dstdize — Direct and indirect standardization

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Description

dstdize produces standardized rates, a weighted average of the stratum-specific rates.

istdize produces indirectly standardized rates that are appropriate when the stratum-specific rates for the population being studied are either unavailable or unreliable.

istdize also calculates a point estimate and exact confidence interval for the study population's standardized mortality ratio (SMR) or the standardized incidence ratio (SIR).

Quick start

Direct standardization

Use reference population saved in mypop.dta to standardize v1 with stratum identifier svar and stratum size v2 for catvar

dstdize v1 v2 svar, by(catvar) using(mypop)

Same as above, but with reference population in memory where catvar = 1dstdize v1 v2 svar, by(catvar) base(1)

```
Same as above, but with reference population in memory where catvar = "nation"
```

dstdize v1 v2 svar, by(catvar) base("nation")

Indirect standardization

Use population cases and size saved in cases and pop to standardize study cases v3 and stratum size v4 at each level of svar

istdize v3 v4 svar using mypop.dta, popvars(cases pop)

Same as above, but standardize subpopulations identified by levels of catvar

isdize v3 v4 svar using mypop.dta, popvars(cases pop) by(catvar)

Same as above, but standardize by population stratum-specific and crude rates saved in srate and crate and display summary of standard population

isdize v3 v4 svar using mypop.dta, rate(srate crate) by(catvar) print

Same as above, but indicate that the crude population rate is 0.01

isdize v3 v4 svar using mypop.dta, rate(srate .01) by(catvar) print

Menu

dstdize

 $\label{eq:statistics} Statistics > \mbox{Epidemiology and related} > \mbox{Other} > \mbox{Direct standardization}$

istdize

Statistics > Epidemiology and related > Other > Indirect standardization

Syntax

Direct standardization

dstdize charvar popvar stratavars [if] [in], by(groupvars) [dstdize_options]

Indirect standardization

```
istdize casevar<sub>s</sub> popvar<sub>s</sub> stratavars [if] [in] using filename,
```

 $\{ \underline{popvars}(casevar_p \ popvar_p) | rate(ratevar_p \{ \# | crudevar_p \}) \}$

[istdize_options]

charvar is the characteristic to be standardized across different subpopulations identified by *groupvars*. *popvar* defines the weights used in standardization.

stratavars defines the strata across which the weights are to be averaged in dstdize. For istdize, stratavars defines the strata for which $casevar_s$ is measured.

casevar_s is the variable name for the study population's number of cases. If by (*groupvars*) is specified, *casevar_s* must be constant or missing within each group defined by combinations of *groupvars*.

popvar_s identifies the number of subjects in each strata in the study population.

filename must be a Stata dataset and contain popvar and stratavars.

Description
study populations
use standard population from Stata dataset
use standard population from a value of grouping variable
set confidence level; default is level(95)
save computed standard population distribution as a Stata dataset
final summary table display format; default is %10.0g
include table summary of standard population in output
suppress storing results in r()

*by(groupvars) is required.

istdize_options	Description
Main	
* $\underline{pop}vars(casevar_p popvar_p)$	for standard population, $casevar_p$ is number of cases and $popvar_p$ is number of individuals
* rate(ratevar _p {# crudevar _p })	$ratevar_p$ is stratum-specific rates and $\#$ or $crudevar_p$ is the crude case rate value or variable
<u>l</u> evel(#)	set confidence level; default is level(95)
Options	
by (groupvars)	variables identifying study populations
<u>f</u> ormat(% <i>fmt</i>)	final summary table display format; default is %10.0g
<u>pr</u> int	include table summary of standard population in output

*Either popvars (*casevar*_p popvar_p) or rate (*ratevar*_p {# | *crudevar*_p}) must be specified.

collect is allowed with dstdize and istdize; see [U] 11.1.10 Prefix commands.

Options for dstdize

(Main)

- by (groupvars) is required for the dstdize command; it specifies the variables identifying the study populations. If base() is also specified, there must be only one variable in the by() group. If you do not have a variable for this option, you can generate one by using something like generate newvar=1 and then use newvar as the argument to this option.
- using(filename) or base(#|string) may be used to specify the standard population. You may not specify both options. using(filename) supplies the name of a .dta file containing the standard population. The standard population must contain the popvar and the stratavars. If using() is not specified, the standard population distribution will be obtained from the data. base(#|string) lets you specify one of the values of groupvar—either a numeric value or a string—to be used as the standard population. If neither base() nor using() is specified, the entire dataset is used to determine an estimate of the standard population.
- level(#) specifies the confidence level, as a percentage, for a confidence interval of the adjusted rate. The default is level(95) or as set by set level; see [U] 20.8 Specifying the width of confidence intervals.

Options

saving(filename) saves the computed standard population distribution as a Stata dataset that can be used in further analyses.

format (% fint) specifies the format in which to display the final summary table. The default is %10.0g.

print includes a table summary of the standard population before displaying the study population results.

nores suppresses storing results in r(). This option is seldom specified. Some results are stored in matrices. If there are more groups than can fit in a matrix, dstdize will report the "unable to allocate matrix" error message. In this case, you must specify nores. The nores option does not change how results are calculated but specifies that results need not be left behind for use by other programs.

Options for istdize

Main

popvars $(casevar_p popvar_p)$ or rate $(ratevar_p \{\# | crudevar_p\})$ must be specified with istdize. Only one of these two options is allowed. These options are used to describe the standard population's data.

With popvars (*casevar_p* popvar_p), *casevar_p* records the number of cases (deaths) for each stratum in the standard population, and popvar_p records the total number of individuals in each stratum (individuals at risk).

With rate $(ratevar_p \{\# | crudevar_p\})$, $ratevar_p$ contains the stratum-specific rates. $\# | crudevar_p$ specifies the crude case rate either by a variable name or by the crude case rate value. If a crude rate variable is used, it must be the same for all observations, although it could be missing for some.

level(#) specifies the confidence level, as a percentage, for a confidence interval of the adjusted rate. The default is level(95) or as set by set level; see [U] 20.8 Specifying the width of confidence intervals.

Options

by (*groupvars*) specifies variables identifying study populations when more than one exists in the data. If this option is not specified, the entire study population is treated as one group.

format (% fmt) specifies the format in which to display the final summary table. The default is %10.0g.

print outputs a table summary of the standard population before displaying the study population results.

Remarks and examples

Remarks are presented under the following headings:

Direct standardization Indirect standardization

In epidemiology and other fields, you will often need to compare rates for some characteristic across different populations. These populations often differ on factors associated with the characteristic under study; thus, directly comparing overall rates may be misleading.

See van Belle et al. (2004, 642–684), Fleiss, Levin, and Paik (2003, chap. 19), or Kirkwood and Sterne (2003, chap. 25) for a discussion of direct and indirect standardization.

Direct standardization

The direct method of adjusting for differences among populations involves computing the overall rates that would result if, instead of having different distributions, all populations had the same standard distribution. The standardized rate is defined as a weighted average of the stratum-specific rates, with the weights taken from the standard distribution. Direct standardization may be applied only when the specific rates for a given population are available.

dstdize generates adjusted summary measures of occurrence, which can be used to compare prevalence, incidence, or mortality rates between populations that may differ on certain characteristics (for example, age, gender, race). These underlying differences may affect the crude prevalence, mortality, or incidence rates.

Example 1

We have data (Rothman 1986, 42) on mortality rates for Sweden and Panama for 1962, and we wish to compare mortality in these two countries:

```
. use https://www.stata-press.com/data/r19/mortality
(1962 Mortality, Sweden & Panama)
. describe
Contains data from https://www.stata-press.com/data/r19/mortality.dta
 Observations:
                            6
                                                1962 Mortality, Sweden & Panama
   Variables:
                            4
                                                14 Apr 2024 16:18
Variable
                         Display
                                    Value
              Storage
                          format
                                    label
                                                Variable label
   name
                 type
nation
                str6
                         %9s
                                                Nation
                         %9.0g
age_category
                byte
                                    age_lbl
                                                Age category
                         %10.0gc
                                                Population in age category
population
                float
deaths
                float
                         %9.0gc
                                                Deaths in age category
```

Sorted by:

. list, sepby(nation) abbrev(12) divider

	nation	age_category	population	deaths
1.	Sweden	0-29	3145000	3,523
2.	Sweden	30-59	3057000	10,928
3.	Sweden	60+	1294000	59,104
4.	Panama	0-29	741,000	3,904
5.	Panama	30-59	275,000	1,421
6.	Panama	60+	59,000	2,456

We divide the total number of cases in the population by the population to obtain the *crude rate*:

. collapse (sum) pop deaths, by(nation)

. list, abbrev(10) divider

	nation	population	deaths
1.	Panama	1075000	7,781
2.	Sweden	7496000	73,555

. generate crude = deaths/pop

. list, abbrev(10) divider

	nation	population	deaths	crude
1.	Panama	1075000	7,781	.0072381
2.	Sweden	7496000	73,555	.0098126

If we examine the total number of deaths in the two nations, the total crude mortality rate in Sweden is higher than that in Panama. From the original data, we see one possible explanation: Swedes are older than Panamanians, making direct comparison of the mortality rates difficult.

Direct standardization lets us remove the distortion caused by the different age distributions. The adjusted rate is defined as the weighted sum of the crude rates, where the weights are given by the standard distribution. Suppose that we wish to standardize these mortality rates to the following age distribution:

```
. use https://www.stata-press.com/data/r19/1962, clear (Standard population distribution)
```

. list, abbrev(12) divider

	age_category	population
1.	0-29	.35
2.	30-59	.35
З.	60+	.3
5.	00+	

```
. save 1962
file 1962.dta saved
```

If we multiply the above weights for the age strata by the crude rate for the corresponding age category, the sum gives us the standardized rate.

```
. list, sepby(age_category) abbrev(12)
```

	nation	age_category	deaths	crude	population	_merge
1.	Sweden	0-29	3,523	.0011202	.35	Matched (3)
2.	Panama	0-29	3,904	.0052686	.35	Matched (3)
3.	Sweden	30–59	10,928	.0035747	.35	Matched (3)
4.	Panama	30–59	1,421	.0051673	.35	Matched (3)
5.	Sweden	60+	59,104	.0456754	.3	Matched (3)
6.	Panama	60+	2,456	.0416271	.3	Matched (3)

. generate product = crude*pop

```
. by nation, sort: egen adj_rate = sum(product)
```

. drop _merge

	nation	age_ca~y	deaths	crude	popula~n	product	adj_rate
1.	Panama	60+	2,456	.0416271	.3	.0124881	.0161407
2.	Panama	30-59	1,421	.0051673	.35	.0018085	.0161407
З.	Panama	0-29	3,904	.0052686	.35	.001844	.0161407
4.	Sweden	0-29	3,523	.0011202	. 35	.0003921	.0153459
5.	Sweden	60+	59,104	.0456754	.3	.0137026	.0153459
6.	Sweden	30-59	10,928	.0035747	.35	.0012512	.0153459

. list, sepby(nation)

Comparing the standardized rates indicates that the Swedes have a slightly lower mortality rate.

To perform the above analysis with dstdize, type

. use https://www.stata-press.com/data/r19/mortality, clear (1962 Mortality, Sweden & Panama)
. dstdize deaths pop age_cat, by(nation) using(1962)
Direct standardization

-> nation = Panama Unadjusted---Std. Pop. Stratum pop. Stratum Pop. Cases dist. rate dist. s*P 0-29 741,000 3,904 0.689 0.0053 0.350 0.0018 0.0052 30-59 275,000 1,421 0.256 0.350 0.0018 60+ 59,000 2,456 0.055 0.0416 0.300 0.0125

Total: 1,075,000 7,781

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 17,351.2 Crude rate = 0.0072 Adjusted rate = 0.0161 95% conf. interval: [0.0156, 0.0166]

= Sweden					
	U	nadjust	ted	Std.	
		Pop.	Stratum	pop.	
Pop.	Cases	dist.	rate	dist.	s*P
3,145,000	3,523	0.420	0.0011	0.350	0.0004
3,057,000	10,928	0.408	0.0036	0.350	0.0013
1,294,000	59,104	0.173	0.0457	0.300	0.0137
	Pop. 3,145,000 3,057,000	Pop. Cases 3,145,000 3,523 3,057,000 10,928	Unadjust Pop. Cases dist. 3,145,000 3,523 0.420 3,057,000 10,928 0.408	Unadjusted Pop. Stratum Pop. Cases dist. rate 3,145,000 3,523 0.420 0.0011 3,057,000 10,928 0.408 0.0036	Unadjusted Std. Pop. Cases dist. rate dist. 3,145,000 3,523 0.420 0.0011 0.350 3,057,000 10,928 0.408 0.0036 0.350

Total: 7,496,000 73,555

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 115,032.5 Crude rate = 0.0098 Adjusted rate = 0.0153 95% conf. interval: [0.0152, 0.0155]

Summary of	Summary of study populations							
nation	Ν	Crude rate	Adjusted rate	[95% conf.	interval]			
Panama Sweden	1,075,000 7,496,000	0.007238 0.009813	0.016141 0.015346	0.015645 0.015235	0.016637 0.015457			

The summary table above lets us make a quick inspection of the results within the study populations, and the detail tables give the behavior among the strata within the study populations.

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Example 2

We have individual-level data on persons in four cities over several years. Included in the data is a variable indicating whether the person has high blood pressure, together with information on the person's age, sex, and race. We wish to obtain standardized high blood pressure rates for each city for 1990 and 1992, using, as the standard, the age, sex, and race distribution of the four cities and two years combined.

Our dataset contains

Contains dat	ta from htt	ne.//uuu et	ata-press o	om/data/r19/hbp.dta
Observation		1,130	ata press.c	
Variable	es:	7		21 Feb 2024 06:42
Variable	Storage	Display	Value	
name	type	format	label	Variable label
id	str10	%10s		Record identification number
city	byte	%8.0g		City
year	int	%8.0g		Year
sex	byte	%8.0g	sexfmt	Sex
age_group	byte	%8.0g	agefmt	Age group
race	byte	%8.0g	racefmt	Race
hbp	byte	%8.0g	yn	High blood pressure

Sorted by:

The dstdize command is designed to work with aggregate data but will work with individual-level data only if we create a variable recording the population represented by each observation. For individual-level data, this is one:

. generate pop = 1

On the next page, we specify print to obtain a listing of the standard population and level(90) to request 90% rather than 95% confidence intervals. Typing if year==1990 | year==1992 restricts the data to the two years for both summary tables and the standard population.

. dstdize hbp pop age race sex if year==1990 | year==1992, by(city year) print

> level(90)

Standard population

	Stratum-		Pop.	Dist.
15-19	Black	Female	35	0.077
15-19	Black	Male	44	0.097
15-19	Hispanic	Female	5	0.011
15-19	Hispanic	Male	10	0.022
15-19	White	Female	7	0.015
15-19	White	Male	5	0.011
20-24	Black	Female	43	0.095
20-24	Black	Male	67	0.147
20-24	Hispanic	Female	14	0.031
20-24	Hispanic	Male	13	0.029
20-24	White	Female	4	0.009
20-24	White	Male	21	0.046
25-29	Black	Female	17	0.037
25-29	Black	Male	44	0.097
25-29	Hispanic	Female	7	0.015
25-29	Hispanic	Male	13	0.029
25-29	White	Female	9	0.020
25-29	White	Male	16	0.035
30-34	Black	Female	16	0.035
30-34	Black	Male	32	0.070
30-34	Hispanic	Female	2	0.004
30-34	Hispanic	Male	3	0.007
30-34	White	Female	5	0.011
30-34	White	Male	23	0.051

Total:

455

(6 observations excluded because of missing values)

Direct standardization

->	city	year	= 1	1990
----	------	------	-----	------

				U	nadjust Pop.	ed Stratum	Std. pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*P
15-19	Black	Female	6	2	0.128	0.3333	0.077	0.0256
15-19	Black	Male	6	0	0.128	0.0000	0.097	0.0000
15-19	Hispanic	Male	1	0	0.021	0.0000	0.022	0.0000
20-24	Black	Female	3	0	0.064	0.0000	0.095	0.0000
20-24	Black	Male	11	0	0.234	0.0000	0.147	0.0000
25-29	Black	Female	4	0	0.085	0.0000	0.037	0.0000
25-29	Black	Male	6	1	0.128	0.1667	0.097	0.0161
25-29	Hispanic	Female	2	0	0.043	0.0000	0.015	0.0000
25-29	White	Female	1	0	0.021	0.0000	0.020	0.0000
30-34	Black	Female	1	0	0.021	0.0000	0.035	0.0000
30-34	Black	Male	6	0	0.128	0.0000	0.070	0.0000

Total:

3

47

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 2.0 Crude rate = 0.0638 Adjusted rate = 0.0418 90% conf. interval: [0.0074, 0.0761]

-> city ye	ear = 1 19	92						
							Std.	
					Pop.	Stratum	pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*P
15-19	Black	Female	3	0	0.054	0.0000	0.077	0.0000
15-19	Black	Male	9	0	0.161	0.0000	0.097	0.0000
15-19	Hispanic	Male	1	0	0.018	0.0000	0.022	0.0000
20-24	Black	Female	7	0	0.125	0.0000	0.095	0.0000
20-24	Black	Male	9	0	0.161	0.0000	0.147	0.0000
20-24	Hispanic	Female	1	0	0.018	0.0000	0.031	0.0000
25-29	Black	Female	2	0	0.036	0.0000	0.037	0.0000
25-29	Black	Male	11	1	0.196	0.0909	0.097	0.0088
25-29	Hispanic	Male	1	0	0.018	0.0000	0.029	0.0000
30-34	Black	Female	7	0	0.125	0.0000	0.035	0.0000
30-34	Black	Male	4	0	0.071	0.0000	0.070	0.0000
30-34	White	Female	1	0	0.018	0.0000	0.011	0.0000
Total:			56	1				

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 0.5 Crude rate = 0.0179Adjusted rate = 0.0088 90% conf. interval: [0.0000, 0.0226]

-> city year = 2 1990

				Unadjusted		ted	Std.	
					Pop.	${\tt Stratum}$	pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*P
15-19	Black	Female	5	0	0.078	0.0000	0.077	0.0000
15-19	Black	Male	7	1	0.109	0.1429	0.097	0.0138
15-19	Hispanic	Male	1	0	0.016	0.0000	0.022	0.0000
20-24	Black	Female	7	1	0.109	0.1429	0.095	0.0135
20-24	Black	Male	8	0	0.125	0.0000	0.147	0.0000
20-24	Hispanic	Female	5	0	0.078	0.0000	0.031	0.0000
20-24	Hispanic	Male	2	0	0.031	0.0000	0.029	0.0000
20-24	White	Male	2	0	0.031	0.0000	0.046	0.0000
25-29	Black	Female	3	0	0.047	0.0000	0.037	0.0000
25-29	Black	Male	9	0	0.141	0.0000	0.097	0.0000
25-29	Hispanic	Female	2	0	0.031	0.0000	0.015	0.0000
25-29	White	Female	1	0	0.016	0.0000	0.020	0.0000
25-29	White	Male	2	1	0.031	0.5000	0.035	0.0176
30-34	Black	Female	1	0	0.016	0.0000	0.035	0.0000
30-34	Black	Male	5	0	0.078	0.0000	0.070	0.0000
30-34	Hispanic	Female	2	0	0.031	0.0000	0.004	0.0000
30-34	White	Female	1	0	0.016	0.0000	0.011	0.0000
30-34	White	Male	1	0	0.016	0.0000	0.051	0.0000

Total:

3

64

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 2.9 Crude rate = 0.0469Adjusted rate = 0.0449 90% conf. interval: [0.0091, 0.0807]

0.147

0.029

0.009

0.037

0.097

0.029

0.020

0.035

0.070

0.051

0.0000

0.0000

0.0000

0.0000

0.0363

0.0000

0.0000

0.0000

0.0234

0.0230

0.046 0.0058

0 0.130 0.0000

0 0.043 0.0000

0 0.029 0.0000

1 0.116 0.1250

0 0.014 0.0000

0.3750

0.0000

0.0000

0.0000

0.3333

0.4545

3 0.116

0 0.058

0 0.014

2 0.087

5 0.159

0 0.087

-> city yea	ar = 2.10	ດາ						
> city ye	ai - 2 13	52		t	Jnadjust	ted	Std.	
					0	Stratum	pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*P
15-10	Plack	Eamolo	1	0	0.015	0.0000	0.077	0 0000
15-19	Black	Female	1	0	0.015	0.0000	0.077	0.0000
15-19	Black	Male Female	5 3	0 0	0.075	0.0000	0.097	0.0000
	Hispanic				0.045	0.0000	0.011	0.0000
	Hispanic	Male	1	0	0.015	0.0000	0.022	0.0000
15-19	White	Male	1	0	0.015	0.0000	0.011	0.0000
20-24	Black	Female	8	0	0.119	0.0000	0.095	0.0000
20-24	Black	Male	11	0	0.164	0.0000	0.147	0.0000
	Hispanic	Female	6	0	0.090	0.0000	0.031	0.0000
	Hispanic	Male	4	2	0.060	0.5000	0.029	0.0143
20-24	White	Female	1	0	0.015	0.0000	0.009	0.0000
20-24	White	Male	2	0	0.030	0.0000	0.046	0.0000
25-29	Black	Female	2	0	0.030	0.0000	0.037	0.0000
25-29	Black	Male	3	0	0.045	0.0000	0.097	0.0000
25-29	Hispanic	Female	2	0	0.030	0.0000	0.015	0.0000
25-29	Hispanic	Male	4	0	0.060	0.0000	0.029	0.0000
25-29	White	Female	4	0	0.060	0.0000	0.020	0.000
25-29	White	Male	2	0	0.030	0.0000	0.035	0.0000
30-34	Black	Female	1	0	0.015	0.0000	0.035	0.0000
30-34	Black	Male	2	0	0.030	0.0000	0.070	0.0000
	Hispanic	Male	1	Ő	0.015	0.0000	0.007	0.0000
30-34	White	Female	2	0	0.030	0.0000	0.007	0.0000
30-34	White	Male	1	0	0.030	0.0000	0.051	0.0000
Total:		_	67	2				
Note: s*P	is Stratu	m rate mult	iplied by St	d. pop.	dist.			
						Adjusted	cases =	1.0
						0	e rate =	
						Adjuste		
				90% cc	onf. in	terval: [(
-> city ye	ar = 3 19	90		-			<i>a</i> . 1	
				[Jnadjus ¹		Std.	
					-	Stratum	pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*F
15-19	Black	Female	3	0	0.043	0.0000	0.077	0.0000
15-19	Black	Male	1	0	0.014	0.0000	0.097	0.0000
	Hispanic	Female	1	0	0.014	0.0000	0.011	0.0000
15-19	White	Female	3	Ő	0.043	0.0000	0.015	0.0000
15-19	White	Male	1	0	0.040	0.0000	0.010	0.0000
20-24	Black	Female	1	0	0.014	0.0000	0.011	0.0000
20 24	DIACK	Temare	1	0	0.014	0.0000	0.035	0.0000

20-24

20-24

20-24

25-29

25-29

25-29

25-29

30-34

30-34

20-24 Hispanic

25-29 Hispanic

Black

White

White

Black

Black

White

White

Black

White

Male

Female

Female

Female

Male

Male

Male

Male

Male

Male

Male

9

3

2

8

1

8

4

1

6

6

11

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 6.1 Crude rate = 0.1594 Adjusted rate = 0.0885 90% conf. interval: [0.0501, 0.1268]

-> city year = 3 1992

	Std. pop.	ed Stratum	nadjust Pop.	U				
S*]	dist.	rate	dist.	Cases	Pop.		Stratum	
0.000	0.077	0.0000	0.054	0	2	Female	Black	15-19
0.000	0.022	0.0000	0.081	0	3	Male	Hispanic	15-19
0.000	0.015	0.0000	0.054	0	2	Female	White	15-19
0.000	0.011	0.0000	0.027	0	1	Male	White	15-19
0.000	0.147	0.0000	0.081	0	3	Male	Black	20-24
0.000	0.031	0.0000	0.027	0	1	Female	Hispanic	20-24
0.000	0.029	0.0000	0.081	0	3	Male	Hispanic	20-24
0.000	0.009	0.0000	0.027	0	1	Female	White	20-24
0.007	0.046	0.1667	0.162	1	6	Male	White	20-24
0.000	0.029	0.0000	0.027	0	1	Male	Hispanic	25-29
0.007	0.035	0.2000	0.135	1	5	Male	White	25-29
0.000	0.070	0.0000	0.027	0	1	Male	Black	30-34
0.031	0.051	0.6250	0.216	5	8	Male	White	30-34

Total:

7

37

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 1.7 Crude rate = 0.1892 Adjusted rate = 0.0463 90% conf. interval: [0.0253, 0.0674]

-> city year = 5 1990

	Std. pop.	ed Stratum	nadjust Pop.	U				
s*	dist.	rate	dist.	Cases	Pop.		Stratum	
0.000	0.077	0.0000	0.196	0	9	Female	Black	15-19
0.000	0.097	0.0000	0.152	0	7	Male	Black	15-19
0.000	0.022	0.0000	0.022	0	1	Male	Hispanic	15-19
0.000	0.011	0.0000	0.022	0	1	Male	White	15-19
0.000	0.095	0.0000	0.087	0	4	Female	Black	20-24
0.000	0.147	0.0000	0.130	0	6	Male	Black	20-24
0.000	0.031	0.0000	0.022	0	1	Female	Hispanic	20-24
0.012	0.037	0.3333	0.065	1	3	Female	Black	25-29
0.000	0.097	0.0000	0.109	0	5	Male	Black	25-29
0.000	0.015	0.0000	0.022	0	1	Female	Hispanic	25-29
0.009	0.020	0.5000	0.043	1	2	Female	White	25-29
0.000	0.035	0.0000	0.043	0	2	Female	Black	30-34
0.000	0.070	0.0000	0.065	0	3	Male	Black	30-34
0.000	0.051	0.0000	0.022	0	1	Male	White	30-34

Total:

2

46

Note: s*P is Stratum rate multiplied by Std. pop. dist.

Adjusted cases = 1.0 Crude rate = 0.0435 Adjusted rate = 0.0223 90% conf. interval: [0.0020, 0.0426]

-> city ye	ear = 5 19	92						
				U	Inadjust	ted	Std.	
					Pop.	Stratum	pop.	
	Stratum		Pop.	Cases	dist.	rate	dist.	s*P
15-19	Black	Female	6	0	0.087	0.0000	0.077	0.0000
15-19	Black	Male	9	0	0.130	0.0000	0.097	0.0000
15-19	Hispanic	Female	1	0	0.014	0.0000	0.011	0.0000
	Hispanic	Male	2	0	0.029	0.0000	0.022	0.0000
15-19	White	Female	2	0	0.029	0.0000	0.015	0.0000
15-19	White	Male	1	0	0.014	0.0000	0.011	0.0000
20-24	Black	Female	13	0	0.188	0.0000	0.095	0.0000
20-24	Black	Male	10	0	0.145	0.0000	0.147	0.0000
20-24	Hispanic	Male	1	0	0.014	0.0000	0.029	0.0000
20-24	White	Male	3	0	0.043	0.0000	0.046	0.0000
25-29	Black	Female	2	0	0.029	0.0000	0.037	0.0000
25-29	Black	Male	2	0	0.029	0.0000	0.097	0.0000
	Hispanic	Male	3	0	0.043	0.0000	0.029	0.0000
25-29	White	Male	1	0	0.014	0.0000	0.035	0.0000
30-34	Black	Female	4	0	0.058	0.0000	0.035	0.0000
30-34	Black	Male	5	0	0.072	0.0000	0.070	0.0000
	Hispanic	Male	2	0	0.029	0.0000	0.007	0.0000
30-34	White	Female	1	0	0.014	0.0000	0.011	0.0000
30-34	White	Male	1	1	0.014	1.0000	0.051	0.0505
				90% co	onf. in		e rate = d rate =	= 0.0145 = 0.0505
Summary of	f study po	pulations	3					
city								
year		N Ci	rude rate	Adjusted	rate	[90%	conf. i	nterval]
1								
1990 1		47	0.063830	0.04	1758	0.00	7427	0.076089
1992 2		56	0.017857	0.00	8791	0.00	0000	0.022579
1990		64	0.046875	0.04	4898	0.00	9072	0.080724
2 1992		67	0.029851	0.01	4286	0.00	2537	0.026035
3 1990		69	0.159420	0.08	8453	0.05	0093	0.126813
3 1992		37	0.189189	0 04	6319	0.02		0.067366
5								
1990 5		46	0.043478	0.02	2344	0.00	2044	0.042644
1992		69	0.014493	0.05	0549	0.05	0549	0.050549

Indirect standardization

Standardization of rates can be performed via the indirect method whenever the stratum-specific rates are either unknown or unreliable. If the stratum-specific rates are known, the direct standardization method is preferred.

To apply the indirect method, you must have the following information:

- The observed number of cases in each population to be standardized, O. For example, if deathrates in two states are being standardized using the US deathrate for the same period, you must know the total number of deaths in each state.
- The distribution across the various strata for the population being studied, n_1, \ldots, n_k . If you are standardizing the deathrate in the two states, adjusting for age, you must know the number of individuals in each of the k age groups.
- The stratum-specific rates for the standard population, p_1, \ldots, p_k . For example, you must have the US deathrate for each stratum (age group).
- The crude rate of the standard population, C. For example, you must have the US mortality rate for the year.

The indirect adjusted rate is then

$$R_{\text{indirect}} = C \frac{O}{E}$$

where E is the expected number of cases (deaths) in each population. See *Methods and formulas* for a more detailed description of calculations.

Example 3

This example is borrowed from Kahn and Sempos (1989, 95–105). We want to compare 1970 mortality rates in California and Maine, adjusting for age. Although we have age-specific population counts for the two states, we lack age-specific deathrates. Direct standardization is not feasible here. We can use the US population census data for the same year to produce indirectly standardized rates for these two states.

From the US census, the standard population for this example was entered into Stata and saved in popkahn.dta.

- . use https://www.stata-press.com/data/r19/popkahn, clear
- . list age pop deaths rate, sep(4)

	age population		deaths	rate
1. 2.	<15 15 - 24	57,900,000 35,441,000	103,062 45,261	.00178 .00128
2. 3. 4.	25-34 35-44	24,907,000 23,088,000	39,193 72,617	.00120
5. 6.	45 - 54 55-64	23,220,000 18,590,000	169,517 308,373	.0073 .01659
7. 8.	65 - 74 75+	12,436,000 7,630,000	445,531 736,758	.03583 .09656

The standard population contains for each age stratum the total number of individuals (pop) and both the age-specific mortality rate (rate) and the number of deaths. The standard population need not contain all three. If we have only the age-specific mortality rate, we can use the rate ($ratevar_p$ crudevar_p) or rate ($ratevar_p$ #) option, where crudevar_p refers to the variable containing the total population's crude deathrate or # is the total population's crude deathrate.

Now, let's look at the states' data (study population):

- . use https://www.stata-press.com/data/r19/kahn
- . list, sep(4)

	state	age	populat~n	death	st	death_~e
1.	California	<15	5,524,000	166,285	1	.0016
2.	California	15-24	3,558,000	166,285	1	.0013
3.	California	25-34	2,677,000	166,285	1	.0015
4.	California	35-44	2,359,000	166,285	1	.0028
5.	California	45-54	2,330,000	166,285	1	.0067
6.	California	55-64	1,704,000	166,285	1	.0154
7.	California	65-74	1,105,000	166,285	1	.0328
8.	California	75+	696,000	166,285	1	.0917
9.	Maine	<15	286,000	11,051	2	.0019
10.	Maine	15-24	168,000		2	.0011
11.	Maine	25-34	110,000		2	.0014
12.	Maine	35-44	109,000		2	.0029
13.	Maine	45-54	110,000	•	2	.0069
14.	Maine	55-64	94,000		2	.0173
15.	Maine	65-74	69,000		2	.039
16.	Maine	75+	46,000		2	.1041

For each state, the number of individuals in each stratum (age group) is contained in the pop variable. The death variable is the total number of deaths observed in the state during the year. It must have the same value for all observations in the group, as for California, or it could be missing in all but one observation per group, as for Maine.

To match these two datasets, the strata variables must have the same name in both datasets and ideally the same levels. If a level is missing from either dataset, that level will not be included in the standardization.

With kahn.dta in memory, we now execute the command. We will use the print option to obtain the standard population's summary table, and because we have both the standard population's age-specific count and deaths, we will specify the popvars($casevar_p \ popvar_p$) option. Or, we could specify the rate(rate 0.00945) option because we know that 0.00945 is the US crude deathrate for 1970.

. is tdize death pop age using <code>https://www.stata-press.com/data/r19/popkahn</code> ,

> by(state) pop(deaths pop) print

Standard population

Stratum	Rate
<15	0.00178
15-24	0.00128
25-34	0.00157
35-44	0.00315
45-54	0.00730
55-64	0.01659
65-74	0.03583
75+	0.09656

Crude rate = 0.00945

Indirect standardization

-> state = California

Stratum	Standard population rate	Observed population	Expected cases
<15 15-24 25-34 35-44 45-54 55-64 65-74 75+	$\begin{array}{c} 0.0018\\ 0.0013\\ 0.0016\\ 0.0031\\ 0.0073\\ 0.0166\\ 0.0358\\ 0.0966\\ \end{array}$	5,524,000 3,558,000 2,677,000 2,359,000 2,330,000 1,704,000 1,105,000 696,000	9,832.72 4,543.85 4,212.46 7,419.59 17,010.10 28,266.14 39,587.63 67,206.23
Total:	SMR exact 95% conf. 95% conf.	SMR (Obs/ interval: [O Crude : Adjusted :	•

-> state = Maine

Stratum	Standard population rate	Observed population	Expected cases
<15	0.0018	286,000	509.08
15-24	0.0013	168,000	214.55
25-34	0.0016	110,000	173.09
35-44	0.0031	109,000	342.83
45-54	0.0073	110,000	803.05
55-64	0.0166	94,000	1,559.28
65-74	0.0358	69,000	2,471.99
75+	0.0966	46,000	4,441.79
Total:		992,000	10,515.67

Observed cases = 11,051 SMR (Obs/Exp) = 1.05 SMR exact 95% conf. interval: [1.0314, 1.0707] Crude rate = 0.0111 Adjusted rate = 0.0099 95% conf. interval: [0.0097, 0.0101]

Summary of study populations, reporting rates

state	Observed cases	Crude rate	Adjusted rate	[95% conf.	interval]
California	166,285	0.008334	0.008824	0.008782	0.008866
Maine	11,051	0.011140	0.009931	0.009747	0.010118

Summary of study populations, reporting SMRs

state	Observed cases	Expected cases	SMR	Exa [95% conf.	
California	166,285	178,078.73	0.934	0.929290	0.938271
Maine	11,051	10,515.67	1.051	1.031405	1.070688

Stored results

dstdize stores the following in r():

Scalars

Sealars	
r(k)	number of populations
Macros	
r(by)	variable names specified in by()
r(c#)	values of r (by) for #th group
Matrices	
r(se)	$1 \times k$ vector of standard errors of adjusted rates
r(ub_adj)	$1 \times k$ vector of upper bounds of confidence intervals for adjusted rates
r(lb_adj)	$1 \times k$ vector of lower bounds of confidence intervals for adjusted rates
r(Nobs)	$1 \times k$ vector of number of observations
r(crude)	$1 \times k$ vector of crude rates (*)
r(adj)	$1 \times k$ vector of adjusted rates (*)

(*) If, in a group, the number of observations is 0, then 9 is stored for the corresponding crude and adjusted rates.

istdize stores the following in r():

Scalars	
r(k)	number of populations
Macros	
r(by)	variable names specified in by()
r(c#)	values of r (by) for #th group
Matrices	
r(cases_obs)	$1 \times k$ vector of number of observed cases
r(cases_exp)	$1 \times k$ vector of number of expected cases
r(ub_adj)	$1 \times k$ vector of upper bounds of confidence intervals for adjusted rates
r(lb_adj)	$1 \times k$ vector of lower bounds of confidence intervals for adjusted rates
r(crude)	$1 \times k$ vector of crude rates

r(adj)	$1 \times k$ vector of adjusted rates
r(smr)	$1 \times k$ vector of SMRs
r(ub_smr)	$1 \times k$ vector of upper bounds of confidence intervals for SMRs
r(lb_smr)	$1 \times k$ vector of lower bounds of confidence intervals for SMRs

Methods and formulas

The directly standardized rate, $S_{\rm R}$, is defined by

$$S_{\rm R} = \frac{\sum_{i=1}^{k} w_i R_i}{\sum_{i=1}^{k} w_i}$$

(Rothman 1986, 44), where R_i is the stratum-specific rate in stratum *i* and w_i is the weight for stratum *i* derived from the standard population.

If n_i is the population of stratum *i*, the standard error, se(S_R), in stratified sampling for proportions (ignoring the finite population correction) is

$$\mathrm{se}(S_{\mathrm{R}}) = \frac{1}{\sum w_i} \sqrt{\sum_{i=1}^k \frac{w_i^2 R_i (1-R_i)}{n_i}}$$

(Cochran 1977, 108), from which the confidence intervals are calculated.

For indirect standardization, define O as the observed number of cases in each population to be standardized; n_1, \ldots, n_k as the distribution across the various strata for the population being studied; R_1, \ldots, R_k as the stratum-specific rates for the standard population; and C as the crude rate of the standard population. The expected number of cases (deaths), E, in each population is obtained by applying the standard population stratum-specific rates, R_1, \ldots, R_k , to the study populations:

$$E = \sum_{i=1}^{k} n_i R_i$$

The indirectly adjusted rate is then

$$R_{\text{indirect}} = C \frac{O}{E}$$

and O/E is the study population's SMR if death is the event of interest or the SIR for studies of disease (or other) incidence.

The exact confidence interval is calculated for each estimated SMR by assuming a Poisson process as described in Breslow and Day (1987, 69–71). These intervals are obtained by first calculating the upper and lower bounds for the confidence interval of the Poisson-distributed observed events, O—say, L and U, respectively—and then computing SMR_L = L/E and SMR_U = U/E.

Acknowledgments

We gratefully acknowledge the collaboration of Dr. Joel A. Harrison, consultant; Dr. José Maria Pacheco de Souza (1936–2023) of the Departamento de Epidemiologia, Faculdade de Saúde Pública/USP, Sao Paulo, Brazil; and Dr. John L. Moran of the Queen Elizabeth Hospital, Woodville, Australia.

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Also see

- [R] Epitab Tables for epidemiologists
- [SVY] Direct standardization Direct standardization of means, proportions, and ratios

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