Description

`irtgraph tif` plots the test information function (TIF) for the currently fitted IRT model.

Quick start

2PL model for binary items b1 to b10

```
irt 2pl b1-b10
```

Plot the TIF for the fitted model

```
irtgraph tif
```

Plot the TIF and its standard error

```
irtgraph tif, se
```

Fit a group 2PL model

```
irt 2pl b1-b9, group(female)
```

Plot the TIFs for the fitted model for both groups

```
irtgraph tif
```

Menu

Statistics > IRT (item response theory)
Syntax

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irtgraph tif [ , options ]
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Options

Plots

`se[ (line_options) ]` requests the standard error of the TIF be plotted. The optional `line_options` specify how the lines are rendered; see [G-3] `line_options`.

`range(# #)` specifies the range of values for $\theta$. This option requires a pair of numbers identifying the minimum and maximum. The default is `range(-4 4)`.

Line

`line_options` affect the rendition of the plotted TIF; see [G-3] `line_options`.

Add plots

`addplot(plot)` allows adding more graph `twoway` plots to the graph; see [G-3] `addplot_option`.

Y axis, X axis, Titles, Legend, Overall

`twoway_options` are any of the options documented in [G-3] `twoway_options`, excluding by(). These include options for titling the graph (see [G-3] `title_options`) and for saving the graph to disk (see [G-3] `saving_option`).

Data

`n(#)` specifies the number of points at which the plotted lines are to be evaluated. The default is `n(300)`.

`data(filename[, replace])` saves the plot data to a Stata data file.
Remarks and examples

`irtgraph tif` plots the TIF after estimating the parameters of an IRT model using `irt`.

In IRT, the term “information” is used to describe reliability or precision of an item or a whole instrument. More reliable instruments measure the latent trait around the estimated difficulty parameter with greater precision.

The TIF is useful in test development where, depending on the specific needs, the test can be chosen to cover the whole spectrum or to focus on a particular range of the ability scale. For tests with alternate formats, TIFs are used to ensure the formats carry the same information across the targeted latent trait range.

➤ Example 1: TIF for binary items

We continue with the 2PL model from example 1 of [IRT] `irt 2pl`. Recall that we fit a 2PL model to the nine binary items.
. use https://www.stata-press.com/data/r16/masc1
(Data from De Boeck & Wilson (2004))
. irt 2pl q1-q9
Fitting fixed-effects model:
Iteration 0: log likelihood = -4275.6606
Iteration 1: log likelihood = -4269.7861
Iteration 2: log likelihood = -4269.7825
Iteration 3: log likelihood = -4269.7825
Fitting full model:
Iteration 0: log likelihood = -4146.9386
Iteration 1: log likelihood = -4119.3568
Iteration 2: log likelihood = -4118.4716
Iteration 3: log likelihood = -4118.4697
Iteration 4: log likelihood = -4118.4697
Two-parameter logistic model
Number of obs = 800
Log likelihood = -4118.4697
|                    | Coef.  | Std. Err. |      z |   P>|z|   | [95% Conf. Interval] |
|--------------------|--------|-----------|--------|--------|----------------------|
| q1 Discrim         | 1.615292 | .2436467  | 6.63   | 0.000  | 1.137754 to 2.092831 |
| Diff               | -.4745635 | .074638 | -6.36 | 0.000 | -.6208513 to -.3282757 |
| q2 Discrim         | .6576171 | .1161756  | 5.66   | 0.000  | .4299171 to .885317  |
| Diff               | -.1513023 | .1202807 | -1.26 | 0.208 | -.3870481 to .0844435 |
| q3 Discrim         | .9245051 | .1569806  | 5.89   | 0.000  | .6168289 to 1.232181 |
| Diff               | -1.70918 | .242266  | -7.05 | 0.000 | -2.184012 to -1.234347 |
| q4 Discrim         | .8186403 | .1284832  | 6.37   | 0.000  | .5668179 to 1.070463 |
| Diff               | .3296791 | .1076105  | 3.06   | 0.002  | .1187663 to .5405919 |
| q5 Discrim         | .8956621 | .1535128  | 5.83   | 0.000  | .5947825 to 1.196542 |
| Diff               | 1.591164 | .2325918  | 6.84   | 0.000  | 1.135293 to 2.047036 |
| q6 Discrim         | .9828441 | .147888   | 6.65   | 0.000  | .6929889 to 1.272699 |
| Diff               | .6229654 | .1114902  | 5.59   | 0.000  | .4044373 to .8414708 |
| q7 Discrim         | .3556064 | .1113146  | 3.19   | 0.001  | .1374337 to .5737791 |
| Diff               | 2.840278 | .8717471  | 3.26   | 0.001  | 1.131685 to 4.548871 |
| q8 Discrim         | 1.399926 | .233963   | 5.98   | 0.000  | .9413668 to 1.858485 |
| Diff               | -1.714416 | .1925531 | -8.90 | 0.000 | -2.091814 to -1.337019 |
| q9 Discrim         | .6378452 | .1223972  | 5.21   | 0.000  | .3979512 to .8777392 |
| Diff               | -1.508254 | .2787386 | -5.41 | 0.000 | -2.054571 to -.9619361 |

In example 1 of [IRT] irtgraph tif, we plotted IIFs and noted that items provided more information over the negative range of the latent trait than over the positive range. This asymmetry is also present in the TIF, which we plot below.
The test provides the most information around the latent trait between approximately $-1.5$ to 0. If we wished for the test to provide more information around a particular latent trait range, we could include additional items that contribute more information within the desired range. Looking at the standard error curve, we observe that the amount of information provided by the test at $\theta$ is inversely related to the precision with which ability is estimated at that point.

**Methods and formulas**

Test information is the negative of the expectation of the second derivative with respect to $\theta$ of the log likelihood defined in *Methods and formulas* of [IRT] *irt hybrid*.

$$I(\theta) = -E\left\{\frac{\partial^2}{\partial \theta^2} \log L(B)\right\}$$

Given an instrument consisting of $I$ items, the formula above reduces to

$$I(\theta) = \frac{1}{\sigma^2_\theta} + \sum_{i=1}^{I} I_i(\theta)$$

where $I_i(\theta)$ is as defined in *Methods and formulas* of [IRT] *irtgraph iif*. Thus, the TIF is the sum of the individual IIFs and the prior variance of the latent trait, $\sigma^2_\theta$. *irt* fits IRT models with $\sigma^2_\theta$ constrained to 1.

The standard error of the TIF is given by

$$se(\hat{\theta}) = \frac{1}{\sqrt{I(\theta)}}$$
Reference


Also see

[IRT] irt — Introduction to IRT models
[IRT] irt 1pl — One-parameter logistic model
[IRT] irt 2pl — Two-parameter logistic model
[IRT] irt 3pl — Three-parameter logistic model
[IRT] irt grm — Graded response model
[IRT] irt hybrid — Hybrid IRT models
[IRT] irt nrm — Nominal response model
[IRT] irt pcm — Partial credit model
[IRT] irt rsm — Rating scale model
[IRT] irtgraph iif — Item information function plot