Example 50g — Latent class model

Description

To demonstrate latent class models, we use the following data:

```
. use https://www.stata-press.com/data/r16/gsem_lca1
(Latent class analysis)
. describe
Contains data from https://www.stata-press.com/data/r16/gsem_lca1.dta
obs: 216 Latent class analysis
vars: 4 17 Jan 2019 12:52
    (_dta has notes)

    variable name type display value label variable label
      accident byte %9.0g would testify against friend in accident case
      play byte %9.0g would give negative review of friend’s play
      insurance byte %9.0g would disclose health concerns to friend’s insurance company
      stock byte %9.0g would keep company secret from friend

Sorted by: accident play insurance stock
```

```
. notes in 1/4
_dta:
1. Data from Samuel A. Stouffer and Jackson Toby, March 1951, "Role conflict and personality", _The American Journal of Sociology_, vol. 56 no. 5, 395-406.
2. Variables represent responses of students from Harvard and Radcliffe who were asked how they would respond to four situations. Respondents selected either a particularistic response (based on obligations to a friend) or universalistic response (based on obligations to society).
3. Each variable is coded with 0 indicating a particularistic response and 1 indicating a universalistic response.
4. For a full description of the questions, type "notes in 5/8".

See _Latent class models_ in [SEM] Intro 5 for background.
```

Remarks and examples

A latent class model is characterized by having a categorical (rather than continuous) latent variable. The levels of the categorical latent variable represent groups in the population and are called classes. We are interested in identifying and understanding these classes.
Goodman (2002) fits a variety of latent class models to the dataset described above with a focus on understanding how groups of individuals differ in response to situations that require making a decision between helping a friend (a particularistic choice) and doing what is right for society (a universalistic choice). Individuals were asked how they would respond in four such situations, and their responses were recorded in the variables accident, play, insurance, and stock. These variables are coded such that 1 is a universalistic response and 0 is a particularistic response.

To fit a latent class model, we must specify the number of classes in the latent variable. In the basic form of the latent class model demonstrated here, we have one categorical latent variable with two classes. The parameters in the model, namely, the intercepts in logistic regression models for the four observed variables, are allowed to vary across the classes.

More specifically, the model that we will fit estimates an intercept, \( \alpha \), for each observed variable for the first class,

\[
\begin{align*}
\Pr(\text{accident} = 1 \mid C = 1) &= \frac{\exp(\alpha_{11})}{1 + \exp(\alpha_{11})} \\
\Pr(\text{play} = 1 \mid C = 1) &= \frac{\exp(\alpha_{21})}{1 + \exp(\alpha_{21})} \\
\Pr(\text{insurance} = 1 \mid C = 1) &= \frac{\exp(\alpha_{31})}{1 + \exp(\alpha_{31})} \\
\Pr(\text{stock} = 1 \mid C = 1) &= \frac{\exp(\alpha_{41})}{1 + \exp(\alpha_{41})}
\end{align*}
\]

and a corresponding intercept for the second class,

\[
\begin{align*}
\Pr(\text{accident} = 1 \mid C = 2) &= \frac{\exp(\alpha_{12})}{1 + \exp(\alpha_{12})} \\
\Pr(\text{play} = 1 \mid C = 2) &= \frac{\exp(\alpha_{22})}{1 + \exp(\alpha_{22})} \\
\Pr(\text{insurance} = 1 \mid C = 2) &= \frac{\exp(\alpha_{32})}{1 + \exp(\alpha_{32})} \\
\Pr(\text{stock} = 1 \mid C = 2) &= \frac{\exp(\alpha_{42})}{1 + \exp(\alpha_{42})}
\end{align*}
\]

We also estimate the probability of being in each class using multinomial logistic regression,

\[
\begin{align*}
\Pr(C = 1) &= \frac{e^{\gamma_1}}{e^{\gamma_1} + e^{\gamma_2}} \\
\Pr(C = 2) &= \frac{e^{\gamma_2}}{e^{\gamma_1} + e^{\gamma_2}}
\end{align*}
\]

where \( \gamma_1 \) and \( \gamma_2 \) are intercepts in the multinomial logit model. By default, the first class will be treated as the base, so \( \gamma_1 = 0 \).
To fit this model, we type

```
  . gsem (accident play insurance stock <- ), logit lclass(C 2)
```

No variables are listed on the right side of the arrow because we are fitting intercept-only models for each observed variable. `logit` specifies that we are fitting logistic regression models for all four variables. The `lclass(C 2)` option specifies that the name of our categorical latent variable is C and that it has two latent classes.

The result of typing our estimation command is

```
  . gsem (accident play insurance stock <- ), logit lclass(C 2)

  Fitting class model:
  Iteration 0:  (class) log likelihood = -149.71979
  Iteration 1:  (class) log likelihood = -149.71979

  Fitting outcome model:
  Iteration 0:  (outcome) log likelihood = -403.97142
  Iteration 1:  (outcome) log likelihood = -398.15909
  Iteration 2:  (outcome) log likelihood = -397.81953
  Iteration 3:  (outcome) log likelihood = -397.8164
  Iteration 4:  (outcome) log likelihood = -397.8164

  Refining starting values:
  Iteration 0:  (EM) log likelihood = -570.24204
  Iteration 1:  (EM) log likelihood = -576.20485
  Iteration 2:  (EM) log likelihood = -577.41464
  Iteration 3:  (EM) log likelihood = -576.88554
  Iteration 4:  (EM) log likelihood = -575.9242
  Iteration 5:  (EM) log likelihood = -573.90567
  Iteration 6:  (EM) log likelihood = -571.99868
  Iteration 7:  (EM) log likelihood = -569.97482
  Iteration 8:  (EM) log likelihood = -567.90955
  Iteration 9:  (EM) log likelihood = -565.86392
  Iteration 10:  (EM) log likelihood = -563.88815
  Iteration 11:  (EM) log likelihood = -562.02165
  Iteration 12:  (EM) log likelihood = -560.29231
  Iteration 13:  (EM) log likelihood = -558.71641
  Iteration 14:  (EM) log likelihood = -557.29974
  Iteration 15:  (EM) log likelihood = -556.03949
  Iteration 16:  (EM) log likelihood = -554.92679
  Iteration 17:  (EM) log likelihood = -553.94914
  Iteration 18:  (EM) log likelihood = -553.09241
  Iteration 19:  (EM) log likelihood = -552.34233
  Iteration 20:  (EM) log likelihood = -551.68539

  Note: EM algorithm reached maximum iterations.

  Fitting full model:
  Iteration 0:  log likelihood = -504.62913
  Iteration 1:  log likelihood = -504.47255
  Iteration 2:  log likelihood = -504.46773
  Iteration 3:  log likelihood = -504.46767
  Iteration 4:  log likelihood = -504.46767

  Generalized structural equation model
  Number of obs = 216
  Log likelihood = -504.46767

  | Coef.    Std. Err.     z     P>|z|    [95% Conf. Interval] |
  |---------|----------------------|-------|--------|-----------------------------|
  1.C (base outcome)                        |
  2.C _cons     -.9482041  .2886333    -3.29  0.001   -1.513915   -.3824933  |
Example 50g — Latent class model

### Class 1
- **Response:** accident
- **Family:** Bernoulli
- **Link:** logit
- **Response:** play
- **Family:** Bernoulli
- **Link:** logit
- **Response:** insurance
- **Family:** Bernoulli
- **Link:** logit
- **Response:** stock
- **Family:** Bernoulli
- **Link:** logit

|        | Coef.  | Std. Err. | z    | P>|z| | [95% Conf. Interval] |
|--------|--------|-----------|------|------|---------------------|
| accident | _cons | .9128742  | .1974695 | 4.62 | 0.000 | .5258411 - 1.299907 |
| play    | _cons | -.7099072 | .2249096 | -3.16| 0.002 | -1.150722 - .2690926 |
| insurance| _cons | -.6014307 | .2123096 | -2.83| 0.005 | -1.01755 - .1853115  |
| stock   | _cons | -1.880142 | .3337665 | -5.63| 0.000 | -2.534312 -1.225972 |

### Class 2
- **Response:** accident
- **Family:** Bernoulli
- **Link:** logit
- **Response:** play
- **Family:** Bernoulli
- **Link:** logit
- **Response:** insurance
- **Family:** Bernoulli
- **Link:** logit
- **Response:** stock
- **Family:** Bernoulli
- **Link:** logit

|        | Coef.  | Std. Err. | z    | P>|z| | [95% Conf. Interval] |
|--------|--------|-----------|------|------|---------------------|
| accident | _cons | 4.983017  | 3.745987 | 1.33 | 0.183 | -2.358982 - 12.32502 |
| play    | _cons | 2.747366  | 1.165853 | 2.36 | 0.018 | .4623372 - 5.032395 |
| insurance| _cons | 2.534582  | .9644841 | 2.63 | 0.009 | .6442279 - 4.424936  |
| stock   | _cons | 1.203416  | .5361735 | 2.24 | 0.025 | .1525356 - 2.254297 |
Notes:

1. The output shows four iteration logs. The first three are for models that are fit to obtain good starting values. Starting values are challenging for latent class models, and `gsem` provides a variety of options for specifying and computing starting values. See `SEM gsem estimation options` and `SEM Intro 12` for more information on these options.

2. The first table in the output provides the estimated coefficients in the multinomial logit model for C.

3. The next two tables are the results for the logistic regression models for the first and second classes.

To better understand this model, let’s examine how the probabilities of giving a universalistic response differ across classes. The `estat lcmean` command reports class-specific marginal means for each variable. Because we are using logistic regression, these means are actually the predicted probabilities.

```
. estat lcmean
Latent class marginal means Number of obs = 216

Delta-method                         [95% Conf. Interval]

<table>
<thead>
<tr>
<th>Marg</th>
<th>Std. Err.</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
 1     | accident | .7135879 | .0403588 | .6285126 | .7858194 |
      | play     | .3296193 | .0496984 | .2403573 | .4331299 |
      | insurance| .3540164 | .0485528 | .2655049 | .4538042 |
      | stock    | .1323726 | .0383331 | .0734875 | .2268872 |
 2     | accident | .9931933 | .0253243 | .9999956 |          |
      | play     | .9397644 | .0659957 | .935191  |          |
      | insurance| .9265309 | .0656538 | .9881667 |          |
      | stock    | .769132  | .0952072 | .6538061 | .9050206 |
```

The first section of this table reports the probabilities for class 1. In this class, the probability of giving a universalistic response to the first question—the question that concerns testifying against a friend who was involved in an accident—is 0.714. The probability of giving a universalistic response to the last question—the question about warning a friend about a stock price that is about to fall—is 0.132.

The second section of the table reports the corresponding probabilities for class 2. We find that the probability of giving a universalistic response to each question is higher in class 2 than in class 1. Class 2 appears to represent a more universalistically inclined group.

We can estimate probabilities of being in each class using `estat lcprob`.

```
. estat lcprob
Latent class marginal probabilities Number of obs = 216

Delta-method                         [95% Conf. Interval]

<table>
<thead>
<tr>
<th>Marg</th>
<th>Std. Err.</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
  C     | 1        | .7207539 | .0580926 | .5944743 | .8196407 |
      | 2        | .2792461 | .0580926 | .1803593 | .4055257 |
```
This indicates that 72% of individuals are expected to be in the less universalistic class and 28% are expected to be in the more universalistic class.

We can use the predictions of the posterior probability of class membership to evaluate an individual’s probability of being in each class.

\[
\text{predict classpost*, classposteriorpr}
\]

\[
\text{list in 1, abbrev(10)}
\]

<table>
<thead>
<tr>
<th>accident</th>
<th>play</th>
<th>insurance</th>
<th>stock</th>
<th>classpost1</th>
<th>classpost2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>.999975</td>
<td>.000025</td>
</tr>
</tbody>
</table>

For the first individual in our dataset, who responded with a particularistic answer to all four questions, the probability of being in class 1, the less universalistic class, is almost 1.

We can determine the expected class for each individual based on whether the posterior probability is greater than 0.5.

\[
\text{generate expclass = 1 + (classpost2>0.5)}
\]

\[
\text{tabulate expclass}
\]

<table>
<thead>
<tr>
<th>expclass</th>
<th>Freq.</th>
<th>Percent</th>
<th>Cum.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>145</td>
<td>67.13%</td>
<td>67.13%</td>
</tr>
<tr>
<td>2</td>
<td>71</td>
<td>32.87%</td>
<td>100.00%</td>
</tr>
</tbody>
</table>

In our dataset, 145 individuals are expected to be in class 1 and 71 individuals are expected to be in class 2.

References


Also see

[SEM] Example 51g — Latent class goodness-of-fit statistics
[SEM] Example 52g — Latent profile model
[SEM] Intro 5 — Tour of models
[SEM] gsem — Generalized structural equation model estimation command
[SEM] estat icmean — Latent class marginal means
[SEM] estat icprob — Latent class marginal probabilities