

nbreg — Negative binomial regression
[Description](#)[Options for nbreg](#)[Methods and formulas](#)[Quick start](#)[Options for gnbreg](#)[References](#)[Menu](#)[Remarks and examples](#)[Also see](#)[Syntax](#)[Stored results](#)

Description

`nbreg` fits a negative binomial regression model for a nonnegative count dependent variable. In this model, the count variable is believed to be generated by a Poisson-like process, except that the variation is allowed to be greater than that of a true Poisson. This extra variation is referred to as overdispersion.

`gnbreg` fits a generalization of the negative binomial mean-dispersion model; the shape parameter α may also be parameterized.

Quick start

Negative binomial model of `y` on `x1` and categorical variable `a`

```
nbreg y x1 i.a
```

As above, but report results as incidence-rate ratios

```
nbreg y x1 i.a, irr
```

As above, and specify exposure variable `evar`

```
nbreg y x1 i.a, irr exposure(evar)
```

Generalized negative binomial model with shape parameter α a function of `x2` and `x3`

```
gnbreg y x1 i.a, lnalpha(x2 x3)
```

Add log of exposure, `lnevar`, as an offset

```
gnbreg y x1 i.a, lnalpha(x2 x3) offset(lnevar)
```

Menu

nbreg

Statistics > Count outcomes > Negative binomial regression

gnbreg

Statistics > Count outcomes > Generalized negative binomial regression

Syntax

Negative binomial regression model

```
nbreg depvar [indepvars] [if] [in] [weight] [, nbreg_options]
```

Generalized negative binomial model

```
gnbreg depvar [indepvars] [if] [in] [weight] [, gnbreg_options]
```

<i>nbreg_options</i>	Description
Model	
<code>noconstant</code>	suppress constant term
<code>dispersion(<u>m</u>ean)</code>	parameterization of dispersion; the default
<code>dispersion(<u>c</u>onstant)</code>	constant dispersion for all observations
<code>exposure(<i>varname</i>_e)</code>	include $\ln(\textit{varname}_e)$ in model with coefficient constrained to 1
<code>offset(<i>varname</i>_o)</code>	include <i>varname</i> _o in model with coefficient constrained to 1
<code>constraints(<i>constraints</i>)</code>	apply specified linear constraints
<code>collinear</code>	keep collinear variables
SE/Robust	
<code>vce(<i>vcetype</i>)</code>	<i>vcetype</i> may be <code>oim</code> , <code>robust</code> , <code>cluster <i>clustvar</i></code> , <code>opg</code> , <code>bootstrap</code> , or <code>jackknife</code>
Reporting	
<code>level(#)</code>	set confidence level; default is <code>level(95)</code>
<code>nolrtest</code>	suppress likelihood-ratio test
<code>irr</code>	report incidence-rate ratios
<code>nocnsreport</code>	do not display constraints
<code>display_options</code>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
<code>maximize_options</code>	control the maximization process; seldom used
<code>coeflegend</code>	display legend instead of statistics

<i>gnbreg_options</i>	Description
Model	
<code>noconstant</code>	suppress constant term
<code>lnalpha(<i>varlist</i>)</code>	dispersion model variables
<code>exposure(<i>varname_e</i>)</code>	include $\ln(\text{varname}_e)$ in model with coefficient constrained to 1
<code>offset(<i>varname_o</i>)</code>	include <i>varname_o</i> in model with coefficient constrained to 1
<code>constraints(<i>constraints</i>)</code>	apply specified linear constraints
<code>collinear</code>	keep collinear variables
SE/Robust	
<code>vce(<i>vcetype</i>)</code>	<i>vcetype</i> may be <code>oim</code> , <code>robust</code> , <code>cluster <i>clustvar</i></code> , <code>opg</code> , <code>bootstrap</code> , or <code>jackknife</code>
Reporting	
<code>level(#)</code>	set confidence level; default is <code>level(95)</code>
<code>irr</code>	report incidence-rate ratios
<code>nocnsreport</code>	do not display constraints
<code>display_options</code>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
<code>maximize_options</code>	control the maximization process; seldom used
<code>coeflegend</code>	display legend instead of statistics

indepvars and *varlist* may contain factor variables; see [U] 11.4.3 **Factor variables**.

depar, *indepvars*, *varname_e*, and *varname_o* may contain time-series operators (nbreg only); see [U] 11.4.4 **Time-series varlists**.

`bayes`, `bootstrap`, `by` (nbreg only), `fmm` (nbreg only), `fp` (nbreg only), `jackknife`, `mfp` (nbreg only), `mi estimate`, `nestreg` (nbreg only), `rolling`, `statsby`, `stepwise`, and `svy` are allowed; see [U] 11.1.10 **Prefix commands**. For more details, see [BAYES] **bayes: gnbreg**, [BAYES] **bayes: nbreg**, and [FMM] **fmm: nbreg**.

`vce(bootstrap)` and `vce(jackknife)` are not allowed with the `mi estimate` prefix; see [MI] **mi estimate**.

Weights are not allowed with the `bootstrap` prefix; see [R] **bootstrap**.

`vce()` and weights are not allowed with the `svy` prefix; see [SVY] **svy**.

`fweights`, `iweights`, and `pweights` are allowed; see [U] 11.1.6 **weight**.

`coeflegend` does not appear in the dialog box.

See [U] 20 **Estimation and postestimation commands** for more capabilities of estimation commands.

Options for nbreg

Model

`noconstant`; see [R] **estimation options**.

`dispersion(mean | constant)` specifies the parameterization of the model. `dispersion(mean)`, the default, yields a model with dispersion equal to $1 + \alpha \exp(\mathbf{x}_j\beta + \text{offset}_j)$; that is, the dispersion is a function of the expected mean: $\exp(\mathbf{x}_j\beta + \text{offset}_j)$. `dispersion(constant)` has dispersion equal to $1 + \delta$; that is, it is a constant for all observations.

`exposure(varnamee)`, `offset(varnameo)`, `constraints(constraints)`, `collinear`; see [R] **estimation options**.

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`, `opg`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] [vce_option](#).

Reporting

`level(#)`; see [R] [estimation options](#).

`nolrtest` suppresses fitting the Poisson model. Without this option, a comparison Poisson model is fit, and the likelihood is used in a likelihood-ratio test of the null hypothesis that the dispersion parameter is zero.

`irr` reports estimated coefficients transformed to incidence-rate ratios, that is, e^{β_i} rather than β_i . Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated or stored. `irr` may be specified at estimation or when replaying previously estimated results.

`nocnsreport`; see [R] [estimation options](#).

`display_options`: `nocl`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [estimation options](#).

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(init_specs)`; see [R] [maximize](#). These options are seldom used.

Setting the optimization type to `technique(bhhh)` resets the default `vcetype` to `vce(opg)`.

The following option is available with `nbreg` but is not shown in the dialog box:

`coeflegend`; see [R] [estimation options](#).

Options for `gnbreg`

Model

`noconstant`; see [R] [estimation options](#).

`lnalpha(varlist)` allows you to specify a linear equation for $\ln\alpha$. Specifying `lnalpha(male old)` means that $\ln\alpha = \gamma_0 + \gamma_1\text{male} + \gamma_2\text{old}$, where γ_0 , γ_1 , and γ_2 are parameters to be estimated along with the other model coefficients. If this option is not specified, `gnbreg` and `nbreg` will produce the same results because the shape parameter will be parameterized as a constant.

`exposure(varnamee)`, `offset(varnameo)`, `constraints(constraints)`, `collinear`; see [R] [estimation options](#).

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`, `opg`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] [vce_option](#).

Reporting

`level(#)`; see [R] [estimation options](#).

`irr` reports estimated coefficients transformed to incidence-rate ratios, that is, e^{β_i} rather than β_i . Standard errors and confidence intervals are similarly transformed. This option affects how results are displayed, not how they are estimated or stored. `irr` may be specified at estimation or when replaying previously estimated results.

`nocnsreport`; see [R] [estimation options](#).

`display_options`: `noci`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [estimation options](#).

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(init_specs)`; see [R] [maximize](#). These options are seldom used.

Setting the optimization type to `technique(bhhh)` resets the default `vcetype` to `vce(opg)`.

The following option is available with `gnbreg` but is not shown in the dialog box:

`coeflegend`; see [R] [estimation options](#).

Remarks and examples

stata.com

Remarks are presented under the following headings:

[Introduction to negative binomial regression](#)
[nbreg](#)
[gnbreg](#)

Introduction to negative binomial regression

Negative binomial regression models the number of occurrences (counts) of an event when the event has extra-Poisson variation, that is, when it has overdispersion. The Poisson regression model is

$$y_j \sim \text{Poisson}(\mu_j)$$

where

$$\mu_j = \exp(\mathbf{x}_j\boldsymbol{\beta} + \text{offset}_j)$$

for observed counts y_j with covariates \mathbf{x}_j for the j th observation. One derivation of the negative binomial mean-dispersion model is that individual units follow a Poisson regression model, but there is an omitted variable ν_j , such that e^{ν_j} follows a gamma distribution with mean 1 and variance α :

$$y_j \sim \text{Poisson}(\mu_j^*)$$

where

$$\mu_j^* = \exp(\mathbf{x}_j\boldsymbol{\beta} + \text{offset}_j + \nu_j)$$

and

$$e^{\nu_j} \sim \text{Gamma}(1/\alpha, \alpha)$$

With this parameterization, a $\text{Gamma}(a, b)$ distribution will have expectation ab and variance ab^2 .

We refer to α as the overdispersion parameter. The larger α is, the greater the overdispersion. The Poisson model corresponds to $\alpha = 0$. `nbreg` parameterizes α as $\text{In}\alpha$. `gnbreg` allows $\text{In}\alpha$ to be modeled as $\text{In}\alpha_j = \mathbf{z}_j\boldsymbol{\gamma}$, a linear combination of covariates \mathbf{z}_j .

`nbreg` will fit two different parameterizations of the negative binomial model. The default, described above and also given by the `dispersion(mean)` option, has dispersion for the j th observation equal to $1 + \alpha \exp(\mathbf{x}_j\boldsymbol{\beta} + \text{offset}_j)$. This is seen by noting that the above implies that

$$\mu_j^* \sim \text{Gamma}(1/\alpha, \alpha\mu_j)$$

and thus

$$\begin{aligned} \text{Var}(y_j) &= E \{ \text{Var}(y_j | \mu_j^*) \} + \text{Var} \{ E(y_j | \mu_j^*) \} \\ &= E(\mu_j^*) + \text{Var}(\mu_j^*) \\ &= \mu_j(1 + \alpha\mu_j) \end{aligned}$$

The alternative parameterization, given by the `dispersion(constant)` option, has dispersion equal to $1 + \delta$; that is, it is constant for all observations. This is so because the constant-dispersion model assumes instead that

$$\mu_j^* \sim \text{Gamma}(\mu_j/\delta, \delta)$$

and thus $\text{Var}(y_j) = \mu_j(1 + \delta)$. The Poisson model corresponds to $\delta = 0$.

For detailed derivations of both models, see [Cameron and Trivedi \(2013, 80–89\)](#). In particular, note that the mean-dispersion model is known as the NB2 model in their terminology, whereas the constant-dispersion model is referred to as the NB1 model.

See [Long and Freese \(2014\)](#) and [Cameron and Trivedi \(2010, chap. 17\)](#) for a discussion of the negative binomial regression model with Stata examples and for a discussion of other regression models for count data.

[Hilbe \(2011\)](#) provides an extensive review of the negative binomial model and its variations, using Stata examples.

nbreg

It is not uncommon to posit a Poisson regression model and observe a lack of model fit. The following data appeared in Rodríguez (1993):

```
. use http://www.stata-press.com/data/r15/rod93
. list, sepby(cohort)
```

	cohort	age_mos	deaths	exposure
1.	1941-1949	0.5	168	278.4
2.	1941-1949	2.0	48	538.8
3.	1941-1949	4.5	63	794.4
4.	1941-1949	9.0	89	1,550.8
5.	1941-1949	18.0	102	3,006.0
6.	1941-1949	42.0	81	8,743.5
7.	1941-1949	90.0	40	14,270.0
8.	1960-1967	0.5	197	403.2
9.	1960-1967	2.0	48	786.0
10.	1960-1967	4.5	62	1,165.3
11.	1960-1967	9.0	81	2,294.8
12.	1960-1967	18.0	97	4,500.5
13.	1960-1967	42.0	103	13,201.5
14.	1960-1967	90.0	39	19,525.0
15.	1968-1976	0.5	195	495.3
16.	1968-1976	2.0	55	956.7
17.	1968-1976	4.5	58	1,381.4
18.	1968-1976	9.0	85	2,604.5
19.	1968-1976	18.0	87	4,618.5
20.	1968-1976	42.0	70	9,814.5
21.	1968-1976	90.0	10	5,802.5

```
. generate logexp = ln(exposure)
. poisson deaths i.cohort, offset(logexp)
```

```
Iteration 0: log likelihood = -2160.0544
Iteration 1: log likelihood = -2159.5162
Iteration 2: log likelihood = -2159.5159
Iteration 3: log likelihood = -2159.5159
```

Poisson regression

```
Number of obs      =          21
LR chi2(2)         =         49.16
Prob > chi2        =         0.0000
Pseudo R2         =         0.0113
```

Log likelihood = -2159.5159

	deaths	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
cohort						
	1960-1967	-.3020405	.0573319	-5.27	0.000	-.4144089 -.1896721
	1968-1976	.0742143	.0589726	1.26	0.208	-.0413698 .1897983
_cons		-3.899488	.0411345	-94.80	0.000	-3.98011 -3.818866
logexp		1	(offset)			

```
. estat gof
      Deviance goodness-of-fit = 4190.689
      Prob > chi2(18)         = 0.0000
      Pearson goodness-of-fit = 15387.67
      Prob > chi2(18)         = 0.0000
```

The extreme significance of the goodness-of-fit χ^2 indicates that the Poisson regression model is inappropriate, suggesting to us that we should try a negative binomial model:

```
. nbreg deaths i.cohort, offset(logexp) nolog
Negative binomial regression          Number of obs   =          21
                                      LR chi2(2)         =           0.40
Dispersion = mean                    Prob > chi2      =          0.8171
Log likelihood = -131.3799            Pseudo R2       =          0.0015
```

deaths	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
cohort						
1960-1967	-.2676187	.7237203	-0.37	0.712	-1.686084	1.150847
1968-1976	-.4573957	.7236651	-0.63	0.527	-1.875753	.9609618
_cons	-2.086731	.511856	-4.08	0.000	-3.08995	-1.083511
logexp	1	(offset)				
/lnalpha	.5939963	.2583615			.0876171	1.100376
alpha	1.811212	.4679475			1.09157	3.005295

```
LR test of alpha=0: chibar2(01) = 4056.27          Prob >= chibar2 = 0.000
```

Our original Poisson model is a special case of the negative binomial—it corresponds to $\alpha = 0$. `nbreg`, however, estimates α indirectly, estimating instead $\ln\alpha$. In our model, $\ln\alpha = 0.594$, meaning that $\alpha = 1.81$ (`nbreg` undoes the transformation for us at the bottom of the output).

To test $\alpha = 0$ (equivalent to $\ln\alpha = -\infty$), `nbreg` performs a likelihood-ratio test. The staggering χ^2 value of 4,056 asserts that the probability that we would observe these data conditional on $\alpha = 0$ is virtually zero, that is, conditional on the process being Poisson. The data are not Poisson. It is not accidental that this χ^2 value is close to the goodness-of-fit statistic from the Poisson regression itself.

□ Technical note

The usual Gaussian test of $\alpha = 0$ is omitted because this test occurs on the boundary, invalidating the usual theory associated with such tests. However, the likelihood-ratio test of $\alpha = 0$ has been modified to be valid on the boundary. In particular, the null distribution of the likelihood-ratio test statistic is not the usual χ^2_1 , but rather a 50:50 mixture of a χ^2_0 (point mass at zero) and a χ^2_1 , denoted as $\bar{\chi}^2_{01}$. See [Gutierrez, Carter, and Drukler \(2001\)](#) for more details. □

□ Technical note

The negative binomial model deals with cases in which there is more variation than would be expected if the process were Poisson. The negative binomial model is not helpful if there is less than Poisson variation—if the variance of the count variable is less than its mean. However, underdispersion is uncommon. Poisson models arise because of independently generated events. Overdispersion comes about if some of the parameters (causes) of the Poisson processes are unknown. To obtain underdispersion, the sequence of events somehow would have to be regulated; that is, events would not be independent but controlled based on past occurrences. □

gnbreg

`gnbreg` is a generalization of `nbreg`, `dispersion(mean)`. Whereas in `nbreg`, one $\ln\alpha$ is estimated, `gnbreg` allows $\ln\alpha$ to vary, observation by observation, as a linear combination of another set of covariates: $\ln\alpha_j = \mathbf{z}_j\boldsymbol{\gamma}$.

We will assume that the number of deaths is a function of age, whereas the $\ln\alpha$ parameter is a function of cohort. To fit the model, we type

```
. gnbreg deaths age_mos, lnalpha(i.cohort) offset(logexp)
Fitting constant-only model:
Iteration 0:  log likelihood =  -187.067   (not concave)
Iteration 1:  log likelihood = -138.13047
Iteration 2:  log likelihood = -133.83164
Iteration 3:  log likelihood = -131.59551
Iteration 4:  log likelihood = -131.5795
Iteration 5:  log likelihood = -131.57948
Iteration 6:  log likelihood = -131.57948
Fitting full model:
Iteration 0:  log likelihood = -124.34327
Iteration 1:  log likelihood = -117.76701
Iteration 2:  log likelihood = -117.56403
Iteration 3:  log likelihood = -117.56164
Iteration 4:  log likelihood = -117.56164
Generalized negative binomial regression
Log likelihood = -117.56164
Number of obs      =          21
LR chi2(1)         =          28.00
Prob > chi2        =          0.0000
Pseudo R2          =          0.1065
```

	deaths	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
deaths							
	age_mos	-.0516657	.0051747	-9.98	0.000	-.061808	-.0415233
	_cons	-1.867225	.2227944	-8.38	0.000	-2.303894	-1.430556
	logexp	1	(offset)				
lnalpha							
	cohort						
	1960-1967	.0939546	.7187747	0.13	0.896	-1.314818	1.502727
	1968-1976	.0815279	.7365476	0.11	0.912	-1.362079	1.525135
	_cons	-.4759581	.5156502	-0.92	0.356	-1.486614	.5346978

We find that age is a significant determinant of the number of deaths. The standard errors for the variables in the $\ln\alpha$ equation suggest that the overdispersion parameter does not vary across cohorts. We can test this assertion by typing

```
. test 2.cohort 3.cohort
( 1)  [lnalpha]2.cohort = 0
( 2)  [lnalpha]3.cohort = 0
      chi2( 2) =      0.02
      Prob > chi2 =      0.9904
```

There is no evidence of variation by cohort in these data.

□ Technical note

Note the intentional absence of a likelihood-ratio test for $\alpha = 0$ in `gnbreg`. The test is affected by the same boundary condition that affects the comparison test in `nbreg`; however, when α is parameterized by more than a constant term, the null distribution becomes intractable. For this reason, we recommend using `nbreg` to test for overdispersion and, if you have reason to believe that overdispersion exists, only then modeling the overdispersion using `gnbreg`. □

Stored results

`nbreg` stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(k)</code>	number of parameters
<code>e(k_aux)</code>	number of auxiliary parameters
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_eq_model)</code>	number of equations in overall model test
<code>e(k_dv)</code>	number of dependent variables
<code>e(df_m)</code>	model degrees of freedom
<code>e(r2_p)</code>	pseudo- <i>R</i> -squared
<code>e(ll)</code>	log likelihood
<code>e(ll_0)</code>	log likelihood, constant-only model
<code>e(ll_c)</code>	log likelihood, comparison model
<code>e(alpha)</code>	value of alpha
<code>e(delta)</code>	value of delta
<code>e(N_clust)</code>	number of clusters
<code>e(chi2)</code>	χ^2
<code>e(chi2_c)</code>	χ^2 for comparison test
<code>e(p)</code>	<i>p</i> -value for model test
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(rank0)</code>	rank of <code>e(V)</code> for constant-only model
<code>e(ic)</code>	number of iterations
<code>e(rc)</code>	return code
<code>e(converged)</code>	1 if converged, 0 otherwise

Macros

<code>e(cmd)</code>	<code>nbreg</code>
<code>e(cmdline)</code>	command as typed
<code>e(depvar)</code>	name of dependent variable
<code>e(wtype)</code>	weight type
<code>e(wexp)</code>	weight expression
<code>e(title)</code>	title in estimation output
<code>e(clustvar)</code>	name of cluster variable
<code>e(offset)</code>	linear offset variable
<code>e(chi2type)</code>	Wald or LR; type of model χ^2 test
<code>e(chi2_ct)</code>	Wald or LR; type of model χ^2 test corresponding to <code>e(chi2_c)</code>
<code>e(dispers)</code>	mean or constant
<code>e(vce)</code>	<i>vctype</i> specified in <code>vce()</code>
<code>e(vcetype)</code>	title used to label Std. Err.
<code>e(opt)</code>	type of optimization
<code>e(which)</code>	max or min; whether optimizer is to perform maximization or minimization
<code>e(ml_method)</code>	type of ml method
<code>e(user)</code>	name of likelihood-evaluator program
<code>e(technique)</code>	maximization technique
<code>e(properties)</code>	<code>b V</code>
<code>e(predict)</code>	program used to implement <code>predict</code>
<code>e(asbalanced)</code>	factor variables <code>fvset</code> as <code>asbalanced</code>
<code>e(asobserved)</code>	factor variables <code>fvset</code> as <code>asobserved</code>

Matrices

e(b)	coefficient vector
e(Cns)	constraints matrix
e(iilog)	iteration log (up to 20 iterations)
e(gradient)	gradient vector
e(V)	variance–covariance matrix of the estimators
e(V_modelbased)	model-based variance

Functions

e(sample)	marks estimation sample
-----------	-------------------------

gnbreg stores the following in e():

Scalars

e(N)	number of observations
e(k)	number of parameters
e(k_eq)	number of equations in e(b)
e(k_eq_model)	number of equations in overall model test
e(k_dv)	number of dependent variables
e(df_m)	model degrees of freedom
e(r2_p)	pseudo- <i>R</i> -squared
e(ll)	log likelihood
e(ll_0)	log likelihood, constant-only model
e(N_clust)	number of clusters
e(chi2)	χ^2
e(p)	<i>p</i> -value for model test
e(rank)	rank of e(V)
e(rank0)	rank of e(V) for constant-only model
e(ic)	number of iterations
e(rc)	return code
e(converged)	1 if converged, 0 otherwise

Macros

e(cmd)	gnbreg
e(cmdline)	command as typed
e(depvar)	name of dependent variable
e(wtype)	weight type
e(wexp)	weight expression
e(title)	title in estimation output
e(clustvar)	name of cluster variable
e(offset1)	linear offset variable
e(chi2type)	Wald or LR; type of model χ^2 test
e(vce)	<i>vcetype</i> specified in vce()
e(vcetype)	title used to label Std. Err.
e(opt)	type of optimization
e(which)	max or min; whether optimizer is to perform maximization or minimization
e(ml_method)	type of ml method
e(user)	name of likelihood-evaluator program
e(technique)	maximization technique
e(properties)	b V
e(predict)	program used to implement predict
e(asbalanced)	factor variables fvset as asbalanced
e(asobserved)	factor variables fvset as asobserved

Matrices

e(b)	coefficient vector
e(Cns)	constraints matrix
e(iilog)	iteration log (up to 20 iterations)
e(gradient)	gradient vector
e(V)	variance–covariance matrix of the estimators
e(V_modelbased)	model-based variance

Functions

e(sample)	marks estimation sample
-----------	-------------------------

Methods and formulas

See [R] [poisson](#) and Johnson, Kemp, and Kotz (2005, chap. 4) for an introduction to the Poisson distribution.

Methods and formulas are presented under the following headings:

Mean-dispersion model
Constant-dispersion model

Mean-dispersion model

A negative binomial distribution can be regarded as a gamma mixture of Poisson random variables. The number of times something occurs, y_j , is distributed as $\text{Poisson}(\nu_j \mu_j)$. That is, its conditional likelihood is

$$f(y_j | \nu_j) = \frac{(\nu_j \mu_j)^{y_j} e^{-\nu_j \mu_j}}{\Gamma(y_j + 1)}$$

where $\mu_j = \exp(\mathbf{x}_j \boldsymbol{\beta} + \text{offset}_j)$ and ν_j is an unobserved parameter with a $\text{Gamma}(1/\alpha, \alpha)$ density:

$$g(\nu) = \frac{\nu^{(1-\alpha)/\alpha} e^{-\nu/\alpha}}{\alpha^{1/\alpha} \Gamma(1/\alpha)}$$

This gamma distribution has mean 1 and variance α , where α is our ancillary parameter.

The unconditional likelihood for the j th observation is therefore

$$f(y_j) = \int_0^\infty f(y_j | \nu) g(\nu) d\nu = \frac{\Gamma(m + y_j)}{\Gamma(y_j + 1) \Gamma(m)} p_j^m (1 - p_j)^{y_j}$$

where $p_j = 1/(1 + \alpha \mu_j)$ and $m = 1/\alpha$. Solutions for α are handled by searching for $\ln \alpha$ because α must be greater than zero.

The log likelihood (with weights w_j and offsets) is given by

$$m = 1/\alpha \quad p_j = 1/(1 + \alpha \mu_j) \quad \mu_j = \exp(\mathbf{x}_j \boldsymbol{\beta} + \text{offset}_j)$$

$$\begin{aligned} \ln L = \sum_{j=1}^n w_j & \left[\ln\{\Gamma(m + y_j)\} - \ln\{\Gamma(y_j + 1)\} \right. \\ & \left. - \ln\{\Gamma(m)\} + m \ln(p_j) + y_j \ln(1 - p_j) \right] \end{aligned}$$

For `gnbreg`, α can vary across the observations according to the parameterization $\ln \alpha_j = \mathbf{z}_j \boldsymbol{\gamma}$.

Constant-dispersion model

The constant-dispersion model assumes that y_j is conditionally distributed as $\text{Poisson}(\mu_j^*)$, where $\mu_j^* \sim \text{Gamma}(\mu_j/\delta, \delta)$ for some dispersion parameter δ (by contrast, the mean-dispersion model assumes that $\mu_j^* \sim \text{Gamma}(1/\alpha, \alpha \mu_j)$). The log likelihood is given by

$$m_j = \mu_j/\delta \quad p = 1/(1 + \delta)$$

$$\ln L = \sum_{j=1}^n w_j \left[\ln\{\Gamma(m_j + y_j)\} - \ln\{\Gamma(y_j + 1)\} - \ln\{\Gamma(m_j)\} + m_j \ln(p) + y_j \ln(1 - p) \right]$$

with everything else defined as before in the calculations for the mean-dispersion model.

`nbreg` and `gnbreg` support the Huber/White/sandwich estimator of the variance and its clustered version using `vce(robust)` and `vce(cluster clustvar)`, respectively. See [P] [_robust](#), particularly [Maximum likelihood estimators](#) and [Methods and formulas](#).

These commands also support estimation with survey data. For details on VCEs with survey data, see [SVY] [variance estimation](#).

References

- Cameron, A. C., and P. K. Trivedi. 2010. *Microeconometrics Using Stata*. Rev. ed. College Station, TX: Stata Press.
- . 2013. *Regression Analysis of Count Data*. 2nd ed. New York: Cambridge University Press.
- Cummings, T. H., J. W. Hardin, A. C. McLain, J. R. Hussey, K. J. Bennett, and G. M. Wingood. 2015. [Modeling heaped count data](#). *Stata Journal* 15: 457–479.
- Deb, P., E. C. Norton, and W. G. Manning. 2017. *Health Econometrics Using Stata*. College Station, TX: Stata Press.
- Deb, P., and P. K. Trivedi. 2006. [Maximum simulated likelihood estimation of a negative binomial regression model with multinomial endogenous treatment](#). *Stata Journal* 6: 246–255.
- Gutierrez, R. G., S. L. Carter, and D. M. Drukker. 2001. [sg160: On boundary-value likelihood-ratio tests](#). *Stata Technical Bulletin* 60: 15–18. Reprinted in *Stata Technical Bulletin Reprints*, vol. 10, pp. 269–273. College Station, TX: Stata Press.
- Harris, T., J. M. Hilbe, and J. W. Hardin. 2014. [Modeling count data with generalized distributions](#). *Stata Journal* 14: 562–579.
- Hilbe, J. M. 1998. [sg91: Robust variance estimators for MLE Poisson and negative binomial regression](#). *Stata Technical Bulletin* 45: 26–28. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 177–180. College Station, TX: Stata Press.
- . 1999. [sg102: Zero-truncated Poisson and negative binomial regression](#). *Stata Technical Bulletin* 47: 37–40. Reprinted in *Stata Technical Bulletin Reprints*, vol. 8, pp. 233–236. College Station, TX: Stata Press.
- . 2011. *Negative Binomial Regression*. 2nd ed. Cambridge: Cambridge University Press.
- . 2014. *Modeling Count Data*. New York: Cambridge University Press.
- Johnson, N. L., A. W. Kemp, and S. Kotz. 2005. *Univariate Discrete Distributions*. 3rd ed. New York: Wiley.
- Long, J. S. 1997. *Regression Models for Categorical and Limited Dependent Variables*. Thousand Oaks, CA: Sage.
- Long, J. S., and J. Freese. 2001. [Predicted probabilities for count models](#). *Stata Journal* 1: 51–57.
- . 2014. *Regression Models for Categorical Dependent Variables Using Stata*. 3rd ed. College Station, TX: Stata Press.
- Miranda, A., and S. Rabe-Hesketh. 2006. [Maximum likelihood estimation of endogenous switching and sample selection models for binary, ordinal, and count variables](#). *Stata Journal* 6: 285–308.
- Rodríguez, G. 1993. [sbe10: An improvement to poisson](#). *Stata Technical Bulletin* 11: 11–14. Reprinted in *Stata Technical Bulletin Reprints*, vol. 2, pp. 94–98. College Station, TX: Stata Press.
- Rogers, W. H. 1991. [sbe1: Poisson regression with rates](#). *Stata Technical Bulletin* 1: 11–12. Reprinted in *Stata Technical Bulletin Reprints*, vol. 1, pp. 62–64. College Station, TX: Stata Press.
- . 1993. [sg16.4: Comparison of nbreg and glm for negative binomial](#). *Stata Technical Bulletin* 16: 7. Reprinted in *Stata Technical Bulletin Reprints*, vol. 3, pp. 82–84. College Station, TX: Stata Press.
- Xu, X., and J. W. Hardin. 2016. [Regression models for bivariate count outcomes](#). *Stata Journal* 16: 301–315.

Also see

[R] **nbreg postestimation** — Postestimation tools for nbreg and gnbreg

[R] **glm** — Generalized linear models

[R] **npregress** — Nonparametric regression

[R] **poisson** — Poisson regression

[R] **tnbreg** — Truncated negative binomial regression

[R] **zinb** — Zero-inflated negative binomial regression

[BAYES] **bayes: gnbreg** — Bayesian generalized negative binomial regression

[BAYES] **bayes: nbreg** — Bayesian negative binomial regression

[FMM] **fmm: nbreg** — Finite mixtures of negative binomial regression models

[ME] **menbreg** — Multilevel mixed-effects negative binomial regression

[MI] **estimation** — Estimation commands for use with mi estimate

[SVY] **svy estimation** — Estimation commands for survey data

[XT] **xtnbreg** — Fixed-effects, random-effects, & population-averaged negative binomial models

[U] **20 Estimation and postestimation commands**