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Description

`lone way` fits one-way analysis-of-variance (ANOVA) models. `lone way` relaxes the restriction imposed by `oneway` that factors must have fewer than 376 levels. The command additionally reports the intraclass correlation, its standard error, and confidence interval; the estimated reliability of the group-averaged mean; the standard deviation of the group effect; and the standard deviation of the within-group effect.

Quick start

One-way ANOVA model of y for factor a

```
lone way y a
```

Report an exact 95% confidence interval for the intraclass correlation

```
lone way y a, exact
```

Same as above, but report a 90% confidence interval

```
lone way y a, exact level(90)
```

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Statistics > Linear models and related > ANOVA/MANOVA > Large one-way ANOVA

Syntax

```
loneway response_var group_var [if] [in] [weight] [ , options ]
```

options	Description
Main	
<code>mean</code>	expected value of F distribution; default is 1
<code>median</code>	median of F distribution; default is 1
<code>exact</code>	exact confidence intervals (groups must be equal with no weights)
<code>level(#)</code>	set confidence level; default is <code>level(95)</code>

`by` and `collect` are allowed; see [\[U\] 11.1.10 Prefix commands](#).

`aweight`s are allowed; see [\[U\] 11.1.6 weight](#).

Options

Main

`mean` specifies that the expected value of the $F_{k-1, N-k}$ distribution be used as the reference point F_m in the estimation of ρ instead of the default value of 1.

`median` specifies that the median of the $F_{k-1, N-k}$ distribution be used as the reference point F_m in the estimation of ρ instead of the default value of 1.

`exact` requests that exact confidence intervals be computed, as opposed to the default asymptotic confidence intervals. This option is allowed only if the groups are equal in size and weights are not used.

`level(#)` specifies the confidence level, as a percentage, for confidence intervals of the coefficients. The default is `level(95)` or as set by `set level`; see [\[U\] 20.8 Specifying the width of confidence intervals](#).

Remarks and examples

`loneway` and `oneway` both fit ANOVA models, but `loneway` presents different ancillary statistics from `oneway`:

Feature	oneway	loneway
Fit one-way model	x	x
on 375 or fewer levels	x	x
on more than 375 levels		x
Bartlett's test for equal variance	x	
Multiple-comparison tests	x	
Intraclass correlation and SE		x
Intraclass correlation confidence interval		x
Est. reliability of group-averaged mean		x
Est. SD of group effect		x
Est. SD within group		x

Remarks are presented under the following headings:

The one-way ANOVA model
 R^2
The random-effects ANOVA model
Intraclass correlation
Estimated reliability of the group-averaged score

The one-way ANOVA model

► Example 1

loneway's output looks like that of oneway, except that loneway presents more information at the end. Using our automobile dataset, we have created a (numeric) variable called `manufacturer_grp` identifying the manufacturer of each car, and within each manufacturer we have retained a maximum of four models, selecting those with the lowest mpg. We can compute the intraclass correlation of mpg for all manufacturers with at least four models as follows:

```
. use https://www.stata-press.com/data/r19/auto7
(1978 automobile data)
. loneway mpg manufacturer_grp if nummake == 4
```

One-way analysis of variance for mpg: Mileage (mpg)

Source	SS	df	MS	F	Prob > F
Between manufacturer~p	621.88889	8	77.736111	3.70	0.0049
Within manufacturer~p	567.75	27	21.027778		
Total	1189.6389	35	33.989683		

Number of obs = 36
R-squared = 0.5228

Intraclass correlation	Asy. S.E.	[95% conf. interval]	
0.40270	0.18770	0.03481	0.77060

Estimated SD of manufacturer~p effect 3.765247
Estimated SD within manufacturer~p 4.585605
Est. reliability of a manufacturer~p mean 0.72950
(evaluated at n=4.00)

◀

In addition to the standard one-way ANOVA output, loneway produces the R^2 , the estimated standard deviation of the group effect, the estimated standard deviation within group, the intragroup correlation, the estimated reliability of the group-averaged mean, and, for unweighted data, the asymptotic standard error and confidence interval for the intragroup correlation.

R^2

The R^2 is, of course, simply the underlying R^2 for a regression of `response_var` on the levels of `group_var`, or mpg on the various manufacturers here.

The random-effects ANOVA model

loneway assumes that we observe a variable, y_{ij} , measured for n_i elements within k groups or classes such that

$$y_{ij} = \mu + \alpha_i + \epsilon_{ij}, \quad i = 1, 2, \dots, k, \quad j = 1, 2, \dots, n_i$$

and α_i and ϵ_{ij} are independent zero-mean random variables with variance σ_α^2 and σ_ϵ^2 , respectively. This is the random-effects ANOVA model, also known as the components-of-variance model, in which it is typically assumed that the y_{ij} are normally distributed.

The interpretation with respect to our example is that the observed value of our response variable, mpg, is created in two steps. First, the i th manufacturer is chosen, and a value, α_i , is determined—the typical mpg for that manufacturer less the overall mpg μ . Then a deviation, ϵ_{ij} , is chosen for the j th model within this manufacturer. This is how much that particular automobile differs from the typical mpg value for models from this manufacturer.

For our sample of 36 car models, the estimated standard deviations are $\sigma_\alpha = 3.8$ and $\sigma_\epsilon = 4.6$. Thus, a little more than half of the variation in mpg between cars is attributable to the car model, with the rest attributable to differences between manufacturers. These standard deviations differ from those that would be produced by a (standard) fixed-effects regression in that the regression would require the sum within each manufacturer of the ϵ_{ij} , ϵ_i , for the i th manufacturer, to be zero, whereas these estimates merely impose the constraint that the sum is *expected* to be zero.

Intraclass correlation

There are various estimators of the intraclass correlation, such as the pairwise estimator, which is defined as the Pearson product-moment correlation computed over all possible pairs of observations that can be constructed within groups. For a discussion of various estimators, see [Donner \(1986\)](#). loneway computes what is termed the analysis of variance, or ANOVA, estimator. This intraclass correlation is the theoretical upper bound on the variation in *response_var* that is explainable by *group_var*, of which R^2 is an overestimate because of the serendipity of fitting. This correlation is comparable to an R^2 —you do not have to square it.

In our example, the intra-manu correlation, the correlation of mpg within manufacturer, is 0.40. Because *aweights* were not used and the default correlation was computed (that is, the mean and median options were not specified), loneway also provided the asymptotic confidence interval and standard error of the intraclass correlation estimate.

Estimated reliability of the group-averaged score

The estimated reliability of the group-averaged score or mean has an interpretation similar to that of the intragroup correlation; it is a comparable number if we average *response_var* by *group_var*, or mpg by manu in our example. It is the theoretical upper bound of a regression of manufacturer-averaged mpg on characteristics of manufacturers. Why would we want to collapse our 36-observation dataset into a 9-observation dataset of manufacturer averages? Because the 36 observations might be a mirage. When General Motors builds cars, do they sometimes put a Pontiac label and sometimes a Chevrolet label on them, so that it appears in our data as if we have two cars when we really have only one, replicated? If that were the case, and if it were the case for many other manufacturers, then we would be forced to admit that we do not have data on 36 cars; we instead have data on nine manufacturer-averaged characteristics.

Stored results

loneway stores the following in `r()`:

Scalars

<code>r(N)</code>	number of observations	<code>r(rho_t)</code>	estimated reliability
<code>r(rho)</code>	intraclass correlation	<code>r(se)</code>	asyp. SE of intraclass correlation
<code>r(lb)</code>	lower bound of 95% CI for rho	<code>r(sd_w)</code>	estimated SD within group
<code>r(ub)</code>	upper bound of 95% CI for rho	<code>r(sd_b)</code>	estimated SD of group effect

Methods and formulas

The mean squares in the loneway's ANOVA table are computed as

$$MS_{\alpha} = \sum_i w_i (\bar{y}_i - \bar{y}_{..})^2 / (k - 1)$$

and

$$MS_{\epsilon} = \sum_i \sum_j w_{ij} (y_{ij} - \bar{y}_i)^2 / (N - k)$$

in which

$$w_i = \sum_j w_{ij} \quad w_{..} = \sum_i w_i \quad \bar{y}_i = \sum_j w_{ij} y_{ij} / w_i \quad \text{and} \quad \bar{y}_{..} = \sum_i w_i \bar{y}_i / w_{..}$$

The corresponding expected values of these mean squares are

$$E(MS_{\alpha}) = \sigma_{\epsilon}^2 + g\sigma_{\alpha}^2 \quad \text{and} \quad E(MS_{\epsilon}) = \sigma_{\epsilon}^2$$

in which

$$g = \frac{w_{..} - \sum_i w_i^2 / w_{..}}{k - 1}$$

In the unweighted case, we get

$$g = \frac{N - \sum_i n_i^2 / N}{k - 1}$$

As expected, $g = m$ for the case of no weights and equal group sizes in the data, that is, $n_i = m$ for all i . Replacing the expected values with the observed values and solving yields the ANOVA estimates of σ_{α}^2 and σ_{ϵ}^2 . Substituting these into the definition of the intraclass correlation

$$\rho = \frac{\sigma_{\alpha}^2}{\sigma_{\alpha}^2 + \sigma_{\epsilon}^2}$$

yields the ANOVA estimator of the intraclass correlation:

$$\rho_A = \frac{F_{\text{obs}} - 1}{F_{\text{obs}} - 1 + g}$$

F_{obs} is the observed value of the F statistic from the ANOVA table. For no weights and equal n_i , $\rho_A = \text{roh}$, which is the intragroup correlation defined by [Kish \(1965\)](#). Two slightly different estimators are available through the `mean` and `median` options ([Gleason 1997](#)). If either of these options is specified, the estimate of ρ becomes

$$\rho = \frac{F_{\text{obs}} - F_m}{F_{\text{obs}} + (g - 1)F_m}$$

For the mean option, $F_m = E(F_{k-1, N-K}) = (N - k)/(N - k - 2)$, that is, the expected value of the ANOVA table's F statistic. For the median option, F_m is simply the median of the F statistic. Setting F_m to 1 gives ρ_A , so for large samples, these different point estimators are essentially the same. Also, because the intraclass correlation of the random-effects model is by definition nonnegative, for any of the three possible point estimators, ρ is truncated to zero if F_{obs} is less than F_m .

For no weighting, interval estimators for ρ_A are computed. If the groups are equal sized (all n_i equal) and the exact option is specified, the following exact (assuming that the y_{ij} are normally distributed) $100(1 - \alpha)\%$ confidence interval is computed:

$$\left\{ \frac{F_{\text{obs}} - F_m F_u}{F_{\text{obs}} + (g - 1) F_m F_u}, \frac{F_{\text{obs}} - F_m F_l}{F_{\text{obs}} + (g - 1) F_m F_l} \right\}$$

with $F_m = 1$, $F_l = F_{\alpha/2, k-1, N-k}$, and $F_u = F_{1-\alpha/2, k-1, N-k}$, $F_{\cdot, k-1, N-k}$ being the cumulative distribution function for the F distribution with $k - 1$ and $N - k$ degrees of freedom. If mean or median is specified, F_m is defined as above. If the groups are equal sized and exact is not specified, the following asymptotic $100(1 - \alpha)\%$ confidence interval for ρ_A is computed,

$$\left[\rho_A - z_{\alpha/2} \sqrt{V(\rho_A)}, \rho_A + z_{\alpha/2} \sqrt{V(\rho_A)} \right]$$

where $z_{\alpha/2}$ is the $100(1 - \alpha/2)$ percentile of the standard normal distribution and $\sqrt{V(\rho_A)}$ is the asymptotic standard error of ρ defined below. This confidence interval is also available for unequal groups. It is not applicable and, therefore, not computed for the estimates of ρ provided by the mean and median options. Again, because the intraclass coefficient is nonnegative, if the lower bound is negative for either confidence interval, it is truncated to zero. As might be expected, the coverage probability of a truncated interval is higher than its nominal value.

The asymptotic standard error of ρ_A , assuming that the y_{ij} are normally distributed, is also computed when appropriate, namely, for unweighted data and when ρ_A is computed (neither the mean option nor the median option is specified):

$$V(\rho_A) = \frac{2(1 - \rho)^2}{g^2} (A + B + C)$$

with

$$A = \frac{\{1 + \rho(g - 1)\}^2}{N - k}$$

$$B = \frac{(1 - \rho)\{1 + \rho(2g - 1)\}}{k - 1}$$

$$C = \frac{\rho^2 \{\sum n_i^2 - 2N^{-1} \sum n_i^3 + N^{-2} (\sum n_i^2)^2\}}{(k - 1)^2}$$

and ρ_A is substituted for ρ (Donner 1986).

The estimated reliability of the group-averaged score, known as the Spearman–Brown prediction formula in the psychometric literature (Winer, Brown, and Michels 1991, 1014), is

$$\rho_t = \frac{t\rho}{1 + (t - 1)\rho}$$

for group size t . loneway computes ρ_t for $t = g$.

The estimated standard deviation of the group effect is $\sigma_\alpha = \sqrt{(\text{MS}_\alpha - \text{MS}_\epsilon)/g}$. This deviation comes from the assumption that an observation is derived by adding a group effect to a within-group effect.

The estimated standard deviation within group is the square root of the mean square due to error, or $\sqrt{\text{MS}_\epsilon}$.

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References

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Also see

- [R] **anova** — Analysis of variance and covariance
- [R] **icc** — Intraclass correlation coefficients
- [R] **oneway** — One-way analysis of variance

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