discrim estat — Postestimation tools for discrim

Postestimation commands	Description for estat	Quick start for estat	Menu for estat
Syntax for estat	Options for estat	Remarks and examples	Stored results
Methods and formulas	References	Also see	

Postestimation commands

The following postestimation commands are of special interest after candisc, discrim knn, discrim lda, discrim logistic, and discrim qda:

Command	Description
estat classtable	classification table
estat errorrate	classification error-rate estimation
estat grsummarize	group summaries
estat list	classification listing
estat summarize	estimation sample summary

There are more postestimation commands of special interest after discrim lda and discrim qda; see [MV] discrim lda postestimation and [MV] discrim qda postestimation.

Description for estat

estat classtable displays a cross-tabulation of the original groups with the classification groups. Classification percentages, average posterior probabilities, group prior probabilities, totals, and leaveone-out results are available.

estat errorrate displays error-rate estimates for the classification. Count-based estimates and both stratified and unstratified posterior-probability-based estimates of the error rate are available. These estimates can be resubstitution or leave-one-out estimates.

estat grsummarize presents estimation sample summary statistics for the discriminating variables for each group defined by the grouping variable. Means, medians, minimums, maximums, standard deviations, coefficients of variation, standard errors of the means, and group sizes may be displayed. Overall sample statistics are also available.

estat list lists group membership, classification, and probabilities for observations.

estat summarize summarizes the variables in the discriminant analysis over the estimation sample.

Quick start for estat

Classification table

Classification table computed using proportional prior probabilities estat classtable, priors(proportional)

Leave-one-out classification table showing average posterior probability of classification into each group estat classtable, looclass probabilities

Classification error-rate estimation

Error-rate table estimated from leave-one-out error count estat errorrate, looclass

Error rates estimated from posterior probabilities using proportional prior probabilities estat errorrate, pp priors(proportional)

Group summaries

Summary statistics by group estat grsummarize

Mean, median, standard deviation, minimum, and maximum by group estat grsummarize, mean median sd min max

Classification listing

Listing of group membership, classification, and probabilities including the leave-one-out results estat list, classification(looclass) probabilities(loopr)

Same as above, but suppress the resubstitution classification

```
estat list, classification(looclass noclass) ///
probabilities(loopr nopr)
```

Estimation sample summary

Summary of variables from the most recent discriminant analysis and displaying variable labels estat summarize, labels

Menu for estat

Statistics > Postestimation

Syntax for estat

Classification table

estat classtable [if] [in] [weight] [, classtable_options]

Classification error-rate estimation

estat errorrate [if] [in] [weight] [, errorrate_options]

Group summaries

estat grsummarize [, grsummarize_options]

Classification listing

estat list [if] [in] [, list_options]

Estimation sample summary

estat <u>su</u>mmarize [, <u>lab</u>els <u>nohea</u>der <u>noweig</u>hts]

classtable_options Description

Main	
<u>cl</u> ass	display the classification table; the default
<u>loo</u> class	display the leave-one-out classification table
Options	
<pre>priors(priors)</pre>	group prior probabilities; defaults to e(grouppriors)
nopriors	suppress display of prior probabilities
<u>tie</u> s(<i>ties</i>)	how ties in classification are to be handled; defaults to e(ties)
<u>tit</u> le(<i>text</i>)	title for classification table
probabilities	display the average posterior probability of being classified into each group
nopercents	suppress display of percentages
nototals	suppress display of row and column totals
<u>norowt</u> otals	suppress display of row totals
<u>nocolt</u> otals	suppress display of column totals
priors	Description
equal	equal prior probabilities
proportional	group-size-proportional prior probabilities
matname	row or column vector containing the group prior probabilities
matrix_exp	matrix expression providing a row or column vector of the group prior probabilities

ties	Description
missing	ties in group classification produce missing values
<u>r</u> andom	ties in group classification are broken randomly
<u>f</u> irst	ties in group classification are set to the first tied group
nearest	ties in group classification are assigned based on the closest observation, or missing if this still results in a tie; after discrim knn only
errorrate_options	Description
Main	
<u>cl</u> ass	display the classification-based error-rate estimates table; the default
<u>loo</u> class	display the leave-one-out classification-based error-rate estimates table
<u>cou</u> nt	use a count-based error-rate estimate
pp[(<i>ppopts</i>)]	use a posterior-probability-based error-rate estimate
Options	
<pre>priors(priors)</pre>	group prior probabilities; defaults to e(grouppriors)
nopriors	suppress display of prior probabilities
<u>tie</u> s(<i>ties</i>)	how ties in classification are to be handled; defaults to e(ties)
<u>tit</u> le(<i>text</i>)	title for error-rate estimate table
<u>not</u> otal	suppress display of total column
ppopts	Description
stratified	nearest stratified regults
<u>s</u> tratified	present unstratified results
grsummarize_options	Description
Main	
n[(% <i>fmt</i>)]	group sizes
<u>m</u> ean[(% <i>fmt</i>)]	means
<pre>median[(%fmt)]</pre>	medians
sd[(% <i>fmt</i>)]	standard deviations
cv[(% <i>fmt</i>)]	coefficients of variation
<pre>semean[(%fmt)]</pre>	standard errors of the means
min[(% <i>fmt</i>)]	minimums
$\max\left[\left(\frac{9}{fmt}\right)\right]$	maximums
Deptions	
Deptions	suppress overall statistics

list_options	Description
Main	
<u>mis</u> classified	list only misclassified and unclassified observations
<u>cl</u> assification(<i>clopts</i>)	control display of classification
<pre>probabilities(propts)</pre>	control display of probabilities
<u>var</u> list[(<i>varopts</i>)]	display discriminating variables
[<u>no</u>]obs	display or suppress the observation number
<pre>id(varname [format(%fmt)])</pre>	display identification variable
Options	
weight[(weightopts)]	display frequency weights
priors(<i>priors</i>)	group prior probabilities; defaults to e(grouppriors)
ties(<i>ties</i>)	how ties in classification are to be handled; defaults to e(ties)
<pre>separator(#)</pre>	display a horizontal separator every # lines
clopts	Description
<u>noc</u> lass	do not display the standard classification
<u>loo</u> class	display the leave-one-out classification
<u>not</u> rue	do not show the group variable
<u>nos</u> tar	do not display stars indicating misclassified observations
<u>nol</u> abel	suppress display of value labels for the group and classification variables
<u>for</u> mat(% <i>fmt</i>)	format for group and classification variables; default is %5.0f for unlabeled numeric variables
propts	Description
nopr	suppress display of standard posterior probabilities
loopr	display leave-one-out posterior probabilities
<pre>format(%fmt)</pre>	format for probabilities; default is format(%7.4f)
varopts	Description
none	do not display discriminating variables: the default
first	display input variables before classifications and probabilities
_ last	display input variables after classifications and probabilities
<u>for</u> mat(% <i>fmt</i>)	format for input variables; default is the input variable format
weightopts	Description
none	do not display the weights
<pre>format(%fmt)</pre>	format for the weight; default is %3.0f for weights < 1,000, %5.0f for 1,000 < weights < 100,000, and %8.0g otherwise

collect is allowed with estat classtable, estat errorrate, estat grsummarize, and estat summarize; see [U] 11.1.10 Prefix commands.

fweights are allowed; see [U] 11.1.6 weight.

Options for estat

Options are presented under the following headings:

Options for estat classtable Options for estat errorrate Options for estat grsummarize Options for estat list Options for estat summarize

Options for estat classtable

Main

- class, the default, displays the classification table. With in-sample observations, this is called the resubstitution classification table.
- looclass displays a leave-one-out classification table, instead of the default classification table. Leaveone-out classification applies only to the estimation sample, and so, in addition to restricting the observations to those chosen with if and in qualifiers, the observations are further restricted to those included in e(sample).

Options

priors (*priors*) specifies the prior probabilities for group membership. If priors() is not specified, e(grouppriors) is used. If nopriors is specified with priors(), prior probabilities are used for calculation of the classification variable but not displayed. The following *priors* are allowed:

priors(equal) specifies equal prior probabilities.

priors (proportional) specifies group-size-proportional prior probabilities.

priors (matname) specifies a row or column vector containing the group prior probabilities.

- priors(*matrix_exp*) specifies a matrix expression providing a row or column vector of the group prior probabilities.
- nopriors suppresses display of the prior probabilities. This option does not change the computations that rely on the prior probabilities specified in priors() or as found by default in e(grouppriors).
- ties (*ties*) specifies how ties in group classification will be handled. If ties() is not specified, e(ties) determines how ties are handled. The following *ties* are allowed:

ties(missing) specifies that ties in group classification produce missing values.

ties (random) specifies that ties in group classification are broken randomly.

ties(first) specifies that ties in group classification are set to the first tied group.

- ties(<u>n</u>earest) specifies that ties in group classification are assigned based on the closest observation, or missing if this still results in a tie. ties(nearest) is available after discrim knn only.
- title(*text*) customizes the title for the classification table.

probabilities specifies that the classification table show the average posterior probability of being classified into each group. probabilities implies norowtotals and nopercents.

nopercents specifies that percentages are to be omitted from the classification table.

nototals specifies that row and column totals are to be omitted from the classification table.

norowtotals specifies that row totals are to be omitted from the classification table.

nocoltotals specifies that column totals are to be omitted from the classification table.

Options for estat errorrate

🛛 Main 🗋

- class, the default, specifies that the classification-based error-rate estimates table be presented. The alternative to class is looclass.
- looclass specifies that the leave-one-out classification error-rate estimates table be presented.
- count, the default, specifies that the error-rate estimates be based on misclassification counts. The alternative to count is pp().
- pp[(ppopts)] specifies that the error-rate estimates be based on posterior probabilities. pp is equivalent to pp(stratified unstratified). stratified indicates that stratified estimates be presented. unstratified indicates that unstratified estimates be presented. One or both may be specified.

Options

priors(*priors*) specifies the prior probabilities for group membership. If priors() is not specified, e(grouppriors) is used. If nopriors is specified with priors(), prior probabilities are used for calculation of the error-rate estimates but not displayed. The following *priors* are allowed:

priors (equal) specifies equal prior probabilities.

priors (proportional) specifies group-size-proportional prior probabilities.

priors (matname) specifies a row or column vector containing the group prior probabilities.

priors(*matrix_exp*) specifies a matrix expression providing a row or column vector of the group prior probabilities.

- nopriors suppresses display of the prior probabilities. This option does not change the computations that rely on the prior probabilities specified in priors() or as found by default in e(grouppriors).
- ties (*ties*) specifies how ties in group classification will be handled. If ties () is not specified, e(ties) determines how ties are handled. The following *ties* are allowed:

ties(missing) specifies that ties in group classification produce missing values.

ties (random) specifies that ties in group classification are broken randomly.

ties(first) specifies that ties in group classification are set to the first tied group.

ties(<u>n</u>earest) specifies that ties in group classification are assigned based on the closest observation, or missing if this still results in a tie. ties(nearest) is available after discrim knn only.

title(*text*) customizes the title for the error-rate estimates table.

nototal suppresses the total column containing overall sample error-rate estimates.

Options for estat grsummarize

🛾 Main 🗋

- n[(%*fmt*)] specifies that group sizes be presented. The optional argument provides a display format. The default options are n and mean.
- mean[(% fmt)] specifies that means be presented. The optional argument provides a display format. The default options are n and mean.

median [(% fmt)] specifies that medians be presented. The optional argument provides a display format.

- sd[(%*fmt*)] specifies that standard deviations be presented. The optional argument provides a display format.
- cv[(% fint)] specifies that coefficients of variation be presented. The optional argument provides a display format.
- semean[(%fmt)] specifies that standard errors of the means be presented. The optional argument provides a display format.

 $\min[(\% fint)]$ specifies that minimums be presented. The optional argument provides a display format.

 $\max[(\% fint)]$ specifies that maximums be presented. The optional argument provides a display format.

Options

nototal suppresses display of the total column containing overall sample statistics.

transpose specifies that the groups are to be displayed by row. By default, groups are displayed by column. If you have more variables than groups, you might prefer the output produced by transpose.

Options for estat list

Main

misclassified lists only misclassified and unclassified observations.

- classification(clopts) controls display of the group variable and classification. By default, the standard classification is calculated and displayed along with the group variable in e(groupvar), using labels from the group variable if they exist. clopts may be one or more of the following:
 - noclass suppresses display of the standard classification. If the observations are those used in the estimation, classification is called resubstitution classification.
 - looclass specifies that the leave-one-out classification be calculated and displayed. The default is that the leave-one-out classification is not calculated. looclass is not allowed after discrim logistic.
 - notrue suppresses the display of the group variable. By default, e(groupvar) is displayed. notrue implies nostar.
 - nostar suppresses the display of stars indicating misclassified observations. A star is displayed by default when the classification is not in agreement with the group variable. nostar is the default when notrue is specified.
 - nolabel specifies that value labels for the group variable, if they exist, not be displayed for the group or classification or used as labels for the probability column names.

- format (% fmt) specifies the format for the group and classification variables. If value labels are used, string formats are permitted.
- probabilities (*propts*) controls the display of group posterior probabilities. *propts* may be one or more of the following:
 - nopr suppresses display of the standard posterior probabilities. By default, the posterior probabilities are shown.
 - loopr specifies that leave-one-out posterior probabilities be displayed. loopr is not allowed after discrim logistic.

format (% fmt) specifies the format for displaying probabilities. The default is format (%7.4f).

varlist[(varopts)] specifies that the discriminating variables found in e(varlist) be displayed and specifies the display options for the variables.

none specifies that discriminating variables are not to be displayed. This is the default.

first specifies variables be displayed before classifications and probabilities.

last specifies variables be displayed after classifications and probabilities.

format (% fmt) specifies the format for the input variables. By default, the variable's format is used.

- [no]obs indicates that observation numbers be or not be displayed. Observation numbers are displayed by default unless id() is specified.
- id(*varname* [format(%*fmt*)]) specifies the identification variable to display and, optionally, the format for that variable. By default, the format of *varname* is used.

Options

weight[(weightopts)] specifies options for displaying weights. By default, if e(wexp) exists, weights are displayed.

none specifies weights not be displayed. This is the default if weights were not used with discrim.

format (% fmt) specifies a display format for the weights. If the weights are < 1,000, %3.0f is the default, %5.0f is the default if 1,000 < weights < 100,000, else %8.0g is used.

priors (*priors*) specifies the prior probabilities for group membership. If priors() is not specified, e(grouppriors) is used. The following *priors* are allowed:

priors(equal) specifies equal prior probabilities.

priors (proportional) specifies group-size-proportional prior probabilities.

priors (matname) specifies a row or column vector containing the group prior probabilities.

- priors(*matrix_exp*) specifies a matrix expression providing a row or column vector of the group prior probabilities.
- ties (*ties*) specifies how ties in group classification will be handled. If ties () is not specified, e(ties) determines how ties are handled. The following *ties* are allowed:

ties(missing) specifies that ties in group classification produce missing values.

ties (random) specifies that ties in group classification are broken randomly.

ties(first) specifies that ties in group classification are set to the first tied group.

- ties (<u>n</u>earest) specifies that ties in group classification are assigned based on the closest observation, or missing if this still results in a tie. ties(nearest) is available after discrim knn only.
- separator(#) specifies a horizontal separator line be drawn every # observations. The default is separator(5).

Options for estat summarize

labels, noheader, and noweights are the same as for the generic estat summarize; see [R] estat summarize.

Remarks and examples

Remarks are presented under the following headings:

Discriminating-variable summaries Discrimination listings Classification tables and error rates

There are several estat commands that apply after all the discrim subcommands. estat summarize and estat grsummarize summarize the discriminating variables over the estimation sample and by-group. estat list displays classifications, posterior probabilities, and more for selected observations. estat classtable and estat errorrate display the classification table, also known as a confusion matrix, and error-rate estimates based on the classification table.

Discriminating-variable summaries

estat summarize and estat grsummarize provide summaries of the variables involved in the preceding discriminant analysis model.

Example 1

Example 3 of [MV] discrim Ida introduces the famous iris data originally from Anderson (1935) and used by Fisher (1936) in the development of linear discriminant analysis. We continue our exploration of the linear discriminant analysis of the iris data and demonstrate the summary estat tools available after all discrim subcommands.

```
use https://www.stata-press.com/data/r19/iris
(Iris data)
discrim lda seplen sepwid petlen petwid, group(iris) notable
```

The notable option of discrim suppressed display of the classification table. We explore the use of estat classtable later.

What can we le	earn about the un	derlying discrimina	iting variables?	estat summarize	gives a sum-
mary of the variab	les involved in th	e discriminant anal	ysis, restricted t	o the estimation sam	iple.

estat summarize						
Estimation sar	nple discrim	Numbe	Number of obs = 150			
Variable	Mean	Std. dev.	Min	Max		
groupvar iris	2	.8192319	1	3		
variables seplen sepwid petlen petwid	5.843333 3.057333 3.758 1.199333	.8280661 .4358663 1.765298 .7622377	4.3 2 1 .1	7.9 4.4 6.9 2.5		

estat summarize displays the mean, standard deviation, minimum, and maximum for the group variable, iris, and the four discriminating variables, seplen, sepwid, petlen, and petwid. Also shown is the number of observations. If we had fit our discriminant model on a subset of the data, estat summarize would have restricted its summary to those observations.

More interesting than an overall summary of the discriminating variables is a summary by our group variable, iris.

. estat grsumma:	rize			
Estimation samp	le discrim ld	a		
Summarized by 1	15			
	iris			
Mean	Setosa	Versicolor	Virginica	Total
seplen	5.006	5.936	6.588	5.843333
sepwid	3.428	2.77	2.974	3.057333
petlen	1.462	4.26	5.552	3.758
petwid	.246	1.326	2.026	1.199333
N	50	50	50	150

By default, estat grsummarize displays means of the discriminating variables for each group and overall (the total column), along with group sizes. The summary is restricted to the estimation sample.

The petal length and width of *Iris setosa* appear to be much smaller than those of the other two species. *Iris versicolor* has petal length and width between that of the other two species.

Other statistics may be requested. A look at the minimums and maximums might provide more insight into the separation of the three iris species.

. estat grsumma	rize, min max			
Estimation samp Summarized by i	le discrim ld ris	a		
	iris			
	Setosa	Versicolor	Virginica	Total
seplen				
Min	4.3	4.9	4.9	4.3
Max	5.8	7	7.9	7.9
sepwid				
- Min	2.3	2	2.2	2
Max	4.4	3.4	3.8	4.4
petlen				
- Min	1	3	4.5	1
Max	1.9	5.1	6.9	6.9
petwid				
- Min	.1	1	1.4	.1
Max	.6	1.8	2.5	2.5

Although this table is helpful, an altered view of it might make comparisons easier. estat grsummarize allows a format to be specified with each requested statistic. We can request a shorter format for the minimum and maximum and specify a fixed format so that the decimal point lines up. estat grsummarize also has a transpose option that places the variables and requested statistics as columns and the groups as rows. If you have fewer discriminating variables than groups, this might be the most natural way to view the statistics. Here we have more variables, but with a narrow display format, the transposed view still works well.

```
. estat grsummarize, min(%4.1f) max(%4.1f) transpose
Estimation sample discrim lda
```

```
Summarized by iris
```

iris	seple	n	sepwie	d	petle	n	petwic	d
	Min	Max	Min	Max	Min	Max	Min	Max
Setosa	4.3	5.8	2.3	4.4	1.0	1.9	0.1	0.6
Versicolor	4.9	7.0	2.0	3.4	3.0	5.1	1.0	1.8
Virginica	4.9	7.9	2.2	3.8	4.5	6.9	1.4	2.5
Total	4.3	7.9	2.0	4.4	1.0	6.9	0.1	2.5

The maximum petal length and width for *Iris setosa* are much smaller than the minimum petal length and width for the other two species. The petal length and width clearly separate *Iris setosa* from the other two species.

You are not limited to one or two statistics with estat grsummarize, and each statistic may have different requested display formats. The total column, or row if the table is transposed, can also be suppressed.

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Using Stata's graph box command is another way of seeing the differences among the three iris species for the four discriminating variables.

- . graph box seplen, over(iris) name(sl)
- . graph box sepwid, over(iris) name(sw)
- . graph box petlen, over(iris) name(pl)
- . graph box petwid, over(iris) name(pw)
- . graph combine sl sw pl pw, title(Characteristics of three iris species)





The box plots confirm the lack of overlap in the petal lengths and widths for *Iris setosa* compared with the other two iris species. Other differences between the species are also seen.

More summary estat commands are available after discrim lda; see [MV] discrim lda postestimation.

Discrimination listings

Listing the true group, classified group, group posterior probabilities, and discriminating variables for observations of interest after discrim is easy with the estat list command.

Example 2

Example 1 of [MV] **discrim** introduced the riding-mower data of Johnson and Wichern (2007) and presented a linear discriminant analysis that concluded with the use of estat list displaying the misclassified observations.

```
use https://www.stata-press.com/data/r19/lawnmower2
(Johnson and Wichern (2007) table 11.1)
discrim lda income lotsize, group(owner) notable
estat list, class(loo) pr(loo) misclassified
```

	Classification			Probabili	ties	LOO Probabilities	
Obs	True	Class.	L00 Cl.	Nonowner	Owner	Nonowner	Owner
1 2 13 14 17	Owner Owner Nonown Nonown Nonown	Nonown * Owner Owner * Nonown Owner *	Nonown * Nonown * Owner * Owner * Owner *	0.7820 0.4945 0.2372 0.5287 0.3776	0.2180 0.5055 0.7628 0.4713 0.6224	0.8460 0.6177 0.1761 0.4313 0.2791	0.1540 0.3823 0.8239 0.5687 0.7209

* indicates misclassified observations

The misclassified option limited the listing to those observations that were misclassified by the linear discriminant model. class(loo) and pr(loo) added leave-one-out (LOO) classifications and probabilities to the resubstitution classifications and probabilities.

We demonstrate a few other options available with estat list. We can limit which observations are displayed with if and in qualifiers and can add the display of the discriminating variables with the varlist option. Here we limit the display to those observations that have income greater than \$110,000.

. estat list if income > 110, varlist

	Data		Classification		Probabilities		
Obs	income	lotsize	True	Class.	Nonowner	Owner	
2	115.5	16.8	Owner	Owner	0.4945	0.5055	
5	117.0	23.6	Owner	Owner	0.0040	0.9960	
6	140.1	19.2	Owner	Owner	0.0125	0.9875	
7	138.0	17.6	Owner	Owner	0.0519	0.9481	
8	112.8	22.4	Owner	Owner	0.0155	0.9845	
10	123.0	20.8	Owner	Owner	0.0196	0.9804	
12	111.0	20.0	Owner	Owner	0.1107	0.8893	
17	114.0	17.6	Nonowner	Owner *	0.3776	0.6224	
1	1		1		1		

* indicates misclassified observations

Starting with the command above, we specify sep(0) to suppress the separator line that, by default, displays after every 5 observations. We eliminate the observation numbers with the noobs option. With the class() option: the looclass suboption adds the LOO classification; the noclass suboption suppress the resubstitution classification; and the nostar suboption eliminates the marking of misclassified observations with asterisks. With pr(loopr nopr) we specify that LOO probabilities are to be displayed and resubstitution probabilities are to be suppressed.

	_				
Data		Classific	ation	LOO Probab	ilities
income	lotsize	True	L00 C1	Nonowner	Owner
115.5	16.8	Owner	Nonowner	0.6177	0.3823
117.0	23.6	Owner	Owner	0.0029	0.9971
140.1	19.2	Owner	Owner	0.0124	0.9876
138.0	17.6	Owner	Owner	0.0737	0.9263
112.8	22.4	Owner	Owner	0.0168	0.9832
123.0	20.8	Owner	Owner	0.0217	0.9783
111.0	20.0	Owner	Owner	0.1206	0.8794
114.0	17.6	Nonowner	Owner	0.2791	0.7209

. estat list if income > 110, sep(0) class(looclass noclass nostar)
> pr(loopr nopr) varlist noobs

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Use the if e(sample) qualifier to restrict the listing from estat list to the estimation sample. Out-of-sample listings are obtained if your selected observations are not part of the estimation sample.

As an alternative to estat list, you can use predict after discrim to obtain the classifications, posterior probabilities, or whatever else is available for prediction from the discrim subcommand that you ran, and then use list to display your predictions; see [D] list and see example 2 of [MV] discrim knn postestimation for an example.

Classification tables and error rates

Classification tables (also known as confusion matrices) and error-rate estimate tables are available with the estat classtable and estat errorrate commands after discrim.

Example 3

Example 2 of [MV] **discrim knn** introduces a head measurement dataset from Rencher and Christensen (2012, 291) with six discriminating variables and three groups. We perform a quadratic discriminant analysis (QDA) on the dataset to illustrate classification tables and error-rate estimation.

. use https://www.stata-press.com/data/r19/head
(Table 8.3. Head measurements, Rencher and Christensen (2012))
. discrim qda wdim circum fbeye eyehd earhd jaw, group(group)
Quadratic discriminant analysis
Resubstitution classification summary

Key

Number Percent				
True group	Classified High school	College	Nonplayer	Total
High school	27	1	2	30
	90.00	3.33	6.67	100.00
College	2	21	7	30
	6.67	70.00	23.33	100.00
Nonplayer	1	4	25	30
	3.33	13.33	83.33	100.00
Total	30	26	34	90
	33.33	28.89	37.78	100.00
Priors	0.3333	0.3333	0.3333	

By default, discrim displayed the resubstitution classification table. A resubstitution classification table is obtained by classifying the observations used in building the discriminant model. The resubstitution classification table is overly optimistic as an indicator of how well you might classify other observations.

This resubstitution classification table shows that from the high school group 27 observations were correctly classified, 1 observation was classified as belonging to the college group, and 2 observations were classified as belonging to the nonplayer group. The corresponding percentages were also presented: 90%, 3.33%, and 6.67%. The college and nonplayer rows are read in a similar manner. For instance, there were 7 observations from the college group that were misclassified as nonplayers. Row and column totals are presented along with the group prior probabilities. See table 9.4 of Rencher and Christensen (2012, 321) for this same classification table.

There are various ways of estimating the error rate for a classification. estat errorrate presents the overall (total) error rate and the error rate for each group. By default, it uses a count-based estimate of the error rate.

or	or rate estimated by error count				
		group High school	College	Nonplayer	Total
	Error rate	.1	.3	.166666667	.188888889
	Priors	. 333333333	. 333333333	.3333333333	

. estat errorrate

Err

This is a resubstitution count-based error-rate estimate corresponding to the classification table previously presented. Three of the 30 high school observations were misclassified—a proportion of 0.1; 9 of the 30 college observations were misclassified—a proportion of 0.3; and 5 of the 30 nonplayers were misclassified—a proportion of 0.1667. The total error rate is computed as the sum of the group error rates times their prior probabilities—here 0.1889.

An error-rate estimate based on the posterior probabilities is also available with estat errorrate.

```
. estat errorrate, pp
Error rate estimated from posterior probabilities
                    group
    Error rate
                    High school
                                      College
                                                 Nonplayer
                                                                     Total
                                   .337824355
      Stratified
                      .08308968
                                                   .2030882
                                                                208000745
                                   .337824355
                                                                .208000745
    Unstratified
                      .08308968
                                                   .2030882
          Priors
                     .3333333333
                                   .3333333333
                                                 .3333333333
```

Because we did not specify otherwise, we obtained resubstitution error-rate estimates. By default both the stratified and unstratified estimates are shown. The stratified estimates give less weight to probabilities where the group sample size is large compared with the group prior probabilities; see *Methods and formulas* for details. Here the stratified and unstratified estimates are the same. This happens when the prior probabilities are proportional to the sample sizes—here we have equal prior probabilities and equal group sizes.

For this example, the count-based and posterior-probability-based estimates are similar to one another.

Leave-one-out (LOO) estimation provides a more realistic assessment of your potential classification success with observations that were not used in building the discriminant analysis model. The loo option of estat classtable and estat errorrate specify a LOO estimation.

```
. estat classtable, loo nopercents nopriors nototals
Leave-one-out classification table
```

Key Number			
True group	LOO Classified High school	College	Nonplayer
High school	26	2	2
College	3	16	11
Nonplayer	4	9	17

To demonstrate some of the available options, we specified the nopercents option to suppress the display of percentages; the nopriors option to suppress the display of the prior probabilities; and the nototals option to suppress row and column totals.

If you compare this LOO classification table with the resubstitution classification table, you will see that fewer observations appear on the diagonal (were correctly classified) in the LOO table. The LOO estimates are less biased than the resubstitution estimates.

We now examine the LOO error-rate estimates by using the loo option with the estat error command. We first produce the count-based estimates and then request the posterior-probability-based estimates. In the first case, we use the nopriors option to demonstrate that you can suppress the display of the prior probabilities. Suppressing the display does not remove their effect on the computations. In the second estat errorrate call, we specify that only the unstratified estimates be presented. (Because the prior probabilities and samples sizes match [are equal], the stratified results will be the same.)

```
. estat err, loo nopriors
Error rate estimated by leave-one-out error count
```

1

	High school	College	Nonplayer	Total
Error rate	.133333333	.466666667	.4333333333	.344444444
. estat err, loo	pp(unstratified	1)		

Error rate estimated from leave-one-out posterior probabilities

Error rate	group High school	College	Nonplayer	Total
Unstratified	.049034154	.354290969	.294376541	.232567222
Priors	. 3333333333	.3333333333	.3333333333	

Instead of displaying percentages below the counts in the classification table, we can display average posterior probabilities. The probabilities option requests the display of average posterior probabilities. We add the nopriors option to demonstrate that the prior probabilities can be suppressed from the table. The classifications are still based on the prior probabilities; they are just not displayed.

```
. estat classtable, probabilities nopriors
```

Resubstitution average-posterior-probabilities classification table

Кеу			
Number Average post	cerior probability		
True group	Classified High school	College	Nonplayer
High school	27	1	2
	0.9517	0.6180	0.5921
College	2	21	7
	0.6564	0.8108	0.5835
Nonplayer	1	4	25
	0.4973	0.5549	0.7456
Total	30	26	34
	0.9169	0.7640	0.7032

Both estat classtable and estat errorrate allow if and in qualifiers so that you can select the observations to be included in the computations and displayed. If you want to limit the table to the estimation sample, use if e(sample). You can also do out-of-sample classification tables and error-rate estimation by selecting observations that were not part of the estimation sample.

4

Technical note

As noted by Huberty (1994, 92), the posterior-probability-based error-rate estimates for the individual groups may be negative. This may happen when there is a discrepancy between group prior probabilities and relative sample size.

Continuing with our last example, if we use prior probabilities of 0.2, 0.1, and 0.7 for the high school, college, and nonplayer groups, the nonplayer stratified error-rate estimate and the high school group unstratified error-rate estimate are negative.

```
. estat error, pp priors(.2, .1, .7)
Error rate estimated from posterior probabilities
```

Error rate	group High school	College	Nonplayer	Total
Stratified	.19121145	.737812235	001699715	.110833713
Unstratified	36619243	.126040785	.29616143	.146678593
Priors	.2	.1	.7	

More examples of the use of estat list, estat classtable, and estat errorrate can be found in the other discrim-related manual entries.

Stored results

estat classtable stores the following in r():

Matrices

r(counts)	group counts
r(percents)	percentages for each group (unless nopercents specified)
r(avgpostprob)	average posterior probabilities classified into each group (probabilities only)

estat errorrate stores the following in r():

Matrices

r(grouppriors)	row vector of group prior probabilities used in the calculations
r(erate_count)	matrix of error rates estimated from error counts (count only)
r(erate_strat)	matrix of stratified error rates estimated from posterior probabilities (pp only)
r(erate_unstrat)	matrix of unstratified error rates estimated from posterior probabilities (pp only)

Matrices	
r(count)	group counts
r(mean)	means (mean only)
r(median)	medians (median only)
r(sd)	standard deviations (sd only)
r(cv)	coefficients of variation (cv only)
r(semean)	standard errors of the means (semean only)
r(min)	minimums (min only)
r(max)	maximums (max only)

estat grsummarize stores the following in r():

Methods and formulas

Let C denote the classification table (also known as the confusion matrix), with rows corresponding to the true groups and columns corresponding to the assigned groups. Let C_{ij} denote the element from row i and column j of C. C_{ij} represents the number of observations from group i assigned to group j. n_i is the number of observations from group i and $N = \sum_{i=1}^{g} n_i$ is the total sample size. $\mathcal{N}_i = \sum_{j=1}^{g} C_{ij}$ is the number of observations from group i that were classified into one of the g groups. If some observations from group i are unclassified (because of ties), $\mathcal{N}_i \neq n_i$ and $\mathcal{N} \neq N$ (where $\mathcal{N} = \sum \mathcal{N}_i$). Let q_i be the prior probability of group i.

estat classtable displays C, with options controlling the display of cell percentages by row, average posterior probabilities, prior probabilities, row totals, and column totals.

McLachlan (2004, chap. 10) devotes a chapter to classification error-rate estimation. The estat errorrate command provides several popular error-rate estimates. Smith (1947) introduced the count-based apparent error-rate estimate. The count-based error-rate estimate for group i is

$$\widehat{E}_i^{(C)} = 1 - C_{ii} / \mathcal{N}_i$$

The overall (total) count-based error-rate estimate is

$$\widehat{E}^{(C)} = \sum_{i=1}^g q_i \widehat{E}_i^{(C)}$$

In general, $\widehat{E}^{(C)} \neq 1 - \sum_{i=1}^{g} C_{ii} / \mathcal{N}$, though some sources, Rencher and Christensen (2012, 319), appear to report this latter quantity.

If C is based on the same data used in the estimation of the discriminant analysis model, the error rates are called apparent error rates. Leave-one-out (LOO) error rates are obtained if C is based on a leave-one-out analysis where each observation to be classified is classified based on the discriminant model built excluding that observation; see Lachenbruch and Mickey (1968) and McLachlan (2004, 342).

Error rates can also be estimated from the posterior probabilities. Huberty (1994, 90–91) discusses hit rates (one minus the error rates) based on posterior probabilities and shows two versions of the posterior-probability based estimate—stratified and unstratified.

Let \mathcal{P}_{ji} be the sum of the posterior probabilities for all observations from group j assigned to group i. The posterior-probability-based unstratified error-rate estimate for group i is

$$\widehat{E}_i^{(Pu)} = 1 - \frac{1}{\mathcal{N}q_i}\sum_{j=1}^g \mathcal{P}_{ji}$$

The overall (total) posterior-probability-based unstratified error-rate estimate is

$$\widehat{E}^{(Pu)} = \sum_{i=1}^{g} q_i \widehat{E}_i^{(Pu)}$$

The posterior-probability-based stratified error-rate estimate for group i is

$$\widehat{E}_i^{(Ps)} = 1 - \frac{1}{q_i} \sum_{j=1}^g \frac{q_j}{\mathcal{N}_j} \mathcal{P}_{ji}$$

The overall (total) posterior-probability-based stratified error-rate estimate is

$$\widehat{E}^{(Ps)} = \sum_{i=1}^{g} q_i \widehat{E}_i^{(Ps)}$$

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Also see

- [MV] discrim Discriminant analysis
- [MV] discrim knn postestimation Postestimation tools for discrim knn
- [MV] discrim Ida postestimation Postestimation tools for discrim Ida
- [MV] discrim logistic postestimation Postestimation tools for discrim logistic
- [MV] discrim qda postestimation Postestimation tools for discrim qda
- [MV] candisc Canonical linear discriminant analysis

[U] 20 Estimation and postestimation commands

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