#### kwallis - Kruskal-Wallis equality-of-populations rank test

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### Description

kwallis performs a Kruskal–Wallis test of the hypothesis that several samples are from the same population. This test is a multisample generalization of the two-sample Wilcoxon (Mann–Whitney) rank-sum test.

### Quick start

Test the equality of distribution of v1 across all levels of categorical variable cvar kwallis v1, by(cvar)

Same as above, but perform the test only for observations with v2 = 1

```
kwallis v1 if v2==1, by(cvar)
```

### Menu

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## Syntax

```
kwallis varname [if ] [in], by(groupvar)
```

collect is allowed; see [U] 11.1.10 Prefix commands.

# Option

by (groupvar) is required. It specifies a variable that identifies the groups.

### **Remarks and examples**

#### Example 1

We have data on the 50 states. The data contain the median age of the population, medage, and the region of the country, region, for each state. We wish to test for the equality of the median age distribution across all four regions simultaneously:

. use https://www.stata-press.com/data/r19/census

- (1980 Census data by state)
- . kwallis medage, by(region)

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region	Obs	Rank sum		
NE	9	376.50		
N Cntrl	12	294.00		
South	16	398.00		
West	13	206.50		
chi2(3) = 17.041 Prob = 0.0007				
chi2(3) with ties = 17.062 Prob = 0.0007				

From the output, we see that we can reject the hypothesis that the populations are the same at any level below 0.07%.

### Stored results

kwallis stores the following in r():

```
Scalars

r(df) degrees of freedom

r(chi2) \chi^2

r(chi2_adj) \chi^2 adjusted for ties
```

#### Methods and formulas

The Kruskal–Wallis test (Kruskal and Wallis 1952, 1953; also see Altman [1991, 213–215]; Conover [1999, 288–297]; and Riffenburgh [2012, sec. 11.6]) is a multiple-sample generalization of the two-sample Wilcoxon (also called Mann–Whitney) rank-sum test (Wilcoxon 1945; Mann and Whitney 1947). Samples of sizes  $n_j$ , j = 1, ..., m, are combined and ranked in ascending order of magnitude. Tied values are assigned the average ranks. Let n denote the overall sample size, and let  $R_j = \sum_{i=1}^{n_j} R(X_{ji})$  denote the sum of the ranks for the *j*th sample. The Kruskal–Wallis one-way analysis-of-variance test, H, is defined as

$$H = \frac{1}{S^2} \left\{ \sum_{j=1}^m \frac{R_j^2}{n_j} - \frac{n(n+1)^2}{4} \right\}$$

where

$$S^2 = \frac{1}{n-1} \left\{ \sum_{\text{all ranks}} R(X_{ji})^2 - \frac{n(n+1)^2}{4} \right\}$$

If there are no ties, this equation simplifies to

$$H = \frac{12}{n(n+1)} \sum_{j=1}^m \frac{R_j^2}{n_j} - 3(n+1)$$

The sampling distribution of H is approximately  $\chi^2$  with m-1 degrees of freedom.

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William Henry Kruskal (1919–2005) was born in New York City. He studied mathematics and statistics at Antioch College, Harvard, and Columbia, and joined the University of Chicago in 1951. He made many outstanding contributions to linear models, nonparametric statistics, government statistics, and the history and methodology of statistics.

Wilson Allen Wallis (1912–1998) was born in Philadelphia. He studied psychology and economics at the Universities of Minnesota and Chicago and at Columbia. He taught at Yale, Stanford, and Chicago, before moving as president (later chancellor) to the University of Rochester in 1962. He also served in several Republican administrations. Wallis served as editor of the *Journal of the American Statistical Association*, coauthored a popular introduction to statistics, and contributed to nonparametric statistics.

### References

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# Also see

- [R] nptrend Tests for trend across ordered groups
- [R] oneway One-way analysis of variance
- [R] ranksum Equality tests on unmatched data
- [R] sdtest Variance-comparison tests

[R] **signrank** — Equality tests on matched data

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