Description

polyeval(c, x) evaluates polynomial c at each value recorded in x, returning the results in a pconformable-with-x vector. For instance, polyeval((4,2,1), (3\5)) returns (4+2*3+3^2 \ 4+2*5+5^2) = (19\39).

polysolve (y, x) returns the minimal-degree polynomial c fitting y = polyeval(c, x). Solution is via Lagrange's interpolation formula.

polytrim(c) returns polynomial c with trailing zeros removed. For instance, polytrim((1,2,3,0)) returns (1,2,3). polytrim((0,0,0,0)) returns (0). Thus if n = cols(polytrim then c records an (n-1)th degree polynomial.

polyderiv(c, i) returns the polynomial that is the *i*th derivative of polynomial c. For instance, polyderiv((4,2,1), 1) returns (2,2) (the derivative of $4 + 2x + x^2$ is 2 + 2x). The value of the first derivative of polynomial c at x is polyeval(polyderiv(c,1),x).

polyinteg(c, i) returns the polynomial that is the *i*th integral of polynomial c. For instance, polyinteg((4,2,1), 1) returns (0,4,1,.3333) (the integral of $4+2x+x^2$ is $0+4x+x^2+.3333x^3$). The value of the integral of polynomial c at x is polyeval(polyinteg(c,1), x).

polyadd(c_1 , c_2) returns the polynomial that is the sum of the polynomials c_1 and c_2 . For instance, polyadd((2,1), (3,5,1)) is (5,6,1) (the sum of 2 + x and $3 + 5x + x^2$ is $5 + 6x + x^2$).

polymult (c_1, c_2) returns the polynomial that is the product of the polynomials c_1 and c_2 . For instance, polymult ((2,1), (3,5,1)) is (6,13,7,1) (the product of 2+x and $3+5x+x^2$ is $6+13x+7x^2+x^3$).

polydiv (c_1, c_2, c_q, c_r) calculates polynomial c_1/c_2 , storing the quotient polynomial in c_q and the remainder polynomial in c_r . For instance, polydiv $((3,5,1), (2,1), c_q, c_r)$ returns $c_q=(3,1)$ and $c_r=(-3)$; that is,

$$\frac{3+5x+x^2}{2+x} = 3 + x$$
 with a remainder of -3

or

 $3 + 5x + x^2 = (3 + x)(2 + x) - 3$

polyroots (c) find the roots of polynomial c and returns them in complex row vector (complex even if c is real). For instance, polyroots((3,5,1)) returns (-4.303+0i, -.697+0i) (the roots of $3+5x+x^2$ are -4.303 and -.697).

Syntax

numeric vector	<pre>polyeval(numeric rowvector c, numeric vector x)</pre>
numeric rowvector	<pre>polysolve(numeric vector y, numeric vector x)</pre>
numeric rowvector	<pre>polytrim(numeric vector c)</pre>
numeric rowvector numeric rowvector	<pre>polyderiv(numeric rowvector c, real scalar i) polyinteg(numeric rowvector c, real scalar i)</pre>
numeric rowvector numeric rowvector void	polyadd(numeric rowvector c_1 , numeric rowvector c_2) polymult(numeric rowvector c_1 , numeric rowvector c_2) polydiv(numeric rowvector c_1 , numeric rowvector c_2 , c_q , c_r)
complex rowvector	polyroots(numeric rowvector c)

In the above, row vector c contains the coefficients for a cols(c) - 1 degree polynomial. For instance,

$$c = (4, 2, 1)$$

records the polynomial

 $4 + 2x + x^2$

Remarks and examples

Given the real or complex coefficients c that define an n-1 degree polynomial in x, polyroots(c) returns the n-1 roots for which

$$0 = c_1 + c_2 x^1 + c_3 x^2 + \dots + c_n x^{n-1}$$

polyroots (c) obtains the roots by calculating the eigenvalues of the companion matrix. The $(n-1) \times (n-1)$ companion matrix for the polynomial defined by c is

	$\left[-c_{n-1}s\right]$	$-c_{n-2}s$	• • •	$-c_2s$	$-c_1s$
<i>C</i> =	1	0	• • •	0	0
	0	1		0	0
	:	:	·.	:	:
	0	0	• • •	1	0
	0	0		0	1

where $s = 1/c_n$ if c is real and

$$s = C \bigg(\frac{\operatorname{Re}(c_n)}{\operatorname{Re}(c_n)^2 + \operatorname{Im}(c_n)^2}, \frac{-\operatorname{Im}(c_n)}{\operatorname{Re}(c_n)^2 + \operatorname{Im}(c_n)^2} \bigg)$$

otherwise.

As in all nonsymmetric eigenvalue problems, the returned roots are complex and sorted from largest to smallest, see [M-5] eigensystem().

Conformability

polyeval(c, x): c: $1 \times n, n > 0$ $r \times 1$ or $1 \times c$ x: result: $r \times 1$ or $1 \times c$ polysolve(y, x): $n \times 1$ or $1 \times n, n \ge 1$ y: $n \times 1$ or $1 \times n$ x: $1 \times k$, 1 < k < nresult: polytrim(c): $1 \times n$ c: $1 \times k$, 1 < k < nresult: polyderiv(c, i): c: $1 \times n$, n > 0i: 1×1 , *i* may be negative result: $1 \times \max(1, n-i)$ polyinteg(c, i): $1 \times n, n > 0$ c: i: 1×1 , *i* may be negative $1 \times \max(1, n+i)$ result: $polyadd(c_1, c_2)$: $1 \times n_1, \quad n_1 > 0$ c_1 : $c_2:$ 1 × $n_2,$ $n_2 > 0$ $1 \times \max(n_1, n_2)$ result: $polymult(c_1, c_2)$: $c_1: \qquad 1\times n_1, \quad n_1>0$ $1 \times n_2, n_2 > 0$ c_2 : *result*: $1 \times n_1 + n_2 - 1$ $polydiv(c_1, c_2, c_q, c_r):$ input: $1 \times n_1, \quad n_1 > 0$ c_1 : $1 \times n_2, \quad n_2 > 0$ c_2 : output: $1 \times k_1, \quad 1 \le k_1 \le \max(n_1 - n_2 + 1, 1)$ c_q : $1 \times k_2, \quad 1 \le k_2 \le \max(n_1 - n_2, 1)$ c_r : polyroots(c): $1 \times n_i$, n > 0c: $1 \times k - 1$, k = cols(polytrim(c))result:

Diagnostics

All functions abort with an error if a polynomial coefficient row vector is void, but they do not necessarily give indicative error messages as to the problem. Polynomial coefficient row vectors may contain missing values.

polyderiv(c, i) returns c when i = 0. It returns polyinteg(c, -i) when i < 0. It returns (0) when i is missing (think of missing as positive infinity).

polyinteg(c, i) returns c when i = 0. It returns polyderiv(c, -i) when i < 0. It aborts with error if i is missing (think of missing as positive infinity).

polyroots(c) returns a vector of missing values if any element of c equals missing.

Also see

[M-4] Mathematical — Important mathematical functions

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