Description Remarks and examples References Also see

## Description

This introduction covers the commands cmroprobit and cmrologit. These estimation commands each fit choice models for rank-ordered alternatives. That is, models in which each decision maker ranks alternatives from a finite set of available alternatives.

# **Remarks and examples**

Remarks are presented under the following headings:

Overview of CM commands for rank-ordered alternatives cmroprobit: Probit regression for rank-ordered alternatives Expected choice probabilities (the margins command) after cmroprobit cmrologit: Logistic regression for rank-ordered alternatives

#### Overview of CM commands for rank-ordered alternatives

Stata has two commands designed for fitting choice models for rank-ordered alternatives. Below, we give you a brief overview of the models fit by these commands.

cmroprobit fits an extension of the multinomial probit choice model for rank-ordered alternatives. It allows both alternative-specific and case-specific predictors. It does not assume IIA; instead, it models the correlation of errors across alternatives. If you are not familiar with IIA, see *Overview of CM commands for discrete choices* in [CM] **Intro 5** and see [CM] **Intro 8**. cmroprobit allows tied ranks, but computation time increases with the number of ties, so in practice, it works best when there are only a small number of ties.

cmrologit fits a choice model for rank-ordered alternatives for the case in which alternatives are not explicitly identified. That is, there is no variable specifying the alternatives. Alternatives are known only by their characteristics as given by a set of alternative-specific variables. All predictors must be alternative-specific variables. This model assumes IIA is true. It allows tied ranks.

#### cmroprobit: Probit regression for rank-ordered alternatives

cmroprobit is similar to cmmprobit. Both are probit regression models, and both likelihoods are computed using simulated integration. Covariance structures are specified in exactly the same manner in each of the commands. Indeed, every option for cmmprobit works with cmroprobit and does the same thing. The difference is, of course, that cmroprobit has ranked alternatives as outcomes and cmmprobit requires a single choice of one alternative.

cmmprobit is described in the introduction [CM] Intro 5 and in its manual entry [CM] cmmprobit. You should read the discussion of cmmprobit in the earlier introduction if you have not already done so.

Just like cmmprobit, cmroprobit models the random-error term of the utility using a multivariate normal distribution and allows the user to specify many different parameterizations for the covariance matrix.

Here is an example using cmroprobit. We use data from the Wisconsin Longitudinal Study cited by Long and Freese (2014, 477). This is a study involving high school graduates who were asked to rank their preferences of four job characteristics: esteem, variety, autonomy, and security.

The case-specific covariates are female (1 if female and 0 if male) and score, a score on a general mental ability test measured in standard deviations. The dataset also includes variables high and low, which indicate whether the respondent's current job is high or low in esteem, variety, autonomy, and security. These two variables together yield three possible ratings for the characteristics of his or her current job—high, low, or neither. From the high and low variables, we create a new variable current job that we include as an alternative-specific variable in our model.

The alternatives were ranked (variable rank) such that 1 is the most preferred alternative and 4 is the least, and respondents were allowed to have ties in their rankings. A variable noties indicates those persons who did not have any ties in their rankings.

Here we prepare our data and list them for three respondents:

```
. use https://www.stata-press.com/data/r19/wlsrank
(1992 Wisconsin Longitudinal Study data on job values)
. keep if noties
(11,244 observations deleted)
. generate currentjob = 1 if low==1
(1,304 missing values generated)
. replace currentjob = 2 if low==0 & high==0
(805 real changes made)
. replace currentjob = 3 if high==1
(499 real changes made)
. label define current 1 "Low" 2 "Neither" 3 "High"
```

. label values currentjob current

. list id jobchar rank female score currentjob in 1/12, sepby(id)

|     | id | jobchar  | rank | female | score    | curren~b |
|-----|----|----------|------|--------|----------|----------|
| 1.  | 13 | Esteem   | 4    | Male   | .3246512 | Low      |
| 2.  | 13 | Variety  | 2    | Male   | .3246512 | High     |
| 3.  | 13 | Autonomy | 1    | Male   | .3246512 | Neither  |
| 4.  | 13 | Security | 3    | Male   | .3246512 | Low      |
| 5.  | 19 | Esteem   | 3    | Female | .0492111 | Neither  |
| 6.  | 19 | Variety  | 2    | Female | .0492111 | Neither  |
| 7.  | 19 | Autonomy | 4    | Female | .0492111 | Neither  |
| 8.  | 19 | Security | 1    | Female | .0492111 | High     |
| 9.  | 22 | Esteem   | 4    | Female | 1.426412 | High     |
| 10. | 22 | Variety  | 1    | Female | 1.426412 | Neither  |
| 11. | 22 | Autonomy | 2    | Female | 1.426412 | High     |
| 12. | 22 | Security | 3    | Female | 1.426412 | Neither  |

Note that we kept only the data without ties for our analysis. cmroprobit handles ties by evaluating the likelihoods of all possible ways of breaking a tie. For example, suppose someone reported ranks (1, 1, 3, 4), where the two 1s indicate a tie. For this person, cmroprobit computes likelihoods for ranks (1, 2, 3, 4) and (2, 1, 3, 4). If there is a 3-way tie among the ranks, 6 different likelihoods are computed. If there is a 4-way tie among the ranks, 24 different likelihoods are computed. If there are ties in your data, cmroprobit will be slower than if there were no ties. For this example, we drop the cases with

ties in these data, just to make it run faster. Running the example with ties takes about 7 times longer, adjusting for the number of cases omitted (which is substantial because 87% of respondents had ties among their rankings).

Before we can run cmroprobit, we must cmset our data:

. cmset id jobchar Case ID variable: id Alternatives variable: jobchar

We can now fit our model. We specify the option reverse because by default a bigger rank indicates a preferred alternative, whereas in these data, it is the opposite—a smaller rank indicates a preferred alternative.

```
. cmroprobit rank i.currentjob, casevars(i.female score) reverse structural
note: variable 2.currentjob has 69 cases that are not alternative-specific;
      there is no within-case variability.
note: variable 3.currentjob has 107 cases that are not alternative-specific;
      there is no within-case variability.
Iteration 0: Log simulated-likelihood = -1102.9667
Iteration 1: Log simulated-likelihood = -1095.0846
                                                     (backed up)
Iteration 2:
             Log simulated-likelihood = -1091.2528
                                                     (backed up)
Iteration 3:
             Log simulated-likelihood = -1086.9763
                                                     (backed up)
Iteration 4: Log simulated-likelihood = -1086.8123
                                                     (backed up)
Iteration 5: Log simulated-likelihood = -1086.3018
                                                     (backed up)
Iteration 6: Log simulated-likelihood = -1086.0779
Iteration 7: Log simulated-likelihood = -1085.7839
Iteration 8: Log simulated-likelihood = -1085.4865
                                                     (backed up)
Iteration 9: Log simulated-likelihood = -1084.9575
Iteration 10: Log simulated-likelihood = -1084.0493
Iteration 11: Log simulated-likelihood = -1083.9447
Iteration 12: Log simulated-likelihood = -1083.1608
Iteration 13: Log simulated-likelihood = -1082.959
Iteration 14: Log simulated-likelihood = -1082.7606
Iteration 15: Log simulated-likelihood = -1081.3702
Iteration 16: Log simulated-likelihood = -1080.8372
Iteration 17: Log simulated-likelihood = -1080.6969
Iteration 18: Log simulated-likelihood = -1080.5508
Iteration 19: Log simulated-likelihood = -1079.9994
Iteration 20: Log simulated-likelihood = -1079.9774
Iteration 21: Log simulated-likelihood = -1079.9741
Iteration 22: Log simulated-likelihood = -1079.9734
Iteration 23: Log simulated-likelihood = -1079.9733
Iteration 24: Log simulated-likelihood = -1079.9733
Reparameterizing to correlation metric and refining estimates
Iteration 0: Log simulated-likelihood = -1079.9733
Iteration 1: Log simulated-likelihood = -1079.9733
```

| Rank-ordered p<br>Case ID varial | probit choice<br>ble: id | Number o<br>Number o | f obs<br>f cases | =<br>=  | 1,660<br>415 |       |           |
|----------------------------------|--------------------------|----------------------|------------------|---------|--------------|-------|-----------|
| Alternatives                     | variable: jobo           | Alts per             | case: min        | =       | 4            |       |           |
|                                  | 0                        |                      |                  | -       | avg          | =     | 4.0       |
|                                  |                          |                      |                  |         | max          | =     | 4         |
| Integration se                   | equence:                 | Hammersley           |                  |         | 1 : 0 (0)    |       |           |
| Integration po                   | oints:                   | 1070 0722            |                  | Wald    | ch12(8)      | =     | 33.92     |
| Log simulated                    | -likelinood =            | -1079.9733           |                  | Prob    | > Ch12       | -     | 0.0000    |
| rank                             | Coefficient              | Std. err.            | Z                | P> z    | [95% co      | nf. : | interval] |
| jobchar                          |                          |                      |                  |         |              |       |           |
| Neither                          | 0694754                  | 1002521              | 0.64             | 0 525   | - 144654     | ٩     | 2836056   |
| High                             | .44359                   | .1216771             | 3.65             | 0.000   | .205107      | 3     | .6820727  |
| Esteem                           | (base alter              | mative)              |                  |         |              |       |           |
|                                  |                          |                      |                  |         |              |       |           |
| Variety                          |                          |                      |                  |         |              |       |           |
| female                           | 4054400                  | 1010001              | 0.70             | 0 4 4 0 | 005000       |       | 4000000   |
| Female                           | .1354483                 | .1843801             | 0.73             | 0.463   | 225930       | 1     | .4968266  |
| score                            | .1407149                 | .0977656             | 1.44             | 0.150   | 050902       | 2     | .3323319  |
| Cons                             | 1.734451                 | .1449841             | 11.96            | 0.000   | 1.45028      | o<br> | 2.018615  |
| Autonomy                         |                          |                      |                  |         |              |       |           |
| female                           |                          |                      |                  |         |              |       |           |
| Female                           | .2562946                 | .1645936             | 1.56             | 0.119   | 066302       | 9     | .5788921  |
| score                            | .189966                  | .0873585             | 2.17             | 0.030   | .018746      | 6     | .3611854  |
| _cons                            | .7007339                 | .1203077             | 5.82             | 0.000   | .464935      | 2     | .9365326  |
| Security                         |                          |                      |                  |         |              |       |           |
| female                           |                          |                      |                  |         |              |       |           |
| Female                           | .2326753                 | .2055824             | 1.13             | 0.258   | 170258       | 9     | .6356095  |
| score                            | 1779948                  | .1101965             | -1.62            | 0.106   | 39397        | 6     | .0379865  |
| _cons                            | 1.343435                 | .1598743             | 8.40             | 0.000   | 1.03008      | 8     | 1.656783  |
| /12                              | 1000520                  | 1600002              | 0.67             | 0 504   | 400100       | A     | 0104017   |
| /insigma3                        | 1088538                  | .1629293             | -0.67            | 0.504   | 428189       | 4     | .2104817  |
| /11151glia4                      | .3101001                 | .115562              | 2.15             | 0.000   | .091002      | . 1   | .5440575  |
| /atanhr3 2                       | 1607581                  | .2035115             | -0.79            | 0.430   | 559633       | 2     | .2381171  |
| /atanhr4 2                       | 2718915                  | .1700903             | -1.60            | 0.110   | 605262       | 4     | .0614793  |
| /atanhr4_3                       | 3839589                  | .2473491             | -1.55            | 0.121   | 868754       | 1     | .1008364  |
|                                  |                          | ()                   |                  |         |              |       |           |
| sigmal                           | 1                        | (pase alter          | mative)          |         |              |       |           |
| sigma2                           | 8968615                  | 1/6125               | illative)        |         | 65168        | 8     | 1 03/073  |
| sigma4                           | 1.374596                 | .1588511             |                  |         | 1.09599      | 5     | 1.724018  |
| 0                                |                          |                      |                  |         |              |       |           |
| rho3_2                           | 1593874                  | .1983414             |                  |         | 507705       | 3     | .2337165  |
| rho4_2                           | 265384                   | .158111              |                  |         | 540783       | 6     | .0614019  |
| rho4_3                           | 3661406                  | .2141897             |                  |         | 700740       | 6     | .100496   |

(jobchar=Esteem is the alternative normalizing location)

(jobchar=Variety is the alternative normalizing scale)

We also specified the option structural to fit a variance-covariance parameterization based on the full  $4 \times 4$  variance-covariance matrix. The postestimation commands, estat covariance and estat correlation, show the estimated covariance and correlations matrices, respectively.

. estat covariance

|   | Esteem           | Variety                 | Autonomy            | Security |
|---|------------------|-------------------------|---------------------|----------|
| Esteem<br>Variety<br>Autonomy<br>Security | 1<br>0<br>0<br>0 | 1<br>1429484<br>3647959 | .8043605<br>4513864 | 1.889515 |

estat correlation

|   | Esteem                               | Variety                      | Autonomy          | Security |
|---|--------------------------------------|------------------------------|-------------------|----------|
| Esteem<br>Variety<br>Autonomy<br>Security | 1.0000<br>0.0000<br>0.0000<br>0.0000 | 1.0000<br>-0.1594<br>-0.2654 | 1.0000<br>-0.3661 | 1.0000   |

By default, cmroprobit fits a covariance matrix parameterized by differences between alternatives, which yields a  $3 \times 3$  matrix. See *Covariance structures* in [CM] **cmmprobit** for details.

### Expected choice probabilities (the margins command) after cmroprobit

As with the other cm estimators, running margins afterward can help us understand the model results.

```
. margins
Predictive margins
Number of obs = 1,660
Model VCE: OIM
Expression: Pr(jobchar), predict(pr1)
```

| I<br>Margin                      | Delta-method<br>std. err.                              | z  | P> z  | [95% conf.   | interval]   |
|----------------------------------|--|--|---|--|---|
| .0228205<br>.4503611<br>.1461409 | .0059232<br>.0238804<br>.0165112                       | 3.85<br>18.86<br>8.85  | 0.000<br>0.000<br>0.000   | .0112112<br>.4035564<br>.1137795   | .0344297<br>.4971658<br>.1785022  |
|                                  | Margin<br>.0228205<br>.4503611<br>.1461409<br>.3806896 | Delta-method<br>Margin std. err.<br>.0228205 .0059232<br>.4503611 .0238804<br>.1461409 .0165112<br>.3806896 .0232362 | Delta-method<br>std. err.         z           .0228205         .0059232         3.85           .4503611         .0238804         18.86           .1461409         .0165112         8.85           .3806896         .0232362         16.38 | Delta-method<br>Margin         z         P> z            .0228205         .0059232         3.85         0.000           .4503611         .0238804         18.86         0.000           .1461409         .0165112         8.85         0.000           .3806896         .0232362         16.38         0.000 | Delta-method<br>Margin         Delta-method           .0228205         .0059232         3.85         0.000         .0112112           .4503611         .0238804         18.86         0.000         .4035564           .1461409         .0165112         8.85         0.000         .1137795           .3806896         .0232362         16.38         0.000         .3351474 |

Typing margins without any options after cmroprobit gives the average predicted probability that a particular outcome is the highest-ranked choice. This is indicated on the output by predict(pr1). Also note that the probabilities sum to one. Here variety has the greatest probability (45%) of being the characteristic ranked first. Security has the second greatest probability (38%) of being ranked first.

The above probabilities from margins are the expected probabilities of ranking these characteristics as most important based on our model and the characteristics of the individuals in this sample. We can also ask questions about what our model tells would happen if covariates change. For instance, what would we expect these probabilities to be if everyone ranked his or her current job as high in security? To answer this, we use the option alternative(security) with margins to select the security alternative, and we set it to the High ranking by specifying 3.currentjob.

| . margins 3.cu                                    | rrentjob, alt            | ernative(Sec | urity) |       |            |           |  |  |  |
|---|--------------------------|--------------|--------|-------|------------|-----------|--|--|--|
| Predictive marginsNumber of obs = 1Model VCE: OIM |                          |              |        |       |            |           |  |  |  |
| Expression: Pr<br>Alternative: Se                 | r(jobchar), p<br>ecurity | redict(pr1)  |        |       |            |           |  |  |  |
|   | Manada                   | Delta-method | _      |       | [05%f      | ÷         |  |  |  |
|   | Margin                   | sta. err.    | Z      | P> Z  | [95% CONI. | intervalj |  |  |  |
| _outcome#   |                          |              |        |       |            |           |  |  |  |
| Esteem#High                                       | .0196645                 | .0053179     | 3.70   | 0.000 | .0092416   | .0300874  |  |  |  |
| Variety#High                                      | .4184274                 | .0252003     | 16.60  | 0.000 | .3690358   | .467819   |  |  |  |
| High<br>Security #                                | .1342234                 | .0160335     | 8.37   | 0.000 | .1027982   | .1656485  |  |  |  |
| High  | .4276949                 | .02543       | 16.82  | 0.000 | .3778529   | .4775369  |  |  |  |

Based on this model, we expect that 43% of individuals whose current job is high in security would rank security as being the most important job characteristic.

See [CM] Intro 1 and [CM] margins for details and more examples of running margins after cm estimators.

#### cmrologit: Logistic regression for rank-ordered alternatives

cmrologit fits a rank-ordered logistic regression model for choice data (Beggs, Cardell, and Hausman 1981). This model is also known as the Plackett-Luce model (Marden 1995), as the exploded logit model (Punj and Staelin 1978), and as the choice-based method of conjoint analysis (Hair et al. 2010).

The model fit by cmrologit is unique among the cm estimators in that the model does not have explicitly identified alternatives. (cmmixlogit and cmxtmixlogit can fit models without identified alternatives as well, but for these commands having no alternatives is optional.) Independent variables for cmrologit must all be alternative specific; that is, they must vary within case. Any purely case-specific variables will be dropped from the estimation.

Like cmroprobit, cmrologit allows the ranks to be tied. However, cmrologit uses a different computational method, and computation with ties is speedy.

Here is an example using cmrologit. We have data on human resource managers ranking their perceived desirability of fictitious applicants. The dataset has 29 cases, each consisting of 10 applicants that are ranked. The variable caseid identifies the cases, and we list the observations for caseid == 7.

| pref | female | age | grades | edufit | workexp    |
|------|--------|-----|--------|--------|------------|
| 0    | yes    | 28  | A/B    | no     | none       |
| 0    | no     | 25  | C/D    | yes    | one year   |
| 0    | no     | 25  | C/D    | yes    | none       |
| 0    | yes    | 25  | C/D    | no     | internship |
| 1    | no     | 25  | C/D    | yes    | one year   |
| 2    | no     | 25  | A/B    | yes    | none       |
| 3    | yes    | 25  | A/B    | yes    | one year   |
| 4    | yes    | 25  | A/B    | yes    | none       |
| 5    | no     | 25  | A/B    | yes    | internship |
| 6    | yes    | 28  | A/B    | yes    | one year   |

. use https://www.stata-press.com/data/r19/evignet, clear (Vignet study employer prefs (Inge de Wolf 2000))

7, noobs

The variable pref contains the managers' ranks, with 6 indicating the applicant they rank the highest and 0 indicating the four least desirable applicants (tied for last). Predictors for the outcome include female, age, grades, edufit (whether the applicant's education fits the job requirements), and workexp (work experience). Note that all of these variables represent characteristics of the applicants. There are no variables representing any of the traits of the managers doing the ranking; such variables would be case specific and would be dropped from the model.

As with all cm commands, the data must be cmset. But here there is no alternatives variable, so we use the noalternatives option and only have to specify the case ID variable.

```
. cmset caseid, noalternatives
     Case ID variable: caseid
Alternatives variable: <none>
```

We now fit our model. We include the baselevels option to show the base levels of the factor variables to make the output more understandable. (The option baselevels can be used with all estimation commands that allow factor variables; see [U] 11.4.3 Factor variables.)

| . cmrologit pi   | ref i.female :  | i.age i.grad   | es i.eduf                       | fit i.wor      | kexp, basele                     | vels                 |
|--|---|--|---------------------------------|----------------|----------------------------------|----------------------|
| Iteration 0:<br>Iteration 1:<br>Iteration 2:<br>Iteration 3:<br>Iteration 4:<br>Refining estim | Log likelihoo<br>Log likelihoo<br>Log likelihoo<br>Log likelihoo<br>Log likelihoo<br>mates: | d = -342.28 $d = -300.81$ $d = -300.2$ | 088<br>224<br>559<br>549<br>549 |                |                                  |                      |
|  | Log likeline  |  | .010                            | N. 1           |                                  | 000                  |
| Case ID varial   | logit choice n  | nodel  |                                 | Number         | of cases =                       | 290<br>29            |
|  | Jie. Caseiu   |  |                                 | Number         | oi cases -                       | 23                   |
| lies adjustmer   | it: exactm  |  |                                 | UDS per        | case:<br>min =<br>avg =<br>max = | 10<br>10.00<br>10    |
|  |   |  |                                 | LR chi2        | (7) =                            | 84.05                |
| Log likelihood   | d = -300.2549   |  |                                 | Prob >         | chi2 =                           | 0.0000               |
| pref   | Coefficient   | Std. err.  | Z                               | P> z           | [95% conf                        | . interval]          |
| female<br>no<br>yes  | 0<br>053564   | (base)<br>.1676711   | -0.32                           | 0.749          | 3821933                          | .2750654             |
| age<br>22<br>25<br>28  | 0<br>.2227<br>0374488   | (base)<br>.2529694<br>.2692834   | 0.88<br>-0.14                   | 0.379<br>0.889 | 2731109<br>5652347               | .7185109<br>.4903371 |
| grades<br>C/D<br>A/B   | 0<br>1.07066  | (base)<br>.1877038   | 5.70                            | 0.000          | .7027673                         | 1.438553             |
| edufit<br>no<br>yes  | 0<br>.4591287   | (base)<br>.174471  | 2.63                            | 0.008          | .1171718                         | .8010855             |
| workexp<br>none<br>internship<br>one year  | 0<br>.6644342<br>1.463883   | (base)<br>.2613156<br>.245367  | 2.54<br>5.97                    | 0.011          | .152265<br>.9829721              | 1.176603<br>1.944793 |

grades, edufit, and workexp are all significant predictors of the ranked outcomes.

The maximum likelihood estimates from cmrologit are obtained as the maximum partial-likelihood estimates of an appropriately specified Cox regression model for waiting time; see [ST] stcox. A higher ranking of an alternative is formally equivalent to a higher hazard rate of failure. A higher stated preference has a shorter waiting time until failure. cmrologit uses stcox to fit the rank-ordered logit model based on such a specification of the data in Cox terms. See Methods and formulas in [CM] cmrologit.

### References

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## Also see

- [CM] Intro 1 Interpretation of choice models
- [CM] Intro 2 Data layout
- [CM] Intro 3 Descriptive statistics
- [CM] Intro 4 Estimation commands
- [CM] cmrologit Rank-ordered logit choice model
- [CM] cmroprobit Rank-ordered probit choice model

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