meprobit — Multilevel mixed-effects probit regression					
Description	Quick start	Menu	Syntax	Options	
Remarks and examples	Stored results	Methods and formulas	References	Also see	

## Description

meprobit fits mixed-effects models for binary or binomial responses. The conditional distribution of the response given the random effects is assumed to be Bernoulli, with success probability determined by the standard normal cumulative distribution function.

# **Quick start**

Two-level probit model of y and covariate x and random intercepts by lev2 meprobit y x || lev2:

Add random coefficients for x

meprobit y x || lev2: x

Same as above, but specify that y records the number of successes from 10 trials meprobit y x || lev2: x, binomial(10)

Same as above, but with the number of trials stored in variable n meprobit y x || lev2: x, binomial(n)

Three-level random-intercept model of y and covariate x with lev2 nested within lev3 meprobit y x || lev3: || lev2:

```
Two-way crossed random effects by factors a and b
meprobit y x || _all:R.a || b:
```

## Menu

 $Statistics > Multilevel \ mixed-effects \ models > Probit \ regression$ 

## Syntax

meprobit depvar fe\_equation [ || re\_equation ] [ || re\_equation ... ] [, options]

where the syntax of *fe\_equation* is

[indepvars] [if] [in] [weight] [, fe\_options]

and the syntax of *re\_equation* is one of the following:

for random coefficients and intercepts

levelvar: [varlist] [, re\_options]

for random effects among the values of a factor variable in a crossed-effects model

levelvar: R.varname

*levelvar* is a variable identifying the group structure for the random effects at that level or is \_all representing one group comprising all observations.

fe_options	Description
Model	
<u>nocons</u> tant	suppress constant term from the fixed-effects equation
<u>off</u> set( <i>varname</i> )	include varname in model with coefficient constrained to 1
asis	retain perfect predictor variables
re_options	Description
Model	
<pre><u>cov</u>ariance(vartype)</pre>	variance-covariance structure of the random effects
<u>nocons</u> tant	suppress constant term from the random-effects equation
<u>fw</u> eight( <i>varname</i> )	frequency weights at higher levels
<u>iw</u> eight( <i>varname</i> )	importance weights at higher levels
<pre>pweight(varname)</pre>	sampling weights at higher levels

### meprobit — Multilevel mixed-effects probit regression 3

options	Description
Model	
<pre>binomial(varname   #)</pre>	set binomial trials if data are in binomial form
<pre>constraints(constraints)</pre>	apply specified linear constraints
SE/Robust	
vce( <i>vcetype</i> )	<i>vcetype</i> may be oim, opg, <u>r</u> obust, or <u>cl</u> uster <i>clustvar</i>
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
<u>nocnsr</u> eport	do not display constraints
<u>notab</u> le	suppress coefficient table
<u>nohead</u> er	suppress output header
nogroup	suppress table summarizing groups
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Integration	
<u>intmethod(intmethod)</u>	integration method
<pre>intpoints(#)</pre>	set the number of integration (quadrature) points for all levels; default is intpoints(7)
Maximization	
maximize_options	control the maximization process; seldom used
<pre>startvalues(symethod)</pre>	method for obtaining starting values
<pre>startgrid[(gridspec)]</pre>	perform a grid search to improve starting values
<u>noest</u> imate	do not fit the model; show starting values instead
dnumerical	use numerical derivative techniques
<u>col</u> linear	keep collinear variables
<u>coefl</u> egend	display legend instead of statistics
vartype	Description
independent	one unique variance parameter per random effect and all covariances 0; the default unless the R. notation is used
<u>exc</u> hangeable	equal variances for random effects and one common pairwise covariance
<u>id</u> entity	equal variances for random effects and all covariances 0; the default if the R. notation is used
<u>un</u> structured	all variances and covariances to be distinctly estimated
<pre>fixed(matname)</pre>	user-selected variances and covariances constrained to specified values; the remaining variances and covariances unrestricted
<pre>pattern(matname)</pre>	user-selected variances and covariances constrained to be equal; the remaining variances and covariances unrestricted

intmethod	Description
<u>mv</u> aghermite	mean-variance adaptive Gauss-Hermite quadrature; the default unless a crossed random-effects model is fit
<u>mc</u> aghermite	mode-curvature adaptive Gauss-Hermite quadrature
ghermite	nonadaptive Gauss–Hermite quadrature
laplace	Laplacian approximation; the default for crossed random-effects models

indepvars and varlist may contain factor variables; see [U] 11.4.3 Factor variables.

depvar, indepvars, and varlist may contain time-series operators; see [U] 11.4.4 Time-series varlists.

bayes, by, collect, and svy are allowed; see [U] 11.1.10 Prefix commands. For more details, see [BAYES] bayes: meprobit.

vce() and weights are not allowed with the svy prefix; see [SVY] svy.

fweights, iweights, and pweights are allowed; see [U] 11.1.6 weight. Only one type of weight may be specified. Weights are not supported under the Laplacian approximation or for crossed models.

startvalues(), startgrid, noestimate, dnumerical, collinear, and coeflegend do not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

### Options

Model

- noconstant suppresses the constant (intercept) term and may be specified for the fixed-effects equation and for any of or all the random-effects equations.
- offset (*varname*) specifies that *varname* be included in the fixed-effects portion of the model with the coefficient constrained to be 1.
- asis forces retention of perfect predictor variables and their associated, perfectly predicted observations and may produce instabilities in maximization; see [R] probit.
- covariance(vartype) specifies the structure of the covariance matrix for the random effects and may be specified for each random-effects equation. vartype is one of the following: independent, exchangeable, identity, unstructured, fixed(matname), or pattern(matname).
  - covariance(independent) covariance structure allows for a distinct variance for each random effect within a random-effects equation and assumes that all covariances are 0. The default is covariance(independent) unless a crossed random-effects model is fit, in which case the default is covariance(identity).
  - covariance(exchangeable) structure specifies one common variance for all random effects and one common pairwise covariance.
  - covariance(identity) is short for "multiple of the identity"; that is, all variances are equal and all covariances are 0.
  - covariance (unstructured) allows for all variances and covariances to be distinct. If an equation consists of p random-effects terms, the unstructured covariance matrix will have p(p+1)/2 unique parameters.
  - covariance(fixed(matname)) and covariance(pattern(matname)) covariance structures provide a convenient way to impose constraints on variances and covariances of random effects. Each specification requires a matname that defines the restrictions placed on variances and covariances. Only elements in the lower triangle of matname are used, and row and column names of

*matname* are ignored. A missing value in *matname* means that a given element is unrestricted. In a fixed (*matname*) covariance structure, (co)variance (i, j) is constrained to equal the value specified in the *i*, *j*th entry of *matname*. In a pattern (*matname*) covariance structure, (co)variances (i, j) and (k, l) are constrained to be equal if *matname*[i, j] = matname[k, l].

fweight(varname) specifies frequency weights at higher levels in a multilevel model, whereas frequency weights at the first level (the observation level) are specified in the usual manner, for example, [fw=fwtvar1]. varname can be any valid Stata variable name, and you can specify fweight() at levels two and higher of a multilevel model. For example, in the two-level model

. mecmd fixed\_portion [fw = wt1] || school: ... , fweight(wt2) ...

the variable wt1 would hold the first-level (the observation-level) frequency weights, and wt2 would hold the second-level (the school-level) frequency weights.

iweight (varname) specifies importance weights at higher levels in a multilevel model, whereas importance weights at the first level (the observation level) are specified in the usual manner, for example, [iw=iwtvar1]. varname can be any valid Stata variable name, and you can specify iweight() at levels two and higher of a multilevel model. For example, in the two-level model

. mecmd fixed\_portion [iw = wt1] || school: ... , iweight(wt2) ...

the variable wt1 would hold the first-level (the observation-level) importance weights, and wt2 would hold the second-level (the school-level) importance weights.

pweight(varname) specifies sampling weights at higher levels in a multilevel model, whereas sampling weights at the first level (the observation level) are specified in the usual manner, for example, [pw=pwtvar1]. varname can be any valid Stata variable name, and you can specify pweight() at levels two and higher of a multilevel model. For example, in the two-level model

. mecmd fixed\_portion [pw = wt1] || school: ... , pweight(wt2) ...

variable wt1 would hold the first-level (the observation-level) sampling weights, and wt2 would hold the second-level (the school-level) sampling weights.

binomial (*varname* | #) specifies that the data are in binomial form; that is, *depvar* records the number of successes from a series of binomial trials. This number of trials is given either as *varname*, which allows this number to vary over the observations, or as the constant #. If binomial() is not specified (the default), *depvar* is treated as Bernoulli, with any nonzero, nonmissing values indicating positive responses.

constraints(constraints); see [R] Estimation options.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (oim, opg), that are robust to some kinds of misspecification (robust), and that allow for intragroup correlation (cluster *clustvar*); see [R] vce\_option. If vce(robust) is specified, robust variances are clustered at the highest level in the multilevel model.

Reporting

```
level(#), nocnsreport; see [R] Estimation options.
```

notable suppresses the estimation table, either at estimation or upon replay.

noheader suppresses the output header, either at estimation or upon replay.

nogroup suppresses the display of group summary information (number of groups, average group size, minimum, and maximum) from the output header.

display\_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels,

<u>allbase</u>levels, <u>nofvlab</u>el, fvwrap(#), fvwrapon(*style*), cformat(%*fmt*), pformat(%*fmt*), sformat(%*fmt*), and nolstretch; see [R] Estimation options.

Integration

intmethod(*intmethod*) specifies the integration method to be used for the random-effects model. mvaghermite performs mean-variance adaptive Gauss-Hermite quadrature; mcaghermite performs mode-curvature adaptive Gauss-Hermite quadrature; ghermite performs nonadaptive Gauss-Hermite quadrature; and laplace performs the Laplacian approximation, equivalent to mode-curvature adaptive Gaussian quadrature with one integration point.

The default integration method is mvaghermite unless a crossed random-effects model is fit, in which case the default integration method is laplace. The Laplacian approximation has been known to produce biased parameter estimates; however, the bias tends to be more prominent in the estimates of the variance components rather than in the estimates of the fixed effects.

For crossed random-effects models, estimation with more than one quadrature point may be prohibitively intensive even for a small number of levels. For this reason, the integration method defaults to the Laplacian approximation. You may override this behavior by specifying a different integration method.

intpoints(#) sets the number of integration points for quadrature. The default is intpoints(7), which means that seven quadrature points are used for each level of random effects. This option is not allowed with intmethod(laplace).

The more integration points, the more accurate the approximation to the log likelihood. However, computation time increases as a function of the number of quadrature points raised to a power equaling the dimension of the random-effects specification. In crossed random-effects models and in models with many levels or many random coefficients, this increase can be substantial.

Maximization

maximize\_options: difficult, technique(algorithm\_spec), iterate(#), [no]log, trace, gradient, showstep, hessian, showtolerance, tolerance(#), ltolerance(#),

<u>nrtol</u>erance(#), <u>nonrtol</u>erance, and from(*init\_specs*); see [R] Maximize. Those that require special mention for meprobit are listed below.

from() accepts a properly labeled vector of initial values or a list of coefficient names with values. A list of values is not allowed.

The following options are available with meprobit but are not shown in the dialog box:

startvalues(symethod), startgrid[(gridspec)], noestimate, and dnumerical; see [ME] meglm. collinear, coeflegend; see [R] Estimation options.

### **Remarks and examples**

Mixed-effects probit regression is probit regression containing both fixed effects and random effects. In longitudinal data and panel data, random effects are useful for modeling intracluster correlation; that is, observations in the same cluster are correlated because they share common cluster-level random effects.

meprobit allows for many levels of random effects. However, for simplicity, we here consider the two-level model, where for a series of M independent clusters, and conditional on a set of fixed effects  $\mathbf{x}_{ij}$  and a set of random effects  $\mathbf{u}_{j}$ ,

$$\Pr(y_{ij} = 1 | \mathbf{x}_{ij}, \mathbf{u}_j) = H(\mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j)$$
(1)

for j = 1, ..., M clusters, with cluster j consisting of  $i = 1, ..., n_j$  observations. The responses are the binary-valued  $y_{ij}$ , and we follow the standard Stata convention of treating  $y_{ij} = 1$  if  $depvar_{ij} \neq 0$  and treating  $y_{ij} = 0$  otherwise. The  $1 \times p$  row vector  $\mathbf{x}_{ij}$  are the covariates for the fixed effects, analogous to the covariates you would find in a standard probit regression model, with regression coefficients (fixed effects)  $\beta$ . For notational convenience here and throughout this manual entry, we suppress the dependence of  $y_{ij}$  on  $\mathbf{x}_{ij}$ .

The  $1 \times q$  vector  $\mathbf{z}_{ij}$  are the covariates corresponding to the random effects and can be used to represent both random intercepts and random coefficients. For example, in a random-intercept model,  $\mathbf{z}_{ij}$  is simply the scalar 1. The random effects  $\mathbf{u}_j$  are M realizations from a multivariate normal distribution with mean  $\mathbf{0}$  and  $q \times q$  variance matrix  $\Sigma$ . The random effects are not directly estimated as model parameters but are instead summarized according to the unique elements of  $\Sigma$ , known as variance components. One special case of (1) places  $\mathbf{z}_{ij} = \mathbf{x}_{ij}$ , so that all covariate effects are essentially random and distributed as multivariate normal with mean  $\beta$  and variance  $\Sigma$ .

Finally, because this is probit regression,  $H(\cdot)$  is the standard normal cumulative distribution function, which maps the linear predictor to the probability of a success  $(y_{ij} = 1)$  with  $H(v) = \Phi(v)$ .

Model (1) may also be stated in terms of a latent linear response, where only  $y_{ij} = I(y_{ij}^* > 0)$  is observed for the latent

$$y_{ij}^* = \mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j + \epsilon_{ij}$$

The errors  $\epsilon_{ij}$  are distributed as a standard normal with mean 0 and variance 1 and are independent of  $\mathbf{u}_j$ .

Below we present two short examples of mixed-effects probit regression; refer to [ME] **me** and [ME] **meglm** for examples of other random-effects models. A two-level probit model can also be fit using xtprobit with the re option; see [XT] **xtprobit**. In the absence of random effects, mixed-effects probit regression reduces to standard probit regression; see [R] **probit**.

#### Example 1: Two-level random-intercept model

Ng et al. (2006) analyzed a subsample of data from the 1989 Bangladesh fertility survey (Huq and Cleland 1990), which polled 1,934 Bangladeshi women on their use of contraception. The women sampled were from 60 districts, identified by the variable district. Each district contained either urban or rural areas (variable urban) or both. The variable c\_use is the binary response, with a value of 1 indicating contraceptive use. Other covariates include mean-centered age and three indicator variables recording number of children.

-	/www.stata-pre ertility Surve		a/r19/bang	ladesh		
. meprobit c_u	use i.urban ag	e i.childre	en    dist	rict:		
Fitting fixed-	- effects model	:				
Iteration 0: Iteration 1: Iteration 2:	Log likelihoo Log likelihoo Log likelihoo	d = -1228.8 d = -1228.2	2466			
Refining start	ting values:					
Grid node 0:	Log likelihoo	d = -1237.3	3973			
Fitting full m	0					
Iteration 0: Iteration 1: Iteration 2: Iteration 3: Iteration 4: Iteration 5: Iteration 6:	Log likelihoo Log likelihoo Log likelihoo Log likelihoo Log likelihoo Log likelihoo	d = -1221.2 $d = -1207.4$ $d = -1206.7$ $d = -1206.5$ $d = -1206.5$	2111 (not 4451 7002 5346 5336	concave concave	-	
Mixed-effects Group variable		sion			of groups =	1,934 60
				ops ber	group:	
					min = avg = max =	2 32.2 118
Integration me	ethod: mvagher	mite		Integra	avg =	32.2
Integration me Log likelihood	-			Integra Wald ch Prob >	avg = max = ation pts. = ai2(5) =	32.2 118
-	-	i	z	Wald ch	avg = max = htion pts. = hi2(5) = chi2 =	32.2 118 7 115.36
Log likelihood	d = −1206.5336	i	z 6.17 -3.38	Wald ch Prob >	avg = max = htion pts. = hi2(5) = chi2 =	32.2 118 7 115.36 0.0000
Log likelihood c_use urban Urban	d = -1206.5336 Coefficient .4490191	Std. err.	6.17	Wald ch Prob > P> z  0.000	avg = max = tion pts. = ti2(5) = chi2 = [95% conf. .3064953	32.2 118 7 115.36 0.0000 . interval] .5915429
Log likelihood c_use urban Urban age children 1 child 2 children	d = -1206.5336 Coefficient .4490191 0162203 .674377 .8281581	Std. err. .0727176 .0048005 .0947829 .1048136	6.17 -3.38 7.11 7.90	Wald ch Prob > P> z  0.000 0.001 0.000 0.000	avg = max = tion pts. = ti2(5) = chi2 = [95% conf. .3064953 0256291 .488606 .6227272	32.2 118 7 115.36 0.0000 . interval] .5915429 0068114 .8601481 1.033589
Log likelihood c_use urban Urban age children 1 child 2 children 3 or more	d = -1206.5336 Coefficient .4490191 0162203 .674377 .8281581 .8137876	Std. err. .0727176 .0048005 .0947829 .1048136 .1073951	6.17 -3.38 7.11 7.90 7.58	Wald ch Prob > P> z  0.000 0.001 0.000 0.000 0.000	avg = max = tion pts. = chi2(5) = [95% conf. .3064953 0256291 .488606 .6227272 .6032972	32.2 118 7 115.36 0.0000 . interval] .5915429 0068114 .8601481 1.033589 1.024278

Probit regression coefficients are most commonly interpreted in terms of partial effects, as we demonstrate in example 1 of [ME] **meprobit postestimation**. For now, we only note that urban women and women with more children are more likely to use contraceptives and that contraceptive use decreases with age. The estimated variance of the random intercept at the district level,  $\hat{\sigma}^2$ , is 0.08 with standard error 0.03. The reported likelihood-ratio test shows that there is enough variability between districts to favor a mixed-effects probit regression over an ordinary probit regression; see *Distribution theory for likelihood-ratio test* in [ME] **me** for a discussion of likelihood-ratio testing of variance components.

#### Example 2: Three-level random-intercept model

Rabe-Hesketh, Toulopoulou, and Murray (2001) analyzed data from a study that measured the cognitive ability of patients with schizophrenia compared with their relatives and control subjects. Cognitive ability was measured as the successful completion of the "Tower of London", a computerized task, measured at three levels of difficulty. For all but one of the 226 subjects, there were three measurements (one for each difficulty level). Because patients' relatives were also tested, a family identifier, family, was also recorded.

We fit a probit model with response dtlm, the indicator of cognitive function, and with covariates difficulty and a set of indicator variables for group, with the controls (group==1) being the base category. We also allow for random effects due to families and due to subjects within families. The first is a random intercept (constant only) at the family level, and the second is a random intercept at the subject level. The order in which these are specified (from left to right) is significant—meprobit assumes that subject is nested within family. The equations are separated by ||.

. use https://www.stata-press.com/data/r19/towerlondon (Tower of London data)						
. meprobit dtlm difficulty i.group    family:    subject:						
Fitting fixed-effects model:						
Iteration 0: Log likelihood = -317.11238 Iteration 1: Log likelihood = -314.50535 Iteration 2: Log likelihood = -314.50121 Iteration 3: Log likelihood = -314.50121						
Refining star	ting values:					
Grid node 0:						
Fitting full r	nodel:					
Iteration 0: Log likelihood = -326.18533 (not concave) Iteration 1: Log likelihood = -313.16256 (not concave) Iteration 2: Log likelihood = -308.47528 Iteration 3: Log likelihood = -305.02228 Iteration 4: Log likelihood = -304.88972 Iteration 5: Log likelihood = -304.88845 Iteration 6: Log likelihood = -304.88845						
Mixed-effects	probit regr	ression		Number	of obs	= 677
Group	ing informat	ion				
Grouj					per group age Maxi	mum
family11825.727subject22623.03						
	•					
	subject	226		Integra	3.0 tion pts.	<u>3</u> = 7
Integration me	subject ethod: mvagh	226 nermite			3.0 tion pts. i2(3)	3
-	subject ethod: mvagh	226 Mermite 845		Integra Wald ch	3.0 tion pts. hi2(3) chi2	3 = 7 = 83.28
Log likelihood	subject ethod: mvagh d = -304.888	226 hermite 345 ht Std. err.	2	Integra Wald ch Prob >	3.0 tion pts. hi2(3) chi2	3 = 7 = 83.28 = 0.0000 f. interval]
Log likelihood dtlm	subject ethod: mvagh d = -304.888 Coefficier	226 hermite 345 ht Std. err. 1037376 3 .204265	2 z	Integra Wald ch Prob > P> z	3.0 tion pts. ti2(3) chi2 [95% con	3 = 7 = 83.28 = 0.0000 f. interval] 7296672 .2371276
Log likelihood dtlm difficulty group 2	subject ethod: mvagh d = -304.888 Coefficier 9329891 1632243	226 hermite 345 ht Std. err. 1037376 3.204265 5.228063	2 z -8.99 -0.80	Integra Wald ch Prob > P> z  0.000 0.424	3.0 tion pts. ti2(3) chi2 [95% con -1.136311 5635763	3 = 7 = 83.28 = 0.0000 f. interval] 7296672 .2371276 1750244
Log likelihood dtlm difficulty group 2 3	subject ethod: mvagh d = -304.888 Coefficien 9329891 1632243 6220196	226 hermite 345 ht Std. err. 1037376 3 .204265 5 .228063 4 .1597223	2 -8.99 -0.80 -2.73	Integra Wald ch Prob > P> z  0.000 0.424 0.006	3.0 tion pts. ti2(3) chi2 [95% con -1.136311 5635763 -1.069015	3 = 7 = 83.28 = 0.0000 f. interval] 7296672 .2371276 1750244 5274654
Log likelihood dtlm difficulty group 2 3 cons family	subject ethod: mvagh d = -304.888 Coefficier 9329891 1632243 6220196 8405154	226 hermite 345 ht Std. err. 1037376 3204265 5228063 41597223 31736281	2 -8.99 -0.80 -2.73	Integra Wald ch Prob > P> z  0.000 0.424 0.006	3.0 tion pts. ti2(3) chi2 [95% con -1.136311 5635763 -1.069015 -1.153565	3 = 7 = 83.28 = 0.0000 f. interval] 7296672 .2371276 1750244 5274654 1.055244

Note: LR test is conservative and provided only for reference.

We see that we have 226 subjects from 118 families. After adjusting for the random-effects structure, the probability of successful completion of the Tower of London decreases dramatically as the level of difficulty increases. Also, people with schizophrenia (group==3) tended not to perform as well as the control subjects.

The above extends to models with more than two levels of nesting by adding more random-effects equations, each separated by ||.

## **Stored results**

```
meprobit stores the following in e():
```

Sca	lars	
	e(N)	number of observations
	e(k)	number of parameters
	e(k_dv)	number of dependent variables
	e(k_eq)	number of equations in e(b)
	e(k_eq_model)	number of equations in overall model test
	e(k_f)	number of fixed-effects parameters
	e(k_r)	number of random-effects parameters
	e(k_rs)	number of variances
	e(k_rc)	number of covariances
	e(df_m)	model degrees of freedom
	e(11)	log likelihood
	e(N_clust)	number of clusters
	e(chi2)	$\chi^2$
	e(p)	<i>p</i> -value for model test
	e(ll_c)	log likelihood, comparison model
	e(chi2_c)	$\chi^2$ , comparison test
	e(df_c)	degrees of freedom, comparison test
	e(p_c)	<i>p</i> -value for comparison test
	e(rank)	rank of e(V)
	e(ic)	number of iterations
	e(rc)	return code
	e(converged)	1 if converged, 0 otherwise
Ma	cros	-
	e(cmd)	meglm
	e(cmd2)	meprobit
	e(cmdline)	command as typed
	e(depvar)	name of dependent variable
	e(wtype)	weight type
	e(wexp)	weight expression (first-level weights)
	e(fweightk)	fweight variable for kth highest level, if specified
	e(iweightk)	iweight variable for kth highest level, if specified
	e(pweightk)	pweight variable for kth highest level, if specified
	e(covariates)	list of covariates
	e(ivars)	grouping variables
	e(model)	probit
	e(title)	title in estimation output
	e(link)	probit
	e(family)	bernoulli or binomial
	e(clustvar)	name of cluster variable
	e(offset)	offset
	e(binomial)	binomial number of trials
	e(intmethod)	integration method
	e(n_quad)	number of integration points
	e(chi2type)	Wald; type of model $\chi^2$
	e(vce)	vcetype specified in vce()
	e(vcetype)	title used to label Std. err.
	e(opt)	type of optimization
	e(which)	max or min; whether optimizer is to perform maximization or minimization
	e(ml_method)	type of ml method

<pre>e(user) e(technique) e(datasignature) e(datasignaturevars) e(properties) e(estat_cmd) e(predict) e(marginsmotok) e(marginswtype) e(marginswexp) e(asbalanced) e(asobserved)</pre>	name of likelihood-evaluator program maximization technique the checksum variables used in calculation of checksum b V program used to implement estat program used to implement predict predictions disallowed by margins weight type for margins weight expression for margins factor variables fvset as asbalanced factor variables fvset as asobserved
Matrices	
e(b)	coefficient vector
e(Cns)	constraints matrix
e(ilog)	iteration log (up to 20 iterations)
e(gradient)	gradient vector
e(N_g) e(g_min)	group counts group-size minimums
e(g_avg)	group-size averages
e(g_avg) e(g_max)	group-size maximums
e(g_max) e(V)	variance–covariance matrix of the estimators
e(V_modelbased)	model-based variance
Functions	
e(sample)	marks estimation sample

In addition to the above, the following is stored in r():

Matrices

r(table)

matrix containing the coefficients with their standard errors, test statistics, *p*-values, and confidence intervals

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

# Methods and formulas

meprobit is a convenience command for meglm with a probit link and a bernoulli or binomial family; see [ME] meglm.

Model (1) assumes Bernoulli data, a special case of the binomial. Because binomial data are also supported by meprobit (option binomial()), the methods presented below are in terms of the more general binomial mixed-effects model.

For a two-level binomial model, consider the response  $y_{ij}$  as the number of successes from a series of  $r_{ij}$  Bernoulli trials (replications). For cluster j, j = 1, ..., M, the conditional distribution of  $\mathbf{y}_j = (y_{j1}, ..., y_{jn_j})'$ , given a set of cluster-level random effects  $\mathbf{u}_j$ , is

$$\begin{split} f(\mathbf{y}_{j}|\mathbf{u}_{j}) &= \prod_{i=1}^{n_{j}} \left[ \begin{pmatrix} r_{ij} \\ y_{ij} \end{pmatrix} \left\{ \Phi(\boldsymbol{\eta}_{ij}) \right\}^{y_{ij}} \left\{ 1 - \Phi(\boldsymbol{\eta}_{ij}) \right\}^{r_{ij} - y_{ij}} \right] \\ &= \exp\left( \sum_{i=1}^{n_{j}} \left[ y_{ij} \log\left\{ \Phi(\boldsymbol{\eta}_{ij}) \right\} - (r_{ij} - y_{ij}) \log\left\{ \Phi(-\boldsymbol{\eta}_{ij}) \right\} + \log \begin{pmatrix} r_{ij} \\ y_{ij} \end{pmatrix} \right] \right) \end{split}$$

for  $\boldsymbol{\eta}_{ij} = \mathbf{x}_{ij}\boldsymbol{\beta} + \mathbf{z}_{ij}\mathbf{u}_j + \text{offset}_{ij}$ .

Defining  $\mathbf{r}_j = (r_{j1}, \ldots, r_{jn_j})'$  and

$$c\left(\mathbf{y}_{j},\mathbf{r}_{j}\right) = \sum_{i=1}^{n_{j}} \log \begin{pmatrix} r_{ij} \\ y_{ij} \end{pmatrix}$$

where  $c(\mathbf{y}_j, \mathbf{r}_j)$  does not depend on the model parameters, we can express the above compactly in matrix notation,

$$f(\mathbf{y}_j|\mathbf{u}_j) = \exp\left[\mathbf{y}_j'\log\left\{\Phi(\boldsymbol{\eta}_j)\right\} - (\mathbf{r}_j - \mathbf{y}_j)'\log\left\{\Phi(-\boldsymbol{\eta}_j)\right\} + c\left(\mathbf{y}_j, \mathbf{r}_j\right)\right]$$

where  $\eta_j$  is formed by stacking the row vectors  $\eta_{ij}$ . We extend the definitions of  $\Phi(\cdot)$ ,  $\log(\cdot)$ , and  $\exp(\cdot)$  to be vector functions where necessary.

Because the prior distribution of  $\mathbf{u}_j$  is multivariate normal with mean  $\mathbf{0}$  and  $q \times q$  variance matrix  $\Sigma$ , the likelihood contribution for the *j*th cluster is obtained by integrating  $\mathbf{u}_j$  out of the joint density  $f(\mathbf{y}_j, \mathbf{u}_j)$ ,

$$\begin{split} \mathcal{L}_{j}(\boldsymbol{\beta},\boldsymbol{\Sigma}) &= (2\pi)^{-q/2} \left|\boldsymbol{\Sigma}\right|^{-1/2} \int f(\mathbf{y}_{j}|\mathbf{u}_{j}) \exp\left(-\mathbf{u}_{j}'\boldsymbol{\Sigma}^{-1}\mathbf{u}_{j}/2\right) d\mathbf{u}_{j} \\ &= \exp\left\{c\left(\mathbf{y}_{j},\mathbf{r}_{j}\right)\right\} (2\pi)^{-q/2} \left|\boldsymbol{\Sigma}\right|^{-1/2} \int \exp\left\{h\left(\boldsymbol{\beta},\boldsymbol{\Sigma},\mathbf{u}_{j}\right)\right\} d\mathbf{u}_{j} \end{split}$$
(2)

where

$$h\left(\boldsymbol{\beta},\boldsymbol{\Sigma},\mathbf{u}_{j}\right) = \mathbf{y}_{j}^{\prime}\log\left\{\Phi(\boldsymbol{\eta}_{j})\right\} - (\mathbf{r}_{j} - \mathbf{y}_{j})^{\prime}\log\left\{\Phi(-\boldsymbol{\eta}_{j})\right\} - \mathbf{u}_{j}^{\prime}\boldsymbol{\Sigma}^{-1}\mathbf{u}_{j}/2$$

and for convenience, in the arguments of  $h(\cdot)$  we suppress the dependence on the observable data  $(\mathbf{y}_i, \mathbf{r}_i, \mathbf{X}_i, \mathbf{Z}_i)$ .

The integration in (2) has no closed form and thus must be approximated; see *Methods and formulas* in [ME] meglm for details.

meprobit supports multilevel weights and survey data; see *Methods and formulas* in [ME] meglm for details.

### References

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- Ng, E. S.-W., J. R. Carpenter, H. Goldstein, and J. Rasbash. 2006. Estimation in generalised linear mixed models with binary outcomes by simulated maximum likelihood. *Statistical Modelling* 6: 23–42. https://doi.org/10.1191/ 1471082X06st106oa.
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### Also see

- [ME] meprobit postestimation Postestimation tools for meprobit
- [ME] mecloglog Multilevel mixed-effects complementary log-log regression
- [ME] melogit Multilevel mixed-effects logistic regression
- [ME] me Introduction to multilevel mixed-effects models
- [BAYES] bayes: meprobit Bayesian multilevel probit regression
- [SEM] Intro 5 Tour of models (Multilevel mixed-effects models)
- [SVY] svy estimation Estimation commands for survey data
- [XT] **xtprobit** Random-effects and population-averaged probit models
- [U] 20 Estimation and postestimation commands

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