

Description

Lags of state variables are not allowed to be included in the structural models specified in the `dsge` and `dsge1` commands. These lags do not fit into the form of a structural model that can be solved for the state-space form. However, this restriction does not prevent us from fitting models that involve the lag of a state variable. This entry shows how to define a new state variable and rewrite the equations in the required structural form.

Remarks and examples

Remarks are presented under the following headings:

A model with a lagged state variable
Parameter estimation

A model with a lagged state variable

The model in (1)–(5) is a standard monetary model in which the state-driving output growth y_t is a second-order autoregressive AR(2) process instead of a first-order autoregressive process.

$$p_t = \beta E_t(p_{t+1}) + \kappa y_t \quad (1)$$

$$y_t = E_t(y_{t+1}) - \{r_t - E_t(p_{t+1}) - z_t\} \quad (2)$$

$$r_t = \frac{1}{\beta} p_t + u_t \quad (3)$$

$$z_{t+1} = \rho_{z1} z_t + \rho_{z2} z_{t-1} + \epsilon_{t+1} \quad (4)$$

$$u_{t+1} = \rho_u u_t + \xi_{t+1} \quad (5)$$

Equation (1) specifies the structural equation for inflation p_t . Inflation is a linear combination of expected future inflation $E_t(p_{t+1})$ and output growth y_t . Equation (2) specifies the structural equation for output growth. Output growth is a linear combination of expected future output growth $E_t(y_{t+1})$, the interest rate r_t , expected future inflation, and the state z_t . The state z_t is an AR(2) process that drives output growth. Equation (3) specifies the structural equation for the interest rate. The interest rate depends on the inflation rate and the state u_t . The state u_t is an AR(1) process that drives the interest rate. The control variables in this model are p_t , y_t , and r_t . The state variables are u_t and z_t .

The AR(2) term in (4) is a problematic term because a lag of a state variable does not fit into the structure required to solve the model for the state-space form. We accommodate this term by defining a new state variable Lz_t that equals z_{t-1} and replacing z_{t-1} in (4) with this new state variable. We define a new state instead of new control because the lagged state is exogenous. These changes yield the model in (6)–(11).

$$p_t = \beta E_t(p_{t+1}) + \kappa y_t \quad (6)$$

$$y_t = E_t(y_{t+1}) - \{r_t - E_t(p_{t+1}) - z_t\} \quad (7)$$

$$r_t = \frac{1}{\beta} p_t + u_t \quad (8)$$

$$z_{t+1} = \rho_{z1} z_t + \rho_{z2} Lz_t + \epsilon_{t+1} \quad (9)$$

$$u_{t+1} = \rho_u u_t + \xi_{t+1} \quad (10)$$

$$Lz_{t+1} = z_t \quad (11)$$

We will estimate the parameters in the model in (6)–(11).

Parameter estimation

We estimate the parameters in the model in (6)–(11) using data on US interest rate r and inflation p .

```
. use https://www.stata-press.com/data/r19/usmacro2
(Federal Reserve Economic Data - St. Louis Fed, 2017-01-15)

. dsge (p      = {beta}*F.p + {kappa}*y)
>      (y      = F.y - (r - F.p - z), unobserved)
>      (r      = (1/{beta})*p + u)
>      (F.u    = {rho1}*u, state)
>      (F.z    = {rhoz1}*z + {rhoz2}*Lz, state)
>      (F.Lz   = z, state noshock)
(setting technique to bfgs)
Iteration 0:  Log likelihood = -9116.0985
Iteration 1:  Log likelihood = -997.95396   (backed up)
Iteration 2:  Log likelihood = -881.53897   (backed up)
Iteration 3:  Log likelihood = -836.47478   (backed up)
Iteration 4:  Log likelihood = -769.37111   (backed up)
(switching technique to nr)
Iteration 5:  Log likelihood = -768.80775   (not concave)
Iteration 6:  Log likelihood = -760.17757   (not concave)
Iteration 7:  Log likelihood = -756.00241   (not concave)
Iteration 8:  Log likelihood = -754.93963   (not concave)
Iteration 9:  Log likelihood = -754.42345
Iteration 10: Log likelihood = -753.67337
Iteration 11: Log likelihood = -753.13078
Iteration 12: Log likelihood = -753.07841
Iteration 13: Log likelihood = -753.07788
Iteration 14: Log likelihood = -753.07788

DSGE model

Sample: 1955q1 thru 2015q4                      Number of obs = 244
Log likelihood = -753.07788
```

	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
/structural						
beta	.5154869	.0770491	6.69	0.000	.3644734	.6665004
kappa	.1662432	.0468473	3.55	0.000	.0744242	.2580622
rho	.6979872	.0452071	15.44	0.000	.6093829	.7865915
rhoz1	.6735503	.2666048	2.53	0.012	.1510145	1.196086
rhoz2	.2709982	.2564615	1.06	0.291	-.2316571	.7736536
sd(e.u)	2.315264	.2992174			1.728809	2.90172
sd(e.z)	.7720659	.1716228			.4356915	1.10844

Looking at the confidence interval on rhoz2 , we find no evidence that the AR(2) term is needed in this model.

Also see

[DSGE] [Intro 2](#) — Learning the syntax

[DSGE] [Intro 4](#) — Writing a DSGE in a solvable form

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