}$ |
| Peto-Peto-Prentice | $\tilde{S}(t_i)$ |
| Fleming-Harrington | $\hat{S}(t_{i-1})^p \big\{ 1 - \hat{S}(t_{i-1}) \big\}^q$ |

where $\hat{S}(t_i)$ is the estimated Kaplan–Meier survivor-function value for the combined sample at failure time t_i , $\tilde{S}(t_i)$ is a modified estimate of the overall survivor function described in Methods and formulas, and n_i is the number of subjects in the risk pool at failure time t_i .

These tests are appropriate for testing the equality of survivor functions across two or more groups. Up to 800 groups are allowed. The "Cox" test is related to the log-rank test but is performed as a likelihood-ratio test (or, alternatively, as a Wald test) on the results from a Cox proportional hazards regression. The log-rank test should be preferable to what we have labeled the Cox test, but with pweighted data the log-rank test is not appropriate. Whether you perform the log-rank or Cox test makes little substantive difference with most datasets.

sts test, trend can be used to test against the alternative hypothesis that the failure rate increases or decreases as the level of the k groups increases or decreases. This test is appropriate only when there is a natural ordering of the comparison groups, for example, when each group represents an increasing or decreasing level of a therapeutic agent.

trend is not valid when cox is specified.

The log-rank test

sts test, by default, performs the log-rank test, which is, to be clear, the exponential scores test (Savage 1956; Mantel and Haenszel 1959; Mantel 1963, 1966). This test is most appropriate when the hazard functions are thought to be proportional across the groups if they are not equal.

This test statistic is constructed by giving equal weights to the contribution of each failure time to the overall test statistic.

In Testing equality of survivor functions in [ST] sts, we demonstrated the use of this command with the heart transplant data, a multiple-record, single-failure st dataset.

```
. use https://www.stata-press.com/data/r19/stan3
(Heart transplant data)
. sts test posttran
        Failure _d: died
  Analysis time _t: t1
       ID variable: id
Equality of survivor functions
Log-rank test
            Observed
                            Expected
              events
posttran
                              events
       0
                   30
                               31.20
                  45
                               43.80
       1
   Total
                   75
                               75.00
                    chi2(1) =
                                0.13
                   Pr>chi2 = 0.7225
```

We cannot reject the hypothesis that the survivor functions are the same.

sts test, logrank can also perform the stratified log-rank test. Say that it is suggested that calendar year of acceptance also affects survival and that there are three important periods: 1967–1969, 1970–1972, and 1973–1974. Therefore, a stratified test should be performed:

```
. stset, noshow
. generate group = 1 if year <= 69
(117 missing values generated)
. replace group=2 if year>=70 & year<=72
(78 real changes made)
. replace group=3 if year>=73
(39 real changes made)
```

| . sts test | z posttran, | strata(group) | | |
|--|--------------|---------------|--|--|
| Equality of survivor functions | | | | |
| | d log-rank t | est | | |
| Strata: gi | roup | | | |
| | Observed | Expected | | |
| posttran | events | events* | | |
| 0 | 30 | 31.51 | | |
| 1 | 45 | 43.49 | | |
| Total | 75 | 75.00 | | |
| * aggregated over stratum-specific results | | | | |
| chi2(1) = 0.20 Pr>chi2 = 0.6547 | | | | |

When a stratified test is requested, Stata computes the expected events under the null hypothesis separately for each stratum, and those results are aggregated over strata.

We now want to show the within-stratum tests, so we type

```
. sts test posttran, strata(group) detail
Equality of survivor functions
Stratified log-rank test
Strata: group
-> group = 1
             Observed
                             Expected
               events
                               events
posttran
       0
                   14
                                13.59
       1
                   17
                                17.41
                   31
   Total
                                31.00
                    chi2(1) =
                                 0.03
                    Pr>chi2 = 0.8558
-> group = 2
             Observed
                             Expected
posttran
               events
                               events
       0
                   13
                                13.63
       1
                   20
                                19.37
                   33
                                33.00
   Total
                    chi2(1) =
                                 0.09
                    Pr>chi2 = 0.7663
-> group = 3
             Observed
                             Expected
               events
posttran
                               events
                                 4.29
       0
                    3
       1
                    8
                                 6.71
   Total
                   11
                                11.00
                    chi2(1) =
                                 0.91
                    Pr>chi2 = 0.3410
```

| -> Total | | |
|-----------|----------------|----------------------|
| | Observed | Expected |
| posttran | events | events* |
| 0 | 30 | 31.51 |
| 1 | 45 | 43.49 |
| I | 10 | 10:15 |
| Total | 75 | 75.00 |
| * aggrega | ted over strat | cum-specific results |
| | chi2 | 2(1) = 0.20 |
| | Pr>c | chi2 = 0.6547 |

The Wilcoxon (Breslow–Gehan) test

sts test, wilcoxon performs the generalized Wilcoxon test of Breslow (1970) and Gehan (1965). This test is appropriate when hazard functions are thought to vary in ways other than proportionally and when censoring patterns are similar across groups.

The Wilcoxon test statistic is constructed by weighting the contribution of each failure time to the overall test statistic by the number of subjects at risk. Thus it gives heavier weights to earlier failure times when the number at risk is higher. As a result, this test is susceptible to differences in the censoring pattern of the groups.

0

sts test, wilcoxon works the same way as sts test, logrank:

```
. sts test posttran, wilcoxon
Equality of survivor functions
Wilcoxon-Breslow-Gehan test
                                             Sum of
            Observed
                             Expected
posttran
               events
                               events
                                              ranks
       0
                   30
                                31.20
                                                -85
                                43.80
                                                 85
       1
                   45
   Total
                   75
                                75.00
                                  chi2(1) =
                                               0.14
                                  Pr>chi2 = 0.7083
```

With the strata() option, sts test, wilcoxon performs the stratified test:

. sts test posttran, wilcoxon strata(group) Equality of survivor functions Stratified Wilcoxon-Breslow-Gehan test Strata: group Observed Expected Sum of events events* ranks* posttran 0 30 31.51 -40 1 45 43.49 40 Total 75 75.00 0 * aggregated over stratum-specific results chi2(1) =0.22 Pr>chi2 = 0.6385

As with sts test, logrank, you can also specify the detail option to see the within-stratum tests.

The Tarone–Ware test

sts test, tware performs a test suggested by Tarone and Ware (1977), with weights equal to the square root of the number of subjects in the risk pool at time t_i .

Like Wilcoxon's test, this test is appropriate when hazard functions are thought to vary in ways other than proportionally and when censoring patterns are similar across groups. The test statistic is constructed by weighting the contribution of each failure time to the overall test statistic by the square root of the number of subjects at risk. Thus, like the Wilcoxon test, it gives heavier weights, although not as large, to earlier failure times. Although less susceptible to the failure and censoring pattern in the data than Wilcoxon's test, this could remain a problem if large differences in these patterns exist between groups.

sts test, tware works the same way as sts test, logrank:

| . sts test | t posttran, | tware | |
|------------------------|------------------------|--------------------|-----------------------------------|
| Equality of Tarone-War | of survivor re test | functions | |
| posttran | Observed events | Expected events | Sum of ranks |
| 0 1 | 30 45 | 31.20 43.80 | |
| Total | 75 | | 0 2(1) = 0.12 2hi2 = 0.7293 |

With the strata() option, sts test, tware performs the stratified test:

```
. sts test posttran, tware strata(group)
Equality of survivor functions
Stratified Tarone-Ware test
Strata: group
            Observed
                                            Sum of
                            Expected
posttran
               events
                              events*
                                             ranks*
                                        -7.4679345
       0
                   30
                               31.51
       1
                   45
                               43.49
                                         7.4679345
   Total
                   75
                               75.00
                                                 0
* aggregated over stratum-specific results
                                 chi2(1) =
                                              0.21
                                 Pr>chi2 = 0.6464
```

As with sts test, logrank, you can also specify the detail option to see the within-stratum tests.

The Peto–Peto–Prentice test

sts test, peto performs an alternative to the Wilcoxon test proposed by Peto and Peto (1972) and Prentice (1978). The test uses as the weight function an estimate of the overall survivor function, which is similar to that obtained using the Kaplan–Meier estimator. See *Methods and formulas* for details.

This test is appropriate when hazard functions are thought to vary in ways other than proportionally, but unlike the Wilcoxon–Breslow–Gehan test, it is not affected by differences in censoring patterns across groups.

sts test, peto works the same way as sts test, logrank:

| . sts test posttran, peto | | | |
|---------------------------|-----------------------------|--------------------|------------------------------|
| 1 V | of survivor -Prentice te | | |
| posttran | Observed events | Expected events | Sum of ranks |
| | events | events | 1 diik5 |
| 0 | 30 | 31.20 | 86708453 |
| 1 | 45 | 43.80 | .86708453 |
| Total | 75 | 75.00 | 0 |
| | | | 2(1) = 0.15 thi2 = 0.6979 |

With the strata() option, sts test, peto performs the stratified test:

```
. sts test posttran, peto strata(group)
Equality of survivor functions
Stratified Peto-Peto-Prentice test
Strata: group
            Observed
                            Expected
                                            Sum of
posttran
                              events*
                                             ranks*
              events
       0
                  30
                               31.51
                                        -1.4212233
                               43.49
                                         1.4212233
       1
                   45
   Total
                   75
                               75.00
                                                 0
* aggregated over stratum-specific results
                                 chi2(1) =
                                              0.43
                                 Pr>chi2 = 0.5129
```

As with the previous tests, you can also specify the detail option to see the within-stratum tests.

The generalized Fleming–Harrington tests

sts test, fh(pq) performs the Harrington and Fleming (1982) class of test statistics. The weight function at each distinct failure time, t, is the product of the Kaplan-Meier survivor estimate at time t-1 raised to the p power and 1 - the Kaplan-Meier survivor estimate at time t-1 raised to the q power. Thus, when specifying the Fleming and Harrington option, you must specify two nonnegative arguments, p and q.

When p > q, the test gives more weights to earlier failures than to later ones. When p < q, the opposite is true, and more weight is given to later failures than to earlier ones. When p and q are both zero, the weight is 1 at all failure times and the test reduces to the log-rank test.

sts test, fh(pq) works the same way as sts test, logrank. If we specify p=0 and q=0 we will get the same results as the log-rank test:

| . sts test | t posttran, | fh(0 0) | |
|------------|---|----------------|------------------------------|
| Fleming-Ha | of survivor arrington te = 0, q = 0 | | |
| | Observed | Expected | Sum of |
| posttran | events | events | ranks |
| 0 | 30 45 | 31.20 43.80 | |
| Total | 75 | 75.00 | 0 |
| | | | 2(1) = 0.13 thi2 = 0.7225 |

We could, for example, give more weight to later failures than to earlier ones.

. sts test posttran, fh(0 3) Equality of survivor functions Fleming-Harrington test Powers: p = 0, q = 3Observed Expected Sum of events events ranks posttran 0 30 31.20 -.10288411 .10288411 1 45 43.80 Total 75 75.00 0 chi2(1) =0.01 Pr>chi2 = 0.9065

Similarly to the previous tests, with the strata() option, sts test, fh() performs the stratified test:

```
. sts test posttran, fh(0 3) strata(group)
Equality of survivor functions
Stratified Fleming-Harrington test
Powers: p = 0, q = 3
Strata: group
            Observed
                            Expected
                                            Sum of
posttran
              events
                              events*
                                             ranks*
       0
                  30
                                       -.05315105
                               31.51
       1
                  45
                               43.49
                                         .05315105
                  75
                               75.00
                                                 0
   Total
* aggregated over stratum-specific results
                                 chi2(1) =
                                              0.00
```

```
Pr>chi2 = 0.9494
```

As with the other tests, you can also specify the detail option to see the within-stratum tests.

The "Cox" test

The term Cox test is our own, and this test is a variation on the log-rank test using Cox regression.

One way of thinking about the log-rank test is as a Cox proportional hazards model on indicator variables for each of the groups. The log-rank test is a test that the coefficients are zero or, if you prefer, that the hazard ratios are one. The log-rank test is, in fact, a score test of that hypothesis performed on a slightly different (partial) likelihood function that handles ties more accurately.

Many researchers think that a (less precise) score test on the precise likelihood function is preferable to a (more precise) likelihood-ratio test on the approximate likelihood function used in Cox regression estimation. In our experience, it makes little difference:

| . sts test | t posttran, | cox | |
|------------|----------------------------|-----------------------|----------------------|
| 1 0 | of survivor ssion-based | | |
| | Observed | Expected | Relative |
| posttran | events | events | hazard |
| 0 | 30 | 31.20 | 0.9401 |
| 1 | 45 | 43.80 | 1.0450 |
| Total | 75 | 75.00 | 1.0000 |
| | | LR chi2(1) Pr>chi2 | 0 = 0.13 = 0.7222 |
| Note: Repo | orting LR mo | odel test from Cox | regression |

on posttran.

By comparison, sts test, logrank also reported $\chi^2 = 0.13$, although the significance level was 0.7225, meaning that the χ^2 values differed in the fourth digit. As mentioned by Kalbfleisch and Prentice (2002, 20), a primary advantage of the log-rank test is the ease with which it can be explained to nonstatisticians, because the test statistic is the difference between the observed and expected number of failures within groups.

Our purpose in offering sts test, cox is not to promote its use instead of the log-rank test but to provide a test for researchers with sample-weighted data.

If you have sample weights (if you specified pweights when you stset the data), you cannot run the log-rank or Wilcoxon tests. The Cox regression model, however, has been generalized to sample-weighted data, and Stata's stcox can fit models with such data. In sample-weighted data, the likelihood-ratio statistic is no longer appropriate, but the Wald test based on the robust estimator of variance is.

Thus if we treated these data as sample-weighted data, we would obtain

```
. generate one = 1
. stset t1 [pw=one], id(id) timeO(_t0) failure(died) noshow
Survival-time data settings
           ID variable: id
         Failure event: died!=0 & died<.
Observed time interval: ( t0, t1]
     Exit on or before: failure
                Weight: [pweight=one]
        172 total observations
          0 exclusions
        172 observations remaining, representing
        103 subjects
         75 failures in single-failure-per-subject data
  31,938.1 total analysis time at risk and under observation
                                                                           0
                                                 At risk from t =
                                     Earliest observed entry t =
                                                                           0
                                           Last observed exit t =
                                                                      1,799
. sts test posttran, cox
Equality of survivor functions
Cox regression-based test
                                        Relative
            Observed
                           Expected
posttran
              events
                             events
                                           hazard
       0
               30.00
                              31.20
                                           0.9401
       1
               45.00
                              43.80
                                           1.0450
               75.00
                              75.00
                                           1.0000
  Total
                           Wald chi2(1) =
                                             0.13
                           Pr>chi2
                                        = 0.7181
Note: Reporting Wald model test from Cox
      regression on posttran.
```

sts test, cox now reports the Wald statistic, which is, to two digits, 0.13, just like all the others.

The trend test

When the groups to be compared have a natural order, such as increasing or decreasing age groups or drug dosage, you may want to test the null hypothesis that there is no difference in failure rate among the groups versus the alternative hypothesis that the failure rate increases or decreases as you move from one group to the next.

We illustrate this test with a dataset from a carcinogenesis experiment reprinted in Marubini and Valsecchi (1995, 126). Twenty-nine experimental animals were exposed to three levels (0, 1.5, 2.0) of a carcinogenic agent. The time in days to tumor formation was recorded. Here are a few of the observations:

. use https://www.stata-press.com/data/r19/marubini, clear

| | time | event | group | dose |
|----------|------|-------|-------|------|
| 1. | 67 | 1 | 2 | 1.5 |
| 2. | 150 | 1 | 2 | 1.5 |
| 2. 3. | 47 | 1 | 3 | 2 |
| 4. | 75 | 0 | 1 | 0 |
| 5. | 58 | 1 | 3 | 2 |
| 6. | 136 | 1 | 2 | 1.5 |
| 7. | 58 | 1 | 3 | 2 |
| 8. | 150 | 1 | 2 | 1.5 |
| 9. | 43 | 0 | 2 | 1.5 |
| | L | | | |

. list time event group dose in 1/9

In these data, there are two variables that indicate exposure level. The group variable is coded 1, 2, and 3, indicating a one-unit separation between exposures. The dose variable records the actual exposure dosage. To test the null hypothesis of no difference among the survival experience of the three groups versus the alternative hypothesis that the survival experience of at least one of the groups is different, it does not matter if we use group or dose.

```
. stset time, fail(event) noshow
Survival-time data settings
         Failure event: event!=0 & event<.
Observed time interval: (0, time]
     Exit on or before: failure
         29 total observations
          0 exclusions
         29 observations remaining, representing
         15 failures in single-record/single-failure data
      2,564 total analysis time at risk and under observation
                                                 At risk from t =
                                                                          0
                                     Earliest observed entry t =
                                                                          0
                                          Last observed exit t =
                                                                        246
. sts test group
Equality of survivor functions
Log-rank test
         Observed
                        Expected
           events
                          events
group
    1
                4
                            6.41
    2
                6
                            6.80
    3
                5
                            1.79
                           15.00
Total
               15
                chi2(2) =
                            8.05
                Pr>chi2 = 0.0179
```

| . sts test dose | | | | |
|---|----------|--------------|--|--|
| Equality of survivor functions Log-rank test | | | | |
| | Observed | Expected | | |
| dose | events | events | | |
| 0 | 4 | 6.41 | | |
| 1.5 | 6 | 6.80 | | |
| 2 | 5 | 1.79 | | |
| Total | 15 | 15.00 | | |
| | chi2 | (2) = 8.05 | | |
| | Pr>cl | ni2 = 0.0179 | | |

For the trend test, however, the distance between the values is important, so using group or dose will produce different results.

| . sts test group, trend | | | |
|---|---------------------------|----------------------------|--|
| Equalit Log-rar | ty of survivor nk test | functions | |
| | Observed | Expected | |
| group | events | events | |
| 1 | 4 | 6.41 | |
| 2 | 6 | 6.80 | |
| 3 | 5 | 1.79 | |
| Total | 15 | 15.00 | |
| | chi2 | (2) = 8.05 | |
| | Pr>cl | ni2 = 0.0179 | |
| Test fo | or trend in su | rvivor functions | |
| | chi2 | (1) = 5.87 | |
| | Pr>cl | ni2 = 0.0154 | |
| . sts t | test dose, tre | nd | |
| Equality of survivor functions Log-rank test | | | |
| | Observed | Expected | |
| dose | events | events | |
| 0 | 4 | 6.41 | |
| 1.5 | 6 | 6.80 | |
| 2 | 5 | 1.79 | |
| Total | 15 | 15.00 | |
| chi2(2) = 8.05 Pr>chi2 = 0.0179 | | | |
| Test fo | or trend in su | rvivor functions | |
| | | (1) = 3.66 ni2 = 0.0557 | |

Although the above trend test was constructed using the log-rank test, any of the previously mentioned weight functions can be used. For example, a trend test on the data can be performed using the same weights as the Peto–Prentice test by specifying the peto option.

| Equality of survivor functions Peto-Peto-Prentice test | | | |
|--|--------------------|----------------------|-----------------------------------|
| dose | Observed events | Expected events | Sum of ranks |
| 0 1.5 2 | 4 6 5 | 6.41 6.80 1.79 | -1.3150418 |
| Total | 15 | | 0 2(2) = 8.39 chi2 = 0.0150 |
| Test for trend in survivor functions chi2(1) = 2.85 Pr>chi2 = 0.0914 | | | |

Video example

How to test the equality of survivor functions using nonparametric tests

Stored results

sts test stores the following in r():

. sts test dose, trend peto

 $\begin{array}{ccc} \text{Scalars} & & \\ \textbf{r}(\text{df}) & \text{degrees of freedom} & \textbf{r}(\text{chi2}) & \chi^2 \\ \textbf{r}(\text{df}_{-}\text{tr}) & \text{degrees of freedom, trend test} & \textbf{r}(\text{chi2}_{-}\text{tr}) & \chi^2, \text{ trend test} \end{array}$

Methods and formulas

Let $t_1 < t_2 < \cdots < t_k$ denote the ordered failure times; let d_j be the number of failures at t_j and n_j be the population at risk just before t_j ; and let d_{ij} and n_{ij} denote the same things for group $i, i = 1, \ldots, r$.

We are interested in testing the null hypothesis

$$H_0: \lambda_1(t) = \lambda_2(t) = \cdots = \lambda_r(t)$$

where $\lambda(t)$ is the hazard function at time t, against the alternative hypothesis that at least one of the $\lambda_i(t)$ is different for some t_i .

As described in Klein and Moeschberger (2003, 205–216), Kalbfleisch and Prentice (2002, 20–22), and Collett (2015, 50–51), if the null hypothesis is true, the expected number of failures in group *i* at time t_i is $e_{ij} = n_{ij}d_j/n_j$, and the test statistic

$$\mathbf{u}' = \sum_{j=1}^{k} W(t_j) (d_{1j} - e_{1j}, \dots, d_{rj} - e_{rj})$$

is formed. $W(t_j)$ is a positive weight function defined as zero when n_{ij} is zero. The various test statistics are obtained by selecting different weight functions, $W(t_j)$. See the table in the *Remarks and examples* section of this entry for a list of these weight functions. For the Peto–Peto–Prentice test,

$$W(t_j) = \tilde{S}(t_j) = \prod_{\ell: t_\ell \leq t_j} \left(1 - \frac{d_\ell}{n_\ell + 1}\right)$$

The variance matrix V for u has elements

$$V_{il} = \sum_{j=1}^{k} \frac{W(t_j)^2 n_{ij} d_j (n_j - d_j)}{n_j (n_j - 1)} \left(\delta_{il} - \frac{n_{ij}}{n_j} \right)$$

where $\delta_{il} = 1$ if i = l and $\delta_{il} = 0$, otherwise.

For the unstratified test, statistic $\mathbf{u}' \mathbf{V}^{-1} \mathbf{u}$ is distributed as χ^2 with r-1 degrees of freedom.

For the stratified test, let \mathbf{u}_s and \mathbf{V}_s be the results of performing the above calculation separately within stratum, and define $\mathbf{u} = \sum_s \mathbf{u}_s$ and $\mathbf{V} = \sum_s \mathbf{V}_s$. The χ^2 test is given by $\mathbf{u}'\mathbf{V}^{-1}\mathbf{u}$ redefined in this way.

The "Cox" test is performed by fitting a (possibly stratified) Cox regression using stcox on r-1 indicator variables, one for each group with one of the indicators omitted. The χ^2 test reported is then the likelihood-ratio test (no pweights) or the Wald test (based on the robust estimate of variance); see [ST] stcox.

The reported relative hazards are the exponentiated coefficients from the Cox regression renormalized, and the renormalization plays no role in calculating the test statistic. The renormalization is chosen so that the expected-number-of-failures-within-group weighted average of the regression coefficients is 0 (meaning that the hazard is 1). Let b_i , i = 1, ..., r-1, be the estimated coefficients, and define $b_r = 0$. The constant K is then calculated with

$$K = \sum_{i=1}^{r} e_i b_i / d$$

where $e_i = \sum_j e_{ij}$ is the expected number of failures for group *i*, *d* is the total number of failures across all groups, and *r* is the number of groups. The reported relative hazards are $\exp(b_i - K)$.

The trend test assumes that there is natural ordering of the r groups, r > 2. Here we are interested in testing the null hypothesis

$$H_0: \lambda_1(t) = \lambda_2(t) = \dots = \lambda_r(t)$$

against the alternative hypothesis

$$H_a: \lambda_1(t) \le \lambda_2(t) \le \dots \le \lambda_r(t)$$

The test uses \mathbf{u} as previously defined with any of the available weight functions. The test statistic is given by



where $a_1 \le a_2 \le \cdots \le a_r$ are scores defining the relationship of interest. A score is assigned to each comparison group, equal to the value of the grouping variable for that group. **a** is the vector of these scores.

References

- Breslow, N. E. 1970. A generalized Kruskal–Wallis test for comparing K samples subject to unequal patterns of censorship. Biometrika 57: 579–594. https://doi.org/10.1093/biomet/57.3.579.
- Collett, D. 2015. Modelling Survival Data in Medical Research. 3rd ed. Boca Raton, FL: Chapman and Hall/CRC.
- Gehan, E. A. 1965. A generalized Wilcoxon test for comparing arbitrarily singly-censored samples. *Biometrika* 52: 203–223. https://doi.org/10.2307/2333825.
- Harrington, D. P., and T. R. Fleming. 1982. A class of rank test procedures for censored survival data. *Biometrika* 69: 553–566. https://doi.org/10.2307/2335991.
- Kalbfleisch, J. D., and R. L. Prentice. 2002. The Statistical Analysis of Failure Time Data. 2nd ed. New York: Wiley.
- Karrison, T. G. 2016. Versatile tests for comparing survival curves based on weighted log-rank statistics. *Stata Journal* 16: 678–690.
- Klein, J. P., and M. L. Moeschberger. 2003. Survival Analysis: Techniques for Censored and Truncated Data. 2nd ed. New York: Springer.
- Mantel, N. 1963. Chi-square tests with one degree of freedom; extensions of the Mantel–Haenszel procedure. Journal of the American Statistical Association 58: 690–700. https://doi.org/10.1080/01621459.1963.10500879.
- ———. 1966. Evaluation of survival data and two new rank-order statistics arising in its consideration. Cancer Chemotherapy Reports 50: 163–170.
- Mantel, N., and W. Haenszel. 1959. Statistical aspects of the analysis of data from retrospective studies of disease. Journal of the National Cancer Institute 22: 719–748. Reprinted in Evolution of Epidemiologic Ideas: Annotated Readings on Concepts and Methods, ed. S. Greenland, pp. 112–141. Newton Lower Falls, MA: Epidemiology Resources.
- Marubini, E., and M. G. Valsecchi. 1995. Analysing Survival Data from Clinical Trials and Observational Studies. New York: Wiley.
- Peto, R., and J. Peto. 1972. Asymptotically efficient rank invariant test procedures. *Journal of the Royal Statistical Society,* A ser., 135: 185–207. https://doi.org/10.2307/2344317.
- Prentice, R. L. 1978. Linear rank tests with right censored data. *Biometrika* 65: 167–179. https://doi.org/10.2307/2335292.
- Savage, I. R. 1956. Contributions to the theory of rank-order statistics—the two-sample case. Annals of Mathematical Statistics 27: 590–615. https://doi.org/10.1214/aoms/1177728170.
- Tarone, R. E., and J. H. Ware. 1977. On distribution-free tests for equality of survival distributions. *Biometrika* 64: 156–160. https://doi.org/10.2307/2335790.
- White, I. R., S. Walker, and A. G. Babiker. 2002. strbee: Randomization-based efficacy estimator. Stata Journal 2: 140–150.
- Wilcoxon, F. 1945. Individual comparisons by ranking methods. *Biometrics* 1: 80-83. https://doi.org/10.2307/3001968.

Also see

- [ST] stcox Cox proportional hazards model
- [ST] sts Generate, graph, list, and test the survivor and related functions
- [ST] sts generate Create variables containing survivor and related functions
- [ST] sts graph Graph the survivor or related function
- [ST] sts list List the survivor or related function
- [ST] **stset** Declare data to be survival-time data
- [PSS-2] power exponential Power analysis for a two-sample exponential test
- [PSS-2] power logrank Power analysis for the log-rank test

Stata, Stata Press, Mata, NetCourse, and NetCourseNow are registered trademarks of StataCorp LLC. Stata and Stata Press are registered trademarks with the World Intellectual Property Organization of the United Nations. StataNow is a trademark of StataCorp LLC. Other brand and product names are registered trademarks or trademarks of their respective companies. Copyright © 1985–2025 StataCorp LLC, College Station, TX, USA. All rights reserved.



For suggested citations, see the FAQ on citing Stata documentation.