roccomp — Tests of equality of ROC areas

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Description

roccomp and rocgold are used to perform receiver operating characteristic (ROC) analyses with rating and discrete classification data.

The two variables *refvar* and *classvar* must be numeric. The reference variable indicates the true state of the observation, such as diseased and nondiseased or normal and abnormal, and must be coded as 0 and 1. The rating or outcome of the diagnostic test or test modality is recorded in *classvar*, which must be at least ordinal, with higher values indicating higher risk.

roccomp tests the equality of two or more ROC areas obtained from applying two or more test modalities to the same sample or to independent samples. roccomp expects the data to be in wide form when comparing areas estimated from the same sample and in long form for areas estimated from independent samples.

rocgold independently tests the equality of the ROC area of each of several test modalities, specified by *classvar*, against a "gold standard" ROC curve, *goldvar*. For each comparison, rocgold reports the raw and the Bonferroni-adjusted *p*-value. Optionally, Šidák's adjustment for multiple comparisons can be obtained.

See [R] rocfit and [R] rocreg for commands that fit maximum-likelihood ROC models.

Quick start

Equality of AUCs for rating v1 of true state true between samples defined by catvar roccomp true v1, by(catvar)

Equality of AUCs for ratings v1 and v2 for the same sample roccomp true v1 v2

reccomp true vi vz

Same as above, but plot ROC curves without reporting summary statistics and test of equality

roccomp true v1 v2, graph

Same as above, but plot v1 with a dashed line and v2 with a solid line

roccomp true v1 v2, graph plot1opts(lpattern(dash)) ///
plot2opts(lpattern(solid))

Use contrast matrix mymat to compare ROC areas for v1, v2, v3, and v4

matrix mymat = (1,0,-1,0 \ 0,1,0,-1)
roccomp true v1 v2 v3 v4, test(mymat)

Test equality of ROC area for v1 against a "gold standard" gold rocgold true gold v1

Menu

roccomp

 $Statistics > {\sf Epidemiology} \ {\sf and} \ {\sf related} > {\sf ROC} \ {\sf analysis} > {\sf Test} \ {\sf equality} \ {\sf of} \ {\sf two} \ {\sf or} \ {\sf more} \ {\sf ROC} \ {\sf areas}$

rocgold

Statistics > Epidemiology and related > ROC analysis > Test equality of ROC area against gold standard

Syntax

Test equality of ROC areas

roccomp refvar classvar [classvars] [if] [in] [weight] [, roccomp_options]

Test equality of ROC area against a standard ROC curve

rocgold refvar goldvar classvar [classvars] [if] [in] [weight] [, rocgold_options]

y variable
x for comparing ROC areas
rve
the 45-degree reference line
urve on its own graph
der the ROC curve
using binormal distribution assumption
the #th binormal fit line
rel; default is level(95)
f the #th ROC curve
the reference line
than by() documented in [G-3] <i>twoway_options</i>

rocgold_options	Description
Main	
<u>sid</u> ak	adjust the p-value by using Šidák's method
<pre>test(matname)</pre>	use contrast matrix for comparing ROC areas
graph	graph the ROC curve
norefline	suppress plotting the 45-degree reference line
separate	place each ROC curve on its own graph
summary	report the area under the ROC curve
<u>bin</u> ormal	estimate areas by using binormal distribution assumption
<u>line#</u> opts(<i>cline_options</i>)	affect rendition of the #th binormal fit line
<u>l</u> evel(#)	set confidence level; default is level(95)
Plot	
<pre>plot#opts(plot_options)</pre>	affect rendition of the #th ROC curve; plot 1 is the "gold standard"
Reference line	
<pre>rlopts(cline_options)</pre>	affect rendition of the reference line
Y axis, X axis, Titles, Legend, Overall	
twoway_options	any options other than by () documented in [G-3] <i>twoway_options</i>
plot_options	Description
marker_options marker_label_options cline_options	change look of markers (color, size, etc.) add marker labels; change look or position change look of the line

collect is allowed with roccomp and rocgold; see [U] 11.1.10 Prefix commands. fweights are allowed; see [U] 11.1.6 weight.

Options

Main

- by (*varname*) (roccomp only) is required when comparing independent ROC areas. The by() variable identifies the groups to be compared.
- sidak (rocgold only) requests that the *p*-value be adjusted for the effect of multiple comparisons by using Šidák's method. Bonferroni's adjustment is reported by default.
- test(*matname*) specifies the contrast matrix to be used when comparing ROC areas. By default, the null hypothesis that all areas are equal is tested.
- graph produces graphical output of the ROC curve.
- norefline suppresses plotting the 45-degree reference line from the graphical output of the ROC curve.
- separate is meaningful only with roccomp and specifies that each ROC curve be placed on its own graph rather than one curve on top of the other.
- summary reports the area under the ROC curve, its standard error, and its confidence interval. This option is needed only when also specifying graph.

- binormal specifies that the areas under the ROC curves to be compared should be estimated using the binormal distribution assumption. By default, areas to be compared are computed using the trapezoidal rule.
- line#opts(cline_options) affect the rendition of the line representing the #th ROC curve drawn using the binormal distribution assumption; see [G-3] cline_options. These lines are drawn only if the binormal option is specified.
- level(#) specifies the confidence level, as a percentage, for the confidence intervals. The default is level(95) or as set by set level; see [R] level.

Plot

plot#opts(plot_options) affect the rendition of the #th ROC curve—the curve's plotted points connected by lines. The plot_options can affect the size and color of markers, whether and how the markers are labeled, and whether and how the points are connected; see [G-3] marker_options, [G-3] marker_label_options, and [G-3] cline_options.

For rocgold, plot1opts() are applied to the ROC for the gold standard.

Reference line

rlopts(*cline_options*) affects the rendition of the reference line; see [G-3] *cline_options*.

∫Y axis, X axis, Titles, Legend, Overall ↓

twoway_options are any of the options documented in [G-3] *twoway_options*. These include options for titling the graph (see [G-3] *title_options*), options for saving the graph to disk (see [G-3] *saving_option*), and the by() option (see [G-3] *by_option*).

Remarks and examples

Remarks are presented under the following headings:

Introduction Comparing areas under the ROC curve Correlated data Independent data Comparing areas with a gold standard

Introduction

roccomp provides comparison of the ROC curves of multiple classifiers. rocgold compares the ROC curves of multiple classifiers with a single "gold standard" classifier. Adjustment of inference for multiple comparisons is also provided by rocgold.

See Pepe (2003) for a discussion of ROC analysis. Pepe has posted Stata datasets and programs used to reproduce results presented in the book (https://www.stata.com/bookstore/pepe.html).

Comparing areas under the ROC curve

The area under multiple ROC curves can be compared by using roccomp. The command syntax is slightly different if the ROC curves are correlated (that is, different diagnostic tests are applied to the same sample) or independent (that is, diagnostic tests are applied to different samples).

Correlated data

Example 1

Hanley and McNeil (1983) presented data from an evaluation of two computer algorithms designed to reconstruct CT images from phantoms. We will call these two algorithms' modalities 1 and 2. A sample of 112 phantoms was selected; 58 phantoms were considered normal, and the remaining 54 were abnormal. Each of the two modalities was applied to each phantom, and the resulting images were rated by a reviewer using a six-point scale: 1 = definitely normal, 2 = probably normal, 3 = possibly normal, $4 = \text{possibly abnormal}, 5 = \text{probably abnormal}, and 6 = definitely abnormal}. Because each modality$ was applied to the same sample of phantoms, the two sets of outcomes are correlated.

We list the first 7 observations:

```
. use https://www.stata-press.com/data/r19/ct
(Reconstruction of CT images)
. list in 1/7, sep(0)
```

	mod1	mod2	status
1.	2	1	0
2.	5	5	1
з.	2	1	0
2. 3. 4.	2	3	0
5.	5	6	1
6.	2	2	0
7.	3	2	0

The data are in wide form, which is required when dealing with correlated data. Each observation corresponds to one phantom. The variable mod1 identifies the rating assigned for the first modality, and mod2 identifies the rating assigned for the second modality. The true status of the phantoms is given by status=0 if they are normal and status=1 if they are abnormal. The observations with at least one missing rating were dropped from the analysis.

ROC Asymptotic normal Obs [95% conf. interval] Std. err. area mod1 112 0.8828 0.0317 0.82067 0.94498 mod2 112 0.9302 0.0256 0.88005 0.98042 H0: area(mod1) = area(mod2) chi2(1) =2.31 Prob>chi2 = 0.1282 1.00 0.75 Sensitivity mod1 ROC area: 0.8828 0.50 mod2 ROC area: 0.9302 Reference 0.25 0.00 0.25 0.75 1.00 0.00 0.50 1-specificity

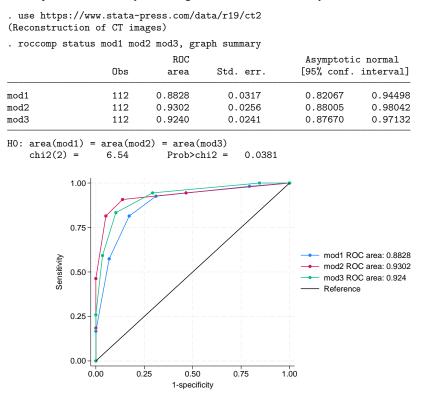
We plot the two ROC curves and compare their areas. . roccomp status mod1 mod2, graph summary

By default, roccomp, with the graph option specified, plots the ROC curves on the same graph. Optionally, the curves can be plotted side by side, each on its own graph, by also specifying separate.

For each curve, roccomp reports summary statistics and provides a test for the equality of the area under the curves, using an algorithm suggested by DeLong, DeLong, and Clarke-Pearson (1988).

Although the area under the ROC curve for modality 2 is larger than that of modality 1, the χ^2 test yielded a *p*-value of 0.1282, suggesting that there is no significant difference between these two areas.

The roccomp command can also be used to compare more than two ROC areas. To illustrate this, we modified the previous dataset by including a fictitious third modality.



By default, roccomp tests whether the areas under the ROC curves are all equal. Other comparisons can be tested by creating a contrast matrix and specifying test(*matname*), where *matname* is the name of the contrast matrix.

For example, assume that we are interested in testing whether the area under the ROC for mod1 is equal to that of mod3. To do this, we can first create an appropriate contrast matrix and then specify its name with the test() option.

Of course, this is a trivial example because we could have just specified

. roccomp status mod1 mod3

without including mod2 to obtain the same test results. However, for illustration, we will continue with this example.

The contrast matrix must have its number of columns equal to the number of *classvars* (that is, the total number of ROC curves) and a number of rows less than or equal to the number of *classvars*, and the elements of each row must add to zero.

		ROC		Asymptoti	c normal
	Obs	area	Std. err.	[95% conf.	interval]
mod1	112	0.8828	0.0317	0.82067	0.94498
mod2	112	0.9302	0.0256	0.88005	0.98042
mod3	112	0.9240	0.0241	0.87670	0.97132

Although all three areas are reported, the comparison is made using the specified contrast matrix.

Perhaps more interesting would be a comparison of the area from mod1 and the average area of mod2 and mod3.

```
. matrix C=(1,-.5,-.5)
```

```
. roccomp status mod1 mod2 mod3, test(C)
```

-	Obs	ROC area	Std. err.	Asymptoti [95% conf.	.c normal interval]
mod1	112	0.8828	0.0317	0.82067	0.94498
mod2	112	0.9302	0.0256	0.88005	0.98042
mod3	112	0.9240	0.0241	0.87670	0.97132

H0: Comparison as defined by contrast matrix: C chi2(1) = 3.43 Prob>chi2 = 0.0642

Other contrasts could be made. For example, we could test if mod3 is different from at least one of the other two by first creating the following contrast matrix:

4

Independent data

Example 2

In example 1, we noted that because each test modality was applied to the same sample of phantoms, the classification outcomes were correlated. Now, assume that we have collected the same data presented by Hanley and McNeil (1983), except that we applied the first test modality to one sample of phantoms and the second test modality to a different sample of phantoms. The resulting measurements are now considered independent.

Here are a few of the observations.

```
. use https://www.stata-press.com/data/r19/ct3
(Reconstruction of CT images)
```

```
. list in 1/7, sep(0)
```

	рор	status	rating	mod
1.	12	0	1	1
2. 3. 4.	31	0	1	2
З.	1	1	1	1
4.	3	1	1	2
5.	28	0	2	1
6.	19	0	2	2
7.	3	1	2	1

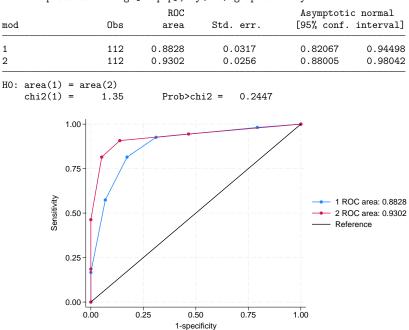
The data are in long form, which is required when dealing with independent data. The data consist of 24 observations: 6 observations corresponding to abnormal phantoms and 6 to normal phantoms evaluated using the first modality, and similarly 6 observations corresponding to abnormal phantoms and 6 to normal phantoms evaluated using the second modality. The number of phantoms corresponding to each observation is given by the pop variable. Once again, we have frequency-weighted data. The variable mod identifies the modality, and rating is the assigned classification.

We can better view our data by using the table command.

```
. table (mod status) (rating) [fw=pop], totals(mod mod#status mod#rating)
```

				Rat	ing		
	1	2	3	4	5	6	Total
Modality							
1							
Status							
0	12	28	8	6	4		58
1	1	3	6	13	22	9	54
Total	13	31	14	19	26	9	112
2							
Status							
0	31	19	5	3			58
1	3	2	5	19	15	10	54
Total	34	21	10	22	15	10	112

The status variable indicates the true status of the phantoms: status = 0 if they are normal and status = 1 if they are abnormal.



We now compare the areas under the two ROC curves.

. roccomp status rating [fw=pop], by(mod) graph summary



Comparing areas with a gold standard

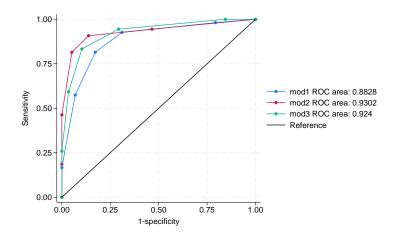
The area under multiple ROC curves can be compared with a gold standard using rocgold. The command syntax is similar to that of roccomp. The tests are corrected for the effect of multiple comparisons.

Example 3

We will use the same data (presented by Hanley and McNeil [1983]) as in the roccomp examples. Let's assume that the first modality is considered to be the standard against which both the second and third modalities are compared.

We want to plot and compare both the areas of the ROC curves of mod2 and mod3 with mod1. Because we consider mod1 to be the gold standard, it is listed first after the reference variable in the rocgold command line.

 use https://www.stata-press.com/data/r19/ct2 (Reconstruction of CT images) rocgold status mod1 mod2 mod3, graph summary 							
		ROC area	Std. err.	chi2	df	Pr>chi2	Bonferroni Pr>chi2
mod1 mod2 mod3	(standard)	0.8828 0.9302 0.9240	0.0317 0.0256 0.0241	2.3146 5.2480	1 1	0.1282 0.0220	0.2563 0.0439



Equivalently, we could have done this in two steps by using the roccomp command.

- . roccomp status mod1 mod2, graph summary
- . roccomp status mod1 mod3, graph summary

Stored results

roccomp stores the following in r():

Scalars

r(N_g) r(p)	number of groups p -value for χ^2 test	r(df) r(chi2)	χ^2 degrees of freedom χ^2
Matrices r(V)	variance-covariance matrix		
rocgold st	ores the following in r():		
Scalars r(N_g)	number of groups		
Matrices r(V) r(chi2) r(df)	variance–covariance matrix χ^2 vector χ^2 degrees-of-freedom vector	r(p) r(p_adj)	vector of p -values for χ^2 tests vector of adjusted p -values

Methods and formulas

Assume that we applied a diagnostic test to each of N_n normal and N_a abnormal subjects. Further assume that the higher the outcome value of the diagnostic test, the higher the risk of the subject being abnormal. Let $\hat{\theta}$ be the estimated area under the curve, and let X_i , $i = 1, 2, ..., N_a$ and Y_j , $j = 1, 2, ..., N_n$ be the values of the diagnostic test for the abnormal and normal subjects, respectively.

Areas under ROC curves are compared using an algorithm suggested by DeLong, DeLong, and Clarke-Pearson (1988). Let $\hat{\theta} = (\widehat{\theta^1}, \widehat{\theta^2}, \dots, \widehat{\theta^k})$ be a vector representing the areas under k ROC curves. See Methods and formulas in [R] roctab for the definition of these area estimates.

For the rth area, define

$$V_{10}^{r}(X_{i}) = \frac{1}{N_{n}}\sum_{j=1}^{N_{n}}\psi(X_{i}^{r},Y_{j}^{r})$$

and for each normal subject, j, define

$$V_{01}^r(Y_j) = \frac{1}{N_a} \sum_{i=1}^{N_a} \psi(X_i^r, Y_j^r)$$

where

$$\psi(X^{r}, Y^{r}) = \begin{cases} 1 & Y^{r} < X^{r} \\ \frac{1}{2} & Y^{r} = X^{r} \\ 0 & Y^{r} > X^{r} \end{cases}$$

Define the $k \times k$ matrix S_{10} such that the (r, s)th element is

$$S_{10}^{r,s} = \frac{1}{N_a - 1} \sum_{i=1}^{N_a} \{ V_{10}^r(X_i) - \widehat{\theta^r} \} \{ V_{10}^s(X_i) - \widehat{\theta^s} \}$$

and S_{01} such that the (r, s)th element is

$$S_{01}^{r,s} = \frac{1}{N_n - 1} \sum_{j=1}^{N_n} \{ V_{01}^r(Y_i) - \widehat{\theta^r} \} \{ V_{01}^s(Y_i) - \widehat{\theta^s} \}$$

Then, the covariance matrix is

$$S = \frac{1}{N_a} S_{10} + \frac{1}{N_n} S_{01}$$

Let L be a contrast matrix defining the comparison, so that

$$(\hat{\boldsymbol{\theta}} - \boldsymbol{\theta})' \mathbf{L}' (\mathbf{LSL}')^{-1} \mathbf{L} (\hat{\boldsymbol{\theta}} - \boldsymbol{\theta})$$

has a χ^2 distribution with degrees of freedom equal to the rank of LSL'.

References

Cleves, M. A. 2002a. Comparative assessment of three common algorithms for estimating the variance of the area under the nonparametric receiver operating characteristic curve. *Stata Journal* 2: 280–289.

— 2002b. From the help desk: Comparing areas under receiver operating characteristic curves from two or more probit or logit models. *Stata Journal* 2: 301–313.

- DeLong, E. R., D. M. DeLong, and D. L. Clarke-Pearson. 1988. Comparing the areas under two or more correlated receiver operating characteristic curves: A nonparametric approach. *Biometrics* 44: 837–845. https://doi.org/10.2307/ 2531595.
- Erdreich, L. S., and E. T. Lee. 1981. Use of relative operating characteristic analysis in epidemiology: A method for dealing with subjective judgment. American Journal of Epidemiology 114: 649–662. https://doi.org/10.1093/oxfordjournals. aje.a113236.
- Hanley, J. A., and B. J. McNeil. 1983. A method of comparing the areas under receiver operating characteristic curves derived from the same cases. *Radiology* 148: 839–843. https://doi.org/10.1148/radiology.148.3.6878708.
- Harbord, R. M., and P. Whiting. 2009. metandi: Meta-analysis of diagnostic accuracy using hierarchical logistic regression. Stata Journal 9: 211–229.
- Juul, S., and M. Frydenberg. 2021. An Introduction to Stata for Health Researchers. 5th ed. College Station, TX: Stata Press.
- Ma, G., and W. J. Hall. 1993. Confidence bands for the receiver operating characteristic curves. Medical Decision Making 13: 191–197. https://doi.org/10.1177/0272989X9301300304.
- Pepe, M. S. 2003. The Statistical Evaluation of Medical Tests for Classification and Prediction. New York: Oxford University Press.
- Reichenheim, M. E., and A. Ponce de Leon. 2002. Estimation of sensitivity and specificity arising from validity studies with incomplete design. *Stata Journal* 2: 267–279.
- Working, H., and H. Hotelling. 1929. Application of the theory of error to the interpretation of trends. Journal of the American Statistical Association 24 (Suppl.): 73–85. https://doi.org/10.2307/2277011.

Also see

- [R] logistic postestimation Postestimation tools for logistic
- [R] **roc** Receiver operating characteristic (ROC) analysis
- [R] rocfit Parametric ROC models
- [R] rocreg Parametric and nonparametric ROC regression
- [R] roctab Nonparametric ROC analysis

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