nptrend — Test for trend across ordered groups

Description

nptrend performs a nonparametric test for trend across ordered groups.

Quick start

Nonparametric test for a trend in v1 across ordered categories of catvar
   nptrend v1, by(catvar)

As above, but for cases where v2 is greater than 0
   nptrend v1 if v2 > 0, by(catvar)

Menu

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nptrend — Test for trend across ordered groups

Syntax

nptrend varname [if] [in], by(groupvar) [nodetail nolabel score(scorevar)]

Options

- by(groupvar) is required; it specifies the group on which the data are to be ordered.
- nodetail suppresses the listing of group rank sums.
- nolabel specifies that group() values be displayed instead of value labels.
- score(scorevar) defines scores for groups. When it is not specified, the values of groupvar are used for the scores.

Remarks and examples

nptrend performs the nonparametric test for trend across ordered groups developed by Cuzick (1985), which is an extension of the Wilcoxon rank-sum test (see [R] ranksum). A correction for ties is incorporated into the test. nptrend is a useful adjunct to the Kruskal–Wallis test; see [R] kwallis.

If your data are not grouped, you can test for trend with the signtest and spearman commands; see [R] signrank and [R] spearman. With signtest, you can perform the Cox and Stuart test, a sign test applied to differences between equally spaced observations of varname. With spearman, you can perform the Daniels test, a test of zero Spearman correlation between varname and a time index. See Conover (1999, 169–175, 323) for a discussion of these tests and their asymptotic relative efficiency.

Example 1

The following data (Altman 1991, 217) show ocular exposure to ultraviolet radiation for 32 pairs of sunglasses classified into three groups according to the amount of visible light transmitted.

<table>
<thead>
<tr>
<th>Group</th>
<th>Transmission of visible light</th>
<th>Ocular exposure to ultraviolet radiation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>&lt; 25%</td>
<td>1.4 1.4 1.4 1.6 2.3 2.5</td>
</tr>
<tr>
<td>2</td>
<td>25 to 35%</td>
<td>0.9 1.0 1.1 1.1 1.2 1.2 1.5 1.9 2.2 2.6</td>
</tr>
<tr>
<td>3</td>
<td>&gt; 35%</td>
<td>0.8 1.7 1.7 1.7 3.4 7.1 8.9 13.5</td>
</tr>
</tbody>
</table>
Entering these data into Stata, we have

```stata
.use https://www.stata-press.com/data/r16/sg
.list, sep(6)
```

<table>
<thead>
<tr>
<th>group</th>
<th>exposure</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>2.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>3.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>4.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>5.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>6.</td>
<td>&lt; 25%</td>
</tr>
<tr>
<td>7.</td>
<td>25% to 35%</td>
</tr>
<tr>
<td></td>
<td>.9</td>
</tr>
<tr>
<td>(output omitted)</td>
<td></td>
</tr>
<tr>
<td>31.</td>
<td>&gt; 35%</td>
</tr>
<tr>
<td>32.</td>
<td>&gt; 35%</td>
</tr>
</tbody>
</table>

We use `nptrend` to test for a trend of (increasing) exposure across the three groups by typing

```stata
.nptrend exposure, by(group)
```

<table>
<thead>
<tr>
<th>group</th>
<th>score</th>
<th>obs</th>
<th>sum of ranks</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt; 25%</td>
<td>1</td>
<td>6</td>
<td>76</td>
</tr>
<tr>
<td>25% to 35%</td>
<td>2</td>
<td>18</td>
<td>290</td>
</tr>
<tr>
<td>&gt; 35%</td>
<td>3</td>
<td>8</td>
<td>162</td>
</tr>
</tbody>
</table>

`z = 1.52`
`Prob > |z| = 0.129`

When the groups are given any equally spaced scores (such as $-1, 0, 1$), we will obtain the same answer as above. To illustrate the effect of changing scores, an analysis of these data with scores 1, 2, and 5 (admittedly not sensible here) produces

```stata
.generate mysc = cond(group==3,5,group)
.nptrend exposure, by(group) score(mysc)
```

<table>
<thead>
<tr>
<th>group</th>
<th>score</th>
<th>obs</th>
<th>sum of ranks</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt; 25%</td>
<td>1</td>
<td>6</td>
<td>76</td>
</tr>
<tr>
<td>25% to 35%</td>
<td>2</td>
<td>18</td>
<td>290</td>
</tr>
<tr>
<td>&gt; 35%</td>
<td>5</td>
<td>8</td>
<td>162</td>
</tr>
</tbody>
</table>

`z = 1.46`
`Prob > |z| = 0.143`

This example suggests that the analysis is not all that sensitive to the scores chosen.

☐

Technical note

The grouping variable may be either a string variable or a numeric variable. If it is a string variable and no score variable is specified, the natural numbers 1, 2, 3, . . . are assigned to the groups in the sort order of the string variable. This may not always be what you expect. For example, the sort order of the strings “one”, “two”, “three” is “one”, “three”, “two”.

☐
Stored results

nptrend stores the following in r():

Scalars
- r(N)  number of observations
- r(z)  z statistic
- r(p)  two-sided p-value
- r(T)  test statistic

Methods and formulas

nptrend is based on a method in Cuzick (1985). The following description of the statistic is from Altman (1991, 215–217). We have k groups of sample sizes \( n_i \) (\( i = 1, \ldots, k \)). The groups are given scores, \( l_i \), which reflect their ordering, such as 1, 2, and 3. The scores do not have to be equally spaced, but they usually are. \( N = \sum n_i \) observations are ranked from 1 to \( N \), and the sums of the ranks in each group, \( R_i \), are obtained. \( L \), the weighted sum of all the group scores, is

\[
L = \sum_{i=1}^{k} l_i n_i
\]

The statistic \( T \) is calculated as

\[
T = \sum_{i=1}^{k} l_i R_i
\]

Under the null hypothesis, the expected value of \( T \) is \( E(T) = 0.5(N+1)L \), and its standard error is

\[
se(T) = \sqrt{ \frac{N+1}{12} \left( N \sum_{i=1}^{k} l_i^2 n_i - L^2 \right) }
\]

so that the test statistic, \( z \), is given by \( z = \frac{T - E(T)}{se(T)} \), which has an approximately standard normal distribution when the null hypothesis of no trend is true.

The correction for ties affects the standard error of \( T \). Let \( \tilde{N} \) be the number of unique values of the variable being tested (\( \tilde{N} \leq N \)), and let \( t_j \) be the number of times the \( j \)th unique value of the variable appears in the data. Define

\[
a = \frac{\sum_{j=1}^{\tilde{N}} t_j (t_j^2 - 1)}{N(N^2 - 1)}
\]

The corrected standard error of \( T \) is \( \tilde{se}(T) = \sqrt{1 - a} \ se(T) \).
Acknowledgments


References


Also see

[R] **Epitab** — Tables for epidemiologists
[R] **kwallis** — Kruskal–Wallis equality-of-populations rank test
[R] **signrank** — Equality tests on matched data
[R] **spearman** — Spearman’s and Kendall’s correlations
[R] **symmetry** — Symmetry and marginal homogeneity tests
[ST] **strate** — Tabulate failure rates and rate ratios