Example 51g — Latent class goodness-of-fit statistics

Description

Here we demonstrate how to obtain goodness-of-fit statistics for latent class models. We continue with [SEM] Example 50g, where we fit a two-class model:

```
. use https://www.stata-press.com/data/r17/gsem_lca1
. gsem (accident play insurance stock <- ), logit lclass(C 2)
```

See Latent class models in [SEM] Intro 5 for background.

Remarks and examples

Remarks are presented under the following headings:

- Likelihood-ratio (G²) test
- Comparing models

Likelihood-ratio (G²) test

For standard latent class models with observed variables that are all categorical, one way to evaluate model fit is to compare the model we have just fit with a saturated model. We can use the estat lcgof command to perform a likelihood-ratio test of whether our model fits as well as the saturated model. The corresponding likelihood-ratio statistic is sometimes referred to as $G^2$ in latent class analysis literature.

```
. estat lcgof
```

<table>
<thead>
<tr>
<th>Fit statistic</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Likelihood ratio</td>
<td></td>
<td></td>
</tr>
<tr>
<td>chi2_ms(6)</td>
<td>2.720</td>
<td>model vs. saturated</td>
</tr>
<tr>
<td>p &gt; chi2</td>
<td>0.843</td>
<td></td>
</tr>
<tr>
<td>Information criteria</td>
<td></td>
<td></td>
</tr>
<tr>
<td>AIC</td>
<td>1026.935</td>
<td>Akaike’s information criterion</td>
</tr>
<tr>
<td>BIC</td>
<td>1057.313</td>
<td>Bayesian information criterion</td>
</tr>
</tbody>
</table>

We fail to reject the null hypothesis that our model fits as well as the saturated model.

estat lcgof also reports Akaike’s information criterion (AIC) and Schwarz’s Bayesian information criterion (BIC). These are useful for comparing models but not useful for determining goodness-of-fit for a single model.
Comparing models

In latent class analysis, we often compare models that have different numbers of classes. Following Goodman (2002), we compare models that allow for one, two, and three latent classes. We have already fit the two-class model using the `gsem` command above. Before we move on, we will store the results of this model.

. estimates store twoclass

Next, we fit the one-class model, store the results, and perform the likelihood-ratio test comparing it with the saturated model.

. quietly gsem (accident play insurance stock <- ), logit lclass(C 1)
. estimates store oneclass
. estat lcgof

<table>
<thead>
<tr>
<th>Fit statistic</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Likelihood ratio</td>
<td></td>
<td></td>
</tr>
<tr>
<td>chi2_ms(11)</td>
<td>81.084</td>
<td>model vs. saturated</td>
</tr>
<tr>
<td>p &gt; chi2</td>
<td>0.000</td>
<td></td>
</tr>
<tr>
<td>Information criteria</td>
<td></td>
<td></td>
</tr>
<tr>
<td>AIC</td>
<td>1095.300</td>
<td>Akaike’s information criterion</td>
</tr>
<tr>
<td>BIC</td>
<td>1108.801</td>
<td>Bayesian information criterion</td>
</tr>
</tbody>
</table>

We reject the null hypothesis in this case. The one-class model does not fit well.

We also fit the three-class model.

. quietly gsem (accident play insurance stock <- ), logit lclass(C 3)
. estimates store threeclass
. estat lcgof

<table>
<thead>
<tr>
<th>Fit statistic</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Likelihood ratio</td>
<td></td>
<td></td>
</tr>
<tr>
<td>chi2_ms(1)</td>
<td>0.387</td>
<td>model vs. saturated</td>
</tr>
<tr>
<td>p &gt; chi2</td>
<td>0.534</td>
<td></td>
</tr>
<tr>
<td>Information criteria</td>
<td></td>
<td></td>
</tr>
<tr>
<td>AIC</td>
<td>1034.602</td>
<td>Akaike’s information criterion</td>
</tr>
<tr>
<td>BIC</td>
<td>1081.856</td>
<td>Bayesian information criterion</td>
</tr>
</tbody>
</table>

Based on this test, the three-class model, like the two-class model, does not fit worse than the saturated model.

We will compare our three models using AIC and BIC. Smaller values of AIC and BIC are better. We could look back at the AIC and BIC values reported by our three `estat lcgof` commands, but we will instead create a table that reports these information criteria for all three models using `estimates stats`. 
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Akaike’s information criterion and Bayesian information criterion

<table>
<thead>
<tr>
<th>Model</th>
<th>N</th>
<th>ll(null)</th>
<th>ll(model)</th>
<th>df</th>
<th>AIC</th>
<th>BIC</th>
</tr>
</thead>
<tbody>
<tr>
<td>oneclass</td>
<td>216</td>
<td>-543.6498</td>
<td>-543.6498</td>
<td>4</td>
<td>1095.3</td>
<td>1108.801</td>
</tr>
<tr>
<td>twoclass</td>
<td>216</td>
<td>-504.4677</td>
<td>-504.4677</td>
<td>9</td>
<td>1026.935</td>
<td>1057.313</td>
</tr>
<tr>
<td>threeclass</td>
<td>216</td>
<td>-503.3011</td>
<td>-503.3011</td>
<td>14</td>
<td>1034.602</td>
<td>1081.856</td>
</tr>
</tbody>
</table>

Note: BIC uses \( N \) = number of observations. See [R] BIC note.

The two-class model has both the smallest AIC and the smallest BIC.

Reference


Also see

[SEM] Example 50g — Latent class model
[SEM] Intro 5 — Tour of models
[SEM] gsem — Generalized structural equation model estimation command
[SEM] estat lcgof — Latent class goodness-of-fit statistics