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**invsym()** — Symmetric real matrix inversion

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# **Description**

invsym(A) returns a generalized inverse of real, symmetric, positive-semidefinite matrix A.

invsym(A, order) does the same but allows you to specify which columns are to be swept first.

 $_{\rm invsym}(A)$  and  $_{\rm invsym}(A, order)$  do the same thing as  ${\rm invsym}(A)$  and  ${\rm invsym}(A, order)$  except that A is replaced with the generalized inverse result rather than the result being returned.  $_{\rm invsym}()$  uses less memory than  ${\rm invsym}()$ .

invsym() and \_invsym() are the routines Stata uses for calculating inverses of symmetric matrices.

Also see [M-5] luinv(), [M-5] qrinv(), and [M-5] pinv() for general matrix inversion.

# **Syntax**

real matrix invsym(real matrix A)

real matrix invsym(real matrix A, real vector order)

void \_invsym(real matrix A)

void \_\_invsym(real matrix A, real vector order)

# Remarks and examples

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Remarks are presented under the following headings:

Definition of generalized inverse Specifying the order in which columns are dropped Determining the rank, or counting the number of dropped columns Extracting linear dependencies

### Definition of generalized inverse

When the matrix is full rank and positive semidefinite, the matrix A becomes positive definite and the generalized inverse equals the inverse, that is, assuming A is  $n \times n$ ,

```
invsym(A)*A = A*invsym(A) = I(n)
```

or, at least the above restriction is true up to roundoff error. When A is not full rank, the generalized inverse invsym() satisfies (ignoring roundoff error)

$$A*invsym(A)*A = A$$

```
invsym(A)*A*invsym(A) = invsym(A)
```

In the generalized case, there are an infinite number of inverse matrices that can satisfy the above restrictions. The one invsym() chooses is one that sets entire columns (and therefore rows) to 0, thus treating A as if it were of reduced dimension. Which columns (rows) are selected is determined on the basis of minimizing roundoff error.

In the above we talk as if determining whether a matrix is of full rank is an easy calculation. That is not true. Because of the roundoff error in the manufacturing and recording of A itself, columns that ought to be perfectly collinear will not be and yet you will still want invsym() to behave as if they were invsym() tolerates a little deviation from collinearity in making the perfectly collinear determination.

#### Specifying the order in which columns are dropped

Left to make the decision itself, invsym() will choose which columns to drop (to set to 0) to minimize the overall roundoff error of the generalized inverse calculation. If column 1 and column 3 are collinear, then invsym() will choose to drop column 1 or column 3.

There are occasions, however, when you would like to ensure that a particular column or set of columns are not dropped. Perhaps column 1 corresponds to the intercept of a regression model and you would much rather, if one of columns 1 and 3 has to be dropped, that it be column 3.

Order allows you to specify the columns of the matrix that you would prefer not be dropped in the generalized inverse calculation. In the above example, to prevent column 1 from being dropped, you could code

```
invsym(A, 1)
```

If you would like to keep columns 1, 5, and 10 from being dropped, you can code

```
invsym(A, (1,5,10))
```

Specifying columns not to be dropped does not guarantee that they will not be dropped because they still might be collinear with each other or they might equal constants. However, if any other column can be dropped to satisfy your desire, it will be.

### Determining the rank, or counting the number of dropped columns

If a column is dropped, 0 will appear on the corresponding diagonal entry. Hence, the rank of the original matrix can be extracted after inversion by invsym():

```
: Ainv = invsym(A)
: rank = rows(Ainv)-diagOcnt(Ainv)
```

See [M-5] diag0cnt().

#### **Extracting linear dependencies**

The linear dependencies can be read from the rows of A\*invsym(A):

The above is interpreted to mean

$$x_1 = -x_2 + x_3$$
$$x_2 = x_2$$
$$x_3 = x_3$$

ignoring roundoff error.

# Conformability

```
invsym(A), invsym(A, order):
               A:
                        n \times n
                                   or k \times 1, k \leq n
           order:
                         1 \times k
                                                             (optional)
           result:
                        n \times n
_{\rm invsym}(A), _{\rm invsym}(A, order):
               A:
                        n \times n
                                   or k \times 1, k \le n (optional)
           order:
                         1 \times k
     output:
               A:
                        n \times n
```

# **Diagnostics**

invsym(A), invsym(A, order),  $\_invsym(A)$ , and  $\_invsym(A, order)$  assume that A is symmetric; they do not check. If A is nonsymmetric, they treat it as if it were symmetric and equal to its upper triangle.

invsym() and \_invsym() return a result containing missing values if A contains missing values.

\_invsym() aborts with error if A is a view. Both functions abort with argument-out-of-range error if order is specified and contains values less than 1, greater than rows (A), or the same value more than once.

invsym() and \_invsym() return a matrix of zeros if A is not positive semidefinite.

### Also see

```
    [M-5] cholinv() — Symmetric, positive-definite matrix inversion
    [M-5] luinv() — Square matrix inversion
    [M-5] qrinv() — Generalized inverse of matrix via QR decomposition
    [M-5] pinv() — Moore-Penrose pseudoinverse
    [M-5] diag0cnt() — Count zeros on diagonal
    [M-4] matrix — Matrix functions
```

[M-4] solvers — Functions to solve AX=B and to obtain A inverse