ghkfast( ) — GHK multivariate normal simulator using pregenerated points

Description Syntax Remarks and examples Conformability Diagnostics Also see

Description

Please see [M-5] **ghk( )**. The routines documented here do the same thing, but `ghkfast()` can be faster at the expense of using more memory. First, code *S* = `ghkfast_init(...)` and then use `ghkfast(`*S*`, ...)` to obtain the simulated values. There is a time savings because the simulation points are generated once in `ghkfast_init()`, whereas for `ghk()` the points are generated on each call to `ghk()`. Also, `ghkfast()` can generate simulated probabilities from the generalized Halton sequence; see [M-5] **halton( )**.

`ghkfast_init(`*n*`,` *npts*`,` *dim*`,` *method*`)` computes the simulation points to be used by `ghkfast()`. Inputs *n*, *npts*, and *dim* are the number of observations, the number of repetitions for the simulation, and the maximum dimension of the multivariate normal (MVN) distribution, respectively. Input *method* specifies the type of points to generate and can be one of `"halton"`, `"hammersley"`, `"random"`, or `"ghalton"`.

`ghkfast(`*S*`,` *X*`,` *V*`)` returns an $n \times 1$ real vector containing the simulated values of the MVN distribution with $dim \times dim$ variance–covariance matrix *V* at the points stored in the rows of the $n \times dim$ matrix *X*.

`ghkfast(`*S*`,` *X*`,` *V*`,` *dfdx*`,` *dfdv*`)` does the same thing as `ghkfast(`*S*`,` *X*`,` *V*`)` but also returns the first-order derivatives of the simulated probability with respect to the rows of *X* in *dfdx* and the simulated probability derivatives with respect to `vech(`*V*`)` in *dfdv*. See `vech()` in [M-5] **vec( )** for details of the half-vectorized operator.

The `ghk_query_n(`*S*`)`, `ghk_query_npts(`*S*`)`, `ghk_query_dim(`*S*`)`, and `ghk_query_method(`*S*`)` functions extract the number of observations, number of simulation points, maximum dimension, and method of point-set generation that is specified in the construction of the transmorphic object *S*. Use `ghk_query_rseed(`*S*`)` to retrieve the uniform random-variate seed used to generate the `"random"` or `"ghalton"` point sets. The `ghkfast_query_pointset_i(`*S*`,` *i*`)` function will retrieve the *i*th point set used to simulate the MVN probability for the *i*th observation.

The `ghkfast_i(`*S*`,` *X*`,` *V*`,` *i*`, ...)` function computes the probability and derivatives for the *i*th observation, $i = 1, \ldots, n$.

Syntax

S = `ghkfast_init(`*real scalar n*`,` *npts*`,` *dim*`,` *string scalar method*`)`

(varies)	`ghkfast_init_pivot(`*S* [`,` *real scalar pivot*]`)`
(varies)	`ghkfast_init_antithetics(`*S* [`,` *real scalar anti*]`)`
real scalar	`ghkfast_query_n(`*S*`)`
real scalar	`ghkfast_query_npts(`*S*`)`
real scalar	`ghkfast_query_dim(`*S*`)`
string scalar	`ghkfast_query_method(`*S*`)`
string scalar	`ghkfast_query_rseed(`*S*`)`
real matrix	`ghkfast_query_pointset_i(`*S*`,` *i*`)`
real colvector	`ghkfast(`*S*`,` *real matrix X*`,` *V*`)`
real colvector	`ghkfast(`*S*`,` *real matrix X*`,` *V*`,` *dfdx*`,` *dfdv*`)`
real scalar	`ghkfast_i(`*S*`,` *real matrix X*`,` *V*`,` *i*`)`
real scalar	`ghkfast_i(`*S*`,` *real matrix X*`,` *V*`,` *i*`,` *dfdx*`,` *dfdv*`)`

where *S*, if it is declared, should be declared

```
transmorphic S
```

and where *method* specified in `ghkfast_init()` is

method	Description
`"halton"`	Halton sequences
`"hammersley"`	Hammersley's variation of the Halton set
`"random"`	pseudorandom uniforms
`"ghalton"`	generalized Halton sequences

Remarks and examples

For problems where repetitive calls to the GHK algorithm are required, `ghkfast()` might be a preferred alternative to `ghk()`. Generating the points once at the outset of a program produces a speed increase. For problems with many observations or many simulation points per observation, `ghkfast()` will be faster than `ghk()` at the cost of requiring more memory.

If `ghkfast()` is used within a likelihood evaluator for `ml` or `optimize()`, you will need to store the transmorphic object *S* as an external global and reuse the object with each likelihood evaluation. Alternatively, the initialization function for `optimize()`, `optimize_init_argument()`, can be used.

Prior to calling `ghkfast()`, call `ghkfast_init_npivot(`*S*`, 1)` to turn off the integration interval pivoting that takes place in `ghkfast()`. By default, `ghkfast()` pivots the wider intervals of integration (and associated rows/columns of the covariance matrix) to the interior of the multivariate integration to improve quadrature accuracy. This option may be useful when `ghkfast()` is used in a likelihood evaluator for [R] **ml** or [M-5] **optimize( )** and few simulation points are used for each observation. Here the pivoting may cause discontinuities when computing numerical second-order derivatives using finite differencing (for the Newton–Raphson technique), resulting in a non–positive-definite Hessian.

Also the sequences `"halton"`, `"hammersley"`, and `"random"`, `ghkfast()` will use the generalized Halton sequence, `"ghalton"`. Generalized Halton sequences have the same uniform coverage (low discrepancy) as the Halton sequences with the addition of a pseudorandom uniform component. Therefore, `"ghalton"` sequences are like `"random"` sequences in that you should set the random-number seed before using them if you wish to replicate the same point set; see [M-5] **runiform( )**.

Conformability

All initialization functions have 1×1 inputs and have 1×1 or *void* outputs, and all query functions have the *transmorphic* input and 1×1 outputs except

`ghkfast_init(`*n*`, `*npts*`, `*dim*`, `*method*`)`:

input:		
	n:	1×1
	npts:	1×1
	dim:	1×1
	method:	1×1
output:		
	result:	*transmorphic*

`ghkfast_query_pointset_i(`*S*`, `*i*`)`:

input:		
	S:	*transmorphic*
	i:	1×1
output:		
	result:	*npts* $\times$ *dim*

`ghkfast(`*S*`, `*X*`, `*V*`)`:

input:		
	S:	*transmorphic*
	X:	*n* $\times$ *dim*
	V:	*dim* $\times$ *dim* (symmetric, positive definite)
output:		
	result:	*n* $\times$ 1

`ghkfast(`*S*`,` *X*`,` *V*`,` *dfdx*`,` *dfdv*`)`:

input:

S:	*transmorphic*
X:	$n \times dim$
V:	$dim \times dim$ (symmetric, positive definite)

output:

result:	$n \times 1$
dfdx:	$n \times dim$
dfdv:	$n \times dim(dim+1)/2$

`ghkfast_i(`*S*`,` *X*`,` *V*`,` *i*`,` *dfdx*`,` *dfdv*`)`:

input:

S:	*transmorphic*
X:	$n \times dim$ or $1 \times dim$
V:	$dim \times dim$ (symmetric, positive definite)
i:	1×1 $(1 \leq i \leq n)$

output:

result:	n × 1
dfdx:	$1 \times dim$
dfdv:	$1 \times dim(dim+1)/2$

Diagnostics

`ghkfast_init(`*n*`,` *npts*`,` *dim*`,` *method*`)` aborts with error if the dimension, *dim*, is greater than 20.

`ghkfast(`*S*`,` *X*`,` *V*`, ...)` and `ghkfast_i(`*S*`,` *X*`,` *V*`,` *i*`, ...)` require that *V* be symmetric and positive definite. If *V* is not positive definite, then the returned vector (scalar) is filled with missings.

Also see

[M-5] **ghk( )** — Geweke–Hajivassiliou–Keane (GHK) multivariate normal simulator

[M-5] **halton( )** — Generate a Halton or Hammersley set

[M-4] **Statistical** — Statistical functions