

Mathematical functions

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## Contents

<code>abs(<i>x</i>)</code>	the absolute value of <i>x</i>
<code>ceil(<i>x</i>)</code>	the unique integer <i>n</i> such that $n - 1 < x \leq n$ ; <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>ceil(.a) = .a</code>
<code>cloglog(<i>x</i>)</code>	the complementary log-log of <i>x</i>
<code>comb(<i>n</i>,<i>k</i>)</code>	the combinatorial function $n!/\{k!(n-k)!\}$
<code>digamma(<i>x</i>)</code>	the <code>digamma()</code> function, $d \ln \Gamma(x)/dx$
<code>exp(<i>x</i>)</code>	the exponential function $e^x$
<code>expm1(<i>x</i>)</code>	$e^x - 1$ with higher precision than <code>exp(<i>x</i>) - 1</code> for small values of $ x $
<code>floor(<i>x</i>)</code>	the unique integer <i>n</i> such that $n \leq x < n + 1$ ; <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>floor(.a) = .a</code>
<code>int(<i>x</i>)</code>	the integer obtained by truncating <i>x</i> toward 0 (thus, <code>int(5.2) = 5</code> and <code>int(-5.8) = -5</code> ); <i>x</i> (not “.”) if <i>x</i> is missing, meaning that <code>int(.a) = .a</code>
<code>invcloglog(<i>x</i>)</code>	the inverse of the complementary log-log function of <i>x</i>
<code>invlogit(<i>x</i>)</code>	the inverse of the logit function of <i>x</i>
<code>ln(<i>x</i>)</code>	the natural logarithm, $\ln(x)$
<code>ln1m(<i>x</i>)</code>	the natural logarithm of $1 - x$ with higher precision than <code>ln(1 - x)</code> for small values of $ x $
<code>ln1p(<i>x</i>)</code>	the natural logarithm of $1 + x$ with higher precision than <code>ln(1 + x)</code> for small values of $ x $
<code>lnfactorial(<i>n</i>)</code>	the natural log of <i>n</i> factorial = $\ln(n!)$
<code>lngamma(<i>x</i>)</code>	$\ln\{\Gamma(x)\}$
<code>log(<i>x</i>)</code>	a synonym for <code>ln(<i>x</i>)</code>
<code>log10(<i>x</i>)</code>	the base-10 logarithm of <i>x</i>
<code>log1m(<i>x</i>)</code>	a synonym for <code>ln1m(<i>x</i>)</code>
<code>log1p(<i>x</i>)</code>	a synonym for <code>ln1p(<i>x</i>)</code>
<code>logit(<i>x</i>)</code>	the log of the odds ratio of <i>x</i> , $\text{logit}(x) = \ln\{x/(1-x)\}$
<code>max(<i>x</i><sub>1</sub>,<i>x</i><sub>2</sub>,...,<i>x</i><sub><i>n</i></sub>)</code>	the maximum value of <i>x</i> <sub>1</sub> , <i>x</i> <sub>2</sub> , ..., <i>x</i> <sub><i>n</i></sub>
<code>min(<i>x</i><sub>1</sub>,<i>x</i><sub>2</sub>,...,<i>x</i><sub><i>n</i></sub>)</code>	the minimum value of <i>x</i> <sub>1</sub> , <i>x</i> <sub>2</sub> , ..., <i>x</i> <sub><i>n</i></sub>
<code>mod(<i>x</i>,<i>y</i>)</code>	the modulus of <i>x</i> with respect to <i>y</i>
<code>reldif(<i>x</i>,<i>y</i>)</code>	the “relative” difference $ x - y /( y  + 1)$ ; 0 if both arguments are the same type of extended missing value; <i>missing</i> if only one argument is missing or if the two arguments are two different types of <i>missing</i>

<code>round(x, y)</code> or <code>round(x)</code>	$x$ rounded in units of $y$ or $x$ rounded to the nearest integer if the argument $y$ is omitted; $x$ (not “.”) if $x$ is missing (meaning that <code>round(.a) = .a</code> and that <code>round(.a, y) = .a</code> if $y$ is not missing) and if $y$ is missing, then “.” is returned
<code>sign(x)</code>	the sign of $x$ : $-1$ if $x < 0$ , $0$ if $x = 0$ , $1$ if $x > 0$ , or <i>missing</i> if $x$ is missing
<code>sqrt(x)</code>	the square root of $x$
<code>sum(x)</code>	the running sum of $x$ , treating missing values as zero
<code>trigamma(x)</code>	the second derivative of <code>lngamma(x) = d<sup>2</sup> lnΓ(x)/dx<sup>2</sup></code>
<code>trunc(x)</code>	a synonym for <code>int(x)</code>

## Functions

`abs(x)`

Description: the absolute value of  $x$   
 Domain:  $-8e+307$  to  $8e+307$   
 Range:  $0$  to  $8e+307$

`ceil(x)`

Description: the unique integer  $n$  such that  $n - 1 < x \leq n$ ;  $x$  (not “.”) if  $x$  is missing, meaning that `ceil(.a) = .a`  
 Also see `floor(x)`, `int(x)`, and `round(x)`.  
 Domain:  $-8e+307$  to  $8e+307$   
 Range: integers in  $-8e+307$  to  $8e+307$

`cloglog(x)`

Description: the complementary log-log of  $x$   

$$\text{cloglog}(x) = \ln\{-\ln(1-x)\}$$
  
 Domain:  $0$  to  $1$   
 Range:  $-8e+307$  to  $8e+307$

`comb(n, k)`

Description: the combinatorial function  $n!/\{k!(n-k)!\}$   
 Domain  $n$ : integers  $1$  to  $1e+305$   
 Domain  $k$ : integers  $0$  to  $n$   
 Range:  $0$  to  $8e+307$  or *missing*

`digamma(x)`

Description: the `digamma()` function,  $d \ln \Gamma(x)/dx$   
 This is the derivative of `lngamma(x)`. The `digamma(x)` function is sometimes called the psi function,  $\psi(x)$ .  
 Domain:  $-1e+15$  to  $8e+307$   
 Range:  $-8e+307$  to  $8e+307$  or *missing*

`exp(x)`

Description: the exponential function  $e^x$   
 This function is the inverse of `ln(x)`. To compute  $e^x - 1$  with high precision for small values of  $|x|$ , use `expm1(x)`.  
 Domain:  $-8e+307$  to  $709$   
 Range:  $0$  to  $8e+307$

**expm1( $x$ )**

Description:  $e^x - 1$  with higher precision than  $\exp(x) - 1$  for small values of  $|x|$

Domain:  $-8e+307$  to  $709$

Range:  $-1$  to  $8e+307$

**floor( $x$ )**

Description: the unique integer  $n$  such that  $n \leq x < n + 1$ ;  $x$  (not “.”) if  $x$  is missing, meaning that  $\text{floor}(.a) = .a$

Also see [ceil\( \$x\$ \)](#), [int\( \$x\$ \)](#), and [round\( \$x\$ \)](#).

Domain:  $-8e+307$  to  $8e+307$

Range: integers in  $-8e+307$  to  $8e+307$

**int( $x$ )**

Description: the integer obtained by truncating  $x$  toward 0 (thus,  $\text{int}(5.2) = 5$  and  $\text{int}(-5.8) = -5$ );  $x$  (not “.”) if  $x$  is missing, meaning that  $\text{int}(.a) = .a$

One way to obtain the closest integer to  $x$  is  $\text{int}(x + \text{sign}(x)/2)$ , which simplifies to  $\text{int}(x + 0.5)$  for  $x \geq 0$ . However, use of the [round\(\)](#) function is preferred. Also see [round\( \$x\$ \)](#), [ceil\( \$x\$ \)](#), and [floor\( \$x\$ \)](#).

Domain:  $-8e+307$  to  $8e+307$

Range: integers in  $-8e+307$  to  $8e+307$

**invcloglog( $x$ )**

Description: the inverse of the complementary log-log function of  $x$

$$\text{invcloglog}(x) = 1 - \exp\{-\exp(x)\}$$

Domain:  $-8e+307$  to  $8e+307$

Range: 0 to 1 or *missing*

**invlogit( $x$ )**

Description: the inverse of the logit function of  $x$

$$\text{invlogit}(x) = \exp(x) / \{1 + \exp(x)\}$$

Domain:  $-8e+307$  to  $8e+307$

Range: 0 to 1 or *missing*

**ln( $x$ )**

Description: the natural logarithm,  $\ln(x)$

This function is the inverse of  $\exp(x)$ . The logarithm of  $x$  in base  $b$  can be calculated via  $\log_b(x) = \log_a(x) / \log_a(b)$ . Hence,

$$\log_5(x) = \ln(x) / \ln(5) = \log(x) / \log(5) = \log_{10}(x) / \log_{10}(5)$$

$$\log_2(x) = \ln(x) / \ln(2) = \log(x) / \log(2) = \log_{10}(x) / \log_{10}(2)$$

You can calculate  $\log_b(x)$  by using the formula that best suits your needs. To compute  $\ln(1 - x)$  and  $\ln(1 + x)$  with high precision for small values of  $|x|$ , use [ln1m\( \$x\$ \)](#) and [ln1p\( \$x\$ \)](#), respectively.

Domain:  $1e-323$  to  $8e+307$

Range:  $-744$  to  $709$

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### `ln1m(x)`

Description: the natural logarithm of  $1 - x$  with higher precision than `ln(1 - x)` for small values of  $|x|$

Domain:  $-8e+307$  to  $1 - c(\text{epsdouble})$

Range:  $-37$  to  $709$

### `ln1p(x)`

Description: the natural logarithm of  $1 + x$  with higher precision than `ln(1 + x)` for small values of  $|x|$

Domain:  $-1 + c(\text{epsdouble})$  to  $8e+307$

Range:  $-37$  to  $709$

### `lnfactorial(n)`

Description: the natural log of  $n$  factorial =  $\ln(n!)$

To calculate  $n!$ , use `round(exp(lnfactorial(n)), 1)` to ensure that the result is an integer. Logs of factorials are generally more useful than the factorials themselves because of overflow problems.

Domain: integers 0 to  $1e+305$

Range: 0 to  $8e+307$

### `lngamma(x)`

Description:  $\ln\{\Gamma(x)\}$

Here the gamma function,  $\Gamma(x)$ , is defined by  $\Gamma(x) = \int_0^\infty t^{x-1}e^{-t}dt$ . For integer values of  $x > 0$ , this is  $\ln((x - 1)!)$ .

`lngamma(x)` for  $x < 0$  returns a number such that `exp(lngamma(x))` is equal to the absolute value of the gamma function,  $\Gamma(x)$ . That is, `lngamma(x)` always returns a real (not complex) result.

Domain:  $-2,147,483,648$  to  $1e+305$  (excluding negative integers)

Range:  $-8e+307$  to  $8e+307$

### `log(x)`

Description: a synonym for `ln(x)`

### `log10(x)`

Description: the base-10 logarithm of  $x$

Domain:  $1e-323$  to  $8e+307$

Range:  $-323$  to  $308$

### `log1m(x)`

Description: a synonym for `ln1m(x)`

### `log1p(x)`

Description: a synonym for `ln1p(x)`

### `logit(x)`

Description: the log of the odds ratio of  $x$ ,  $\text{logit}(x) = \ln\{x/(1 - x)\}$

Domain: 0 to 1 (exclusive)

Range:  $-8e+307$  to  $8e+307$  or *missing*

$\max(x_1, x_2, \dots, x_n)$

Description: the maximum value of  $x_1, x_2, \dots, x_n$

Unless all arguments are *missing*, missing values are ignored.

$\max(2, 10, ., 7) = 10$

$\max(., ., .) = .$

Domain  $x_1$ :  $-8e+307$  to  $8e+307$  or *missing*

Domain  $x_2$ :  $-8e+307$  to  $8e+307$  or *missing*

...

Domain  $x_n$ :  $-8e+307$  to  $8e+307$  or *missing*

Range:  $-8e+307$  to  $8e+307$  or *missing*

$\min(x_1, x_2, \dots, x_n)$

Description: the minimum value of  $x_1, x_2, \dots, x_n$

Unless all arguments are *missing*, missing values are ignored.

$\min(2, 10, ., 7) = 2$

$\min(., ., .) = .$

Domain  $x_1$ :  $-8e+307$  to  $8e+307$  or *missing*

Domain  $x_2$ :  $-8e+307$  to  $8e+307$  or *missing*

...

Domain  $x_n$ :  $-8e+307$  to  $8e+307$  or *missing*

Range:  $-8e+307$  to  $8e+307$  or *missing*

$\text{mod}(x, y)$

Description: the modulus of  $x$  with respect to  $y$

$\text{mod}(x, y) = x - y \text{ floor}(x/y)$

$\text{mod}(x, 0) = .$

Domain  $x$ :  $-8e+307$  to  $8e+307$

Domain  $y$ : 0 to  $8e+307$

Range: 0 to  $8e+307$

$\text{reldif}(x, y)$

Description: the “relative” difference  $|x - y|/(|y| + 1)$ ; 0 if both arguments are the same type of extended missing value; *missing* if only one argument is missing or if the two arguments are two different types of *missing*

Domain  $x$ :  $-8e+307$  to  $8e+307$  or *missing*

Domain  $y$ :  $-8e+307$  to  $8e+307$  or *missing*

Range:  $-8e+307$  to  $8e+307$  or *missing*

`round(x, y)` or `round(x)`

Description:  $x$  rounded in units of  $y$  or  $x$  rounded to the nearest integer if the argument  $y$  is omitted;  $x$  (not “.”) if  $x$  is missing (meaning that `round(.a) = .a` and that `round(.a, y) = .a` if  $y$  is not missing) and if  $y$  is missing, then “.” is returned

For  $y = 1$ , or with  $y$  omitted, this amounts to the closest integer to  $x$ ; `round(5.2, 1)` is 5, as is `round(4.8, 1)`; `round(-5.2, 1)` is -5, as is `round(-4.8, 1)`. The rounding definition is generalized for  $y \neq 1$ . With  $y = 0.01$ , for instance,  $x$  is rounded to two decimal places; `round(sqrt(2), .01)` is 1.41.  $y$  may also be larger than 1; `round(28, 5)` is 30, which is 28 rounded to the closest multiple of 5. For  $y = 0$ , the function is defined as returning  $x$  unmodified. Also see `int(x)`, `ceil(x)`, and `floor(x)`.

Domain  $x$ :  $-8e+307$  to  $8e+307$

Domain  $y$ :  $-8e+307$  to  $8e+307$

Range:  $-8e+307$  to  $8e+307$

`sign(x)`

Description: the sign of  $x$ : -1 if  $x < 0$ , 0 if  $x = 0$ , 1 if  $x > 0$ , or *missing* if  $x$  is missing

Domain:  $-8e+307$  to  $8e+307$  or *missing*

Range: -1, 0, 1 or *missing*

`sqrt(x)`

Description: the square root of  $x$

Domain: 0 to  $8e+307$

Range: 0 to  $1e+154$

`sum(x)`

Description: the running sum of  $x$ , treating missing values as zero

For example, following the command `generate y=sum(x)`, the  $j$ th observation on  $y$  contains the sum of the first through  $j$ th observations on  $x$ . See [D] [egen](#) for an alternative sum function, `total()`, that produces a constant equal to the overall sum.

Domain: all real numbers or *missing*

Range:  $-8e+307$  to  $8e+307$  (excluding *missing*)

`trigamma(x)`

Description: the second derivative of  $\text{ln}\gamma(x) = d^2 \ln\Gamma(x)/dx^2$

The `trigamma()` function is the derivative of `digamma(x)`.

Domain:  $-1e+15$  to  $8e+307$

Range: 0 to  $8e+307$  or *missing*

`trunc(x)`

Description: a synonym for `int(x)`

## Video example

[How to round a continuous variable](#)

## References

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## Also see

- [FN] [Functions by category](#)
- [D] [egen](#) — Extensions to generate
- [D] [generate](#) — Create or change contents of variable
- [M-4] [Intro](#) — Categorical guide to Mata functions
- [U] [13.3 Functions](#)