Title

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tnbreg — Truncated negative binomial regression

Description

`tnbreg` estimates the parameters of a truncated negative binomial model by maximum likelihood. The dependent variable *depvar* is regressed on *indepvars*, where *depvar* is a positive count variable whose values are all above the truncation point.

Quick start

Truncated negative binomial regression of `y` on `x` with truncation at 0

```
tnbreg y x
```

Report incidence-rate ratios

```
tnbreg y x, irr
```

Add categorical variable `a` using factor variable syntax

```
tnbreg y x i.a
```

As above, but specify a constant truncation point of 2

```
tnbreg y x i.a, ll(2)
```

With exposure variable `exp`

```
tnbreg y x i.a, exposure(exp)
```

As above, but specifying a variable truncation point stored in variable `min`

```
tnbreg y x i.a, exposure(exp) ll(min)
```

With cluster–robust standard errors clustering by the levels of `cvar`

```
tnbreg y x i.a, exposure(exp) ll(min) vce(cluster cvar)
```

Menu

Statistics > Count outcomes > Truncated negative binomial regression

Syntax

```
tnbreg depvar [indepvars] [if] [in] [weight] [, options]
```

options	Description
Model	
noconstant	suppress constant term
ll(# | *varname*)	truncation point; default value is ll(0), zero truncation
dispersion(mean)	parameterization of dispersion; the default
dispersion(constant)	constant dispersion for all observations
exposure(*varname*$_e$)	include ln(*varname*$_e$) in model with coefficient constrained to 1
offset(*varname*$_o$)	include *varname*$_o$ in model with coefficient constrained to 1
constraints(*constraints*)	apply specified linear constraints
SE/Robust	
vce(*vcetype*)	*vcetype* may be oim, robust, cluster *clustvar*, opg, bootstrap, or jackknife
Reporting	
level(#)	set confidence level; default is level(95)
nolrtest	suppress likelihood-ratio test
irr	report incidence-rate ratios
nocnsreport	do not display constraints
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
maximize_options	control the maximization process; seldom used
collinear	keep collinear variables
coeflegend	display legend instead of statistics

indepvars may contain factor variables; see [U] **11.4.3 Factor variables**.

depvar and *indepvars* may contain time-series operators; see [U] **11.4.4 Time-series varlists**.

bayes, bootstrap, by, fp, jackknife, rolling, statsby, and svy are allowed; see [U] **11.1.10 Prefix commands**. For more details, see [BAYES] **bayes: tnbreg**.

Weights are not allowed with the bootstrap prefix; see [R] **bootstrap**.

vce() and weights are not allowed with the svy prefix; see [SVY] **svy**.

fweights, iweights, and pweights are allowed; see [U] **11.1.6 weight**.

collinear and coeflegend do not appear in the dialog box.

See [U] **20 Estimation and postestimation commands** for more capabilities of estimation commands.

Options

Model

noconstant; see [R] **Estimation options**.

ll(# | *varname*) specifies the truncation point, which is a nonnegative integer. The default is zero truncation, ll(0).

`dispersion(mean | constant)` specifies the parameterization of the model. `dispersion(mean)`, the default, yields a model with dispersion equal to $1+\alpha\exp(\mathbf{x}_j\boldsymbol{\beta}+\text{offset}_j)$; that is, the dispersion is a function of the expected mean: $\exp(\mathbf{x}_j\boldsymbol{\beta}+\text{offset}_j)$. `dispersion(constant)` has dispersion equal to $1+\delta$; that is, it is a constant for all observations.

`exposure(`*varname*$_e$`)`, `offset(`*varname*$_o$`)`, `constraints(`*constraints*`)`; see [R] **Estimation options**.

SE/Robust

`vce(`*vcetype*`)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`, `opg`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster` *clustvar*), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] ***vce_option***.

Reporting

`level(#)`; see [R] **Estimation options**.

`nolrtest` suppresses fitting the Poisson model. Without this option, a comparison Poisson model is fit, and the likelihood is used in a likelihood-ratio test of the null hypothesis that the dispersion parameter is zero.

`irr` reports estimated coefficients transformed to incidence-rate ratios, that is, e^{β_i} rather than β_i. Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated or stored. `irr` may be specified at estimation or when replaying previously estimated results.

`nocnsreport`; see [R] **Estimation options**.

display_options: `noci`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(`*style*`)`, `cformat(%`*fmt*`)`, `pformat(%`*fmt*`)`, `sformat(%`*fmt*`)`, and `nolstretch`; see [R] **Estimation options**.

Maximization

maximize_options: `difficult`, `technique(`*algorithm_spec*`)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(`*init_specs*`)`; see [R] **Maximize**. These options are seldom used.

Setting the optimization type to `technique(bhhh)` resets the default *vcetype* to `vce(opg)`.

The following options are available with `tnbreg` but are not shown in the dialog box:

`collinear`, `coeflegend`; see [R] **Estimation options**.

Remarks and examples

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Grogger and Carson (1991) showed that overdispersion causes inconsistent estimation of the mean in the truncated Poisson model. To solve this problem, they proposed using the truncated negative binomial model as an alternative. If data are truncated but do not exhibit overdispersion, the truncated Poisson model is more appropriate; see [R] **tpoisson**. For an introduction to negative binomial regression, see Cameron and Trivedi (2005, 2010) and Long and Freese (2014). For an introduction to truncated negative binomial models, see Cameron and Trivedi (2013) and Long (1997, chap. 8).

tnbreg fits the mean-dispersion and the constant-dispersion parameterizations of truncated negative binomial models. These parameterizations extend those implemented in nbreg; see [R] **nbreg**.

▷ Example 1

We illustrate the truncated negative binomial model using the 1997 MedPar dataset (Hilbe 1999). The data are from 1,495 patients in Arizona who were assigned to a diagnostic-related group (DRG) of patients having a ventilator. Length of stay (los), the dependent variable, is a positive integer; it cannot have zero values. The data are truncated because there are no observations on individuals who stayed for zero days.

The objective of this example is to determine whether the length of stay was related to the binary variables: died, hmo, type1, type2, and type3.

The died variable was recorded as a 0 unless the patient died, in which case, it was recorded as a 1. The other variables also adopted this encoding. The hmo variable was set to 1 if the patient belonged to a health maintenance organization (HMO).

The type1–type3 variables indicated the type of admission used for the patient. The type1 variable indicated an emergency admit. The type2 variable indicated an urgent admit—that is, the first available bed. The type3 variable indicated an elective admission. Because type1–type3 were mutually exclusive, only two of the three could be used in the truncated negative binomial regression shown below.

```
. use https://www.stata-press.com/data/r16/medpar
. tnbreg los died hmo type2-type3, vce(cluster provnum) nolog
Truncated negative binomial regression          Number of obs     =      1,495
Truncation point: 0                             Wald chi2(4)      =      36.01
Dispersion          = mean                      Prob > chi2       =     0.0000
Log pseudolikelihood =  -4737.535               Pseudo R2         =     0.0139
                                (Std. Err. adjusted for 54 clusters in provnum)
```

los	Coef.	Robust Std. Err.	z	P>|z|	[95% Conf.	Interval]
died	-.2521884	.061533	-4.10	0.000	-.3727908	-.1315859
hmo	-.0754173	.0533132	-1.41	0.157	-.1799091	.0290746
type2	.2685095	.0666474	4.03	0.000	.137883	.3991359
type3	.7668101	.2183505	3.51	0.000	.338851	1.194769
_cons	2.224028	.034727	64.04	0.000	2.155964	2.292091
/lnalpha	-.630108	.0764019			-.779853	-.480363
alpha	.5325343	.0406866			.4584734	.6185588

Because observations within the same hospital (provnum) are likely to be correlated, we specified the vce(cluster provnum) option. The results show that whether the patient died in the hospital and the type of admission have significant effects on the patient's length of stay.

◁

▷ Example 2

To illustrate truncated negative binomial regression with more complex data than the previous example, similar data were created from 100 hospitals. Each hospital had its own way of tracking patient data. In particular, hospitals only recorded data from patients with a minimum length of stay, denoted by the variable minstay.

Definitions for minimum length of stay varied among hospitals, typically, from 5 to 18 days. The objective of this example is the same as before: to determine whether the length of stay, recorded in `los`, was related to the binary variables: `died`, `hmo`, `type1`, `type2`, and `type3`.

The binary variables encode the same information as in example 1 above. The `minstay` variable was used to allow for varying truncation points.

```
. use https://www.stata-press.com/data/r16/medproviders
. tnbreg los died hmo type2-type3, ll(minstay) vce(cluster hospital) nolog
Truncated negative binomial regression          Number of obs     =      2,144
Truncation points: minstay                      Wald chi2(4)      =      15.22
Dispersion           = mean                     Prob > chi2       =     0.0043
Log pseudolikelihood = -7864.0928               Pseudo R2         =     0.0007
                              (Std. Err. adjusted for 100 clusters in hospital)
------------------------------------------------------------------------------
             |               Robust
         los |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-------------+----------------------------------------------------------------
        died |    .078104   .0303598     2.57   0.010     .0185998    .1376081
         hmo |  -.0731132   .0368897    -1.98   0.047    -.1454158   -.0008107
       type2 |    .0294132   .0390166     0.75   0.451     -.047058    .1058845
       type3 |    .0626348   .0540123     1.16   0.246    -.0432273     .168497
       _cons |    3.014964   .0290895   103.64   0.000      2.95795    3.071978
-------------+----------------------------------------------------------------
    /lnalpha |   -.996512   .0828691                     -1.158932   -.8340916
-------------+----------------------------------------------------------------
       alpha |    .3691649   .0305923                      .313821    .4342688
------------------------------------------------------------------------------
```

In this analysis, two variables have a statistically significant relationship with length of stay. On average, patients who died in the hospital had longer lengths of stay ($p = 0.01$). Because the coefficient for HMO is negative, that is, $b_{\text{HMO}} = -0.073$, on average, patients who were insured by an HMO had shorter lengths of stay ($p = 0.047$). The type of admission was not statistically significant ($p > 0.05$).

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Stored results

tnbreg stores the following in e():

Scalars

e(N)	number of observations
e(k)	number of parameters
e(k_aux)	number of auxiliary parameters
e(k_eq)	number of equations in e(b)
e(k_eq_model)	number of equations in overall model test
e(k_dv)	number of dependent variables
e(df_m)	model degrees of freedom
e(r2_p)	pseudo-R^2
e(ll)	log likelihood
e(ll_0)	log likelihood, constant-only model
e(ll_c)	log likelihood, comparison model
e(alpha)	value of alpha
e(delta)	value of delta
e(N_clust)	number of clusters
e(chi2)	χ^2
e(chi2_c)	χ^2 for comparison test
e(p)	p-value for model test
e(rank)	rank of e(V)
e(rank0)	rank of e(V) for constant-only model
e(ic)	number of iterations
e(rc)	return code
e(converged)	1 if converged, 0 otherwise

Macros

e(cmd)	tnbreg
e(cmdline)	command as typed
e(depvar)	name of dependent variable
e(llopt)	contents of ll(), or 0 if not specified
e(wtype)	weight type
e(wexp)	weight expression
e(title)	title in estimation output
e(clustvar)	name of cluster variable
e(offset)	linear offset variable
e(chi2type)	Wald or LR; type of model χ^2 test
e(chi2_ct)	Wald or LR; type of model χ^2 test corresponding to e(chi2_c)
e(dispers)	mean or constant
e(vce)	*vcetype* specified in vce()
e(vcetype)	title used to label Std. Err.
e(opt)	type of optimization
e(which)	max or min; whether optimizer is to perform maximization or minimization
e(ml_method)	type of ml method
e(user)	name of likelihood-evaluator program
e(technique)	maximization technique
e(properties)	b V
e(predict)	program used to implement predict
e(asbalanced)	factor variables fvset as asbalanced
e(asobserved)	factor variables fvset as asobserved

Matrices

e(b)	coefficient vector
e(Cns)	constraints matrix
e(ilog)	iteration log (up to 20 iterations)
e(gradient)	gradient vector
e(V)	variance–covariance matrix of the estimators
e(V_modelbased)	model-based variance

Functions

e(sample)	marks estimation sample

In addition to the above, the following is stored in r():

Matrices
r(table) matrix containing the coefficients with their standard errors, test statistics, p-values, and confidence intervals

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

Methods and formulas

Methods and formulas are presented under the following headings:

Mean-dispersion model

A negative binomial distribution can be regarded as a gamma mixture of Poisson random variables. The number of times an event occurs, y_j, is distributed as Poisson$(\nu_j\mu_j)$. That is, its conditional likelihood is

$$f(y_j \mid \nu_j) = \frac{(\nu_j\mu_j)^{y_j} e^{-\nu_j\mu_j}}{\Gamma(y_j+1)}$$

where $\mu_j = \exp(\mathbf{x}_j\boldsymbol{\beta} + \text{offset}_j)$ and ν_j is an unobserved parameter with a Gamma$(1/\alpha, \alpha)$ density:

$$g(\nu) = \frac{\nu^{(1-\alpha)/\alpha} e^{-\nu/\alpha}}{\alpha^{1/\alpha}\Gamma(1/\alpha)}$$

This gamma distribution has a mean of 1 and a variance of α, where α is our ancillary parameter.

The unconditional likelihood for the jth observation is therefore

$$f(y_j) = \int_0^\infty f(y_j \mid \nu) g(\nu)\, d\nu = \frac{\Gamma(m+y_j)}{\Gamma(y_j+1)\Gamma(m)}\, p_j^m (1-p_j)^{y_j}$$

where $p_j = 1/(1+\alpha\mu_j)$ and $m = 1/\alpha$. Solutions for α are handled by searching for $\ln\alpha$ because α must be greater than zero. The conditional probability of observing y_j events given that y_j is greater than the truncation point τ_j is

$$\Pr(Y = y_j \mid y_j > \tau_j, \mathbf{x}_j) = \frac{f(y_j)}{\Pr(Y > \tau_j \mid \mathbf{x}_j)}$$

The log likelihood (with weights w_j and offsets) is given by

$$m = 1/\alpha \qquad p_j = 1/(1+\alpha\mu_j) \qquad \mu_j = \exp(\mathbf{x}_j\boldsymbol{\beta} + \text{offset}_j)$$

$$\ln L = \sum_{j=1}^{n} w_j \Big[\ln\{\Gamma(m+y_j)\} - \ln\{\Gamma(y_j+1)\} - \ln\{\Gamma(m)\} + m\ln(p_j) + y_j\ln(1-p_j) - \ln\{\Pr(Y > \tau_j \mid p_j, m)\} \Big]$$

Constant-dispersion model

The constant-dispersion model assumes that y_j is conditionally distributed as Poisson(μ_j^*), where $\mu_j^* \sim$ Gamma$(\mu_j/\delta, \delta)$ for some dispersion parameter δ [by contrast, the mean-dispersion model assumes that $\mu_j^* \sim$ Gamma$(1/\alpha, \alpha\mu_j)$]. The log likelihood is given by

$$m_j = \mu_j/\delta \qquad p = 1/(1+\delta)$$

$$\ln L = \sum_{j=1}^{n} w_j \Big[\ln\{\Gamma(m_j + y_j)\} - \ln\{\Gamma(y_j + 1)\} - \ln\{\Gamma(m_j)\} + m_j \ln(p) + y_j \ln(1-p) - \ln\{\Pr(Y > \tau_j \,|\, p, m_j)\} \Big]$$

with everything else defined as shown above in the calculations for the mean-dispersion model.

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using `vce(robust)` and `vce(cluster` *clustvar*`)`, respectively. See [P] **_robust**, particularly *Maximum likelihood estimators* and *Methods and formulas*.

`tnbreg` also supports estimation with survey data. For details on VCEs with survey data, see [SVY] **Variance estimation**.

Acknowledgment

We gratefully acknowledge the previous work by Joseph Hilbe (1944–2017) (1999), a former editor of the *Stata Technical Bulletin* and coauthor of the Stata Press book *Generalized Linear Models and Extensions*.

References

Cameron, A. C., and P. K. Trivedi. 2005. *Microeconometrics: Methods and Applications*. New York: Cambridge University Press.

——. 2010. *Microeconometrics Using Stata*. Rev. ed. College Station, TX: Stata Press.

——. 2013. *Regression Analysis of Count Data*. 2nd ed. New York: Cambridge University Press.

Grogger, J. T., and R. T. Carson. 1991. Models for truncated counts. *Journal of Applied Econometrics* 6: 225–238.

Hardin, J. W., and J. M. Hilbe. 2015. Regression models for count data from truncated distributions. *Stata Journal* 15: 226–246.

Hilbe, J. M. 1999. sg102: Zero-truncated Poisson and negative binomial regression. *Stata Technical Bulletin* 47: 37–40. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 233–236. College Station, TX: Stata Press.

Long, J. S. 1997. *Regression Models for Categorical and Limited Dependent Variables*. Thousand Oaks, CA: SAGE.

Long, J. S., and J. Freese. 2014. *Regression Models for Categorical Dependent Variables Using Stata*. 3rd ed. College Station, TX: Stata Press.

Simonoff, J. S. 2003. *Analyzing Categorical Data*. New York: Springer.

Also see

[R] **tnbreg postestimation** — Postestimation tools for tnbreg

[R] **nbreg** — Negative binomial regression

[R] **poisson** — Poisson regression

[R] **tpoisson** — Truncated Poisson regression

[R] **zinb** — Zero-inflated negative binomial regression

[R] **zip** — Zero-inflated Poisson regression

[BAYES] **bayes: tnbreg** — Bayesian truncated negative binomial regression

[SVY] **svy estimation** — Estimation commands for survey data

[XT] **xtnbreg** — Fixed-effects, random-effects, & population-averaged negative binomial models

[U] **20 Estimation and postestimation commands**