zinb — Zero-inflated negative binomial regression

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Description

zinb fits a zero-inflated negative binomial (ZINB) model to overdispersed count data with excess zero counts. The ZINB model assumes that the excess zero counts come from a logit or probit model and the remaining counts come from a negative binomial model.

Quick start

Zero-inflated negative binomial model of y on x1 and x2 with inflation modeled using x3 zinb y x1 x2, inflate(x3)

And conduct likelihood-ratio test against ZIP model

zinb y x1 x2, inflate(x3) zip

Use a probit model instead of a logit model to predict excess zeros zinb y x1 x2, inflate(x3) probit

Menu

Statistics > Count outcomes > Zero-inflated negative binomial regression

Syntax

zinb depvar [indepvars] [if] [in] [weight],

inflate(varlist[, offset(varname)]|_cons)[options]

options	Description
Model	
* <u>inf</u> late()	equation that determines whether the count is zero
<u>nocons</u> tant	suppress constant term
$exposure(varname_e)$	include $ln(varname_e)$ in model with coefficient constrained to 1
$\underline{off}set(varname_o)$	include varname _o in model with coefficient constrained to 1
<pre><u>const</u>raints(constraints)</pre>	apply specified linear constraints
probit	use probit model to characterize excess zeros; default is logit
SE/Robust	
vce(<i>vcetype</i>)	<pre>vcetype may be oim, robust, cluster clustvar, opg, bootstrap, or jackhnife</pre>
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
irr	report incidence-rate ratios
zip	perform ZIP likelihood-ratio test
<u>nocnsr</u> eport	do not display constraints
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
maximize_options	control the maximization process; seldom used
<u>col</u> linear	keep collinear variables
<u>coefl</u> egend	display legend instead of statistics

*<u>inf</u>late(*varlist*[, <u>off</u>set(*varname*)]|_cons) is required.

indepvars and varlist may contain factor variables; see [U] 11.4.3 Factor variables.

bayes, bayesboot, bootstrap, by, collect, fp, jackknife, rolling, statsby, and svy are allowed; see [U] 11.1.10 Prefix commands. For more details, see [BAYES] bayes: zinb.

Weights are not allowed with the bootstrap prefix; see [R] bootstrap.

vce(), zip, and weights are not allowed with the svy prefix; see [SVY] svy.

fweights, iweights, and pweights are allowed; see [U] 11.1.6 weight.

collinear and coeflegend do not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

Model

inflate(varlist[, offset(varname)]|_cons) specifies the equation that determines whether the observed count is zero. Conceptually, omitting inflate() would be equivalent to fitting the model with nbreg.

inflate(*varlist*[, offset(*varname*)]) specifies the variables in the equation. You may optionally include an offset for this *varlist*.

inflate(_cons) specifies that the equation determining whether the count is zero contains only an intercept. To run a zero-inflated model of *depvar* with only an intercept in both equations, type zinb *depvar*, inflate(_cons).

```
noconstant, exposure(varname_e), offset(varname_o), constraints(constraints); see [R] Estimation options.
```

probit requests that a probit, instead of logit, model be used to characterize the excess zeros in the data.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (oim, opg), that are robust to some kinds of misspecification (robust), that allow for intragroup correlation (cluster *clustvar*), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [R] vce_option.

Reporting

level(#); see [R] Estimation options.

- irr reports estimated coefficients transformed to incidence-rate ratios, that is, e^{β_i} rather than β_i . Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated or stored. irr may be specified at estimation or when replaying previously estimated results.
- zip requests that a likelihood-ratio test comparing the ZINB model with the zero-inflated Poisson model be included in the output.

nocnsreport; see [R] Estimation options.

display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(%fmt), pformat(%fmt), sformat(%fmt), and nolstretch; see [R] Estimation options.

Maximization

maximize_options: difficult, technique(algorithm_spec), iterate(#), [no]log, trace, gradient, showstep, hessian, showtolerance, tolerance(#), ltolerance(#), nrtolerance(#), nonrtolerance, and from(init_specs); see [R] Maximize. These options are seldom used.

Setting the optimization type to technique(bhhh) resets the default vcetype to vce(opg).

The following options are available with zinb but are not shown in the dialog box:

collinear, coeflegend; see [R] Estimation options.

Remarks and examples

Zero-inflated negative binomial (ZINB) models are used to model count data that have a higher fraction of zeros than is likely to be generated by a standard negative binomial model. To account for excess zeros, ZINB models assume that these excess zeros come from a model other than the negative binomial model. A zero that comes from this other model is known as a "degenerate zero".

The negative binomial overdispersion parameter, α , differentiates the ZINB model from the zeroinflated Poisson (ZIP) model (see [R] zip). Here overdispersion refers to the fact that the negative binomial variance is greater than its mean, whereas the Poisson variance is equal to its mean. Thus, values of $\alpha > 1$ indicate overdispersion. The larger the α , the greater the negative binomial variance. See *Methods and formulas* in [R] **nbreg** for further discussion of negative binomial overdispersion.

The zinb command fits ZINB models and provides two choices for modeling the excess zeros: the default logit function or, when the probit option is specified, the probit function. Both functions are symmetric about zero, but the logistic function has more area under the tails.

See Long (1997, 242-247) and Cameron and Trivedi (2005, 680-681) for a discussion of zero-modified count models.

Example 1: Fitting a ZINB model

In example 1 of [R] zip, we fit a zero-inflated Poisson model using the zip command to the fictional data on the number of fish caught by visitors to a national park. Let's fit a ZINB model to these data.

Just like with zip, we use the required the inflate() option to model whether a visitor fishes as a function of the number of accompanying children (child) and whether the visitor is camping (camper). Next, we assume the response variable, count, depends on whether the visitor used a live bait (livebait) and the number of persons in the party (persons), which includes the visitor plus other adults and children.

. use https:// (Fictional fis		ss.com/data/	/r19/fish			
. zinb count p	ersons liveba	it, inflate	(child ca	mper)		
Fitting consta	nt-only model	:				
Iteration 0: Iteration 1: Iteration 2: Iteration 3: Iteration 4: Iteration 5: Iteration 6: Iteration 7: Iteration 8: Fitting full m Iteration 0: Iteration 1: Iteration 2: Iteration 3: Iteration 4: Iteration 5:	Log likelihoo Log likelihoo	d = -519.333 $d = -451.386$ $d = -442.962$ $d = -442.962$ $d = -442.662$	562 118 272 565 531 299 299 299 (not 107 (not 334 586 013	concave concave		
Iteration 7:	el: logit	d = -401.547 d = -401.547	776 776		Number of ob Nonzero obs Zero obs LR chi2(2) Prob > chi2	s = 250 = 108 = 142 = 82.23 = 0.0000
count	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
count						
persons livebait _cons	.9742984 1.557523 -2.730064	.1034938 .4124424 .476953	9.41 3.78 -5.72	0.000 0.000 0.000	.7714543 .7491503 -3.664874	2.365895
persons livebait	1.557523	.4124424	3.78	0.000	.7491503	2.365895 -1.795253 4.649808 3117567
persons livebait _cons inflate child camper	1.557523 -2.730064 3.185999 -2.020951	.4124424 .476953 .7468551 .872054	3.78 -5.72 4.27 -2.32	0.000 0.000 0.000 0.020	.7491503 -3.664874 1.72219 -3.730146	1.177142 2.365895 -1.795253 4.649808 3117567 9453189 .8671323

The coefficients in the first equation of the coefficient table, labeled count, correspond to the negative binomial model for individuals who fished. For instance, among visitors who fished, using a live bait increases the expected number of caught fish by a factor of $\exp(1.5575) \approx 4.7$, holding other covariates constant.

The confidence interval for alpha indicates that the ZINB model is more appropriate than the ZIP model. To confirm this, you can run zinb and specify the zip option to obtain the ZIP likelihood-ratio test.

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The inflate equation models whether the visitor does not fish. We can use margins to obtain a better understanding of how the inflate equation affects the occurrence of the excess zero counts. We specify margins's options dydx(child camper) and predict(pr). pr is predict's option for estimating the probability of a degenerate zero or, in our example, the probability of not fishing; see the *margins* section in [R] **zinb postestimation**.

```
. margins, dydx(child camper) predict(pr)
Average marginal effects Number of obs = 250
Model VCE: OIM
Expression: Pr(count=0), predict(pr)
dy/dx wrt: child camper
Delta-method
dy/dx std. err. z P>|z| [95% conf. interval]
```

 62144 45878

The margins output tells us that a visitor is less likely to be visiting the park to fish if accompanied by children and more likely to fish if camping.

You also may want to evaluate whether a standard negative binomial model is adequate to fit the data. This can be done using information criteria; see example 2 in [R] zip.

Stored results

zinb stores the following in e():

Scal	ars	
	e(N)	number of observations
e(N_zero)		number of zero observations
e(k)		number of parameters
e(k_eq)		number of equations in e(b)
	e(k_eq_model)	number of equations in overall model test
	e(k_aux)	number of auxiliary parameters
	e(k_dv)	number of dependent variables
	e(df_m)	model degrees of freedom
	e(11)	log likelihood
	e(11_0)	log likelihood, constant-only model
	e(df_c)	degrees of freedom for comparison test
	e(N_clust)	number of clusters
	e(chi2)	χ^2
	e(p)	<i>p</i> -value for model test
	e(chi2_cp)	χ^2 for test of $\alpha = 0$
	e(rank)	rank of e(V)
	e(ic)	number of iterations
	e(rc)	return code
	e(converged)	1 if converged, 0 otherwise
Mac	ros	
	e(cmd)	zinb
	e(cmdline)	command as typed
	e(depvar)	name of dependent variable
	e(inflate)	logit or probit
	e(wtype)	weight type
	e(wexp)	weight expression

	e(title)	title in estimation output
	e(clustvar)	name of cluster variable
	e(offset1)	offset
	e(offset2)	offset for inflate()
	e(chi2type)	Wald or LR; type of model χ^2 test
	e(chi2_cpt)	Wald or LR; type of model χ^2 test corresponding to e(chi2_cp)
	e(vce)	vcetype specified in vce()
	e(vcetype)	title used to label Std. err.
	e(opt)	type of optimization
	e(which)	max or min; whether optimizer is to perform maximization or minimization
	e(ml_method)	type of ml method
	e(user)	name of likelihood-evaluator program
	e(technique)	maximization technique
	e(properties)	b V
	e(predict)	program used to implement predict
	e(asbalanced)	factor variables fvset as asbalanced
	e(asobserved)	factor variables fvset as asobserved
Mat	rices	
	e(b)	coefficient vector
	e(Cns)	constraints matrix
	e(ilog)	iteration log (up to 20 iterations)
	e(gradient)	gradient vector
	e(V)	variance-covariance matrix of the estimators
	e(V_modelbased)	model-based variance
Fun	ctions	
	e(sample)	marks estimation sample
	-	*

In addition to the above, the following is stored in r():

Matrices

r(table) matrix conta

matrix containing the coefficients with their standard errors, test statistics, *p*-values, and confidence intervals

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

Methods and formulas

The zinb command maximizes a likelihood function that is a mixture of the logistic (or probit) and negative binomial distributions. The logistic distribution models the unobserved process that creates the excess zeros, and the negative binomial distribution models the counts. Define

```
\begin{split} \xi_j^\beta &= \mathbf{x}_j \boldsymbol{\beta} + \mathrm{offset}_j^\beta \\ \xi_j^\gamma &= \mathbf{z}_j \boldsymbol{\gamma} + \mathrm{offset}_j^\gamma \\ \mu_j &= \exp(\xi_j^\beta) \\ p_j &= 1/(1+\alpha\mu_j) \\ m &= 1/\alpha \end{split}
```

Here the vector \mathbf{x}_j contains the covariates specified in *indepvars* for the *j*th observation, and \mathbf{z}_j contains the covariates specified in the inflate() option. Similarly, estimates for β are found in the first equation of the zinb coefficient table (labeled after *depvar*), and the estimates for γ are found in the second equation of the coefficient table (labeled inflate). The parameter α is the negative binomial

overdispersion parameter, and its estimate is the ancillary parameter labeled alpha in the coefficient table. Parameters p_j , m, and μ_j are parameters of a negative binomial distribution; see Methods and formulas in [R] **nbreg** for details.

The log likelihood maximized by zinb is

$$\begin{split} \ln L &= \sum_{j \in S} w_j \ln \left\{ F_j + (1-F_j) p_j^m \right\} + \\ &\sum_{j \notin S} w_j \Big\{ \ln(1-F_j) + \ln \Gamma(m+y_j) - \ln \Gamma(y_j+1) \\ &- \ln \Gamma(m) + m \ln p_j + y_j \ln(1-p_j) \Big\} \end{split}$$

where w_j are the weights, S is the set of observations for which the observed outcome $y_j = 0$, and F_j is the logistic distribution function

$$F_j = F(\xi_j^\gamma) = \exp(\xi_j^\gamma) / \{1 + \exp(\xi_j^\gamma)\}$$

or, if the probit option is specified, the standard normal distribution function

$$F_j = F(\xi_j^\gamma) = \Phi(\xi_j^\gamma)$$

From Long (1997), the variance of the mixture distribution is

$$\operatorname{Var}(y_j | \mathbf{x}_i, \mathbf{z}_i) = \mu_j (1 - F_j) \{ 1 + \mu_j (F_j + \alpha) \}$$

When F_j is zero, we have the variance of the negative binomial distribution; when $F_j > 0$, the variance can exceed that of the negative binomial distribution.

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using vce(robust) and vce(cluster *clustvar*), respectively. See [P] **_robust**, particularly *Maximum likelihood estimators* and *Methods and formulas*.

zinb also supports estimation with survey data. For details on VCEs with survey data, see [SVY] Variance estimation.

References

- Cameron, A. C., and P. K. Trivedi. 2005. *Microeconometrics: Methods and Applications*. New York: Cambridge University Press.
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Xia, Y., Y. Zhou, and T. Cai. 2019. gidm: A command for generalized inflated discrete models. Stata Journal 19: 698-718.

Also see

- [R] zinb postestimation Postestimation tools for zinb
- [R] zip Zero-inflated Poisson regression
- [R] nbreg Negative binomial regression
- [R] poisson Poisson regression
- [R] tnbreg Truncated negative binomial regression
- [R] tpoisson Truncated Poisson regression
- [BAYES] bayes: zinb Bayesian zero-inflated negative binomial regression
- [SVY] svy estimation Estimation commands for survey data
- [XT] xtnbreg Fixed-effects, random-effects, & population-averaged negative binomial models
- [U] 20 Estimation and postestimation commands

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