

**bootstrap** — Bootstrap sampling and estimation

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## Description

`bootstrap` performs nonparametric bootstrap estimation of specified statistics (or expressions) for a Stata command or a user-written program. Statistics are bootstrapped by resampling the data in memory with replacement. `bootstrap` is designed for use with nonestimation commands, functions of coefficients, or user-written programs. To bootstrap coefficients, we recommend using the `vce(bootstrap)` option when allowed by the estimation command.

## Quick start

Bootstrap the mean of `v1` returned by `summarize` in `r(mean)`

```
bootstrap mean=r(mean): summarize v1
```

Bootstrap the statistic `r(mystat)` returned by program `myprog1`

```
bootstrap stat=r(mystat): myprog1 v1
```

As above, but use 100 replications

```
bootstrap stat=r(mystat), reps(100): myprog1 v1
```

As above, and save the results from each replication in `mydata.dta`

```
bootstrap stat=r(mystat), reps(100) saving(mydata): myprog1 v1
```

Bootstrap a difference in coefficients estimated by `regress`

```
bootstrap diff=(_b[x2]-_b[x1]): regress y x1 x2 x3
```

Bootstrap the coefficients stored in `e(b)` by `myprog2`

```
bootstrap _b: myprog2 y x1 x2 x3
```

As above, but with bootstrap samples taken independently within strata identified by `svar`

```
bootstrap _b, strata(svar): myprog2 y x1 x2 x3
```

Resample clusters defined by `cvar` and create `newcvar` identifying resampled clusters

```
bootstrap _b, cluster(cvar) idcluster(newcvar): myprog2 y x1 x2 x3
```

## Menu

Statistics > Resampling > Bootstrap estimation

## Syntax

```
bootstrap exp_list [ , options eform_option ] : command
```

<i>options</i>	Description
Main	
<code>reps(#)</code>	perform # bootstrap replications; default is <code>reps(50)</code>
Options	
<code>strata(varlist)</code>	variables identifying strata
<code>size(#)</code>	draw samples of size #; default is <code>_N</code>
<code>cluster(varlist)</code>	variables identifying resampling clusters
<code>idcluster(newvar)</code>	create new cluster ID variable
<code>saving(filename, ...)</code>	save results to <i>filename</i> ; save statistics in double precision; save results to <i>filename</i> every # replications
<code>bca</code>	compute acceleration for $BC_a$ confidence intervals
<code>ties</code>	adjust BC/BCa confidence intervals for ties
<code>mse</code>	use MSE formula for variance estimation
Reporting	
<code>level(#)</code>	set confidence level; default is <code>level(95)</code>
<code>notable</code>	suppress table of results
<code>noheader</code>	suppress table header
<code>nolegend</code>	suppress table legend
<code>verbose</code>	display the full table legend
<code>nodots</code>	suppress replication dots
<code>dots(#)</code>	display dots every # replications
<code>noisily</code>	display any output from <i>command</i>
<code>trace</code>	trace <i>command</i>
<code>title(text)</code>	use <i>text</i> as title for bootstrap results
<code>display_options</code>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
<code>eform_option</code>	display coefficient table in exponentiated form
Advanced	
<code>nodrop</code>	do not drop observations
<code>nowarn</code>	do not warn when <code>e(sample)</code> is not set
<code>force</code>	do not check for <i>weights</i> or <i>svy</i> commands; seldom used
<code>reject(exp)</code>	identify invalid results
<code>seed(#)</code>	set random-number seed to #
<code>group(varname)</code>	ID variable for groups within <code>cluster()</code>
<code>jackknifeopts(jkopts)</code>	options for <code>jackknife</code> ; see [R] <code>jackknife</code>
<code>coeflegend</code>	display legend instead of statistics

*command* is any command that follows standard Stata syntax. *weights* are not allowed in *command*. *collect* and *svy* are allowed; see [U] 11.1.10 Prefix commands. *group()*, *jackknifeopts()*, and *coeflegend* do not appear in the dialog box. See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

```
exp_list contains      (name: elist)
                       elist
                       eexp
elist contains        newvar = (exp)
                       (exp)
eexp is               specname
                       [eqno]specname
specname is          _b
                       _b []
                       _se
                       _se []
eqno is              ##
                       name
```

*exp* is a standard Stata expression; see [U] 13 Functions and expressions.

Distinguish between [], which are to be typed, and [], which indicate optional arguments.

## Options

### Main

**reps**(#) specifies the number of bootstrap replications to be performed. The default is 50. A total of 50–200 replications are generally adequate for estimates of standard error and thus are adequate for normal-approximation confidence intervals; see [Mooney and Duval \(1993, 11\)](#). Estimates of confidence intervals using the percentile or bias-corrected methods typically require 1,000 or more replications.

### Options

**strata**(*varlist*) specifies the variables that identify strata. If this option is specified, bootstrap samples are taken independently within each stratum.

**size**(#) specifies the size of the samples to be drawn. The default is `_N`, meaning to draw samples of the same size as the data. If specified, # must be less than or equal to the number of observations within `strata()`.

If `cluster()` is specified, the default size is the number of clusters in the original dataset. For unbalanced clusters, resulting sample sizes will differ from replication to replication. For cluster sampling, # must be less than or equal to the number of clusters within `strata()`.

**cluster**(*varlist*) specifies the variables that identify resampling clusters. If this option is specified, the sample drawn during each replication is a bootstrap sample of clusters.

**idcluster**(*newvar*) creates a new variable containing a unique identifier for each resampled cluster. This option requires that `cluster()` also be specified.

`saving(filename [ , suboptions ])` creates a Stata data file (.dta file) consisting of (for each statistic in *exp\_list*) a variable containing the replicates.

`double` specifies that the results for each replication be saved as `doubles`, meaning 8-byte reals.

By default, they are saved as `floats`, meaning 4-byte reals. This option may be used without the `saving()` option to compute the variance estimates by using double precision.

`every(#)` specifies that results be written to disk every *#*th replication. `every()` should be specified only in conjunction with `saving()` when *command* takes a long time for each replication. This option will allow recovery of partial results should some other software crash your computer.

See [P] [postfile](#).

`replace` specifies that *filename* be overwritten if it exists. This option does not appear in the dialog box.

`bca` specifies that `bootstrap` estimate the acceleration of each statistic in *exp\_list*. This estimate is used to construct  $BC_a$  confidence intervals. Type `estat bootstrap, bca` to display the  $BC_a$  confidence interval generated by the `bootstrap` command.

`ties` specifies that `bootstrap` adjust for ties in the replicate values when computing the median bias used to construct BC and  $BC_a$  confidence intervals.

`mse` specifies that `bootstrap` compute the variance by using deviations of the replicates from the observed value of the statistics based on the entire dataset. By default, `bootstrap` computes the variance by using deviations from the average of the replicates.

---

Reporting

`level(#)`; see [R] [Estimation options](#).

`notable` suppresses the display of the table of results.

`noheader` suppresses the display of the table header. This option implies `nolegend`. This option may also be specified when replaying estimation results.

`nolegend` suppresses the display of the table legend. This option may also be specified when replaying estimation results.

`verbose` specifies that the full table legend be displayed. By default, coefficients and standard errors are not displayed. This option may also be specified when replaying estimation results.

`nodots` and `dots(#)` specify whether to display replication dots. By default, one dot character is displayed for each successful replication. A red 'x' is displayed if *command* returns an error or if any value in *exp\_list* is missing. You can also control whether dots are displayed using `set dots`; see [R] [set](#).

`nodots` suppresses display of the replication dots.

`dots(#)` displays dots every *#* replications. `dots(0)` is a synonym for `nodots`.

`noisily` specifies that any output from *command* be displayed. This option implies the `nodots` option.

`trace` causes a trace of the execution of *command* to be displayed. This option implies the `noisily` option.

`title(text)` specifies a title to be displayed above the table of bootstrap results. The default title is the title stored in `e(title)` by an estimation command, or if `e(title)` is not filled in, `Bootstrap results` is used. `title()` may also be specified when replaying estimation results.

*display\_options*: `nocl`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [Estimation options](#).

*eform\_option* causes the coefficient table to be displayed in exponentiated form; see [R] [eform\\_option](#).

*command* determines which of the following are allowed (`eform(string)` and `eform` are always allowed):

<i>eform_option</i>	Description
<code>eform(string)</code>	use <i>string</i> for the column title
<code>eform</code>	exponentiated coefficient, <i>string</i> is <code>exp(b)</code>
<code>hr</code>	hazard ratio, <i>string</i> is <code>Haz. ratio</code>
<code>shr</code>	subhazard ratio, <i>string</i> is <code>SHR</code>
<code>irr</code>	incidence-rate ratio, <i>string</i> is <code>IRR</code>
<code>or</code>	odds ratio, <i>string</i> is <code>Odds ratio</code>
<code>rrr</code>	relative-risk ratio, <i>string</i> is <code>RRR</code>

#### Advanced

`nodrop` prevents observations outside `e(sample)` and the `if` and `in` qualifiers from being dropped before the data are resampled.

`nowarn` suppresses the display of a warning message when *command* does not set `e(sample)`.

`force` suppresses the restriction that *command* not specify weights or be a `svy` command. This is a rarely used option. Use it only if you know what you are doing.

`reject(exp)` identifies an expression that indicates when results should be rejected. When *exp* is true, the resulting values are reset to missing values.

`seed(#)` sets the random-number seed. Specifying this option is equivalent to typing the following command prior to calling `bootstrap`:

```
. set seed #
```

The following options are available with `bootstrap` but are not shown in the dialog box:

`group(varname)` re-creates *varname* containing a unique identifier for each group across the resampled clusters. This option requires that `idcluster()` also be specified.

This option is useful for maintaining unique group identifiers when sampling clusters with replacement. Suppose that cluster 1 contains 3 groups. If the `idcluster(newclid)` option is specified and cluster 1 is sampled multiple times, `newclid` uniquely identifies each copy of cluster 1. If `group(newgroupid)` is also specified, `newgroupid` uniquely identifies each copy of each group.

`jackknifeopts(jkopts)` identifies options that are to be passed to `jackknife` when it computes the acceleration values for the  $BC_a$  confidence intervals; see [R] [jackknife](#). This option requires the `bca` option and is mostly used for passing the `eclass`, `rclass`, or `n(#)` option to `jackknife`.

`coeflegend`; see [R] [Estimation options](#).

## Remarks and examples

Remarks are presented under the following headings:

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[Using bootstrap](#)  
[Regression coefficients](#)  
[Expressions](#)  
[Combining bootstrap datasets](#)  
[A note about macros](#)  
[Achieved significance level](#)  
[Bootstrapping a ratio](#)  
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[Bootstrapping statistics from data with a complex structure](#)

## Introduction

With few assumptions, bootstrapping provides a way of estimating standard errors and other measures of statistical precision (Efron 1979; Efron and Stein 1981; Efron 1982; Efron and Tibshirani 1986; Efron and Tibshirani 1993; also see Davison and Hinkley [1997]; Guan [2003]; Mooney and Duval [1993]; Poi [2004]; and Stine [1990]). It provides a way to obtain such measures when no formula is otherwise available or when available formulas make inappropriate assumptions. Cameron and Trivedi (2010, chap. 13) discuss many bootstrapping topics and demonstrate how to do them in Stata.

To illustrate bootstrapping, suppose that you have a dataset containing  $N$  observations and an estimator that, when applied to the data, produces certain statistics. You draw, with replacement,  $N$  observations from the  $N$ -observation dataset. In this random drawing, some of the original observations will appear once, some more than once, and some not at all. Using the resampled dataset, you apply the estimator and collect the statistics. This process is repeated many times; each time, a new random sample is drawn and the statistics are recalculated.

This process builds a dataset of replicated statistics. From these data, you can calculate the standard error by using the standard formula for the sample standard deviation

$$\widehat{\text{se}} = \left\{ \frac{1}{k-1} \sum (\hat{\theta}_i - \bar{\hat{\theta}})^2 \right\}^{1/2}$$

where  $\hat{\theta}_i$  is the statistic calculated using the  $i$ th bootstrap sample and  $k$  is the number of replications. This formula gives an estimate of the standard error of the statistic, according to Hall and Wilson (1991). Although the average,  $\bar{\hat{\theta}}$ , of the bootstrapped estimates is used in calculating the standard deviation, it is not used as the estimated value of the statistic itself. Instead, the original observed value of the statistic,  $\hat{\theta}$ , is used, meaning the value of the statistic computed using the original  $N$  observations.

You might think that  $\bar{\hat{\theta}}$  is a better estimate of the parameter than  $\hat{\theta}$ , but it is not. If the statistic is biased, bootstrapping exaggerates the bias. In fact, the bias can be estimated as  $\bar{\hat{\theta}} - \hat{\theta}$  (Efron 1982, 33). Knowing this, you might be tempted to subtract this estimate of bias from  $\hat{\theta}$  to produce an unbiased statistic. The bootstrap bias estimate has an indeterminate amount of random error, so this unbiased estimator may have greater mean squared error than the biased estimator (Mooney and Duval 1993; Hinkley 1978). Thus,  $\hat{\theta}$  is the best point estimate of the statistic.

The logic behind the bootstrap is that all measures of precision come from a statistic's sampling distribution. When the statistic is estimated on a sample of size  $N$  from some population, the sampling distribution tells you the relative frequencies of the values of the statistic. The sampling distribution, in turn, is determined by the distribution of the population and the formula used to estimate the statistic.

Sometimes the sampling distribution can be derived analytically. For instance, if the underlying population is distributed normally and you calculate means, the sampling distribution for the mean is also normal but has a smaller variance than that of the population. In other cases, deriving the sampling distribution is difficult, such as when means are calculated from nonnormal populations. Sometimes, as in the case of means, it is not too difficult to derive the sampling distribution as the sample size goes to infinity ( $N \rightarrow \infty$ ). However, such asymptotic distributions may not perform well when applied to finite samples.

If you knew the population distribution, you could obtain the sampling distribution by simulation: you could draw random samples of size  $N$ , calculate the statistic, and make a tally. Bootstrapping does precisely this, but it uses the observed distribution of the sample in place of the true population distribution. Thus, the bootstrap procedure hinges on the assumption that the observed distribution is a good estimate of the underlying population distribution. In return, the bootstrap produces an estimate, called the bootstrap distribution, of the sampling distribution. From this, you can estimate the standard error of the statistic, produce confidence intervals, etc.

The accuracy with which the bootstrap distribution estimates the sampling distribution depends on the number of observations in the original sample and the number of replications in the bootstrap. A crudely estimated sampling distribution is adequate if you are going to extract, say, only a standard error. A better estimate is needed if you want to use the 2.5th and 97.5th percentiles of the distribution to produce a 95% confidence interval. To extract many features simultaneously about the distribution, an even better estimate is needed. Generally, replications on the order of 1,000 produce very good estimates, but only 50–200 replications are needed for estimates of standard errors. See [Poi \(2004\)](#) for a method to choose the number of bootstrap replications.

## Using bootstrap

### Typing

```
. bootstrap exp_list, reps(#): command
```

executes *command* multiple times, bootstrapping the statistics in *exp\_list* by resampling observations (with replacement) from the data in memory *#* times. This method is commonly referred to as the nonparametric bootstrap.

*command* defines the statistical command to be executed. Most Stata commands and user-written programs can be used with `bootstrap`, as long as they follow standard Stata syntax; see [\[U\] 11 Language syntax](#). If the `bca` option is supplied, *command* must also work with `jackknife`; see [\[R\] jackknife](#). The `by` prefix may not be part of *command*.

*exp\_list* specifies the statistics to be collected from the execution of *command*. If *command* changes the contents in `e(b)`, *exp\_list* is optional and defaults to `_b`.

Because bootstrapping is a random process, if you want to be able to reproduce results, set the random-number seed by specifying the `seed(#)` option or by typing

```
. set seed #
```

where *#* is a seed of your choosing, before running `bootstrap`; see [\[R\] set seed](#).

## Regression coefficients

### ► Example 1

Let's say that we wish to compute bootstrap estimates for the standard errors of the coefficients from the following regression:

```
. use https://www.stata-press.com/data/r17/auto
(1978 automobile data)
```

```
. regress mpg weight gear foreign
```

Source	SS	df	MS	Number of obs	=	74
Model	1629.67805	3	543.226016	F(3, 70)	=	46.73
Residual	813.781411	70	11.6254487	Prob > F	=	0.0000
				R-squared	=	0.6670
				Adj R-squared	=	0.6527
Total	2443.45946	73	33.4720474	Root MSE	=	3.4096

  

mpg	Coefficient	Std. err.	t	P> t	[95% conf. interval]
weight	-.006139	.0007949	-7.72	0.000	-.0077245 - .0045536
gear_ratio	1.457113	1.541286	0.95	0.348	-1.616884 4.53111
foreign	-2.221682	1.234961	-1.80	0.076	-4.684735 .2413715
_cons	36.10135	6.285984	5.74	0.000	23.56435 48.63835

To run the bootstrap, we simply prefix the above regression command with the `bootstrap` command (specifying its options before the colon separator). We must set the random-number seed before calling `bootstrap`.

```
. bootstrap, reps(100) seed(1): regress mpg weight gear foreign
(running regress on estimation sample)
```

```
Bootstrap replications (100)
```

```
-----| 1 -----| 2 -----| 3 -----| 4 -----| 5
..... 50
..... 100
```

```
Linear regression
```

```
Number of obs = 74
Replications = 100
Wald chi2(3) = 167.13
Prob > chi2 = 0.0000
R-squared = 0.6670
Adj R-squared = 0.6527
Root MSE = 3.4096
```

mpg	Observed coefficient	Bootstrap std. err.	z	P> z	Normal-based [95% conf. interval]
weight	-.006139	.0006063	-10.13	0.000	-.0073273 - .0049507
gear_ratio	1.457113	1.367917	1.07	0.287	-1.223954 4.138181
foreign	-2.221682	1.169727	-1.90	0.058	-4.514305 .070942
_cons	36.10135	5.20581	6.93	0.000	25.89815 46.30455

The displayed confidence interval is based on the assumption that the sampling (and hence bootstrap) distribution is approximately normal (see [Methods and formulas](#) below). Because this confidence interval is based on the standard error, it is a reasonable estimate if normality is approximately true, even for a few replications. Other types of confidence intervals are available after `bootstrap`; see [\[R\] bootstrap postestimation](#).



We could instead supply names to our expressions when we run `bootstrap`. For example,

```
. bootstrap diff=(_b[weight]-_b[gear]): regress mpg weight gear foreign
```

would bootstrap a statistic, named `diff`, equal to the difference between the coefficients on `weight` and `gear_ratio`.

◀

## □ Technical note

`regress`, like many estimation commands, allows the `vce(bootstrap)` option. For any estimation command that allows this option, we recommend using `vce(bootstrap)` over `bootstrap` because the estimation command automatically handles clustering and other model-specific details for you.

□

## Expressions

### ▷ Example 2

When we use `bootstrap`, the list of statistics can contain complex expressions, as long as each expression is enclosed in parentheses. For example, to bootstrap the range of a variable `x`, we could type

```
. bootstrap range=(r(max)-r(min)), reps(1000): summarize x
```

Of course, we could also bootstrap the minimum and maximum and later compute the range.

```
. bootstrap max=r(max) min=r(min), reps(1000) saving(mybs): summarize x
. use mybs, clear
. (bootstrap: summarize)
. generate range = max - min
. bstat range, stat(19.5637501)
```

The difference between the maximum and minimum of `x` in the sample is 19.5637501.

The `stat()` option to `bstat` specifies the observed value of the statistic (`range`) to be summarized. This option is useful when, as shown above, the statistic of ultimate interest is not specified directly to `bootstrap` but instead is calculated by other means.

Here the observed values of `r(max)` and `r(min)` are stored as characteristics of the dataset created by `bootstrap` and are thus available for retrieval by `bstat`; see [R] [bstat](#). The observed range, however, is unknown to `bstat`, so it must be specified.

◀

## Combining bootstrap datasets

You can combine two datasets from separate runs of `bootstrap` by using `append` (see [D] [append](#)) and then get the bootstrap statistics for the combined datasets by running `bstat`. The runs must have been performed independently (having different starting random-number seeds), and the original dataset, command, and bootstrap statistics must have been all the same.

## A note about macros

In [example 2](#), we executed the command

```
. bootstrap max=r(max) min=r(min), reps(1000) saving(mybs): summarize x
```

We did not enclose `r(max)` and `r(min)` in single quotes, as we would in most other contexts, because it would not produce what was intended:

```
. bootstrap 'r(max)' 'r(min)', reps(1000) saving(mybs): summarize x
```

To understand why, note that `'r(max)'`, like any reference to a local macro, will evaluate to a literal string containing the contents of `r(max)` *before* `bootstrap` is even executed. Typing the command above would appear to Stata as if we had typed

```
. bootstrap 14.5441234 33.4393293, reps(1000) saving(mybs): summarize x
```

Even worse, the current contents of `r(min)` and `r(max)` could be empty, producing an even more confusing result. To avoid this outcome, refer to statistics by name (for example, `r(max)`) and by value (for example, `'r(max)'`).

## Achieved significance level

### ► Example 3

Suppose that we wish to estimate the *achieved significance level* (ASL) of a test statistic by using the bootstrap. ASL is another name for  $p$ -value. An example is

$$\text{ASL} = \Pr(\hat{\theta}^* \geq \hat{\theta} | H_0)$$

for an upper-tailed, alternative hypothesis, where  $H_0$  denotes the null hypothesis,  $\hat{\theta}$  is the observed value of the test statistic, and  $\hat{\theta}^*$  is the random variable corresponding to the test statistic, assuming that  $H_0$  is true.

Here we will compare the mean miles per gallon (mpg) between foreign and domestic cars by using the two-sample  $t$  test with unequal variances. The following results indicate the  $p$ -value to be 0.0034 for the two-sided test using Satterthwaite's approximation. Thus, assuming that mean mpg is the same for foreign and domestic cars, we would expect to observe a  $t$  statistic more extreme (in absolute value) than 3.1797 in about 0.3% of all possible samples of the type that we observed. Thus, we have evidence to reject the null hypothesis that the means are equal.

```
. use https://www.stata-press.com/data/r17/auto
(1978 automobile data)
. ttest mpg, by(foreign) unequal
Two-sample t test with unequal variances
```

Group	Obs	Mean	Std. err.	Std. dev.	[95% conf. interval]	
Domestic	52	19.82692	.657777	4.743297	18.50638	21.14747
Foreign	22	24.77273	1.40951	6.611187	21.84149	27.70396
Combined	74	21.2973	.6725511	5.785503	19.9569	22.63769
diff		-4.945804	1.555438		-8.120053	-1.771556

```
diff = mean(Domestic) - mean(Foreign)          t = -3.1797
H0: diff = 0          Satterthwaite's degrees of freedom = 30.5463
Ha: diff < 0          Ha: diff != 0          Ha: diff > 0
Pr(T < t) = 0.0017    Pr(|T| > |t|) = 0.0034    Pr(T > t) = 0.9983
```

We also place the value of the test statistic in a scalar for later use.

```
. scalar tobs = r(t)
```

Efron and Tibshirani (1993, 224) describe an alternative to Satterthwaite's approximation that estimates the ASL by bootstrapping the statistic from the test of equal means. Their idea is to recenter the two samples to the combined sample mean so that the data now conform to the null hypothesis but that the variances within the samples remain unchanged.

```
. summarize mpg, meanonly
. scalar omean = r(mean)
. summarize mpg if foreign==0, meanonly
. replace mpg = mpg - r(mean) + scalar(omean) if foreign==0
variable mpg was int now float
(52 real changes made)
. summarize mpg if foreign==1, meanonly
. replace mpg = mpg - r(mean) + scalar(omean) if foreign==1
(22 real changes made)
. sort foreign
. by foreign: summarize mpg
```

```
-> foreign = Domestic
```

Variable	Obs	Mean	Std. dev.	Min	Max
mpg	52	21.2973	4.743297	13.47037	35.47038

```
-> foreign = Foreign
```

Variable	Obs	Mean	Std. dev.	Min	Max
mpg	22	21.2973	6.611187	10.52457	37.52457

Each sample (foreign and domestic) is a stratum, so the bootstrapped samples must have the same number of foreign and domestic cars as the original dataset. This requirement is facilitated by the `strata()` option to `bootstrap`. By typing the following, we bootstrap the test statistic using the modified dataset and save the values in `bsauto2.dta`:

```

. keep mpg foreign
. set seed 1
. bootstrap t=r(t), rep(1000) strata(foreign) saving(bsauto2) nodots: ttest mpg,
> by(foreign) unequal
warning: ttest does not set e(sample), so no observations will be excluded
        from the resampling because of missing values or other reasons. To
        exclude observations, press Break, save the data, drop any
        observations that are to be excluded, and rerun bootstrap.

Bootstrap results
Number of strata = 2                                Number of obs = 74
                                                    Replications = 1,000

Command: ttest mpg, by(foreign) unequal
t: r(t)

```

	Observed coefficient	Bootstrap std. err.	z	P> z	Normal-based [95% conf. interval]	
t	1.75e-07	1.051867	0.00	1.000	-2.061622	2.061622

We can use the data in `bsauto2.dta` to estimate ASL via the fraction of bootstrap test statistics that are more extreme than 3.1797.

```

. use bsauto2, clear
(bootstrap: ttest)
. generate indicator = abs(t)>=abs(scalar(tobs))
. summarize indicator, meanonly
. display "ASLboot = " r(mean)
ASLboot = .004

```

The result is  $ASL_{boot} = 0.004$ . Assuming that the mean mpg is the same between foreign and domestic cars, we would expect to observe a  $t$  statistic more extreme (in absolute value) than 3.1797 in about 0.4% of all possible samples of the type we observed. This finding is still strong evidence to reject the hypothesis that the means are equal.

◀

## Bootstrapping a ratio

### ▶ Example 4

Suppose that we wish to produce a bootstrap estimate of the ratio of two means. Because `summarize` stores results for only one variable, we must call `summarize` twice to compute the means. Actually, we could use `collapse` to compute the means in one call, but calling `summarize` twice is much faster. Thus, we will have to write a small program that will return the results we want.

We write the program below and save it to a file called `ratio.ado` (see [U] 17 Ado-files). Our program takes two variable names as input and saves them in the local macros `y` (first variable) and `x` (second variable). It then computes one statistic: the mean of 'y' divided by the mean of 'x'. This value is returned as a scalar in `r(ratio)`. `ratio` also returns the ratio of the number of observations used to the mean for each variable.

```

program myratio, rclass
    version 17.0
    args y x
    confirm var `y'
    confirm var `x'
    tempname ymean yn
    summarize `y', meanonly
    scalar `ymean' = r(mean)
    return scalar n_`y' = r(N)
    summarize `x', meanonly
    return scalar n_`x' = r(N)
    return scalar ratio = `ymean'/r(mean)
end

```

Remember to test any newly written commands before using them with `bootstrap`.

```

. use https://www.stata-press.com/data/r17/auto, clear
(1978 automobile data)
. summarize price

```

Variable	Obs	Mean	Std. dev.	Min	Max
price	74	6165.257	2949.496	3291	15906

```

. scalar mean1=r(mean)
. summarize weight

```

Variable	Obs	Mean	Std. dev.	Min	Max
weight	74	3019.459	777.1936	1760	4840

```

. scalar mean2=r(mean)
. di scalar(mean1)/scalar(mean2)
2.0418412
. myratio price weight
. return list
scalars:
    r(ratio) = 2.041841210168278
    r(n_weight) = 74
    r(n_price) = 74

```

The results of running `bootstrap` on our program are

```
. use https://www.stata-press.com/data/r17/auto
(1978 automobile data)
. set seed 1
. bootstrap ratio=r(ratio), reps(1000) nowarn nodots: myratio price weight
Bootstrap results                                     Number of obs =    74
                                                    Replications = 1,000

Command: myratio price weight
ratio: r(ratio)
```

	Observed coefficient	Bootstrap std. err.	z	P> z	Normal-based [95% conf. interval]	
ratio	2.041841	.0953559	21.41	0.000	1.854947	2.228735

As mentioned previously, we should specify the `saving()` option if we wish to save the bootstrap dataset. ◀

## Warning messages and `e(sample)`

`bootstrap` is not meant to be used with weighted calculations. `bootstrap` determines the presence of weights by parsing the prefixed command with standard syntax. However, commands like `stcox` and `streg` require that weights be specified in `stset`, and some user commands may allow weights to be specified by using an option instead of the standard syntax. Both cases pose a problem for `bootstrap` because it cannot determine the presence of weights under these circumstances. In these cases, we can only assume that you know what you are doing.

`bootstrap` does not know which variables of the dataset in memory matter to the calculation at hand. You can speed their execution by dropping unnecessary variables because, otherwise, they are included in each bootstrap sample.

You should thus drop observations with missing values. Leaving in missing values causes no problem in one sense because all Stata commands deal with missing values gracefully. It does, however, cause a statistical problem. Bootstrap sampling is defined as drawing, with replacement, samples of size  $N$  from a set of  $N$  observations. `bootstrap` determines  $N$  by counting the number of observations in memory, not counting the number of nonmissing values on the relevant variables. The result is that too many observations are resampled; the resulting bootstrap samples, because they are drawn from a population with missing values, are of unequal sizes.

If the number of missing values relative to the sample size is small, this will make little difference. If you have many missing values, however, you should first drop the observations that contain them.

### ▷ Example 5

To illustrate, we use the previous example but replace some of the values of `price` with missing values. The number of values of `price` used to compute the mean for each bootstrap is not constant. This is the purpose of the Warning message.

```

. use https://www.stata-press.com/data/r17/auto
(1978 automobile data)
. replace price = . if inlist(_n,1,3,5,7)
(4 real changes made, 4 to missing)
. set seed 1
. bootstrap ratio=r(ratio) np=r(n_price) nw=r(n_weight), reps(100) nodots:
> myratio price weight
warning: myratio does not set e(sample), so no observations will be excluded
from the resampling because of missing values or other reasons. To
exclude observations, press Break, save the data, drop any
observations that are to be excluded, and rerun bootstrap.
Bootstrap results                                     Number of obs = 74
                                                    Replications = 100

```

```

Command: myratio price weight
ratio: r(ratio)
np: r(n_price)
nw: r(n_weight)

```

	Observed coefficient	Bootstrap std. err.	z	P> z	Normal-based [95% conf. interval]	
ratio	2.063051	.0981706	21.01	0.000	1.870641	2.255462
np	70	2.071939	33.78	0.000	65.93908	74.06092
nw	74	.	.	.	.	.

◀

## Bootstrapping statistics from data with a complex structure

Here we describe how to bootstrap statistics from data with a complex structure, for example, longitudinal or panel data, or matched data. `bootstrap`, however, is not designed to work with complex survey data. It is important to include all necessary information about the structure of the data in the `bootstrap` syntax to obtain correct bootstrap estimates for standard errors and confidence intervals.

`bootstrap` offers several options identifying the specifics of the data. These options are `strata()`, `cluster()`, `idcluster()`, and `group()`. The usage of `strata()` was described in [example 3](#) above. Below, we demonstrate several examples that require specifying the other three options.

### ▶ Example 6

Suppose that `auto.dta` in [example 1](#) above are clustered by `rep78`. We want to obtain bootstrap estimates for the standard errors of the difference between the coefficients on `weight` and `gear_ratio`, taking into account clustering.

We supply the `cluster(rep78)` option to `bootstrap` to request resampling from clusters rather than from observations in the dataset.

```

. use https://www.stata-press.com/data/r17/auto, clear
(1978 automobile data)
. keep if rep78<.
(5 observations deleted)
. bootstrap diff=(_b[weight]-_b[gear]), seed(1) cluster(rep78): regress mpg
> weight gear foreign
(running regress on estimation sample)
Bootstrap replications (50)
-----|----- 1 -----|----- 2 -----|----- 3 -----|----- 4 -----|----- 5
.....|..... 50
Linear regression                                     Number of obs = 69
                                                Replications = 50

Command: regress mpg weight gear foreign
diff: _b[weight]-_b[gear]

(Replications based on 5 clusters in rep78)

```

	Observed coefficient	Bootstrap std. err.	z	P> z	Normal-based [95% conf. interval]	
diff	-1.910396	2.538558	-0.75	0.452	-6.885879	3.065087

We drop missing values in `rep78` before issuing the command because `bootstrap` does not allow missing values in `cluster()`. See the section above about using `bootstrap` when variables contain missing values.

We can also obtain these same results by using the following syntax:

```

. bootstrap diff=(_b[weight]-_b[gear]), seed(1): regress mpg weight gear foreign,
> vce(cluster rep78)

```

When only clustered information is provided to the command, `bootstrap` can pick up the `vce(cluster clustvar)` option from the main command and use it to resample from clusters.

◀

## ► Example 7

Suppose now that we have matched data and want to use `bootstrap` to obtain estimates of the standard errors of the exponentiated difference between two coefficients (or, equivalently, the ratio of two odds ratios) estimated by `clogit`. Consider the example of matched case–control data on birthweight of infants described in [example 2](#) of [R] `clogit`.

The infants are paired by being matched on mother's age. All groups, defined by the `paired` variable, have 1:1 matching. `clogit` requires that the matching information, `paired`, be supplied to the `group()` (or, equivalently, `strata()`) option to be used in computing the parameter estimates. Because the data are matched, we need to resample from groups rather than from the whole dataset. However, simply supplying the grouping variable `paired` in `cluster()` is not enough with `bootstrap`, as it is with clustered data.





## □ Technical note

Similarly, when you have panel (longitudinal) data, all resampled panels must be unique in each of the bootstrap samples to obtain correct bootstrap estimates of statistics. Therefore, both `cluster(panelvar)` and `idcluster(newpanelvar)` must be specified with `bootstrap`, and `i(newpanelvar)` must be used with the main command. Moreover, you must clear the current `xtset` settings by typing `xtset, clear` before calling `bootstrap`. □

## ▷ Example 8

Continuing with our birthweight data, suppose that we have more information about doctors supervising women's pregnancies. We believe that the data on the pairs of infants from the same doctor may be correlated and want to adjust standard errors for possible correlation among the pairs. `clogit` offers the `vce(cluster clustvar)` option to do this.

Let's add a cluster variable to our dataset. One thing to keep in mind is that to use `vce(cluster clustvar)`, groups in `group()` must be nested within clusters.

```
. use https://www.stata-press.com/data/r17/lowbirth2, clear
(Appplied Logistic Regression, Hosmer & Lemeshow)
. set seed 12345
. by pairid, sort: egen byte doctor = total(int(2*runiform()+1)*(_n == 1))
. clogit low lwt smoke ptd ht ui i.race, group(pairid) vce(cluster doctor)

Iteration 0:  log pseudolikelihood = -26.768693
Iteration 1:  log pseudolikelihood = -25.810476
Iteration 2:  log pseudolikelihood = -25.794296
Iteration 3:  log pseudolikelihood = -25.794271
Iteration 4:  log pseudolikelihood = -25.794271

Conditional (fixed-effects) logistic regression      Number of obs =    112
Wald chi2(1) = .
Prob > chi2 = .
Pseudo R2 = 0.3355

Log pseudolikelihood = -25.794271
                                (Std. err. adjusted for 2 clusters in doctor)
```

low	Coefficient	Robust std. err.	z	P> z	[95% conf. interval]	
lwt	-.0183757	.0020314	-9.05	0.000	-.0223571	-.0143942
smoke	1.400656	.3067525	4.57	0.000	.7994322	2.00188
ptd	1.808009	.2092246	8.64	0.000	1.397936	2.218082
ht	2.361152	1.410341	1.67	0.094	-.4030665	5.12537
ui	1.401929	.9406248	1.49	0.136	-.4416617	3.24552
race						
Black	.5713643	.9992656	0.57	0.567	-1.38716	2.529889
Other	-.0253148	.8453206	-0.03	0.976	-1.682113	1.631483

To obtain correct bootstrap standard errors of the exponentiated difference between the two coefficients in this example, we need to make sure that both resampled clusters and groups within resampled clusters are unique in each of the bootstrap samples. To achieve this, `bootstrap` needs the information about clusters in `cluster()`, the variable name of the new identifier for clusters in `idcluster()`, and the information about groups in `group()`. We demonstrate the corresponding syntax of `bootstrap` below.



## Stored results

`bootstrap` stores the following in `e()`:

### Scalars

<code>e(N)</code>	sample size
<code>e(N_reps)</code>	number of complete replications
<code>e(N_misreps)</code>	number of incomplete replications
<code>e(N_strata)</code>	number of strata
<code>e(N_clust)</code>	number of clusters
<code>e(k_eq)</code>	number of equations in <code>e(b)</code>
<code>e(k_exp)</code>	number of standard expressions
<code>e(k_eeexp)</code>	number of extended expressions (i.e., <code>_b</code> )
<code>e(k_extra)</code>	number of extra equations beyond the original ones from <code>e(b)</code>
<code>e(level)</code>	confidence level for bootstrap CIs
<code>e(bs_version)</code>	version for bootstrap results
<code>e(rank)</code>	rank of <code>e(V)</code>

### Macros

<code>e(cmdname)</code>	command name from <i>command</i>
<code>e(cmd)</code>	same as <code>e(cmdname)</code> or <code>bootstrap</code>
<code>e(command)</code>	<i>command</i>
<code>e(cmdline)</code>	command as typed
<code>e(prefix)</code>	<code>bootstrap</code>
<code>e(title)</code>	title in estimation output
<code>e(strata)</code>	strata variables
<code>e(cluster)</code>	cluster variables
<code>e(rngstate)</code>	random-number state used
<code>e(size)</code>	from the <code>size(#)</code> option
<code>e(exp#)</code>	expression for the <code>#</code> th statistic
<code>e(ties)</code>	<code>ties</code> , if specified
<code>e(mse)</code>	<code>mse</code> , if specified
<code>e(vce)</code>	<code>bootstrap</code>
<code>e(vctype)</code>	title used to label Std. err.
<code>e(properties)</code>	<code>b V</code>

### Matrices

<code>e(b)</code>	observed statistics
<code>e(b_bs)</code>	bootstrap estimates
<code>e(reps)</code>	number of nonmissing results
<code>e(bias)</code>	estimated biases
<code>e(se)</code>	estimated standard errors
<code>e(z0)</code>	median biases
<code>e(accel)</code>	estimated accelerations
<code>e(ci_normal)</code>	normal-approximation CIs
<code>e(ci_percentile)</code>	percentile CIs
<code>e(ci_bc)</code>	bias-corrected CIs
<code>e(ci_bca)</code>	bias-corrected and accelerated CIs
<code>e(V)</code>	bootstrap variance–covariance matrix
<code>e(V_modelbased)</code>	model-based variance

When `exp_list` is `_b`, `bootstrap` will also carry forward most of the results already in `e()` from *command*.

In addition to the above, the following is stored in `r()`:

### Matrices

<code>r(table)</code>	matrix containing the coefficients with their standard errors, test statistics, <i>p</i> -values, and confidence intervals
-----------------------	--

Note that results stored in `r()` are updated when the command is replayed and will be replaced when any `r`-class command is run after the estimation command.

## Methods and formulas

Let  $\hat{\theta}$  be the observed value of the statistic, that is, the value of the statistic calculated with the original dataset. Let  $i = 1, 2, \dots, k$  denote the bootstrap samples, and let  $\hat{\theta}_i$  be the value of the statistic from the  $i$ th bootstrap sample.

When the `mse` option is specified, the standard error is estimated as

$$\widehat{\text{se}}_{\text{MSE}} = \left\{ \frac{1}{k} \sum_{i=1}^k (\hat{\theta}_i - \hat{\theta})^2 \right\}^{1/2}$$

Otherwise, the standard error is estimated as

$$\widehat{\text{se}} = \left\{ \frac{1}{k-1} \sum_{i=1}^k (\hat{\theta}_i - \bar{\theta})^2 \right\}^{1/2}$$

where

$$\bar{\theta} = \frac{1}{k} \sum_{i=1}^k \hat{\theta}_i$$

The variance–covariance matrix is similarly computed. The bias is estimated as

$$\widehat{\text{bias}} = \bar{\theta} - \hat{\theta}$$

Confidence intervals with nominal coverage rates  $1 - \alpha$  are calculated according to the following formulas. The normal-approximation method yields the confidence intervals

$$[\hat{\theta} - z_{1-\alpha/2} \widehat{\text{se}}, \hat{\theta} + z_{1-\alpha/2} \widehat{\text{se}}]$$

where  $z_{1-\alpha/2}$  is the  $(1 - \alpha/2)$ th quantile of the standard normal distribution. If the `mse` option is specified, `bootstrap` will report the normal confidence interval using  $\widehat{\text{se}}_{\text{MSE}}$  instead of  $\widehat{\text{se}}$ . `estat bootstrap` only uses  $\widehat{\text{se}}$  in the normal confidence interval.

The percentile method yields the confidence intervals

$$[\theta_{\alpha/2}^*, \theta_{1-\alpha/2}^*]$$

where  $\theta_p^*$  is the  $p$ th quantile (the 100th percentile) of the bootstrap distribution  $(\hat{\theta}_1, \dots, \hat{\theta}_k)$ .

Let

$$z_0 = \Phi^{-1}\{\#(\hat{\theta}_i \leq \hat{\theta})/k\}$$

where  $\#(\hat{\theta}_i \leq \hat{\theta})$  is the number of elements of the bootstrap distribution that are less than or equal to the observed statistic and  $\Phi$  is the standard cumulative normal.  $z_0$  is known as the median bias of  $\hat{\theta}$ . When the `ties` option is specified,  $z_0$  is estimated as  $\#(\hat{\theta}_i < \hat{\theta}) + \#(\hat{\theta}_i = \hat{\theta})/2$ , which is the number of elements of the bootstrap distribution that are less than the observed statistic plus half the number of elements that are equal to the observed statistic.

Let

$$a = \frac{\sum_{i=1}^n (\bar{\theta}_{(\cdot)} - \hat{\theta}_{(i)})^3}{6\{\sum_{i=1}^n (\bar{\theta}_{(\cdot)} - \hat{\theta}_{(i)})^2\}^{3/2}}$$

where  $\hat{\theta}_{(i)}$  are the leave-one-out (jackknife) estimates of  $\hat{\theta}$  and  $\bar{\theta}_{(\cdot)}$  is their mean. This expression is known as the jackknife estimate of acceleration for  $\hat{\theta}$ . Let

$$p_1 = \Phi \left\{ z_0 + \frac{z_0 - z_{1-\alpha/2}}{1 - a(z_0 - z_{1-\alpha/2})} \right\}$$

$$p_2 = \Phi \left\{ z_0 + \frac{z_0 + z_{1-\alpha/2}}{1 - a(z_0 + z_{1-\alpha/2})} \right\}$$

where  $z_{1-\alpha/2}$  is the  $(1-\alpha/2)$ th quantile of the normal distribution. The bias-corrected and accelerated ( $BC_a$ ) method yields confidence intervals

$$[\theta_{p_1}^*, \theta_{p_2}^*]$$

where  $\theta_p^*$  is the  $p$ th quantile of the bootstrap distribution as defined previously. The bias-corrected (but not accelerated) method is a special case of  $BC_a$  with  $a = 0$ .

## References

- Ängquist, L. 2010. *Stata tip 92: Manual implementation of permutations and bootstraps*. *Stata Journal* 10: 686–688.
- Cameron, A. C., and P. K. Trivedi. 2010. *Microeconometrics Using Stata*. Rev. ed. College Station, TX: Stata Press.
- Davison, A. C., and D. V. Hinkley. 1997. *Bootstrap Methods and Their Application*. Cambridge: Cambridge University Press.
- Dorta, M., and G. Sanchez. 2021. *Bootstrap unit-root test for random walk with drift: The bsrwalkdrift command*. *Stata Journal* 21: 39–50.
- Efron, B. 1979. Bootstrap methods: Another look at the jackknife. *Annals of Statistics* 7: 1–26. <https://doi.org/10.1214/aos/1176344552>.
- . 1982. *The Jackknife, the Bootstrap and Other Resampling Plans*. Philadelphia: Society for Industrial and Applied Mathematics.
- Efron, B., and C. Stein. 1981. The jackknife estimate of variance. *Annals of Statistics* 9: 586–596. <https://doi.org/10.1214/aos/1176345462>.
- Efron, B., and R. J. Tibshirani. 1986. Bootstrap methods for standard errors, confidence intervals, and other measures of statistical accuracy. *Statistical Science* 1: 54–77. <https://doi.org/10.1214/ss/1177013815>.
- . 1993. *An Introduction to the Bootstrap*. New York: Chapman & Hall/CRC.
- Field, C. A., and A. H. Welsh. 2007. Bootstrapping clustered data. *Journal of the Royal Statistical Society, Series B* 69: 369–390. <https://doi.org/10.1111/j.1467-9868.2007.00593.x>.
- Guan, W. 2003. *From the help desk: Bootstrapped standard errors*. *Stata Journal* 3: 71–80.
- Hall, P., and S. R. Wilson. 1991. Two guidelines for bootstrap hypothesis testing. *Biometrics* 47: 757–762. <https://doi.org/10.2307/2532163>.
- Hinkley, D. V. 1978. Improving the jackknife with special reference to correlation estimation. *Biometrika* 65: 13–22. <https://doi.org/10.1093/biomet/65.1.13>.
- Holmes, S., C. N. Morris, and R. J. Tibshirani. 2003. Bradley Efron: A conversation with good friends. *Statistical Science* 18: 268–281. <https://doi.org/10.1214/ss/1063994981>.
- Huber, C. 2013. Measures of effect size in Stata 13. *The Stata Blog: Not Elsewhere Classified*. <http://blog.stata.com/2013/09/05/measures-of-effect-size-in-stata-13/>.
- Mooney, C. Z., and R. D. Duval. 1993. *Bootstrapping: A Nonparametric Approach to Statistical Inference*. Newbury Park, CA: SAGE.
- Ng, E. S.-W., R. Grieve, and J. R. Carpenter. 2013. Two-stage nonparametric bootstrap sampling with shrinkage correction for clustered data. *Stata Journal* 13: 141–164.

- Poi, B. P. 2004. From the help desk: Some bootstrapping techniques. *Stata Journal* 4: 312–328.
- Roodman, D., J. G. MacKinnon, M. O. Nielsen, and M. D. Webb. 2019. Fast and wild: Bootstrap inference in Stata using `boottest`. *Stata Journal* 19: 4–60.
- Royston, P., and W. Sauerbrei. 2009. Bootstrap assessment of the stability of multivariable models. *Stata Journal* 9: 547–570.
- Ruhe, C. 2019. Bootstrap pointwise confidence intervals for covariate-adjusted survivor functions in the Cox model. *Stata Journal* 19: 185–199.
- Schwarz, C. 2019. `lsemantica`: A command for text similarity based on latent semantic analysis. *Stata Journal* 19: 129–142.
- Stine, R. 1990. An introduction to bootstrap methods: Examples and ideas. In *Modern Methods of Data Analysis*, ed. J. Fox and J. S. Long, 353–373. Newbury Park, CA: SAGE.

## Also see

- [R] [bootstrap postestimation](#) — Postestimation tools for bootstrap
- [R] [jackknife](#) — Jackknife estimation
- [R] [permute](#) — Monte Carlo permutation tests
- [R] [simulate](#) — Monte Carlo simulations
- [R] [set rngstream](#) — Specify the stream for the stream random-number generator
- [SVY] [svy bootstrap](#) — Bootstrap for survey data
- [U] [13.5 Accessing coefficients and standard errors](#)
- [U] [13.6 Accessing results from Stata commands](#)
- [U] [20 Estimation and postestimation commands](#)