#### meta esize — Compute effect sizes and declare meta-analysis data

Description	Quick start
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# Description

meta esize computes effect sizes from study summary data and uses the results to declare the data in memory to be meta data, informing Stata of key variables and their roles in a meta-analysis. It computes various effect sizes and their respective standard errors for two-group comparisons of continuous and binary outcomes and for estimating a single proportion of a binary outcome or a correlation between two variables. It then uses the computed effect sizes and standard errors to declare the data in memory to be meta data. If you do not have the summary data from individual studies and, instead, you have precalculated effect sizes, you can use meta set to declare your meta-analysis data. You must use meta esize or meta set to perform univariate meta-analysis using the meta command; see [META] meta data.

If you need to update some of the meta settings after the data declaration, see [META] meta update. To display current meta settings, use meta query; see [META] meta update.

# Quick start

Compute Hedges's g standardized mean differences and their standard errors from variables nt (sample size in treatment group), meant (mean of treatment group), sdt (standard deviation in treatment group), and their counterparts in the control group: nc, meanc, and sdc

meta esize nt meant sdt nc meanc sdc

Same as above, but compute Cohen's d instead of the default Hedges's q, and use the DerSimonian–Laird estimation method instead of the default REML method

meta esize nt meant sdt nc meanc sdc, esize(cohend) random(dlaird)

Compute log odds-ratios and their standard errors from variables nst (number of successes in treatment group), nft (number of failures in treatment group), and their respective counterparts in control group: nsc and nfc

meta esize nst nft nsc nfc

Same as above, but compute the log risk-ratios instead of the default log odds-ratios

meta esize nst nft nsc nfc, esize(lnrratio)

Same as above, but request a common-effect meta-analysis

meta esize nst nft nsc nfc, esize(lnrratio) common

Compute transformed proportions using the default Freeman-Tukey double-arcsine transformation and their standard errors from variables ns (number of successes) and n (study sample size)

meta esize ns n

Same as above, but compute the logit-transformed proportions instead of the default Freeman–Tukey-transformed proportions

meta esize ns n, esize(logitprop)

Compute Fisher's z-transformed correlations and their standard errors from variables r (correlation) and n (study sample size)

meta esize r n, fisherz

Same as above, but use the untransformed (raw) correlations and compute their standard errors meta esize r n, correlation

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Statistics > Meta-analysis

# **Syntax**

Compute and declare effect sizes for two-group comparison of continuous outcomes

meta esize n1 mean1 sd1 n2 mean2 sd2 [if] [in] [, options\_continuous options]

Compute and declare effect sizes for two-group comparison of binary outcomes

meta esize n11 n12 n21 n22 [if] [in] [, options\_binary options]

Compute and declare effect sizes for estimating a single proportion (prevalence)

meta <u>es</u>ize ns n [if] [in] [, options\_proportion options]

Compute and declare effect sizes for estimating a correlation

meta <u>es</u>ize *r* n [*if*] [*in*], { fisherz | <u>corr</u>elation } [ *options\_correlation options* ]

- Variables *n1*, *mean1*, and *sd1* contain sample sizes, means, and standard deviations from individual studies for group 1 (treatment), and variables *n2*, *mean2*, and *sd2* contain the respective summaries for group 2 (control).
- Variables *n11* and *n12* contain numbers of successes and numbers of failures from individual studies for group 1 (treatment), and variables *n21* and *n22* contain the respective numbers for group 2 (control). A single observation defined by variables *n11*, *n12*, *n21*, and *n22* represents a 2 × 2 table from an individual study. Therefore, variables *n11*, *n12*, *n21*, and *n22* represent a sample of 2 × 2 tables from all studies. We will thus refer to observations on these variables as 2 × 2 tables and to values of these variables as cells.
- Variables *ns* and *n* contain number of successes and sample sizes from individual studies. Here, the values of the variable *ns* (number of successes) and the values of an implicit "variable" n ns (number of failures) are referred to as cells.

Variables r and n contain correlations and sample sizes from individual studies.

options_continuous	Description
Main <u>es</u> ize( <i>esspeccnt</i> )	specify effect size for two-group comparison of continuous outcomes to be used in the meta-analysis
Model random[( <i>remethod</i> )] common fixed	random-effects meta-analysis; default is random(reml) common-effect meta-analysis; implies inverse-variance method fixed-effects meta-analysis; implies inverse-variance method

options_binary	Description
Main	
<u>es</u> ize( <i>estypebin</i> )	specify effect size for two-group comparison of binary outcomes to be used in the meta-analysis
Model	
<pre>random[ (remethod) ]</pre>	random-effects meta-analysis; default is random(reml)
common[( <i>cefemethod</i> )]	common-effect meta-analysis
<pre>fixed[(cefemethod)]</pre>	fixed-effects meta-analysis
Options	
zerocells( <i>zcspec</i> )	adjust for zero cells during computation; default is to add 0.5 to all cells of those $2 \times 2$ tables that contain zero cells
options_proportion	Description
Main	
<u>es</u> ize( <i>estypeprop</i> )	specify effect size for estimating a single proportion to be used in the meta-analysis
Model	
random[( <i>remethod</i> )]	random-effects meta-analysis; default is random(reml)
common	common-effect meta-analysis; implies inverse-variance method
fixed	fixed-effects meta-analysis; implies inverse-variance method
Options	
<pre>zerocells(zcspec)</pre>	adjust for zero cells during computation; default is to add 0.5 to all cells of studies with zero successes or failures
options_correlation	Description
Main	
$^{+*}$ fisherz	Fisher's z-transformed correlation
+* <u>corr</u> elation	untransformed (raw) correlation
<sup>+</sup> <u>es</u> ize( <i>estypecorr</i> )	synonym for fisherz or correlation
Model	
random[( <i>remethod</i> )]	random-effects meta-analysis; default is random(reml)
common	common-effect meta-analysis; implies inverse-variance method
fixed	fixed-effects meta-analysis; implies inverse-variance method

<sup>+</sup>These features are part of StataNow.

\* Either fisherz or correlation is required.

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options	Description
Options	
<pre>studylabel(varname)</pre>	variable to be used to label studies in all meta-analysis output
<u>eslab</u> el( <i>string</i> )	effect-size label to be used in all meta-analysis output; default is eslabel(Effect size)
<u>l</u> evel(#)	confidence level for all subsequent meta-analysis commands
[no]metashow	display or suppress meta settings with other meta commands

## The syntax of esspeccnt is

# estypecnt [ , esopts ]

estypecnt	Description	
hedgesg	Hedges's $g$ standardized mean difference; the default	
<u>coh</u> end	Cohen's d standardized mean difference	
glassdelta2	Glass's $\Delta$ mean difference standardized by group 2 (control)	
	standard deviation; more common than glassdelta1	
glassdelta1	Glass's $\Delta$ mean difference standardized by group 1 (treatment) standard deviation	
<u>md</u> iff	(unstandardized) mean difference	
estypebin	Description	
<u>lnor</u> atio	log odds-ratio; the default	
<u>lnrr</u> atio	log risk-ratio (also known as log rate-ratio and log relative-risk)	
<u>rd</u> iff	risk difference	
lnorpeto	Peto's log odds-ratio	
estypeprop	Description	
ftukeyprop	Freeman–Tukey-transformed proportion; the default	
logitprop	logit-transformed proportion	
proportion	untransformed (raw) proportion	
estypecorr	Description	
fisherz	Fisher's z-transformed correlation	
<u>corr</u> elation	untransformed (raw) correlation	
remethod	Description	
reml	restricted maximum likelihood; the default	
mle	maximum likelihood	
<u>eb</u> ayes	empirical Bayes	
<u>dl</u> aird	DerSimonian–Laird	
sjonkman	Sidik–Jonkman	
hedges	Hedges	
<u>hs</u> chmidt	Hunter-Schmidt	

cefemethod	Description
mhaenszel	Mantel-Haenszel
<u>invvar</u> iance	inverse variance
<u>iv</u> ariance	synonym for invvariance

# Options

Main

esize(*esspec*) specifies the effect size to be used in the meta-analysis. For a two-group comparison of continuous outcomes, *esspec* is *estypecnt* [, *esopts*]. For binary outcomes, *esspec* is *estypebin* for a two-group comparison or *estypeprop* for estimating a single proportion (prevalence). For correlation data, *esspec* is *estypecorr*.

For a two-group comparison of continuous outcomes, *estypecnt* is one of the following: hedgesg, cohend, glassdelta2, glassdelta1, or mdiff. Below, we describe each type with its specific options, *esopts*.

- hedgesg [, exact holkinse] computes the effect size as the Hedges's g (1981) standardized mean difference. This is the default. For consistency with meta-analysis literature, hedgesg uses an approximation to compute g rather than the exact computation (see *Methods and formulas*), as provided by esize's option hedgesg. You can use the exact suboption to match the results from esize (see [R] esize).
- cohend [ , holkinse ] computes the effect size as the Cohen's d (1969, 1988) standardized mean difference.
- glassdelta2 computes the effect size as the Glass's  $\Delta$  standardized mean difference, where the standardization uses the standard deviation of the group 2 (control group). glassdelta2 is more common in practice than glassdelta1.
- glassdelta1 computes the effect size as the Glass's  $\Delta$  standardized mean difference, where the standardization uses the standard deviation of the group 1 (treatment group). glassdelta2 is more common in practice than glassdelta1.
- mdiff [, unequal] computes the effect size as the unstandardized or raw mean difference.

esopts are exact, holkinse, and unequal.

- exact specifies that the exact computation be used for the bias-correction factor in Hedges's g instead of an approximation used by default.
- holkinse specifies that the standard error of Hedges's g and Cohen's d be computed as described in Hedges and Olkin (1985). This is another approximation to the standard error of these effect sizes sometimes used in practice.
- unequal specifies that the computation of the standard error of the mean difference (esize(mdiff)) assume unequal group variances.

For a two-group comparison of binary outcomes, *estypebin* is one of the following: lnoratio, lnrratio, rdiff, or lnorpeto.

- Inoratio specifies that the effect size be the log odds-ratio. This is the default.
- Inrratio specifies that the effect size be the log risk-ratio, also known as a log relative-risk and a log risk-rate.

rdiff specifies that the effect size be the risk difference.

Inorpeto specifies that the effect size be the log odds-ratio as defined by Peto et al. (1977). This effect size is preferable with rare events.

For estimating a proportion from one-sample binary or prevalence data, *estypeprop* is one of the following: ftukeyprop, logitprop, or proportion.

- ftukeyprop specifies that the effect size be the Freeman–Tukey-transformed proportion (Freeman and Tukey 1950). This is the default. The Freeman–Tukey transformation is a variance-stabilizing transformation and is preferable when the estimated proportions are close to 0 or 1. This effect size does not require a zero-cell adjustment (continuity correction) for studies with zero successes or failures.
- logitprop specifies that the effect size be the logit-transformed proportion. When a study proportion is close to 0 or 1, the estimated variance of this effect size is very large, and thus the study is assigned an artificially small weight in the meta-analysis.
- proportion specifies that the effect size be the untransformed (raw) proportion. When a study proportion is close to 0 or 1, its estimated variance is very small, and thus the study is assigned an artificially large weight in the meta-analysis. Moreover, the study confidence limits may fall outside the [0, 1] range.

For correlation data, *estypecorr* is one of fisherz or correlation.

fisherz specifies that the effect size be the Fisher's z-transformed correlation.

correlation specifies that the effect size be the untransformed (raw) correlation.

For effect sizes in the log metric such as log odds-ratios, the results by default are displayed in the log metric. You can use *eform\_option* of meta summarize to obtain exponentiated results such as odds ratios. For effect sizes ftukeyprop and logitprop, the results by default are displayed in the respective Freeman-Tukey and logit metrics. You can use options transform() and proportion of meta summarize to report results as proportions. For effect size fisherz, the results are displayed as Fisher's z-transformed correlations. You can use options transform() and correlation of meta summarize to report results as correlations.

Model

Options random(), common(), and fixed() declare the meta-analysis model globally throughout the entire meta-analysis; see *Declaring a meta-analysis model* in [META] **meta data**. In other words, once you set your meta-analysis model using meta esize, all subsequent meta commands will assume that same model. You can update the declared model by using meta update or change it temporarily by specifying the corresponding option with the meta commands. Options random(), common(), and fixed() may not be combined. If these options are omitted, random(reml) is assumed; see *Default meta-analysis model and method* in [META] **meta data**. Also see *Meta-analysis models* in [META] **Intro**.

- random and random(*remethod*) specify that a random-effects model be assumed for meta-analysis; see *Random-effects model* in [META] Intro.
  - remethod specifies the type of estimator for the between-study variance  $\tau^2$ . remethod is one of reml, mle, ebayes, dlaird, sjonkman, hedges, or hschmidt. random is a synonym for random(reml). Below, we provide a short description for each method based on Veroniki et al. (2016). Also see Declaring a meta-analysis estimation method in [META] meta data.

- rem1, the default, specifies that the REML method (Raudenbush 2009) be used to estimate  $\tau^2$ . This method produces an unbiased, nonnegative estimate of the between-study variance and is commonly used in practice. Method rem1 requires iteration.
- mle specifies that the ML method (Hardy and Thompson 1996) be used to estimate  $\tau^2$ . It produces a nonnegative estimate of the between-study variance. With a few studies or small studies, this method may produce biased estimates. With many studies, the ML method is more efficient than the REML method. Method mle requires iteration.
- ebayes specifies that the empirical Bayes estimator (Berkey et al. 1995), also known as the Paule-Mandel estimator (Paule and Mandel 1982), be used to estimate  $\tau^2$ . From simulations, this method, in general, tends to be less biased than other random-effects methods, but it is also less efficient than reml or dlaird. Method ebayes produces a nonnegative estimate of  $\tau^2$  and requires iteration.
- dlaird specifies that the DerSimonian–Laird method (DerSimonian and Laird 1986) be used to estimate  $\tau^2$ . This method, historically, is one of the most popular estimation methods because it does not make any assumptions about the distribution of random effects and does not require iteration. But it may underestimate the true between-study variance, especially when the variability is large and the number of studies is small. This method may produce a negative value of  $\tau^2$  and is thus truncated at zero in that case.
- sjonkman specifies that the Sidik–Jonkman method (Sidik and Jonkman 2005) be used to estimate  $\tau^2$ . This method always produces a nonnegative estimate of the between-study variance and thus does not need truncating at 0, unlike the other noniterative methods. Method sjonkman does not require iteration.
- hedges specifies that the Hedges method (Hedges 1983) be used to estimate  $\tau^2$ . When the sampling variances of effect-size estimates can be estimated without bias, this estimator is exactly unbiased (before truncation), but it is not widely used in practice (Veroniki et al. 2016). Method hedges does not require iteration.
- hschmidt specifies that the Hunter–Schmidt method (Schmidt and Hunter 2015) be used to estimate  $\tau^2$ . Although this estimator achieves a lower MSE than other methods, except ML, it is known to be negatively biased. Method hschmidt does not require iteration.
- common specifies that a common-effect model be assumed for meta-analysis; see Common-effect ("fixedeffect") model in [META] Intro. It uses the inverse-variance estimation method; see Meta-analysis estimation methods in [META] Intro. Also see the discussion in [META] meta data about commoneffect versus fixed-effects models.
- common and common(cefemethod) specify that a common-effect model be assumed for meta-analysis; see Common-effect ("fixed-effect") model in [META] Intro. Also see the discussion in [META] meta data about common-effect versus fixed-effects models.
  - common implies common(mhaenszel) for effect sizes lnoratio, lnrratio, and rdiff and common(invvariance) for all other effect sizes.
  - *cefemethod* is one of mhaenszel or invvariance (synonym ivariance). Below, we provide a short description for each method. Also see *Declaring a meta-analysis estimation method* in [META] **meta data**.

mhaenszel is available only for a two-group comparison of binary outcomes. It specifies a metaanalysis using the Mantel-Haenszel method to estimate the overall effect size. This method is the default for effect sizes lnoratio, lnrratio, and rdiff but is not available for effect size lnorpeto.

invvariance specifies a meta-analysis using the inverse-variance method to estimate the overall effect size. This method is available for all types of analyses and effect sizes. It is the default for a two-group comparison of continuous outcomes, for a two-group comparison of binary outcomes using effect size lnorpeto, for correlation data, and for estimating a single proportion (or prevalence).

ivariance is a synonym for invvariance.

fixed and fixed(*cefemethod*) specify that a fixed-effects model be assumed for meta-analysis; see *Fixed-effects model* in [META] **Intro**. Also see the discussion in [META] **meta data** about fixed-effects versus common-effect models.

fixed implies fixed(mhaenszel) for effect sizes lnoratio, lnrratio, and rdiff and fixed(invvariance) for all other effect sizes.

cefemethod is one of mhaenszel or invvariance (synonym ivariance); see descriptions above.

fixed specifies that a fixed-effects model be assumed for meta-analysis; see *Fixed-effects model* in [META] **Intro**. It uses the inverse-variance estimation method; see *Meta-analysis estimation methods* in [META] **Intro**. Also see the discussion in [META] **meta data** about fixed-effects versus common-effect models.

Options

- zerocells(zcspec) is for use with binary outcomes when the effect size is either lnoratio or lnrratio for the two-sample case or either logitprop or proportion for the one-sample case. It specifies the adjustment to be used for the cells in the presence of zero cells. The cells are the values of variables n11, n12, n21, and n22 for the two-sample case and the number of successes and the number of failures for the one-sample case. The adjustment is applied during computation—the original data are not modified. The default is zerocells(0.5, only0); it adds 0.5 to all cells of studies with at least one zero cell. To request no adjustment, specify zerocells(none). More generally, the syntax of zcspec is
  - #[, zcadj]

where # is the adjustment value, also known as the continuity-correction value in the meta-analysis literature, and *zcadj* is only0 or allif0.

- only0 specifies that # be added to all cells of only those studies with at least one zero cell. For the two-sample case, during computation, # is added to each observation defined by variables n11, n12, n21, and n22 if that observation contains a value of zero in any of those variables. For the one-sample case, # is added to all values (cells) corresponding to zero successes and to zero failures.
- allif0 specifies that # be added to all cells of all studies but only if there is at least one study with a zero cell. For the two-sample case, during computation, # is added to all values of variables n11, n12, n21, and n22 but only if there is a zero value in one of the four variables. For the one-sample case, # is added to all cells (number of successes and number of failures) if at least one study contains zero successes or zero failures.

For the effect size lnoratio, *zcspec* may also be tacc, which implements the treatment-arm continuity correction of Sweeting, Sutton, and Lambert (2004). This method estimates the group-specific adjustment values from the data to minimize the bias of the overall odds-ratio estimator in the presence of zero cells. This method is recommended when the groups are unbalanced.

- tudylabel(varname) specifies a string variable containing labels for the individual studies to be used in all applicable meta-analysis output. The default study labels are Study 1, Study 2, ..., Study K, where K is the total number of studies in the meta-analysis.
- eslabel (*string*) specifies that *string* be used as the effect-size label in all relevant meta-analysis output. The default label is Effect size.
- level(#) specifies the confidence level, as a percentage, for confidence intervals. It will be used by all subsequent meta-analysis commands when computing confidence intervals. The default is level(95) or as set by set level; see [R] level. After the declaration, you can specify level() with meta update to update the confidence level to be used throughout the rest of the meta-analysis session. You can also specify level() directly with the meta commands to modify the confidence level, temporarily, during the execution of the command.
- metashow and nometashow display or suppress the meta setting information in the output of other meta commands. By default, this information is displayed at the top of their output. You can also specify nometashow with meta update to suppress the meta setting output for the entire meta-analysis session after the declaration.

## **Remarks and examples**

Remarks are presented under the following headings:

Meta-analysis for two-group comparison of binary outcomes Meta-analysis for two-group comparison of continuous outcomes Meta-analysis for estimating a single proportion Meta-analysis for correlation data

meta esize computes various effect sizes, their standard errors, and CIs for continuous and binary outcomes from the summary data provided for each study. It then declares the computed effect-size data as the meta data; see [META] meta data. Different types of effect sizes may be specified in the esize() option. They depend on the type of analysis and outcome, so we describe them separately for various situations below, together with other data-specific options. Also see *Declaring meta-analysis information* in [META] meta data.

## Meta-analysis for two-group comparison of binary outcomes

Meta-analysis is often used with studies comparing two groups. The first group is commonly referred to as the experimental or treatment group. The second group is commonly referred to as the control group.

For two-sample binary data, each study typically reports cell counts from the following  $2 \times 2$  table.

group	success	failure	size
treatment	$n_{11}$	$n_{12}$	$n_1 = n_{11} + n_{12}$
control	$n_{21}$	$n_{22}$	$n_2 = n_{21} + n_{22}$

The cells of the table are composed of the numbers of "successes" and "failures" within each of the comparison groups. If a subject experiences an event of interest, it is a success; otherwise, it is a failure. Thus, the summary data for a two-group comparison of binary outcomes include the above  $2 \times 2$  table for each study.

In this case, meta esize requires that four variables be specified containing the numbers of successes and failures in the treatment and control groups.

The goal of each study is to compare the probabilities of a success between the two groups. Various effect-size measures can be used for the comparison. For two-sample binary data, meta esize provides the following effect sizes: log odds-ratios (including Peto's log odds-ratios), the default; log risk-ratios; and risk differences. These are specified, respectively, as lnoratio, lnorpeto, lnrratio, and rdiff in the esize() option.

As described in *Declaring a meta-analysis model* in [META] **meta data**, you can choose between a random-effects, a fixed-effects, or a common-effect model. You can also choose from a number of estimation methods that are specific to the chosen model. For fixed-effects and common-effect models, in addition to the inverse-variance method, the Mantel-Haenszel method is available (and is the default) with effect sizes lnoratio, lnrratio, and rdiff; see *Declaring a meta-analysis estimation method* in [META] **meta data** and *Meta-analysis estimation methods* in [META] **Intro** for details.

Zero cell counts are known to create computational difficulties for odds ratios and risk ratios. A common solution is to add a small number, say, 0.5, to all cells of tables containing zero cells. This and other zero-cells adjustments are available in the zerocells() option.

Let's now look at several examples. Consider the following fictional meta-analysis dataset:

. use https: (Fictional d		*		metaesbin	
. describe					
Contains dat	a from http	ps://www.st	ata-press.	com/data/r19/metaesbin.dta	
Observation	s:	4		Fictional data for binary	
				outcomes	
Variable	s:	5 23 Apr 2024 12:14			
Variable	Storage	Display	Value		
name	type	format	label	Variable label	
study	str7	%9s		Study label	
tdead	byte	%9.0g Deaths in treatment gr		Deaths in treatment group	
tsurv	int	%9.0g		Survivors in treatment group	
cdead	byte	%9.0g Deaths in control group		Deaths in control group	
csurv	csurv int %9.0g Survivors in control group				

Sorted by:

We will use this dataset to demonstrate how to compute effect sizes, specify different meta-analysis models, and adjust for zero cells with two-sample binary data.

#### Example 1: A simple case

When working with meta-analysis data that do not have precomputed effect sizes, we can choose to compute effect sizes in a few different ways such as odds ratios and risk ratios. Using the simplest syntactical specification, we can compute the effect sizes, their standard errors, and the corresponding confidence intervals by specifying the number of successes and failures for one group, as well as the successes and failures for the second group, in that order.

```
. meta esize tdead tsurv cdead csurv
Meta-analysis setting information
 Study information
   No. of studies: 4
       Study label: Generic
        Study size: _meta_studysize
      Summary data: tdead tsury cdead csury
       Effect size
              Type: lnoratio
            Label: Log odds-ratio
          Variable: meta es
  Zero-cells adj.: 0.5, only0
         Precision
         Std. err.: meta se
                CI: [ meta cil, meta ciu]
          CI level: 95%
 Model and method
            Model: Random effects
           Method: REML
```

The output indicates that there are 4 studies in the meta-analysis and, by default, a random-effects metaanalysis is to be assumed, where the heterogeneity parameter  $\tau^2$  is estimated via the REML method. The default computed effect size is the log odds-ratio. meta esize creates multiple system variables (see *System variables* in [META] meta data) that store the effect-size values, their standard errors, and the upper and lower limits of the CIs for the effect sizes.

We can now use, for example, meta summarize to list the individual log odds-ratios and the overall log odds-ratio, which is denoted as theta.

```
. meta summarize
  Effect-size label: Log odds-ratio
        Effect size: _meta_es
          Std. err.: _meta_se
Meta-analysis summary
                                           Number of studies =
                                                                      4
Random-effects model
                                           Heterogeneity:
Method: REML
                                                        tau2 = 1.4417
                                                      I2 (%) =
                                                                 69.33
                                                          H2 =
                                                                  3.26
            Study
                    Log odds-ratio
                                       [95% conf. interval] % weight
          Study 1
                             -0.600
                                         -2.079
                                                       0.879
                                                                 27.80
          Study 2
                              0.351
                                         -2.510
                                                       3.212
                                                                  15.65
                                         -0.031
          Study 3
                              0.778
                                                       1.586
                                                                 34.69
          Study 4
                             -2.567
                                         -4.638
                                                      -0.495
                                                                 21.85
            theta
                             -0.403
                                         -1.869
                                                       1.063
Test of theta = 0: z = -0.54
                                                   Prob > |z| = 0.5899
Test of homogeneity: Q = chi2(3) = 9.93
                                                    Prob > Q = 0.0192
```

#### See [META] meta summarize for details.

If we have a variable that stores the labels for each study, perhaps noting the study authors or journal, we can specify it in the studylabel() option with meta esize. Because we do not have such a variable in this dataset, each study is denoted generically by Study #. See example 4 in [META] meta set for an example of how to specify the study label and effect-size label.

### Example 2: Specify the effect size

The default is to compute the log odds-ratio for the effect size. To specify another metric, we can use the esize() option. For example, below we use the risk ratio (on the log scale) as our effect size by specifying esize(lnrratio):

```
. meta esize tdead tsurv cdead csurv, esize(lnrratio)
Meta-analysis setting information
Study information
   No. of studies: 4
      Study label: Generic
        Study size: _meta_studysize
      Summary data: tdead tsurv cdead csurv
       Effect size
              Type: lnrratio
             Label: Log risk-ratio
          Variable: meta es
  Zero-cells adj.: 0.5, only0
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
         CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

#### Example 3: Sparse data and adjustments for zero cells

Note that when we list the data, one of the studies has zero deaths.

. list tdead tsurv cdead csurv

	tdead	tsurv	cdead	csurv
1.	2	116	17	541
2.	0	15	15	682
з.	8	61	37	614
4.	1	421	9	291

By default, meta esize adds a constant value of 0.5 (that is, option zerocells(0.5, only0) is assumed) to each cell of a study that has a zero cell; see Zero-cells adj.: in the output of meta set in example 1. We can modify this adjustment by specifying a different constant factor. For example, we might add 0.003 to each zero cell:

```
. meta esize tdead tsurv cdead csurv, zerocells(.003)
Meta-analysis setting information
 Study information
   No. of studies: 4
       Study label: Generic
        Study size: _meta_studysize
      Summary data: tdead tsurv cdead csurv
       Effect size
              Type: lnoratio
            Label: Log odds-ratio
          Variable: meta es
  Zero-cells adj.: .003, only0
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
         CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

Or we may instead choose a different type of continuity correction, for example, the treatment-arm continuity correction (TACC), which we specify as zerocells(tacc):

```
. meta esize tdead tsurv cdead csurv, zerocells(tacc)
Meta-analysis setting information
 Study information
   No. of studies: 4
      Study label: Generic
       Study size: _meta_studysize
      Summary data: tdead tsurv cdead csurv
      Effect size
              Type: lnoratio
             Label: Log odds-ratio
          Variable: _meta_es
  Zero-cells adj.: tacc
         Precision
         Std. err.: _meta_se
                CI: [ meta cil, meta ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

Note that this option can be specified only when using the log odds-ratio as the effect size.

### Example 4: Specify the meta-analysis model

In the examples above, we have been using the default random-effects model, but we could specify a different model. For example, we can use a common-effect model using the Mantel–Haenszel method to estimate the overall effect size:

```
. meta esize tdead tsurv cdead csurv, common(mhaenszel)
Meta-analysis setting information
 Study information
   No. of studies: 4
      Study label: Generic
       Study size: _meta_studysize
      Summary data: tdead tsurv cdead csurv
       Effect size
              Type: lnoratio
             Label: Log odds-ratio
         Variable: meta es
  Zero-cells adj.: 0.5, only0
         Precision
         Std. err.: _meta_se
                CI: [ meta cil, meta ciu]
         CI level: 95%
 Model and method
            Model: Common effect
           Method: Mantel-Haenszel
```

In the above, we could have specified simply common because the Mantel-Haenszel method is the default for a common-effect model with log odds-ratios.

4

#### Meta-analysis for two-group comparison of continuous outcomes

We can also use meta-analysis to compare two groups for continuous outcomes. As before, the first group is commonly referred to as the experimental or treatment group, and the second group is commonly referred to as the control group.

For a two-group comparison of continuous outcomes, each study often reports the numbers of observations, means, and standard deviations in the two groups. Various effect sizes are then computed from these summary data for each study. Thus, to compute effect sizes for two-sample continuous data, meta esize requires that six variables be specified containing the numbers of observations, means, and standard deviations of the treatment and control groups. The supported effect sizes are the raw mean difference, esize(mdiff), and standardized mean differences: Hedges's g, esize(hedgesg) (the default); Cohen's d, esize(cohend); and Glass's  $\Delta$ s, esize(glassdelta2) and esize(glassdelta1); see Methods and formulas for their definitions.

As described in *Declaring a meta-analysis model* in [META] **meta data**, you can choose between a random-effects, a fixed-effects, and a common-effect model. You can also choose from several estimation methods for random-effects models. Fixed-effects and common-effect models assume the inverse-variance estimation method. Also see *Declaring a meta-analysis estimation method* in [META] **meta data** and *Meta-analysis estimation methods* in [META] **Intro** for details.

Let's now demonstrate several usages of meta esize for a two-group comparison of continuous outcomes. Consider the following fictional meta-analysis dataset:

```
. use https://www.stata-press.com/data/r19/metaescnt, clear
(Fictional summary data for continuous outcomes)
. describe
Contains data from https://www.stata-press.com/data/r19/metaescnt.dta
 Observations:
                           10
                                               Fictional summary data for
                                                 continuous outcomes
    Variables:
                            6
                                               19 Apr 2024 14:00
Variable
              Storage
                        Display
                                    Value
    name
                         format
                                    label
                                               Variable label
                 type
                         %9.0g
n1
                byte
                                               Study sizes of group 1
m1
                float
                         %9.0g
                                               Means of group 1
sd1
                float
                         %9.0g
                                               Std. dev. of group 1
n2
                byte
                         %9.0g
                                               Study sizes of group 2
m2
                                               Means of group 2
                float
                         %9.0g
sd2
                float
                                               Std. dev. of group 2
                         %9.0g
```

Sorted by:

We will use this dataset to demonstrate different usages of the meta esize command with continuousoutcomes meta-analysis data.

#### Example 5: The assumed model

In the simplest specification, meta esize requires that we specify the sample sizes, means, and standard deviations for each group in the meta-analysis.

```
. meta esize n1 m1 sd1 n2 m2 sd2
Meta-analysis setting information
 Study information
   No. of studies: 10
       Study label: Generic
       Study size: meta studysize
      Summary data: n1 m1 sd1 n2 m2 sd2
       Effect size
              Type: hedgesg
             Label: Hedges's g
          Variable: _meta_es
  Bias correction: Approximate
         Precision
         Std. err.: _meta_se
   Std. err. adj.: None
                CI: [ meta cil, meta ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

We see from the output that the Hedges's g standardized mean difference is used for the effect size, and, as for binary outcomes, a random-effects REML model is assumed. See *Meta settings with meta esize* in [META] **meta data** for a detailed description of all settings for this dataset.

#### Example 6: Selecting an effect size

If we do not feel the need to standardize the mean differences, we could instead use the raw mean difference as the effect size by specifying esize(mdiff).

```
. meta esize n1 m1 sd1 n2 m2 sd2, esize(mdiff)
Meta-analysis setting information
 Study information
   No. of studies: 10
      Study label: Generic
        Study size: meta studysize
      Summary data: n1 m1 sd1 n2 m2 sd2
       Effect size
              Type: mdiff
             Label: Mean diff.
          Variable: _meta_es
         Precision
         Std. err.: _meta_se
   Std. err. adj.: None
                CI: [_meta_cil, _meta_ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

```
4
```

Example 7: Specifying different meta-analysis models and methods

Rather than using the default REML estimation method, we may want to use a different method, such as the DerSimonian–Laird method. We can specify this method in the random() option.

```
. meta esize n1 m1 sd1 n2 m2 sd2, random(dlaird)
Meta-analysis setting information
 Study information
   No. of studies: 10
      Study label: Generic
       Study size: _meta_studysize
      Summary data: n1 m1 sd1 n2 m2 sd2
      Effect size
              Type: hedgesg
             Label: Hedges's g
          Variable: _meta_es
  Bias correction: Approximate
         Precision
         Std. err.: _meta_se
   Std. err. adj.: None
                CI: [ meta cil, meta ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: DerSimonian-Laird
```

Or, instead of the random-effects model, we may specify a fixed-effects model, which implies the inverse-variance estimation method.

```
. meta esize n1 m1 sd1 n2 m2 sd2, fixed
Meta-analysis setting information
Study information
   No. of studies: 10
       Study label: Generic
        Study size: _meta_studysize
      Summarv data: n1 m1 sd1 n2 m2 sd2
       Effect size
              Type: hedgesg
            Label: Hedges's g
          Variable: meta es
  Bias correction: Approximate
         Precision
         Std. err.: meta se
   Std. err. adj.: None
                CI: [_meta_cil, _meta_ciu]
         CI level: 95%
 Model and method
            Model: Fixed effects
            Method: Inverse-variance
```

1

## Meta-analysis for estimating a single proportion

Meta-analysis is also used to estimate an overall proportion (or prevalence) from one-sample binary data by pooling proportions from single-arm studies whenever this is sensible.

The data contain the number of successes (or the number of events) and the study sample size for each study. (Success is a generic term and occurs when a subject experiences an event of interest.) To estimate a proportion, meta esize provides the following effect sizes: Freeman-Tukey-transformed proportions (the default), logit-transformed proportions, and untransformed (raw) proportions. These are specified, respectively, as ftukeyprop, logitprop, and proportion in the esize() option.

As described in *Declaring a meta-analysis model* in [META] **meta data**, you can choose between a random-effects, a fixed-effects, or a common-effect model. You can also choose from several estimation methods for random-effects models. Fixed-effects and common-effect models assume the inverse-variance estimation method. Also see *Declaring a meta-analysis estimation method* in [META] **meta data** and *Meta-analysis estimation methods* in [META] **Intro** for details.

Let's now look at several examples. Consider the following fictional meta-analysis dataset:

```
. use https://www.stata-press.com/data/r19/metaesprop, clear
(Fictional summary data to estimate proportion)
. describe
Contains data from https://www.stata-press.com/data/r19/metaesprop.dta
Observations:
                                               Fictional summary data to
                            6
                                                  estimate proportion
   Variables:
                            3
                                                26 Apr 2024 11:14
Variable
              Storage
                         Display
                                    Value
   name
                         format
                                    label
                                                Variable label
                 type
                str7
                         %9s
                                                Study label
study
                         %9.0g
nsucc
                byte
                                               Number of successes
                int
                         %9.0g
                                               Study sample size
ssize
```

We will use this dataset to demonstrate different usages of the meta esize command to declare the data for meta-analysis of a single proportion.

## Example 8: The default setting

In its most basic form, meta esize requires that we specify the number of successes (nsucc) and the study sample sizes (ssize).

```
. meta esize nsucc ssize
Meta-analysis setting information
 Study information
   No. of studies: 6
       Study label: Generic
        Study size: _meta_studysize
      Summary data: nsucc ssize
       Effect size
              Type: ftukeyprop
             Label: Freeman-Tukey's p
          Variable: _meta_es
         Precision
         Std. err.: _meta_se
                CI: [ meta cil, meta ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

The output shows that the summary data are defined by variables nsucc and ssize and that, by default, the Freeman–Tukey-transformed proportion is used as the effect size. A random-effects REML model is assumed. Other settings are exactly as described in example 1.

4

## Example 9: Specify the effect size

Instead of using the default Freeman–Tukey-transformed proportion, we can choose a different effect size, such as the logit-transformed proportion, using the esize() option.

```
. meta esize nsucc ssize, esize(logitprop)
Meta-analysis setting information
 Study information
   No. of studies: 6
      Study label: Generic
       Study size: _meta_studysize
      Summary data: nsucc ssize
      Effect size
              Type: logitprop
             Label: Logit proportion
          Variable: _meta_es
  Zero-cells adj.: None; no zero cells
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

The output differs from that in example 8 in the Effect size section. It now reflects that logittransformed proportion is the effect size of choice instead of the default Freeman–Tukey-transformed proportion. There is also a new row for the zero-cells adjustment. This row did not show up in the output of example 8 because the Freeman–Tukey-transformed proportion does not need continuity correction. In our dataset, there are no zero cells, so the output in that row shows that no zero-cells adjustment was applied.

The logit-transformed proportion (and the untransformed proportion, esize(proportion)) should be avoided when there are study proportions that are close to 0 or 1.

4

## Example 10: Specify an alternative meta-analysis model and method

Instead of using the default REML estimation method, you may specify an alternative random-effects method, such as the DL method. This can be done via the random() option.

```
. meta esize nsucc ssize, random(dlaird)
Meta-analysis setting information
Study information
   No. of studies: 6
      Study label: Generic
       Study size: meta studysize
      Summary data: nsucc ssize
      Effect size
             Type: ftukeyprop
            Label: Freeman-Tukey's p
          Variable: meta es
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, meta ciu]
          CT level: 95%
 Model and method
            Model: Random effects
           Method: DerSimonian-Laird
```

Or perhaps you believe that your proportions are similar across the studies and that a common-effect model is adequate to synthesize the overall proportion. You may request a common-effect model with the inverse-variance method by specifying the common option.

```
. meta esize nsucc ssize, common
Meta-analysis setting information
Study information
   No. of studies: 6
      Study label: Generic
        Study size: _meta_studysize
      Summary data: nsucc ssize
      Effect size
             Type: ftukeyprop
            Label: Freeman-Tukey's p
          Variable: meta es
         Precision
         Std. err.: meta se
                CI: [ meta cil, meta ciu]
         CI level: 95%
 Model and method
            Model: Common effect
           Method: Inverse-variance
```

## Meta-analysis for correlation data

Meta-analysis is similarly used to estimate an overall correlation in studies examining relationships between two variables. This technique involves pooling correlations from multiple studies, each of which explores the relationship between the two specific variables. In this context, the data include the correlations and their respective sample sizes for each study. To estimate a correlation, meta esize provides two effect sizes: Fisher's z-transformed correlations and untransformed (raw) correlations. These are specified, respectively, as options fisherz and correlation with meta esize.

As described in *Declaring a meta-analysis model* in [META] **meta data**, you can choose between a random-effects, a fixed-effects, or a common-effect model. You can also choose from several estimation methods for random-effects models. Fixed-effects and common-effect models assume the inverse-variance estimation method. Also see *Declaring a meta-analysis estimation method* in [META] **meta data** and *Meta-analysis estimation methods* in [META] **Intro** for details.

Let's now look at a few examples. Consider the following fictional meta-analysis dataset:

```
. use https://www.stata-press.com/data/r19/metaescorr, clear
(Fictional summary data for meta-analysis of correlations)
. describe
Contains data from https://www.stata-press.com/data/r19/metaescorr.dta
Observations:
                            7
                                               Fictional summary data for
                                                 meta-analysis of correlations
   Variables:
                            3
                                               8 Dec 2024 09:14
                                    Value
Variable
              Storage
                        Display
                                    label
                                               Variable label
   name
                 type
                         format
studv
                str7
                        %9s
                                               Study label
n
                int
                        %9.0g
                                               Sample size of the study
                double %6.3f
rho
                                               Correlation coefficient
```

Sorted by:

We will use this dataset to demonstrate different usages of the meta esize command to declare the data for meta-analysis of correlations.

## Example 11: Specify the effect size and the default setting

When we deal with correlation data, the most rudimentary syntax of meta esize requires that we specify the correlations (rho) and the study sample sizes (n). We must also specify one of fisherz (Fisher's z-transformed correlations) or correlation (untransformed correlations) as the effect size.

```
. meta esize rho n, fisherz
Meta-analysis setting information
 Study information
   No. of studies: 7
      Study label: Generic
        Study size: _meta_studysize
      Summary data: rho n
       Effect size
              Type: fisherz
             Label: Fisher's z
          Variable: meta es
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
         CI level: 95%
 Model and method
            Model: Random effects
            Method: REML
```

The output shows that the summary data are defined by variables rho and n and that the Fisher's *z*-transformed correlation is used as the effect size. A random-effects REML model is assumed. Other settings are exactly as described in example 1.

Instead of using the Fisher's z-transformed correlation, we can choose the untransformed (raw) correlation as the effect size by using the correlation option.

```
. meta esize rho n, correlation
Meta-analysis setting information
 Study information
   No. of studies: 7
      Study label: Generic
        Study size: _meta_studysize
      Summary data: rho n
       Effect size
              Type: correlation
             Label: Correlation
          Variable: meta es
         Precision
         Std. err.: meta se
                CI: [ meta_cil, _meta_ciu]
          CI level: 95%
  Model and method
            Model: Random effects
            Method: REML
```

The output differs from that above in the Effect size section. It now reflects that the untransformed (raw) correlation is the effect size of choice instead of the Fisher's z-transformed correlation.

Many authors (Borenstein and Hedges 2019) argue that untransformed correlations should be avoided particularly when there are study correlations that are close to -1 or 1.

#### Example 12: Specify an alternative meta-analysis model and method

Instead of using the default REML estimation method, you may specify an alternative random-effects method, such as the DL method. This can be done via the random() option.

```
. meta esize rho n. fisherz random(dlaird)
Meta-analysis setting information
 Study information
   No. of studies: 7
      Study label: Generic
        Study size: _meta_studysize
      Summary data: rho n
       Effect size
              Type: fisherz
             Label: Fisher's z
          Variable: _meta_es
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
          CI level: 95%
 Model and method
            Model: Random effects
            Method: DerSimonian-Laird
```

Or perhaps you believe that your correlations are similar across the studies and that a common-effect model is adequate to synthesize the overall correlation. You may request a common-effect model with the inverse-variance method by specifying the common option.

```
. meta esize rho n, fisherz common
Meta-analysis setting information
 Study information
   No. of studies: 7
       Study label: Generic
       Study size: _meta_studysize
      Summary data: rho n
      Effect size
              Type: fisherz
             Label: Fisher's z
          Variable: _meta_es
         Precision
         Std. err.: _meta_se
                CI: [_meta_cil, _meta_ciu]
          CI level: 95%
 Model and method
            Model: Common effect
            Method: Inverse-variance
```

## Stored results

meta esize stores the following characteristics and system variables:

Characteristics

```
_dta[_meta_marker]
                                      "_meta_ds_1"
                                     number of studies in the meta-analysis
    _dta[_meta_K]
    _dta[_meta_studylabel]
                                     name of string variable containing study labels or Generic
    _dta[_meta_estype]
                                     type of effect size; varies
    _dta[_meta_eslabelopt]
                                     eslabel(eslab), if specified
    _dta[_meta_eslabel]
                                     effect-size label from eslabel(); default varies
    _dta[_meta_eslabeldb]
                                     effect-size label for dialog box
    _dta[_meta_esvardb]
                                      _meta_es
    _dta[_meta_level]
                                     default confidence level for meta-analysis
                                     esize(estype), if specified
    _dta[_meta_esizeopt]
                                     exact, if esize(, exact) is specified
    _dta[_meta_esopt_exact]
                                     holkinse, if esize(, holkinse) is specified
    _dta[_meta_esopt_holkinse]
    _dta[_meta_esopt_unequal]
                                     unequal, if esize(, unequal) is specified
                                     meta-analysis model label: Random effects, Common effect, or
    _dta[_meta_modellabel]
                                        Fixed effects
    _dta[_meta_model]
                                     meta-analysis model: random, common, or fixed
    _dta[_meta_methodlabel]
                                     meta-analysis method label; varies by meta-analysis model
    _dta[_meta_method]
                                     meta-analysis method; varies by meta-analysis model
                                     random(remethod), if specified
    _dta[_meta_randomopt]
    _dta[_meta_zcopt]
                                     zerocells(zcspec), if specified
    _dta[_meta_zcadj]
                                     type of adjustment for zero cells, if zerocells()
                                        specified
    _dta[_meta_zcvalue]
                                      value added to cells to adjust for zero cells, if specified
    _dta[_meta_show]
                                     empty or nometashow
    _dta[_meta_n1var]
                                     name of group 1 sample-size variable; for two-sample continuous data
                                     name of group 1 mean variable; for two-sample continuous data
    _dta[_meta_mean1var]
                                     name of group 1 std. dev. variable; for two-sample continuous data
    _dta[_meta_sd1var]
    _dta[_meta_n2var]
                                     name of group 2 sample-size variable; for two-sample continuous data
                                     name of group 2 mean variable; for two-sample continuous data
    _dta[_meta_mean2var]
                                     name of group 2 std. dev. variable; for two-sample continuous data
    _dta[_meta_sd2var]
                                     name of n11 variable; for two-sample binary data (contingency table)
    _dta[_meta_n11var]
                                     name of n12 variable; for two-sample binary data (contingency table)
    _dta[_meta_n12var]
    _dta[_meta_n21var]
                                     name of n21 variable; for two-sample binary data (contingency table)
                                     name of n22 variable; for two-sample binary data (contingency table)
    _dta[_meta_n22var]
    _dta[_meta_nsvar]
                                     name of ns variable; for one-sample binary data (proportion)
    _dta[_meta_nvar]
                                     name of n variable; for one-sample binary data (proportion) or correlation data
                                     name of r variable; for correlation data
    _dta[_meta_rvar]
    _dta[_meta_datatype]
                                     data type; continuous, binary, proportion, or correlation
                                     variables specified with meta esize
    _dta[_meta_datavars]
    _dta[_meta_setcmdline]
                                     meta esize command line
                                     if specification
    _dta[_meta_ifexp]
                                     in specification
    _dta[_meta_inexp]
System variables
    _meta_id
                                     study ID variable
                                     variable containing effect sizes
    _meta_es
    meta se
                                     variable containing effect-size standard errors
                                      variable containing lower bounds of CIs for effect sizes
    _meta_cil
    _meta_ciu
                                     variable containing upper bounds of CIs for effect sizes
    _meta_studylabel
                                     string variable containing study labels
                                     variable containing total sample size per study
    _meta_studysize
```

# Methods and formulas

Methods and formulas are presented under the following headings:

Effect sizes for two-group comparison of continuous outcomes Unstandardized mean difference Standardized mean difference Effect sizes for two-group comparison of binary outcomes Odds ratio Risk ratio (rate ratio) Risk difference Zero-cells adjustments for two-sample case Effect sizes for estimating a single proportion Untransformed (raw) proportion Freeman-Tukey-transformed proportion Logit-transformed proportion Zero-cells adjustments for one-sample case Effect sizes for correlation data Untransformed (raw) correlation Fisher's z-transformed correlation Confidence intervals for effect sizes

#### Effect sizes for two-group comparison of continuous outcomes

As we described in *Meta-analysis* for two-group comparison of continuous outcomes, meta-analysis often compares two groups: experimental (or treated) group and control group.

When the response (measurement) is continuous, studies typically report a mean and standard deviation for each group. For a given study, the following table denotes the underlying population parameters and the reported summary statistics (data) for each group.

	population		sample		
group	mean	sd	mean	sd	size
treatment	$\mu_1$	$\sigma_1$	$\overline{x}_1$	$s_1$	$n_1$
control	$\mu_2$	$\sigma_2$	$\overline{x}_2$	$s_2$	$n_2$

The majority of this section is based on Borenstein (2009).

#### Unstandardized mean difference

Consider the population mean difference

$$\theta = \mu_1 - \mu_2$$

For each study in the meta-analysis, meta esize with option esize(mdiff) estimates  $\theta$  using the difference in sample means,

$$D = \overline{x}_1 - \overline{x}_2$$

The variance of D, assuming that the two population standard deviations are equal, is estimated by

$$\widehat{\operatorname{Var}}(D) = \left(\frac{1}{n_1} + \frac{1}{n_2}\right) s^2$$

where s is the pooled sample standard deviation

$$s = \sqrt{\frac{\left(n_1 - 1\right)s_1^2 + \left(n_2 - 1\right)s_2^2}{n_1 + n_2 - 2}}$$

For unequal population standard deviations, use option esize(mdiff, unequal); then the variance of D is estimated by

$$\widehat{\operatorname{Var}}(D) = \frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}$$

Unstandardized (raw) mean differences are not comparable across studies if the underlying means are measured on different scales.

#### Standardized mean difference

The standardized mean difference is

$$\theta = \frac{\mu_1 - \mu_2}{\sigma}$$

Note that  $\theta$  does not depend on the scale of measurement. The definition of the standardized mean difference implicitly assumes that the population standard deviations,  $\sigma_1$  and  $\sigma_2$ , are the same:  $\sigma_1 = \sigma_2 = \sigma$ .

meta esize with option esize (cohend) estimates  $\theta$  using Cohen's d statistic (Cohen 1969, 1988),

$$d = \frac{\overline{x}_1 - \overline{x}_2}{s}$$

The estimated variance of d is given by

$$\widehat{\text{Var}}(d) = \frac{n_1 + n_2}{n_1 n_2} + \frac{d^2}{2(n_1 + n_2)}$$

Hedges (1981) introduced an adjustment to Cohen's d for small samples that accounts for a small upward bias in the absolute value of  $\theta$ . meta esize with option esize(hedgesg, exact) computes Hedges's g as

$$g = c(m) \times d$$

where  $m = n_1 + n_2 - 2$  is the degrees of freedom used to estimate s and

$$c(m) = \frac{\Gamma\left(\frac{m}{2}\right)}{\sqrt{\frac{m}{2}}\Gamma\left(\frac{m-1}{2}\right)}$$

The adjustment c(m) is less than 1 and approaches 1 as m gets large. The variance estimate of Hedges's g is

$$\widehat{\operatorname{Var}}(g) = c(m)^2 \times \widehat{\operatorname{Var}}(d)$$

Hedges (1981) also introduced an accurate approximation for c(m) that has been traditionally used in meta-analysis. The approximation for c(m) is

$$J = 1 - \frac{3}{4m - 1}$$

meta esize with option esize(hedgesg) computes Hedges's g using J for c(m); thus,

$$g = J \times d$$

and

$$\widehat{\mathrm{Var}}(g) = J^2 \times \widehat{\mathrm{Var}}(d)$$

meta esize with option esize (glassdelta2) estimates  $\theta$  using Glass's  $\Delta$  (Smith and Glass 1977),

$$\Delta = \frac{\overline{x}_1 - \overline{x}_2}{s_2}$$

Notice that the standard deviation in the denominator is  $s_2$ , the sample standard deviation from the control group, which is considered to be a more reliable estimate of the common variance. The estimated variance of  $\Delta$  is given by

$$\widehat{\mathrm{Var}}(\Delta) = \frac{n_1+n_2}{n_1n_2} + \frac{\Delta^2}{2\left(n_2-1\right)}$$

In the absence of the control group, such as in observational studies, Kline (2013), among others, suggests providing statistics standardized by the standard deviation of each group. Glass's  $\Delta$  where standardization is based on the treatment group may be computed via option esize(glassdelta1).

Alternative standard error estimators are available for Hedges's g and Cohen's d effect sizes.

Hedges and Olkin (1985, eq. 8, 80) provide another commonly used estimator for the variance of Hedges's g.

$$\widehat{\mathrm{Var}}(g) = \frac{n_1 + n_2}{n_1 n_2} + \frac{g^2}{2\left(m - 1.94\right)}$$

meta esize uses this formula when option esize(hedgesg, holkinse) is specified.

The alternative variance estimator of d is given by

$$\widehat{\mathrm{Var}}(d) = \frac{n_1 + n_2}{n_1 n_2} + \frac{d^2}{2\left(n_1 + n_2 - 2\right)}$$

This variance estimator may be requested via option esize(cohend, holkinse).

#### Effect sizes for two-group comparison of binary outcomes

As we described in *Meta-analysis for two-group comparison of binary outcomes*, meta-analysis often compares two groups: experimental (or treated) group and control group. When the response (measurement) is binary, each study typically reports cell counts from the following  $2 \times 2$  table.

group	success	failure	size
treatment	a	b	$n_1 = a + b$
control	c	d	$n_2=c+d$

Here, for simplicity, we use a different notation for the cell counts (a, b, c, and d) compared with the similar table in Meta-analysis for two-group comparison of binary outcomes.

For the treatment group,  $n_1$  is assumed fixed,  $a \sim \text{binomial}(n_1, \pi_1)$ , and  $\pi_1$  is the probability of a success. For the control group,  $n_2$  is assumed fixed,  $c \sim \text{binomial}(n_2, \pi_2)$ , and  $\pi_2$  is the probability of a success. The goal of each study is to compare the two success probabilities,  $\pi_1$  and  $\pi_2$ .

Estimates of the success probabilities are  $\hat{\pi}_1 = a/n_1$  for the treatment group and  $\hat{\pi}_2 = c/n_2$  for the control group.

#### Odds ratio

meta esize with option esize(lnoratio) computes estimates of the log odds-ratios. Odds ratio is the ratio of the odds of a success in the treatment group over the odds of a success in the control group.

$$\mathrm{OR} = \frac{{{\pi _1}/\left( {1 - {\pi _1}} \right)}}{{{\pi _2}/\left( {1 - {\pi _2}} \right)}}$$

The odds ratio is estimated by

$$\widehat{OR} = \frac{ad}{bc}$$

The distribution of  $\widehat{OR}$  is typically skewed, but the natural logarithm of  $\widehat{OR}$ ,  $\ln(\widehat{OR})$ , is asymptotically normally distributed. The estimate of the variance of  $\ln(\widehat{OR})$  is

$$\widehat{\operatorname{Var}}\left\{\ln(\widehat{\operatorname{OR}})\right\} = \frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}$$

meta esize with option esize (lnorpeto) computes estimates of effect size using Peto's log oddsratio (Peto et al. 1977; Yusuf et al. 1985). Peto's odds ratio and log odds-ratio are

$$\begin{split} \widehat{\mathrm{OR}}^{\mathrm{Peto}} &= \exp\left\{\frac{a - E\left(a\right)}{\mathrm{Var}\left(a\right)}\right\}\\ &\ln\left(\widehat{\mathrm{OR}}^{\mathrm{Peto}}\right) = \frac{a - E\left(a\right)}{\mathrm{Var}\left(a\right)} \end{split}$$

where the expectation and variance of a are estimated assuming a hypergeometric distribution:

$$\begin{split} E\left(a\right) &= \frac{(a+c)n_1}{n}\\ \text{Var}\left(a\right) &= \frac{n_1n_2\left(a+c\right)\left(b+d\right)}{n^2\left(n-1\right)} \end{split}$$

The variance estimate of  $\ln\left(\widehat{OR}^{Peto}\right)$  is

$$\widehat{\operatorname{Var}}\left\{\ln\left(\widehat{\operatorname{OR}}^{\operatorname{Peto}}\right)\right\} = \frac{1}{\operatorname{Var}\left(a\right)}$$

See, for instance, Fleiss 1993, Fleiss, Levin, and Paik 2003, and Bradburn et al. (2007) for a discussion of potential bias of Peto's odds ratio and its performance in sparse data.

#### **Risk ratio (rate ratio)**

meta esize with option esize(lnrratio) computes estimates of the log risk-ratios. The risk ratio (RR), also known as the rate ratio or relative risk in the health sciences, is

$$\mathrm{RR} = \frac{\pi_1}{\pi_2}$$

RR is estimated by

$$\widehat{\mathrm{RR}} = \frac{a/n_1}{c/n_2}$$

Similarly to odds ratios,  $\widehat{RR}$  typically has a skewed distribution, but the natural logarithm of  $\widehat{RR}$ ,  $\ln(\widehat{RR})$ , is asymptotically normally distributed. The estimate of the variance of  $\ln(\widehat{RR})$  is

$$\widehat{\operatorname{Var}}\left\{\,\ln\left(\widehat{\operatorname{RR}}\right)\right\} = \frac{1}{a} + \frac{1}{c} - \frac{1}{a+b} - \frac{1}{c+d}$$

#### **Risk difference**

meta esize with option esize(rdiff) computes estimates of the risk differences. The risk difference is  ${\rm RD}=\pi_1-\pi_2$ 

and is estimated by

$$\widehat{\mathrm{RD}} = \frac{a}{n_1} - \frac{c}{n_2}$$

 $\widehat{\text{RD}}$  is asymptotically normally distributed and is thus typically used without a transformation in metaanalysis.

The estimated variance of  $\widehat{RD}$  is

$$\widehat{\operatorname{Var}}\left(\widehat{\operatorname{RD}}\right) = \frac{ab}{n_1^3} + \frac{cd}{n_2^3}$$

#### Zero-cells adjustments for two-sample case

The variance estimates of  $\ln(\widehat{OR})$  and  $\ln(\widehat{RR})$  are not defined if there are any empty (zero count) cells in a 2 × 2 table. In this case, it is customary to add a small value, often referred to as "continuity correction", to each cell prior to computing the log odds- or risk-ratio.

By default, meta esize adds 0.5 to each cell of  $2 \times 2$  tables containing empty cells (Gart and Zweifel 1967 and Gart, Pettigrew, and Thomas 1985). Alternatively, you can add a different number or add a number to each cell of all  $2 \times 2$  tables, as long as there is at least one  $2 \times 2$  table with zero cells; see option zerocells().

For odds ratios, Sweeting, Sutton, and Lambert (2004) proposed the treatment-arm continuity correction (TACC) method, which estimates the continuity-correction values from the data separately for each group; see zerocells(tacc).

#### Effect sizes for estimating a single proportion

As we described in *Meta-analysis for estimating a single proportion*, meta-analysis may be used to aggregate proportions of a certain event of interest in single-group or single-arm studies. Each study typically reports the number of successes (number of events), e, and the study sample size, n. The number of successes e is assumed to follow a binomial(n, p) distribution, where p is the probability of success. For details, see Barendregt et al. (2013) and Nyaga, Arbyn, and Aerts (2014).

#### Untransformed (raw) proportion

meta esize with option esize(proportion) computes estimates of proportions for each study and uses them as effect sizes in the meta-analysis. The proportion is estimated by

$$\hat{p} = \frac{e}{n}$$

When the proportion p is near 0.5 and when n is sufficiently large, the binomial distribution of e is well approximated by the normal distribution, and a meta-analysis may be performed in the natural (untransformed) metric.

The estimated variance of  $\hat{p}$  is

$$\widehat{\operatorname{Var}}\left(\widehat{p}\right) = \frac{\widehat{p}\left(1-\widehat{p}\right)}{n}$$

Because the expression of the variance depends on  $\hat{p}$ , meta-analysis of this effect size tends to assign artificially large weights for studies with  $\hat{p}$  close to 0 or 1. In this case, the variance of  $\hat{p}$  is close to 0, and the study weights, which are the inverse variances, will be large. Also, study-specific CI limits may fall outside the range of [0, 1] and, in practice, are truncated when this happens.

#### Freeman–Tukey-transformed proportion

By default (or with option esize(ftukeyprop)), metaesize computes the Freeman-Tukeytransformed proportions and uses them as effect sizes in the meta-analysis. The Freeman-Tukey transformation is also known as the Freeman-Tukey double-arcsine transformation in the literature. The Freeman-Tukey-transformed proportion is given by

$$\hat{p}_{\rm FT} = \operatorname{asin}\left(\sqrt{\frac{e}{n+1}}\right) + \operatorname{asin}\left(\sqrt{\frac{e+1}{n+1}}\right) \tag{1}$$

with the corresponding estimated variance

$$\widehat{\mathrm{Var}}\,(\hat{p}_{\mathrm{FT}}) = \frac{1}{n+0.5}$$

This is a variance-stabilizing transformation (variance does not depend on e) and is particularly preferable when  $\hat{p}$  is close to 0 or 1. This transformation also addresses the issue of assigning artificially small or large weights to studies in the meta-analysis when e is close to 0 or n. And it guarantees that the backtransformed CIs (see Inverse Freeman–Tukey transformation in Methods and formulas in [META] meta summarize) fall within the [0, 1] range.

#### Logit-transformed proportion

meta esize with option esize(logitprop) computes logit-transformed proportions and uses them as effect sizes in the meta-analysis. The logit-transformed proportion is estimated by

$$\operatorname{logit}\left(\hat{p}\right) = \, \ln\left(\frac{\hat{p}}{1-\hat{p}}\right)$$

with the corresponding estimated variance

$$\widehat{\operatorname{Var}}\left\{\operatorname{logit}\left(\hat{p}\right)\right\} = \frac{1}{n\hat{p}} + \frac{1}{n-n\hat{p}}$$

This transformation allows aggregating the proportions in a metric that is closer to normality and guarantees that the back-transformed CI limits (computed using the invlogit() function) are between 0 and 1 (inclusive). Because the expression of the variance depends on  $\hat{p}$ , meta-analysis of this effect size tends to assign artificially low weights for studies with  $\hat{p}$  close to 0 or 1. In this case, the variances for such studies are large, and the study weights, which are the inverse variances, will be low.

#### Zero-cells adjustments for one-sample case

When a study reports a zero cell (zero successes or zero failures), the variance of  $\hat{p}$  is equal to 0, and the variance of  $logit(\hat{p})$  is not defined. In this case, it is customary to add a small value, often referred to as "continuity correction", to each cell prior to computing the proportion or the logit-transformed proportion.

By default, meta esize adds 0.5 to each cell of studies containing zero cells (Gart and Zweifel 1967 and Gart, Pettigrew, and Thomas 1985). In other words, for a study reporting zero cells, the number of successes, e, will be incremented by 0.5, the number of failures will be incremented by 0.5, and therefore, the total sample size, n, will increase by 1.

Alternatively, you can add a different number or add a number to each cell of all studies, as long as there is at least one study with zero cells; see option zerocells().

#### Effect sizes for correlation data

As we described in Meta-analysis for correlation data, meta-analysis may be used to aggregate correlations between two variables of interest. Each study typically reports the sample correlation, r, and the study sample size, n. For details, see Borenstein and Hedges (2019).

#### Untransformed (raw) correlation

The estimate of the correlation parameter  $\rho$  is the sample correlation, denoted by r. The estimated variance of r is given by

$$\widehat{\operatorname{Var}}\left(r\right) = \frac{\left(1 - r^{2}\right)^{2}}{n - 1}$$

When you deal with the sample correlation, it is well known that the large-sample theory does not hold up well for small sample sizes, particularly when r is close to 1 or -1. In contrast, large-sample theory of the Fisher z-transformed correlation often yields reliable results with sample sizes of 20 or more (Hedges 2019). Therefore, it is generally recommended to apply the Fisher's z-transformation for analyses where correlations are used as the measure of effect size.

#### Fisher's *z*-transformed correlation

When the fisherz option is specified, meta esize computes the Fisher's z-transformed correlations and uses them as effect sizes in the meta-analysis. The Fisher's z-transformed correlation is given by

$$f_z = \frac{1}{2} \log \left( \frac{1+r}{1-r} \right) = \operatorname{atanh}(r)$$

where atanh(.) is the inverse hyperbolic tangent function. The corresponding estimated variance is

$$\widehat{\operatorname{Var}}\left(f_z\right) = \frac{1}{n-3}$$

This is a variance-stabilizing transformation (variance does not depend on r) and is particularly preferable when r is close to -1 or 1.

### Confidence intervals for effect sizes

For the *j*th study in a given meta-analysis, let  $\hat{\theta}_j$  be one of the effect-size estimators described above; then the asymptotic  $100(1-\alpha)$ % confidence interval computed by meta esize is

$$\hat{\theta}_j \pm z_{1-\alpha/2} \sqrt{\mathrm{Var}}(\hat{\theta}_j)$$

where  $z_{1-\alpha/2}$  is the usual critical value from the standard normal distribution.

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# Also see

- [META] meta data Declare meta-analysis data
- [META] meta set Declare meta-analysis data using generic effect sizes
- [META] meta update Update, describe, and clear meta-analysis settings
- [META] meta Introduction to meta
- [META] Glossary
- [META] Intro Introduction to meta-analysis
- [R] esize Effect size based on mean comparison

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