ciwidth onemean — Precision analysis for a one-mean CI

Description Options References

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Description

ciwidth onemean computes sample size, CI width, and probability of CI width for a CI for a population mean. It can compute sample size for a given CI width and probability of CI width. Alternatively, it can compute CI width for a given sample size and probability of CI width. It can also compute probability of CI width for a given sample size and CI width. Also see [PSS-3] **ciwidth** for PrSS analysis for other CI methods.

For power and sample-size analysis for a one-sample mean test, see [PSS-2] power onemean.

Quick start

Sample size for a two-sided 95% CI for a population mean given a CI width of 5 and a standard deviation of 12, with the probability of CI width of 0.9

ciwidth onemean, width(5) probwidth(0.9) sd(12)

Same as above, but for an upper one-sided CI with a 90% confidence level

ciwidth onemean, width(5) probwidth(0.9) sd(12) level(90) upper

Sample size for a two-sided 95% CI for a population mean given a CI width of 5, assuming a known population standard deviation of 12

ciwidth onemean, width(5) sd(12) knownsd

CI width for sample sizes of 50, 60, 70, and 80, given a probability of CI width of 0.9 ciwidth onemean, n(50(10)80) probwidth(0.9) sd(12)

Same as above, but display results in a graph of CI width versus sample size ciwidth onemean, n(50(10)80) probwidth(0.9) sd(12) graph

Probability that the width of a two-sided 95% CI is no larger than 5 for a sample size of 100 ciwidth onemean, n(100) width(5) sd(12)

Menu

Statistics > Power, precision, and sample size

Syntax

Compute sample size

ciwidth onemean, width(numlist) probwidth(numlist) [options]

Compute CI width

ciwidth onemean, probwidth(numlist) n(numlist) [options]

Compute probability of CI width

ciwidth onemean, width(numlist) n(numlist) [options]

options	Description
Main	
* <u>l</u> evel(<i>numlist</i>)	confidence level; default is level(95)
* <u>a</u> lpha(<i>numlist</i>)	significance level; default is alpha(0.05)
* probwidth(numlist)	probability of CI width; required to compute sample size and CI width
* <u>w</u> idth(<i>numlist</i>)	CI width; required to compute sample size and probability of CI width
* n(<i>numlist</i>)	sample size; required to compute CI width and probability of CI width
<u>nfrac</u> tional	allow fractional sample sizes
* sd(<i>numlist</i>)	standard deviation; default is sd(1)
knownsd	request computation assuming a known standard deviation; default is to assume an unknown standard deviation
* fpc(numlist)	finite population correction (FPC) as a sampling rate or as a population size
lower	lower one-sided CI; default is two-sided CI
upper	upper one-sided CI; default is two-sided CI
<u>onesid</u> ed	synonym for option upper
<u>par</u> allel	treat number lists in starred options or in command arguments as parallel when multiple values per option or argument are specified (do not enumerate all possible combinations of values)

<pre>Table [no]table[(tablespec)] saving(filename [, replace])</pre>	<pre>suppress table or display results as a table; see [PSS-3] ciwidth, table save the table data to filename; use replace to overwrite existing filename</pre>
Graph	
<pre>graph[(graphopts)]</pre>	graph results; see [PSS-3] ciwidth, graph
Iteration	
<pre>init(#)</pre>	initial value for sample size; default is to use a closed-form normal approximation
<u>iter</u> ate(#)	maximum number of iterations; default is iterate(500)
<u>tol</u> erance(#)	parameter tolerance; default is tolerance(1e-12)
<pre>ftolerance(#)</pre>	function tolerance; default is ftolerance(1e-12)
[no]log	suppress or display iteration log
[no]dots	suppress or display iterations as dots
notitle	suppress the title

*Specifying a list of values in at least two starred options, or at least two command arguments, or at least one starred option and one argument results in computations for all possible combinations of the values; see

[U] **11.1.8 numlist**. Also see the parallel option.

collect is allowed; see [U] 11.1.10 Prefix commands.

notitle does not appear in the dialog box.

where *tablespec* is

column[:label] [column[:label] [...]] [, tableopts]

column is one of the columns defined below, and *label* is a column label (may contain quotes and compound quotes).

column	Description	Symbol
level	confidence level	$100(1 - \alpha)$
alpha	significance level	α
N	number of subjects	N
Pr_width	probability of CI width	p_{width}
width	CI width	w
sd	standard deviation	σ
fpc	FPC as population size	$N_{ m pop}$
	FPC as sampling rate	γ
_all	display all supported columns	

Column alpha is shown in the default table in place of column level if alpha() is specified.

Column fpc is shown in the default table if fpc() is specified.

Options

Main

level(), alpha(), probwidth(), width(), n(), nfractional; see [PSS-3] ciwidth. probwidth()
 may not be combined with knownsd. The nfractional option is allowed only for sample-size determination.

- sd(numlist) specifies the population standard deviation or its estimate. The default is sd(1). By default, sd() specifies an estimate for the unknown population standard deviation. If knownsd is specified, sd() specifies the known value for the population standard deviation.
- knownsd requests that the standard deviation be treated as known in the computation. By default, the standard deviation is treated as unknown, and the computation is performed for a Student's t-based CI. If knownsd is specified, the computation is performed for a normal-based CI. knownsd may not be combined with probwidth() and is not allowed when computing the probability of CI width.
- fpc(*numlist*) requests that a finite population correction be used in the computation. If fpc() has values between 0 and 1, it is interpreted as a sampling rate, n/N, where N is the total number of units in the population. When sample size n is specified, if fpc() has values greater than n, it is interpreted as a population size, but it is an error to have values between 1 and n. For sample-size determination, fpc() with a value greater than 1 is interpreted as a population size. It is an error for fpc() to have a mixture of sampling rates and population sizes.

lower, upper, onesided, parallel; see [PSS-3] ciwidth.

Table

table, table(), notable; see [PSS-3] ciwidth, table.

saving(); see [PSS-3] ciwidth.

Graph

graph, graph(); see [PSS-3] ciwidth, graph. Also see the *column* table for a list of symbols used by the graphs.

Iteration

init(#) specifies an initial value for the sample size when iteration is used to compute the sample size. The default is to use a closed-form normal approximation to compute an initial sample size.

iterate(), tolerance(), ftolerance(), log, nolog, dots, nodots; see [PSS-3] ciwidth.

The following option is available with ciwidth onemean but is not shown in the dialog box:

notitle; see [PSS-3] ciwidth.

Remarks and examples

Remarks are presented under the following headings:

Introduction Using ciwidth onemean Computing sample size Computing CI width Computing probability of CI width This entry describes the ciwidth onemean command and the methodology for PrSS analysis for a CI for a population mean. See [PSS-3] **Intro (ciwidth)** for a general introduction to PrSS analysis, and see [PSS-3] **ciwidth** for a general introduction to the ciwidth command. For PSS analysis for hypothesis tests, see [PSS-2] **power**.

Introduction

Mean estimation is one of the most popular statistical analyses. Schools may measure the mean test score for their students. Factories may measure the mean strength of new alloys or the mean lifetime of bulbs. CIs are often used for inference about the population mean μ . They provide the ranges for plausible values for the mean based on a random sample from a population of interest. The wider the ranges, the less precise the CI.

The precision of a CI is commonly measured by its width w or, for a symmetric CI such as the CI for a population mean, by its half-width d, also known as the margin of error. For example, a two-sided one-mean CI is formed as $[\hat{\mu} - d, \hat{\mu} + d]$, where $\hat{\mu}$ is the mean point estimate. The CI width, the distance between the upper and lower limits, is w = 2d; it does not depend on the mean estimate. The smaller the d or w the more precise the CI.

In PrSS analysis, it is usually of interest to determine the sample size that would be sufficient for a CI to have a prespecified width in a future study. Generally, larger sample sizes lead to more precise CIs. To compute the required sample size, we need to know the expression for w. The expression for w depends on various assumptions.

Suppose that we have a random sample of n i.i.d. observations from a normal distribution with mean μ and standard deviation σ . If we know a population standard deviation σ , $w = 2z_{1-\alpha/2}\sigma/\sqrt{n}$, where $z_{1-\alpha/2}$ is the $(1-\alpha/2)$ th quantile of the standard normal distribution. If we do not know a σ and estimate it from the sample using the sample standard deviation s, $w = 2t_{n-1,1-\alpha/2} s/\sqrt{n}$, where $t_{n-1,1-\alpha/2}$ is the $(1-\alpha/2)$ th quantile of the Student's t distribution with n-1 degrees of freedom. $100(1-\alpha)\%$ is the confidence level of a CI. Using the relationship between CIs and hypothesis tests, a $100(1-\alpha)\%$ one-mean CI can be viewed as a set of hypothetical values of a mean that cannot be rejected by the corresponding one-sample mean test at the significance level α .

In the case of an unknown standard deviation, the CI width w depends on the sample estimate s of the standard deviation and thus will vary from one sample to another. To ensure that, in a future study, a CI has the desired width, this sampling variability of w must be accounted for when computing the required sample size. Kupper and Hafner (1989) introduce what we call the probability of CI width that specifies the probability of a future CI to have the width of no larger than some prespecified CI width for a given sample size. This probability is defined based on the assumption of a χ^2 distribution for the sample variance s^2 ; see Methods and formulas for details.

The random sample is typically drawn from an infinite population. When the sample is drawn from a population of a fixed size, sampling variability must be adjusted for a finite population size.

You can use ciwidth onemean to perform PrSS analysis for a CI for a population mean. We discuss the command details in the next section.

Using ciwidth onemean

ciwidth onemean computes sample size, CI width, or probability of CI width for a one-mean CI. By default, a two-sided CI is assumed, and the confidence level is set to 95%. You may change the confidence level by specifying the level() option. Alternatively, you can specify the significance level in the alpha() option. You can specify the upper and lower options to request upper and lower onesided CIs.

To compute sample size, you must specify the CI width in the width() option and the probability of CI width in the probwidth() option. To compute CI width, you must specify the sample size in the n() option and the probability of CI width in the probwidth() option. You can also compute the probability of CI width given the sample size in n() and CI width in width().

For CIs for means, the CI width does not depend on the mean point estimate, the sample mean, so it is not needed in the computations.

By default, all computations assume an unknown standard deviation and use a default value of 1 as the estimate of the standard deviation. You may specify other values for the standard deviation in the sd() option. For a known standard deviation, you can specify the knownsd option to request a normal-based CI instead of the default Student's *t*-based CI. In this case, the sd() option specifies the actual population standard deviation.

By default, the computed sample size is rounded up. You can specify the nfractional option to see the corresponding fractional sample size; see *Fractional sample sizes* in [PSS-4] **Unbalanced designs** for an example. The nfractional option is allowed only for sample-size determination.

Some of ciwidth onemean's computations require iteration. For example, when the standard deviation is unknown, the sample-size computation requires iteration. The default initial value of the estimated sample size is obtained by using a closed-form normal approximation. It may be changed by specifying the init() option. See [PSS-3] ciwidth for the descriptions of other options that control the iteration procedure.

All computations assume an infinite population. For a finite population, use the fpc() option to specify a sampling rate or a population size.

In the following sections, we describe the use of ciwidth onemean accompanied by examples for computing sample size, CI width, and probability of CI width.

Computing sample size

To compute the sample size required for a one-mean CI to have the width no larger than a target width, you must specify the target CI width in the width() option and the desired probability of achieving the target CI width in the probwidth() option.

Example 1: Sample size for a one-mean CI

Consider an example from Meeker, Hahn, and Escobar (2017, 152) of an experiment that measures the mean tensile strength of a new alloy. The number of specimens needed to be tested is of interest. We assume that the strength follows a normal distribution and the true population standard deviation is unknown. We use a conservative estimate of 2,500 kg for it in this example. We want to compute the sample size required for the two-sided 95% CI for the mean tensile strength to have the width of no larger than 3,000 kg. In addition to the sample size, the CI width depends on the standard deviation. Because we assume an unknown standard deviation, the CI width may vary from one study to another. We must

account for this sampling variability when estimating the sample size. So, to ensure that the CI will have the width of at most 3,000 kg, we must also specify the probability of achieving the target CI width. If we do not, our results will be based on the assumption that a future sample will have the standard deviation of 2,500 kg, which may not be a realistic assumption given an unknown standard deviation. In our example, we will use the probability of CI width of 0.96. To compute the sample size, we type

We find that a sample of 20 specimens is required to obtain a two-sided 95% CI for the mean that, with a probability of 0.96, will have the width of no more than 3,000 kg.

As we mentioned in *Using ciwidth onemean* and as is also indicated in the output, sample-size computation requires iteration when the standard deviation is unknown. The iteration log is suppressed by default, but you can display it by specifying the log option.

```
Example 2: Known variance
```

If we know the population standard deviation, we can use the knownsd option to compute results for a normal z-based CI. Because we assume a known standard deviation, the probwidth() option is not needed. In fact, it is not allowed in combination with knownsd.

The output now indicates that the computation is based on a normal CI instead of the default Student's t CI. We find that a smaller sample of 11 subjects is required for the mean CI to achieve the same CI width as in example 1 when the standard deviation is known.

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Computing CI width

To compute the CI width, you must specify the sample size in the n() option and the desired probability of achieving the target CI width in the probwidth() option.

Example 3: Precision of a one-mean CI

Continuing with example 1, we can compute the CI width for a given sample size. Suppose we want to compute the CI width corresponding to the sample size of 20 from example 1. We replace the width(3000) option with the n(20) option:

```
. ciwidth onemean, sd(2500) probwidth(0.96) n(20)
Estimated width for a one-mean CI
Student's t two-sided CI
Study parameters:

    level = 95.00

    N = 20

Pr_width = 0.9600

    sd = 2500.0000
Estimated width:

    width = 2990.8196
```

The estimated CI width is about 2,991 kg and is smaller than the width of 3,000 kg used in example 1. The actual sample size corresponding to the CI width of 3,000 is slightly smaller than 20. You can see this by specifying the nfractional option in example 1 to report a fractional sample size. By default, ciwidth methods round the actual sample size up to the nearest integer. The CI width corresponding to a larger sample size will be smaller.

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Example 4: One-sided CI

You can specify the upper or lower option to request an upper or lower one-sided CI. Continuing with example 3, we estimate the CI width for an upper 95% CI.

```
. ciwidth onemean, sd(2500) probwidth(0.96) n(20) upper
Estimated width for a one-mean CI
Student's t upper CI
Study parameters:
    level = 95.00
    N = 20
Pr_width = 0.9600
    sd = 2500.0000
Estimated width:
    width = 1235.4192
```

The upper bound for the mean tensile strength of a new alloy is about 1,235 kg from its point estimate.

Example 5: Multiple values of study parameters

To investigate the effect of the sample size on the CI width, we can specify a list of sample sizes in the n() option:

```
. ciwidth onemean, sd(2500) probwidth(0.96) n(10(10)50)
Estimated width for a one-mean CI
Student's t two-sided CI
```

level	N Pr_width		width	sd
95	10	.96	5003	2500
95	20	.96	2991	2500
95	30	.96	2289	2500
95	40	.96	1912	2500
95	50	.96	1669	2500

As expected, when the sample size increases, the CI width decreases. The decrease is particularly prominent when the sample size increases from 10 to 20.

For multiple values of parameters, the results are automatically displayed in a table, as we see above. For more examples of tables, see [PSS-3] **ciwidth**, **table**. If you wish to produce sample-size and other curves, see [PSS-3] **ciwidth**, **graph**.

```
4
```

Computing probability of CI width

To compute the probability that the width of a future CI will be no larger than the specified width, you must specify the sample size in the n() option and the target CI width in the width() option.

Example 6: Computing probability of CI width for a one-mean CI

Continuing with example 1, we may also want to know the probability that the CI width in a future study will be no larger than a prespecified value for a given sample size. To compute the probability of CI width, we specify the sample size of 20 in n() and the CI width of 3,000 in width(). We use the same estimate of 2,500 for the standard deviation.

```
. ciwidth onemean, sd(2500) n(20) width(3000)
Estimated probability of width for a one-mean CI
Student's t two-sided CI
Study parameters:
    level = 95.00
    N = 20
    width = 3000.0000
    sd = 2500.0000
Estimated probability of width:
    Pr_width = 0.9619
```

The estimated probability is about 96%, which is consistent with what we used in example 1.

Stored results

ciwidth onemean stores the following in r():

Scalars

	r(level)	confidence level
	r(alpha)	significance level
	r(N)	sample size
	r(nfractional)	1 if nfractional is specified, 0 otherwise
	r(onesided)	1 for a one-sided CI, 0 otherwise
	r(Pr_width)	probability of CI width
	r(Pr_width_a)	actual probability of CI width (for sample-size determination when probwidth() specified)
	r(width)	CI width
	r(width_a)	actual CI width (for sample-size determination when knownsd specified)
	r(sd)	standard deviation
	r(knownsd)	1 if option knownsd is specified, 0 otherwise
	r(fpc)	finite population correction (if specified)
	r(separator)	number of lines between separator lines in the table
	r(divider)	1 if divider is requested in the table, 0 otherwise
	r(init)	initial value for sample size
	r(maxiter)	maximum number of iterations
	r(iter)	number of iterations performed
	r(tolerance)	requested parameter tolerance
	r(deltax)	final parameter tolerance achieved
	r(ftolerance)	requested distance of the objective function from zero
	r(function)	final distance of the objective function from zero
	r(converged)	1 if iteration algorithm converged, 0 otherwise
Mac	ros	
	r(type)	ci
	r(method)	onemean
	r(onesidedci)	upper or lower (for a one-sided CI)
	r(columns)	displayed table columns
	r(labels)	table column labels
	r(widths)	table column widths
	r(formats)	table column formats
Mat	rices	
	r(pss_table)	table of results

Methods and formulas

Let $\mathbf{x} = (x_1, \dots, x_n)$ be a random sample of i.i.d. observations from a normal population with mean μ and variance σ^2 . A general two-sided CI is defined as $[\ll(\mathbf{x}), ul(\mathbf{x})]$, a lower one-sided CI as $[\ll(\mathbf{x}), \infty)$, and an upper one-sided CI as $(-\infty, ul(\mathbf{x})]$, where $\ll(\mathbf{x}) = \ll$ and $ul(\mathbf{x}) = ul$ are the respective lower and upper confidence limits. Let w be the CI width.

Let

$$\overline{x} = \frac{1}{n}\sum_{i=1}^n x_i \qquad \text{and} \qquad s^2 = \frac{1}{n-1}\sum_{i=1}^n (x_i - \overline{x})^2$$

be the sample mean and the sample variance, respectively.

A two-sided CI for the population mean μ is constructed as

$$[\overline{x} - w/2, \overline{x} + w/2]$$

where w/2 is the half-width or margin of error.

Lower and upper one-sided CIs are constructed as

$$[\overline{x} - w, \infty)$$
$$(-\infty, \overline{x} + w]$$

We use the CI width w as our measure of CI precision. Let $100(1 - \alpha)$ % denote the confidence level, where $0 \le \alpha \le 1$ is the corresponding significance level.

The formulas below are based on Kupper and Hafner (1989), Ryan (2013), Dixon and Massey (1983), Zar (2010), and Chow et al. (2018).

Methods and formulas are presented under the following headings:

Known standard deviation Unknown standard deviation Finite population size

Known standard deviation

In the case of a known standard deviation, the sampling distribution of the statistic $z = \sqrt{n}(\overline{x} - \mu)/\sigma$ follows the standard normal distribution. Let $z_{1-\alpha}$ be the $(1 - \alpha)$ th quantile of the standard normal distribution.

Based on the normal distribution of z, the corresponding two-sided, lower, and upper CIs are

$$\begin{bmatrix} \overline{x} - z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}}, \overline{x} + z_{1-\alpha/2} \frac{\sigma}{\sqrt{n}} \end{bmatrix}$$
$$\begin{bmatrix} \overline{x} - z_{1-\alpha} \frac{\sigma}{\sqrt{n}}, \infty \end{pmatrix}$$
$$\begin{pmatrix} -\infty, \overline{x} + z_{1-\alpha} \frac{\sigma}{\sqrt{n}} \end{bmatrix}$$

The corresponding CI width is

$$w = \begin{cases} \frac{2z_{1-\alpha/2}\sigma}{\sqrt{n}} & \text{for a two-sided CI} \\ \frac{z_{1-\alpha}\sigma}{\sqrt{n}} & \text{for lower and upper one-sided CI} \end{cases}$$
(1)

The sample size n is computed by inverting (1):

$$n = \begin{cases} \left(\frac{2z_{1-\alpha/2}\sigma}{w}\right)^2 & \text{for a two-sided CI} \\ \left(\frac{z_{1-\alpha}\sigma}{w}\right)^2 & \text{for lower and upper one-sided CI} \end{cases}$$
(2)

Unknown standard deviation

In the case of an unknown standard deviation, an unbiased estimator s is used in place of σ in the definition of a z statistic from Known standard deviation. The sampling distribution of the corresponding statistic $t = \sqrt{n}(\overline{x} - \mu)/s$ follows a Student's t distribution with n-1 degrees of freedom. Let $t_{n-1,1-\alpha}$ be the $(1-\alpha)$ th quantile of the Student's t distribution with n-1 degrees of freedom.

The corresponding two-sided, lower, and upper CIs are

$$\begin{split} \left[\overline{x} - t_{n-1,1-\alpha/2} \frac{s}{\sqrt{n}}, \overline{x} + t_{n-1,1-\alpha/2} \frac{s}{\sqrt{n}}\right] \\ & \left[\overline{x} - t_{n-1,1-\alpha} \frac{s}{\sqrt{n}}, \infty\right) \\ & \left(-\infty, \overline{x} + t_{n-1,1-\alpha} \frac{s}{\sqrt{n}}\right] \end{split}$$

The CI width depends on the sample standard deviation s, which will vary between random samples. To account for the sampling variability of s and consequently of the CI width, Kupper and Hafner (1989) consider the probability of CI width, Pr(w), such that

$$\Pr\left(2t_{n-1,1-\alpha/2}\frac{s}{\sqrt{n}} \le w\right) \ge \Pr(w) \tag{3}$$

The above is for a two-sided CI, but a similar expression can be constructed for a one-sided CI. Pr(w) is the probability that the width of a future CI will not exceed some prespecified width w.

Formula (3) can be rewritten as

$$\Pr\left\{\frac{(n-1)s^2}{\sigma^2} \ge \frac{n(n-1)w^2}{4\sigma^2 t_{n-1,1-\alpha/2}^2}\right\} \ge \Pr(w) \tag{4}$$

When data **x** are normally distributed, the sampling distribution of the statistic $(n-1)s^2/\sigma^2$ is a χ^2 distribution with n-1 degrees of freedom. Then, using (4), we can compute the probability of CI width as follows:

$$\Pr(w) = \begin{cases} \chi_{n-1}^2 \left\{ \frac{n(n-1)w^2}{4\sigma^2 t_{n-1,1-\alpha/2}^2} \right\} & \text{for a two-sided CI} \\ \chi_{n-1}^2 \left\{ \frac{n(n-1)w^2}{\sigma^2 t_{n-1,1-\alpha}^2} \right\} & \text{for lower and upper one-sided CIs} \end{cases}$$
(5)

where $\chi^2_{n-1}(\cdot)$ is the c.d.f. of a χ^2 distribution with n-1 degrees of freedom.

We can compute the CI width from (5) as follows:

$$w = \begin{cases} 2t_{n-1,1-\alpha/2}\sigma \sqrt{\frac{\chi^2_{n-1},\mathbf{Pr}_{(w)}}{n(n-1)}} & \text{for a two-sided CI} \\ t_{n-1,1-\alpha}\sigma \sqrt{\frac{\chi^2_{n-1},\mathbf{Pr}_{(w)}}{n(n-1)}} & \text{for lower and upper one-sided CI} \end{cases}$$
(6)

where $\chi^2_{n-1,p}$ is the *p*th quantile of a χ^2 distribution with n-1 degrees of freedom.

We solve for the sample size iteratively using (6) with initial values obtained from (2).

Finite population size

The above formulas assume that the random sample is drawn from an infinite population. In cases when the size of the population is known, we need to make the following adjustment to the standard deviation,

$$\sigma_{\rm fpc} = \sigma \sqrt{\left(1 - \frac{n}{N}\right)}$$

where $\sigma_{\rm fpc}$ is the population standard deviation adjusted for finite population size.

If the nfractional option is not specified, the computed sample size is rounded up.

References

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Also see

[PSS-3] ciwidth — Precision and sample-size analysis for CIs

[PSS-3] ciwidth, graph — Graph results from the ciwidth command

[PSS-3] ciwidth, table — Produce table of results from the ciwidth command

[PSS-2] power onemean — Power analysis for a one-sample mean test

[PSS-5] Glossary

[R] ci — Confidence intervals for means, proportions, and variances

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