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Description

`intreg` fits a linear model with an outcome measured as point data, interval data, left-censored data, or right-censored data. As such, it is a generalization of the model fit by `tobit`.

Quick start

Regression on `x1` and `x2` of an interval-measured dependent variable with lower endpoint `y_lower` and upper endpoint `y_upper`

```
intreg y_lower y_upper x1 x2
```

With robust standard errors

```
intreg y_lower y_upper x1 x2, vce(robust)
```

Model heteroskedasticity in the conditional variance as a function of `x3`

```
intreg y_lower y_upper x1 x2, het(x3)
```

Adjust for complex survey design using `svyset` data

```
svy: intreg y_lower y_upper x1 x2
```

Menu

Statistics > Linear models and related > Censored regression > Interval regression

Syntax

```
intreg depvar1 depvar2 [indepvars] [if] [in] [weight] [, options]
```

*depvar*₁ and *depvar*₂ should have the following form:

Type of data		<i>depvar</i> ₁	<i>depvar</i> ₂
point data	$a = [a, a]$	<i>a</i>	<i>a</i>
interval data	$[a, b]$	<i>a</i>	<i>b</i>
left-censored data	$(-\infty, b]$.	<i>b</i>
right-censored data	$[a, +\infty)$	<i>a</i>	.
missing		.	.

<i>options</i>	Description
Model	
<code>noconstant</code>	suppress constant term
<code>het(<i>varlist</i> [, <code>noconstant</code>])</code>	independent variables to model the variance; use <code>noconstant</code> to suppress constant term
<code>offset(<i>varname</i>)</code>	include <i>varname</i> in model with coefficient constrained to 1
<code>constraints(<i>constraints</i>)</code>	apply specified linear constraints
<code>collinear</code>	keep collinear variables
SE/Robust	
<code>vce(<i>vcetype</i>)</code>	<i>vcetype</i> may be <code>oim</code> , <code>robust</code> , <code>cluster <i>clustvar</i></code> , <code>opg</code> , <code>bootstrap</code> , or <code>jackknife</code>
Reporting	
<code>level(#)</code>	set confidence level; default is <code>level(95)</code>
<code>nocnsreport</code>	do not display constraints
<code>display_options</code>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
<code>maximize_options</code>	control the maximization process; seldom used
<code>coeflegend</code>	display legend instead of statistics

indepvars and *varlist* may contain factor variables; see [U] 11.4.3 **Factor variables**.

*depvar*₁, *depvar*₂, *indepvars*, and *varlist* may contain time-series operators; see [U] 11.4.4 **Time-series varlists**.

`bayes`, `bootstrap`, `by`, `fmm`, `fp`, `jackknife`, `mfp`, `nestreg`, `rolling`, `statsby`, `stepwise`, and `svy` are allowed; see [U] 11.1.10 **Prefix commands**. For more details, see [BAYES] **bayes: intreg** and [FMM] **fmm: intreg**.

Weights are not allowed with the `bootstrap` prefix; see [R] **bootstrap**.

`aweight`s are not allowed with the `jackknife` prefix; see [R] **jackknife**.

`vce()` and weights are not allowed with the `svy` prefix; see [SVY] **svy**.

`aweight`s, `fweight`s, `iweight`s, and `pweight`s are allowed; see [U] 11.1.6 **weight**.

`coeflegend` does not appear in the dialog box.

See [U] 20 **Estimation and postestimation commands** for more capabilities of estimation commands.

Options

Model

`noconstant`; see [R] [estimation options](#).

`het(varlist [, noconstant])` specifies that the logarithm of the standard deviation be modeled as a linear combination of *varlist*. The constant is included unless `noconstant` is specified.

`offset(varname)`, `constraints(constraints)`, `collinear`; see [R] [estimation options](#).

SE/Robust

`vce(vcetype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`oim`, `opg`), that are robust to some kinds of misspecification (`robust`), that allow for intragroup correlation (`cluster clustvar`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [R] [vce_option](#).

Reporting

`level(#)`; see [R] [estimation options](#).

`nocnsreport`; see [R] [estimation options](#).

`display_options`: `nocl`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `noliststretch`; see [R] [estimation options](#).

Maximization

`maximize_options`: `difficult`, `technique(algorithm_spec)`, `iterate(#)`, `[no]log`, `trace`, `gradient`, `showstep`, `hessian`, `showtolerance`, `tolerance(#)`, `ltolerance(#)`, `nrtolerance(#)`, `nonrtolerance`, and `from(init_specs)`; see [R] [maximize](#). These options are seldom used.

Setting the optimization type to `technique(bhhh)` resets the default *vcetype* to `vce(opg)`.

The following option is available with `intreg` but is not shown in the dialog box:

`coeflegend`; see [R] [estimation options](#).

Remarks and examples

[stata.com](http://www.stata.com)

`intreg` fits a linear model to an outcome that may be either observed exactly or unobserved but known to fall within some interval. The values of the outcome variable may be observed (point data), unobserved but known to fall within an interval with fixed endpoints (interval-censored data), unobserved but known to fall within an interval that has a fixed upper endpoint (left-censored data), or unobserved but known to fall within an interval that has a fixed lower endpoint (right-censored data). Such censored data arise naturally in many contexts, such as wage data. Often you know only that, for example, a person's salary is between \$30,000 and \$40,000.

The interval regression model fit by `intreg` is a generalization of the models fit by `tobit` because it extends censoring beyond left-censored data or right-censored data; see Cameron and Trivedi (2010, 548–550) for additional discussion of these data types. See Wooldridge (2016, sec. 17.4) for an introduction to censored and truncated regression models.

Regardless of the type of censoring, `intreg` requires the outcome to be stored in the dataset as interval data. That is, two dependent variables, `depvar1` and `depvar2`, are used to hold the endpoints of the interval. If the data are left-censored, the lower endpoint is $-\infty$ and is represented by a missing value in `depvar1`. If the data are right-censored, the upper endpoint is $+\infty$ and is represented by a missing value in `depvar2`. Point data are represented by the two endpoints being equal. Truly missing values of the dependent variable must be represented by missing values in both `depvar1` and `depvar2`.

▷ Example 1: Interval regression

`womenwage2.dta` contains the yearly wages of working women in interval form. Women were asked to indicate a category for their yearly income from employment. The categories were \$5,000 or less, \$5,001–\$10,000, . . . , \$25,001–\$30,000, \$30,001–\$40,000, \$40,001–\$50,000, and more than \$50,000. The lower and upper endpoints of the wage categories (in \$1,000s) are recorded in variables `wage1` and `wage2`. Below we list the first 10 observations in `wage1` and `wage2`.

```
. use http://www.stata-press.com/data/r15/womenwage2
(Wages of women, fictional data)
. list wage1 wage2 in 1/10
```

	wage1	wage2
1.	.	5
2.	5	10
3.	5	10
4.	10	15
5.	15	20
6.	20	25
7.	25	30
8.	30	40
9.	40	50
10.	50	.

We see, for example, that the first respondent made \$5,000 or less in a year, that the second respondent made between \$5,001 and \$10,000 in a year, and so on. The tenth respondent made at least \$50,000 a year.

We now fit an interval regression model of women’s wages using social and demographic characteristics as explanatory variables. The variables include the subject’s age (`age`), years of schooling (`school`), job tenure (`tenure`), a dummy for living in a rural area (`rural`), and a dummy for never being married (`nev_mar`).

```

. intreg wage1 wage2 age c.age#c.age i.nev_mar i.rural school tenure
Fitting constant-only model:
Iteration 0:   log likelihood = -967.24956
Iteration 1:   log likelihood = -967.1368
Iteration 2:   log likelihood = -967.1368
Fitting full model:
Iteration 0:   log likelihood = -856.65324
Iteration 1:   log likelihood = -856.33294
Iteration 2:   log likelihood = -856.33293
Interval regression
                Number of obs   =           488
                Uncensored      =             0
                Left-censored   =             14
                Right-censored  =              6
                Interval-cens.  =           468
                LR chi2(6)      =           221.61
                Prob > chi2     =            0.0000
Log likelihood = -856.33293

```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.7914438	.4433604	1.79	0.074	-.0775265	1.660414
c.age#c.age	-.0132624	.0073028	-1.82	0.069	-.0275757	.0010509
1.nev_mar	-.2075022	.8119581	-0.26	0.798	-1.798911	1.383906
1.rural	-3.043044	.7757324	-3.92	0.000	-4.563452	-1.522637
school	1.334721	.1357873	9.83	0.000	1.068583	1.600859
tenure	.8000664	.1045077	7.66	0.000	.5952351	1.004898
_cons	-12.70238	6.367117	-1.99	0.046	-25.1817	-.2230583
/lnsigma	1.987823	.0346543	57.36	0.000	1.919902	2.055744
sigma	7.299626	.2529634			6.82029	7.81265

Because the conditional mean modeled by interval regression is linear, the coefficients are interpreted the same way they are in ordinary least-squares regression; see [\[R\] regress](#). For example, residing in a rural area lowers the expected income by \$3,043 and each additional year of schooling raises the expected income by \$1,335.

□ Technical note

Instead of using intervals to record wages, we could treat the outcome as categorical with a higher category corresponding to a higher wage. Here we fit an ordered probit model for `wagecat`, created based on groups defined by the intervals, by using `oprobit` (see [R] [oprobit](#)) with the same covariates:

```
. oprobit wagecat age c.age#c.age i.nev_mar i.rural school tenure
Iteration 0:  log likelihood = -881.1491
Iteration 1:  log likelihood = -764.31729
Iteration 2:  log likelihood = -763.31191
Iteration 3:  log likelihood = -763.31049
Iteration 4:  log likelihood = -763.31049

Ordered probit regression                Number of obs   =       488
                                         LR chi2(6)      =       235.68
                                         Prob > chi2     =       0.0000
                                         Pseudo R2      =       0.1337

Log likelihood = -763.31049
```

wagecat	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.1674519	.0620333	2.70	0.007	.0458689	.289035
c.age#c.age	-.0027983	.0010214	-2.74	0.006	-.0048001	-.0007964
1.nev_mar	-.0046417	.1126737	-0.04	0.967	-.225478	.2161946
1.rural	-.5270036	.1100449	-4.79	0.000	-.7426875	-.3113196
school	.2010587	.0201189	9.99	0.000	.1616263	.2404911
tenure	.0989916	.0147887	6.69	0.000	.0700063	.127977
/cut1	2.650637	.8957245			.8950495	4.406225
/cut2	3.941018	.8979167			2.181134	5.700903
/cut3	5.085205	.9056582			3.310148	6.860263
/cut4	5.875534	.9120933			4.087864	7.663204
/cut5	6.468723	.918117			4.669247	8.268199
/cut6	6.922726	.9215455			5.11653	8.728922
/cut7	7.34471	.9237628			5.534168	9.155252
/cut8	7.963441	.9338881			6.133054	9.793828

We can directly compare the log likelihoods for the `intreg` and `oprobit` models because both likelihoods are discrete. If we had point data in our `intreg` estimation, the likelihood would be a mixture of discrete and continuous terms, and we could not compare it directly with the `oprobit` likelihood.

Here the `oprobit` log likelihood is significantly larger (that is, less negative), so it fits better than the `intreg` model. The `intreg` model assumes normality, but the distribution of wages is skewed and definitely nonnormal. Normality is more closely approximated if we model the log of wages.

```

. generate logwage1 = log(wage1)
(14 missing values generated)
. generate logwage2 = log(wage2)
(6 missing values generated)
. intreg logwage1 logwage2 age c.age#c.age i.nev_mar i.rural school tenure
Fitting constant-only model:
Iteration 0:   log likelihood = -889.23647
Iteration 1:   log likelihood = -889.06346
Iteration 2:   log likelihood = -889.06346
Fitting full model:
Iteration 0:   log likelihood = -773.81968
Iteration 1:   log likelihood = -773.36566
Iteration 2:   log likelihood = -773.36563
Interval regression
Number of obs   =      488
Uncensored     =         0
Left-censored  =        14
Right-censored =         6
Interval-cens. =       468
LR chi2(6)     =       231.40
Prob > chi2    =         0.0000
Log likelihood = -773.36563

```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.0645589	.0249954	2.58	0.010	.0155689	.1135489
c.age#c.age	-.0010812	.0004115	-2.63	0.009	-.0018878	-.0002746
1.nev_mar	-.0058151	.0454867	-0.13	0.898	-.0949674	.0833371
1.rural	-.2098361	.0439454	-4.77	0.000	-.2959675	-.1237047
school	.0804832	.0076783	10.48	0.000	.0654341	.0955323
tenure	.0397144	.0058001	6.85	0.000	.0283464	.0510825
_cons	.7084023	.3593193	1.97	0.049	.0041495	1.412655
/lnsigma	-.906989	.0356265	-25.46	0.000	-.9768157	-.8371623
sigma	.4037381	.0143838			.3765081	.4329373

The log likelihood of this intreg model is close to the oprobit log likelihood, and the z statistics for both models are similar. □

Stored results

`intreg` stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(N_unc)</code>	number of uncensored observations
<code>e(N_ltc)</code>	number of left-censored observations
<code>e(N_rc)</code>	number of right-censored observations
<code>e(N_int)</code>	number of interval observations
<code>e(k)</code>	number of parameters
<code>e(k_aux)</code>	number of auxiliary parameters
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_eq_model)</code>	number of equations in overall model test
<code>e(k_dv)</code>	number of dependent variables
<code>e(df_m)</code>	model degrees of freedom
<code>e(ll)</code>	log likelihood
<code>e(ll_0)</code>	log likelihood, constant-only model
<code>e(N_clust)</code>	number of clusters
<code>e(chi2)</code>	χ^2
<code>e(p)</code>	p -value for model χ^2 test
<code>e(sigma)</code>	sigma
<code>e(se_sigma)</code>	standard error of sigma
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(rank0)</code>	rank of <code>e(V)</code> for constant-only model
<code>e(ic)</code>	number of iterations
<code>e(rc)</code>	return code
<code>e(converged)</code>	1 if converged, 0 otherwise

Macros

<code>e(cmd)</code>	<code>intreg</code>
<code>e(cmdline)</code>	command as typed
<code>e(depvar)</code>	names of dependent variables
<code>e(wtype)</code>	weight type
<code>e(wexp)</code>	weight expression
<code>e(title)</code>	title in estimation output
<code>e(clustvar)</code>	name of cluster variable
<code>e(offset)</code>	linear offset variable
<code>e(chi2type)</code>	Wald or LR; type of model χ^2 test
<code>e(vce)</code>	<code>vcetype</code> specified in <code>vce()</code>
<code>e(vcetype)</code>	title used to label Std. Err.
<code>e(het)</code>	heteroskedasticity, if <code>het()</code> specified
<code>e(ml_score)</code>	program used to implement <code>scores</code>
<code>e(opt)</code>	type of optimization
<code>e(which)</code>	max or min; whether optimizer is to perform maximization or minimization
<code>e(ml_method)</code>	type of ml method
<code>e(user)</code>	name of likelihood-evaluator program
<code>e(technique)</code>	maximization technique
<code>e(properties)</code>	<code>b V</code>
<code>e(predict)</code>	program used to implement <code>predict</code>
<code>e(marginsok)</code>	predictions allowed by <code>margins</code>
<code>e(asbalanced)</code>	factor variables <code>fvset</code> as <code>asbalanced</code>
<code>e(asobserved)</code>	factor variables <code>fvset</code> as <code>asobserved</code>

Matrices

<code>e(b)</code>	coefficient vector
<code>e(Cns)</code>	constraints matrix
<code>e(ilog)</code>	iteration log (up to 20 iterations)
<code>e(gradient)</code>	gradient vector
<code>e(V)</code>	variance-covariance matrix of the estimators
<code>e(V_modelbased)</code>	model-based variance

Functions

<code>e(sample)</code>	marks estimation sample
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Methods and formulas

The regression equation of interest is

$$y_j = \mathbf{x}_j\boldsymbol{\beta} + \epsilon_j$$

where y_j is a continuous outcome for the j th observation—either observed or unobserved—with covariates \mathbf{x}_j and corresponding coefficients $\boldsymbol{\beta}$. The model assumes that the error term is normally distributed; $\epsilon \sim N(0, \sigma^2)$.

For observations $j \in \mathcal{C}$, we observe y_j , that is, point data. Observations $j \in \mathcal{I}$ are intervals; we know only that the unobserved y_j is in the interval $[y_{1j}, y_{2j}]$. For these observations, the likelihood contribution is $\Pr(y_{1j} \leq Y_j \leq y_{2j})$, where Y_j denotes the random variable representing the dependent variable in the model. Observations $j \in \mathcal{L}$ are left-censored; we know only that the unobserved y_j is less than or equal to $y_{\mathcal{L}j}$, a censoring value that we do know. Similarly, observations $j \in \mathcal{R}$ are right-censored; we know only that the unobserved y_j is greater than or equal to $y_{\mathcal{R}j}$. The likelihoods for these censored observations contain terms of the form $\Pr(Y_j \leq y_{\mathcal{L}j})$ for left-censored data and $\Pr(Y_j \geq y_{\mathcal{R}j})$ for right-censored data.

The log likelihood is

$$\begin{aligned} \ln L = & -\frac{1}{2} \sum_{j \in \mathcal{C}} w_j \left\{ \left(\frac{y_j - \mathbf{x}_j\boldsymbol{\beta}}{\sigma} \right)^2 + \log 2\pi\sigma^2 \right\} \\ & + \sum_{j \in \mathcal{L}} w_j \log \Phi \left(\frac{y_{\mathcal{L}j} - \mathbf{x}_j\boldsymbol{\beta}}{\sigma} \right) \\ & + \sum_{j \in \mathcal{R}} w_j \log \left\{ 1 - \Phi \left(\frac{y_{\mathcal{R}j} - \mathbf{x}_j\boldsymbol{\beta}}{\sigma} \right) \right\} \\ & + \sum_{j \in \mathcal{I}} w_j \log \left\{ \Phi \left(\frac{y_{2j} - \mathbf{x}_j\boldsymbol{\beta}}{\sigma} \right) - \Phi \left(\frac{y_{1j} - \mathbf{x}_j\boldsymbol{\beta}}{\sigma} \right) \right\} \end{aligned}$$

where $\Phi(\cdot)$ is the cumulative standard normal distribution and w_j is the weight for the j th observation. If no weights are specified, $w_j = 1$. If `aweight`s are specified, $w_j = 1$, and σ is replaced by $\sigma/\sqrt{a_j}$ in the above, where a_j are the `aweight`s normalized to sum to N .

When the `het()` option is specified, σ is modeled as $\ln(\sigma) = z'_j\boldsymbol{\gamma}$, where z represents the variables in `het()` and $\boldsymbol{\gamma}$ is a vector of the estimated parameters to model the variance.

Note that the likelihood for `intreg` subsumes that of the `tobit` models; see [R] [tobit](#).

Maximization is as described in [R] [maximize](#). `intreg` stores the estimated σ in `e(b)` in the log metric; therefore, if you want to provide an initial value for σ or to specify a constraint on it, ensure you do so on the log scale.

This command supports the Huber/White/sandwich estimator of the variance and its clustered version using `vce(robust)` and `vce(cluster clustvar)`, respectively. See [P] [_robust](#), particularly [Maximum likelihood estimators](#) and [Methods and formulas](#).

`intreg` also supports estimation with survey data. For details on VCEs with survey data, see [SVY] [variance estimation](#).

References

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Also see

- [R] **intreg postestimation** — Postestimation tools for intreg
- [R] **regress** — Linear regression
- [R] **tobit** — Tobit regression
- [BAYES] **bayes: intreg** — Bayesian interval regression
- [FMM] **fmm: intreg** — Finite mixtures of interval regression models
- [ME] **meintreg** — Multilevel mixed-effects interval regression
- [ST] **stintreg** — Parametric models for interval-censored survival-time data
- [SVY] **svy estimation** — Estimation commands for survey data
- [XT] **xtintreg** — Random-effects interval-data regression models
- [XT] **xttobit** — Random-effects tobit models
- [U] **20 Estimation and postestimation commands**