Intro 5 — Models for discrete choices

Description Remarks and examples References Also see

Description

This introduction covers the commands cmclogit, cmmixlogit, cmmprobit, and nlogit. These estimation commands fit discrete choice models, that is, models in which each decision maker chooses a single alternative from a finite set of available alternatives.

Remarks and examples

Remarks are presented under the following headings:

Overview of CM commands for discrete choices

cmclogit: McFadden's choice model
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cmmixlogit: Mixed logit choice models

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Overview of CM commands for discrete choices

Stata has four commands designed for fitting discrete choice models. Here we give you a brief overview of the similarities and differences in the models fit by these commands.

Each of these commands allows both alternative-specific and case-specific predictors, and each one handles unbalanced choice sets properly. Each of these models can be derived as a random utility model in which each decision maker selects the alternative that provides the highest utility. See [CM] Intro 8 for more information on the random utility model formulation of these discrete choice models.

The difference in these models largely hinges on an assumption known as independence of irrelevant alternatives (IIA). Briefly, the IIA assumption means that relative probability of selecting alternatives should not change if we introduce or eliminate another alternative. As an example, suppose that a restaurant has one chicken entree and one steak entree on the menu and that these are equally likely to be selected. If a vegetarian option is introduced, the probabilities of selecting chicken and steak will both decrease, but they should still be equal to each other if the IIA assumption holds. If the probability of selecting steak now is greater than the probability of selecting chicken, or vice versa, the IIA assumption does not hold. More technically, the IIA assumption means that the error terms cannot be correlated across alternatives. See [CM] Intro 8 for more information on this assumption and how it applies to each choice model.

cmclogit fits McFadden's choice model using conditional logistic regression. Of the four models discussed in this entry, McFadden's choice model has the most straightforward formulation. However, it does require that you make the IIA assumption.

cmmixlogit fits a mixed logit regression for choice models. This model allows random coefficients on one or more of the alternative-specific predictors in the model. This means that the coefficients on these variables are allowed to vary across individuals. We do not estimate the coefficients for each individual. Instead, we assume that the coefficients follow a distribution such as normal distribution, and we estimate the parameters of that distribution. Through these random coefficients, the model allows correlation across alternatives. In this way, the mixed logit model relaxes the IIA assumption.

cmmprobit fits a multinomial probit choice model. Like cmclogit, this command estimates fixed coefficients for all predictors, but it relaxes the IIA assumption in another way. It directly models the correlation between the error terms for the different alternatives.

nlogit fits a nested logit choice model. With this model, similar alternatives—alternatives whose errors are likely to be correlated—can be grouped into nests. Extending our restaurant example, suppose there are now seven entrees. Three include chicken, two include steak, and two are vegetarian. The researcher could specify a nesting structure where entrees are grouped by type. The nested logit model then accounts for correlation of alternatives within the same nest and thus relaxes the IIA assumption.

Below, we provide further introductions to these models, demonstrate how to fit and interpret them using Stata, and tell you more about their relationships with each other and with other Stata estimation commands.

cmclogit: McFadden's choice model

McFadden's choice model is fit using conditional logistic regression. In Stata, this model can also be fit by the command clogit. In fact, cmclogit calls clogit to fit McFadden's choice model. However, cmclogit is designed for choice data and has features that clogit does not. cmclogit properly handles missing values for choice models, checks for errors in the alternatives variable and case-specific variables, and has appropriate postestimation commands such as the special version of margins designed for use after CM estimation.

To demonstrate cmclogit, we use the same dataset we used in [CM] Intro 2. We load the data, list the first three cases, and use cmset.

- . use https://www.stata-press.com/data/r19/carchoice (Car choice data)
- . list consumerid car purchase gender income dealers if consumerid <= 3,
- > sepby(consumerid) abbrev(10)

	consumerid	car	purchase	gender	income	dealers
1.	1	American	1	Male	46.7	9
2.	1	Japanese	0	Male	46.7	11
3.	1	European	0	Male	46.7	5
4.	1	Korean	0	Male	46.7	1
5.	2	American	1	Male	26.1	10
6.	2	Japanese	0	Male	26.1	7
7.	2	European	0	Male	26.1	2
8.	2	Korean	0	Male	26.1	1
9.	3	American	0	Male	32.7	8
10.	3	Japanese	1	Male	32.7	6
11.	3	European	0	Male	32.7	2

. cmset consumerid car

note: alternatives are unbalanced across choice sets; choice sets of different sizes found.

Case ID variable: consumerid Alternatives variable: car

We passed cmset the case ID variable consumerid and the alternatives variable car, which contains possible choices of the nationality of car purchased, American, Japanese, European, or Korean.

The 0/1 variable purchase indicates which nationality of car was purchased. It is our dependent variable for cmclogit. Before we fit our model, let's run cmtab to see the observed choices in the data.

. cmtab, choice(purchase)

Tabulation of chosen alternatives (purchase = 1)

Nationality of car	Freq.	Percent	Cum.
American	384	43.39	43.39
Japanese	326	36.84	80.23
European	135	15.25	95.48
Korean	40	4.52	100.00
Total	885	100.00	

Most of the people in these data purchased American cars (43%), followed by Japanese cars (37%) and European cars (15%). Korean cars were purchased the least (5%).

For predictors, we have the case-specific variables gender and income, and the alternative-specific variable dealers, which contains the number of dealerships of each nationality in the consumer's community. We fit the model:

. cmclogit purchase dealers, casevars(i.gender income) Iteration 0: Log likelihood = -959.21405 Iteration 1: Log likelihood = -948.48587 Iteration 2: Log likelihood = -948.1217 Iteration 3: Log likelihood = -948.12096 Iteration 4: Log likelihood = -948.12096 Conditional logit choice model Number of obs 3.075 Case ID variable: consumerid Number of cases 862 Alternatives variable: car Alts per case: min = 3 avg = 3.6 4 max = Wald chi2(7) 51.03 Log likelihood = -948.12096Prob > chi2 0.0000 Std. err. P>|z| [95% conf. interval] purchase Coefficient z car .0448082 .0262818 1.70 0.088 -.0067032 .0963196 dealers American (base alternative) Japanese gender Male -.379326 .1712399 -2.22 0.027 -.71495 -.0437021 income .0154978 .0065145 2.38 0.017 .0027296 .0282659 _cons -.4787261 .331378 -1.440.149 -1.128215 .1707628 European gender .2647694 Male .653345 2.47 0.014 .1344065 1.172283 .0080286 4.28 0.000 .0501006 income .0343647 .0186289 _cons -2.839606 .461613 -6.150.000 -3.744351 -1.934861 Korean gender .0679233 .4464535 0.15 0.879 -.8071094 .942956 Male -2.380.017 -.068824 -.0067191 income -.0377716 .0158434 _cons .0511728 .8033048 0.06 0.949 -1.523276 1.625621

Note that alternative-specific variables (if any) follow the dependent variable. Case-specific variables (if any) are placed in the option casevars(). Because cmclogit requires us to specify which variables are alternative specific and which are case specific, it can verify that our data are coded as we expect. It checks whether the specified case-specific variables are truly case specific. If they are not, we get an error.

You may also see messages from cmclogit about the alternative-specific variables. For example,

note: variable **dealers** has 2 cases that are not alternative-specific; there is no within-case variability.

Alternative-specific variables can vary by alternative and by case, but they do not have to vary by alternative for every case. This message tells us that there are two cases for which the alternative-specific variable is constant within case. If an alternative-specific variable is constant within case for a large proportion of the cases, we might question how alternative specific that variable really is and be concerned about its predictive value. If a variable that is supposed to be alternative specific is in fact case specific, we will get an error.

Looking at the results from cmclogit, we first see that the coefficient on dealers is positive; based on this model, we expect the probability of purchasing a vehicle of any nationality to increase as the number of dealerships increases. However, notice that this coefficient is different from 0 at the 10% level but not at the 5% level.

American cars are chosen as the base alternative, so coefficients on the alternative-specific variables are interpreted relative to them. For instance, for the Japanese alternative, the coefficient on Male is negative, which indicates that males are less likely to select a Japanese car than an American car.

Looking at cases with missing values using cmsample

From the header of the cmclogit output, we see that our model was fit using 862 cases in our model. However, we see from the previous cmtab output that there are a total of 885 cases in the data. There must be missing values in one or more of the variables. Let's track down the variables and the cases with missing values using cmsample. First, we run cmsample specifying all the variables we used with cmclogit. The only difference is that the dependent variable goes in the choice() option.

. cmsample dealers, choice(purchase) casevars(i.gender income)

Reason for exclusion	Freq.	Percent	Cum.
observations included casevars missing	3,075 85	97.31 2.69	97.31 100.00
Total	3,160	100.00	

The results tell us that the missing values are in the *casevars*, either gender or income or both. Note that the tabulation produced by cmsample shows counts of observations not cases.

Second, we look at gender alone with cmsample:

. cmsample, casevars(i.gender) generate(flag)

Reason for exclusion	Freq.	Percent	Cum.
observations included casevar missing	3,075 85	97.31 2.69	97.31 100.00
Total	3,160	100.00	

These are the cases with missing values. We also specified the generate() option to create a variable whose nonzero values indicate cases with missing values or other problems. We list these cases:

- . sort consumerid car
- . list consumerid car gender flag if flag != 0, sepby(consumerid) abbr(10)

	consumerid	car	gender	flag
509. 510. 511. 512.	142 142 142 142	American Japanese European Korean	Male Male Male	casevar missing casevar missing casevar missing casevar missing
516. 517. 518.	144 144 144	American Japanese European	Male Male	casevar missing casevar missing casevar missing

(output omitted)

We could have listed the observations with missing values of gender by typing list if missing (gender). But using cmsample in this way allows us to list entire cases, potentially giving us a way to fix the problem. In this example, we could decide all the nonmissing values of gender are valid and fill in the missing values with the nonmissing ones for that case. However, we will not do this for the purpose of our example.

See [CM] cmsample and example 3 in [CM] cmclogit for more on missing values in choice data.

margins after CM estimation

Above, we interpreted a few of the coefficients from the clogit results. In [CM] Intro 1, we showed you that you can use margins to further interpret the results of your choice model. Here we demonstrate how we can apply some of margins special choice model features to interpret the results of this model.

First, we type margins without any arguments to get the average predicted probabilities for the different alternatives.

. margins

Predictive margins Model VCE: OIM

Number of obs = 3.075

Expression: Pr(car|1 selected), predict()

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
outcome						
American	.4361949	.016755	26.03	0.000	.4033556	.4690342
Japanese	.3665893	.0162405	22.57	0.000	.3347585	.3984202
European	.1508121	.0119794	12.59	0.000	.1273328	.1742913
Korean	.0464037	.0069301	6.70	0.000	.032821	.0599865

Based on this model and assuming we have a random or otherwise representative sample, these are the expected proportions in the population.

margins can produce many types of estimates. Suppose we want to know how the probability of a person selecting a European car changes when the number of European dealerships increases. If this probability increases (as we expect it to), the increase must come at the expense of American, Japanese, or Korean cars. Which one of these is affected the most?

First, let's estimate the expected probability of purchasing each nationality of car if each community adds a new European dealership. We can use the at(dealers=(dealers+1) option to request this computation.

. margins, at(dealers=generate(dealers+1)) alternative(European)

Predictive margins Number of obs = 3,075

Model VCE: OIM

Expression: Pr(car|1 selected), predict()

Alternative: European At: dealers = dealers+1

	Margin	Delta-method std. err.	z	P> z	[95% conf.	interval]
outcome						
American	.4333003	.0168164	25.77	0.000	.4003407	.4662598
Japanese	.3641274	.0162604	22.39	0.000	.3322577	.3959971
European	. 1564365	.0127751	12.25	0.000	.1313978	.1814752
Korean	.0461358	.0068959	6.69	0.000	.0326201	.0596516

These look similar to the expected probabilities we estimated using the original number of dealerships in each community. By using the contrast() option, we can estimate the differences between these probabilities and the original ones. We include the nowald option to simplify the output.

```
. margins, at(dealers=generate(dealers)) at(dealers=generate(dealers+1))
```

> alternative(European) contrast(atcontrast(r) nowald)

Contrasts of predictive margins Number of obs = 3,075

Model VCE: OIM

Expression: Pr(car|1 selected), predict()

Alternative: European

1._at: dealers = dealers
2. at: dealers = dealers+1

	Contrast	Delta-method std. err.	[95% conf.	interval]
_at0_outcome (2 vs 1) American (2 vs 1) Japanese (2 vs 1) European (2 vs 1) Korean	0028946	.0017268	0062791	.0004899
	0024619	.0014701	0053434	.0004195
	.0056244	.0033521	0009456	.0121944
	0002679	.0001686	0005983	.0000625

Increasing the number of European dealerships by one increases the expected probability of selecting a European car by 0.0056. This increase comes at the expense of American cars slightly more than Japanese cars. The probability of someone purchasing an American car decreases by 0.0029, and the probability of someone purchasing a Japanese car decreases by 0.0025. The probability of buying a Korean car is barely changed, only a tiny decrease of 0.0003 in the probability. All of these changes are very small. We can look at the 95% confidence intervals to see that none of these changes in probabilities is significantly different from 0 at the 5% level.

We will ignore the lack of significance for now and explore one of margins's features specific to choice models. As we mentioned before, the choice sets are unbalanced. Some consumers do not have the choice of a Korean car (corresponding to car == 4) as one of their available alternatives.

. cmchoiceset

Tabulation of choice-set possibilities

Choice set	Freq.	Percent	Cum.
1 2 3 1 2 3 4	380 505	42.94 57.06	42.94 100.00
Total	885	100.00	

Note: Total is number of cases.

How does margins handle the fact that some persons do not have the choice of Korean cars among their alternatives? By default, margins sets the probability of buying a Korean car for these consumers to zero and keeps it fixed at zero.

If we want to look at only those consumers who have Korean in their choice set, we can use the outcome(..., altsubpop) option.

```
. margins, at(dealers=generate(dealers)) at(dealers=generate(dealers+1))
> alternative(European) contrast(atcontrast(r) nowald) outcome(Korean, altsubpop)
Contrasts of predictive margins
                                                         Number of obs = 3.075
```

Model VCE: OIM

Expression: Pr(car|1 selected), predict()

Alternative: European Outcome: Korean 1. at: dealers = dealers 2._at: dealers = dealers+1

	Delta-method Contrast std. err.		[95% conf.	interval]
_at (2 vs 1)	0004722	.0002972	0010547	.0001103

The probability of buying a Korean car among those who have the choice of buying a Korean decreases by 0.0005 when a European dealership is added. This change is bigger than what we estimated earlier, as we expect, because we omitted all those persons whose change was fixed at zero.

When we model these data, it seems reasonable to keep the probability of buying a Korean car fixed at zero for those consumers who do not have Korean in their choice set. The result gives a picture of the total population represented by the sample; to omit them gives a picture of only those communities with Korean dealerships. See [CM] margins for more examples and another discussion of this issue.

If you have not already read [CM] Intro 1, we recommend that you also read the examples of interpreting results of cm commands using margins that are provided in that entry. For more information on margins, see its main entry in the Stata manuals, [R] margins. You will also want to see the separate entry for it in this manual, [CM] margins, which describes the special features of this command when used after cm commands and includes lots of choice model examples.

cmmixlogit: Mixed logit choice models

cmmixlogit fits a mixed logit regression for choice data. Like cmclogit, cmmixlogit is used to model the probability that a decision maker chooses one alternative from a set of available alternatives.

In the mixed logit model, the coefficients on alternative-specific variables can be treated as fixed or random. Specifying random coefficients can model correlation of choices across alternatives, thereby relaxing the IIA property that is imposed by McFadden's choice model. In this sense, the mixed logit model fit by cmmixlogit is more general than models fit by cmclogit. McFadden and Train (2000) show that the mixed logit model can approximate a wide class of choice representations. See [CM] Intro 8 for a description of the IIA property and how mixed logit models can fit deviations from it.

We continue with the same dataset we have been using in this introduction: consumer data on choices of nationalities of cars. The data arrangement required by cmmixlogit is exactly the same as that for cmclogit.

Mixed logit choice models can fit random coefficients for alternative-specific variables. We take dealers, the number of dealers of each nationality in each consumer's community, which is an alternative-specific variable, and fit random coefficients for it.

```
. cmmixlogit purchase, random(dealers) casevars(i.gender income)
note: alternatives are unbalanced.
Fitting fixed parameter model:
Fitting full model:
Iteration 0:
              Log simulated-likelihood = -966.81349
              Log simulated-likelihood = -949.54388
Iteration 1:
              Log simulated-likelihood = -948.15757
Iteration 2:
Iteration 3:
              Log simulated-likelihood = -948.12546
Iteration 4:
              Log simulated-likelihood = -948.12106
              Log simulated-likelihood = -948.12099
Iteration 5:
Iteration 6:
              Log simulated-likelihood = -948.12097
Iteration 7: Log simulated-likelihood = -948.12096
                                                 Number of obs
                                                                            3.075
Mixed logit choice model
Case ID variable: consumerid
                                                 Number of cases
                                                                               862
Alternatives variable: car
                                                 Alts per case: min =
                                                                                 3
                                                                               3.6
                                                                 avg =
                                                                 max =
                                                                                 4
Integration sequence:
                            Hammersley
Integration points:
                                   623
                                                    Wald chi2(7)
                                                                            51.03
Log simulated-likelihood = -948.12096
                                                    Prob > chi2
                                                                            0.0000
    purchase
               Coefficient
                             Std. err.
                                                  P>|z|
                                                             [95% conf. interval]
                                             z
car
     dealers
                  .0448203
                             .0262821
                                           1.71
                                                  0.088
                                                            -.0066917
                                                                          .0963323
/Normal
  sd(dealers)
                  .0001994
                             .1981032
American
                 (base alternative)
Japanese
      gender
                                                                        -.0437032
       Male
                -.3793276
                             .1712401
                                          -2.22
                                                  0.027
                                                             -.714952
                             .0065144
                                           2.38
                                                  0.017
                                                               .00273
                                                                          .0282661
      income
                   .015498
       _cons
                 -.4786729
                             .3313762
                                          -1.44
                                                  0.149
                                                            -1.128158
                                                                          .1708125
European
      gender
                             .2647746
                                           2.47
                                                  0.014
                                                             .1343706
                                                                         1.172268
       Male
                  .6533193
                             .0080288
                                           4.28
                                                  0.000
                                                                         .0501017
      income
                  .0343656
                                                             .0186295
       _cons
                -2.839604
                             .4616206
                                          -6.15
                                                  0.000
                                                            -3.744363
                                                                        -1.934844
Korean
      gender
       Male
                  .0676844
                             .4464111
                                           0.15
                                                  0.879
                                                            -.8072653
                                                                          .9426341
                             .0158428
                                          -2.38
                                                  0.017
                                                            -.0688128
                                                                          -.00671
      income
                -.0377614
       _cons
                  .0511088
                             .8032683
                                           0.06
                                                  0.949
                                                            -1.523268
                                                                         1.625486
```

The estimated standard deviation for the random coefficient is small, and the likelihood-ratio test shown at the bottom of the table that compares this random-coefficients model with a fixed-coefficient model

LR test vs. fixed parameters: chibar2(01) =

We used the default distribution for the random coefficients: a normal (Gaussian) distribution. Let's fit the model again using a lognormal distribution for the coefficient of dealers.

is not significant. A model with random coefficients for dealers is no better than one with a fixed coefficient. Note that this fixed-coefficient model is precisely the model fit earlier by cmclogit.

0.00 Prob >= chibar2 = 0.5000

Because the lognormal distribution is only defined over positive real values, the coefficient values coming from this distribution will only be positive. This constrains the coefficient to be positive. Is this constraint okay? We believe that increasing the number of dealerships in a community of a given nationality should always increase the probability that someone in the community buys that type of car and never decrease the probability. So constraining the coefficient to be positive is what we want. (If we want to constrain the coefficient to be negative, we could create a variable equal to -dealers and fit a random lognormal coefficient for it.)

```
. cmmixlogit purchase, random(dealers, lognormal) casevars(i.gender income)
note: alternatives are unbalanced.
Fitting fixed parameter model:
Fitting full model:
              Log simulated-likelihood = -948.13062
Iteration 0:
              Log simulated-likelihood = -948.1226
Iteration 1:
Iteration 2: Log simulated-likelihood = -948.12155
Iteration 3: Log simulated-likelihood = -948.12106
Iteration 4: Log simulated-likelihood = -948.12096
Iteration 5: Log simulated-likelihood = -948.12096
Mixed logit choice model
                                                Number of obs
                                                                            3.075
Case ID variable: consumerid
                                                Number of cases
                                                                              862
Alternatives variable: car
                                                Alts per case: min =
                                                                                3
                                                                              3.6
                                                                avg =
                                                                max =
Integration sequence:
                            Hammersley
                                                                            79.14
Integration points:
                                   623
                                                    Wald chi2(7)
Log simulated-likelihood = -948.12096
                                                    Prob > chi2
                                                                           0.0000
               Coefficient
                             Std. err.
                                                 P>|z|
                                                            [95% conf. interval]
   purchase
car
                -3.105499
                                         -5.29
                                                 0.000
                                                           -4.255971
     dealers
                             .5869861
                                                                       -1.955028
/Lognormal
  sd(dealers)
                 .0036636
                             4.480108
American
                 (base alternative)
Japanese
      gender
      Male
                -.3793272
                             .1712406
                                         -2.22
                                                 0.027
                                                           -.7149526
                                                                       -.0437018
                 .0154978
                             .0065145
                                          2.38
                                                 0.017
                                                            .0027296
                                                                         .0282661
      income
       _cons
                -.4787181
                             .3313811
                                         -1.44
                                                 0.149
                                                           -1.128213
                                                                          .170777
European
      gender
       Male
                 .6533465
                             .2647669
                                          2.47
                                                 0.014
                                                            .1344129
                                                                          1.17228
      income
                 .0343648
                             .0080286
                                          4.28
                                                 0.000
                                                            .0186291
                                                                         .0501005
       _cons
                 -2.83959
                             .4616219
                                         -6.15
                                                 0.000
                                                           -3.744353
                                                                       -1.934828
Korean
      gender
       Male
                 .0679287
                             .4464459
                                          0.15
                                                 0.879
                                                           -.8070892
                                                                         .9429466
                -.0377715
                             .0158431
                                         -2.38
                                                 0.017
                                                           -.0688234
                                                                       -.0067196
      income
                 .0511891
                             .8033007
                                          0.06
                                                           -1.523251
                                                                         1.62563
       cons
                                                 0.949
LR test vs. fixed parameters: chibar2(01) =
                                                 0.00 \text{ Prob} >= \text{chibar2} = 0.5000
```

The random-coefficients model is still not significantly different from a fixed coefficient model.

At first glance, the requirement of including random coefficients on alternative-specific variables in this model may seem limiting. What if we do not have alternative-specific variables for which random coefficients are appropriate? Note that the constants in the model are alternative specific. They are automatically included in the model for us, but we could have equivalently typed i.car in the list of alternative-specific variables to include indicators for the alternatives. We can turn any of or all the constants into random intercepts. Let's do this with the constant for the European alternative. Now we need to use the factor-variable specification for the alternative-specific constants. Because we want fixed coefficients on Japanese and Korean indicators, we type i(24).car in the fixed portion of the model. To get random coefficients for the European constant, we type random (i3.car). We also specify the options no constant and collinear (or else cmmixlogit would drop the constants).

```
. cmmixlogit purchase dealers i(2 4).car, random(i3.car)
> casevars(i.gender income) noconstant collinear
note: alternatives are unbalanced.
Fitting fixed parameter model:
Fitting full model:
Iteration 0:
             Log simulated-likelihood = -1717.8292
                                                    (not concave)
Iteration 1:
             Log simulated-likelihood = -1471.6665
                                                    (not concave)
             Log simulated-likelihood = -1456.0693 (not concave)
Iteration 2:
Iteration 3:
             Log simulated-likelihood = -1431.4506 (not concave)
Iteration 4:
             Log simulated-likelihood = -1412.2678
                                                    (not concave)
Iteration 5:
             Log simulated-likelihood = -1382.4808
                                                     (not concave)
Iteration 6:
             Log simulated-likelihood = -1359.4781
                                                     (not concave)
             Log simulated-likelihood = -1341.5917
Iteration 7:
                                                     (not concave)
             Log simulated-likelihood = -1327.6059
Iteration 8:
                                                     (not concave)
Iteration 9: Log simulated-likelihood = -1316.6209
                                                     (not concave)
Iteration 10: Log simulated-likelihood = -1307.9616
                                                     (not concave)
Iteration 11: Log simulated-likelihood = -1301.1157
                                                     (not concave)
Iteration 12: Log simulated-likelihood = -1290.3121
                                                     (not concave)
Iteration 13: Log simulated-likelihood = -1157.6292
                                                     (not concave)
Iteration 14: Log simulated-likelihood = -1009.2526
Iteration 15: Log simulated-likelihood = -951.50739
Iteration 16: Log simulated-likelihood = -949.17526
Iteration 17: Log simulated-likelihood = -949.16756
Iteration 18: Log simulated-likelihood = -949.16753
```

_

Mixed logit ch Case ID variab			Number Number	of obs = of cases =	3,075 862	
Alternatives v	variable: car		Alts pe	r case: min = avg = max =	3 3.6 4	
Integration se Integration po Log simulated	oints:	Hammersley 623 -949.16753			chi2(9) = > chi2 =	200.60
purchase	Coefficient	Std. err.	z	P> z	[95% conf.	interval]
car dealers	.0501926	.0259821	1.93	0.053	0007313	.1011166
car Korean European	.2925999 -2.590904	.7850805 .4270635	0.37 -6.07	0.709	-1.24613 -3.427933	1.83133 -1.753875
/Normal sd(3.car)	.0002269	1.624703				<u>.</u>
American	(base alter	native)				
Japanese gender Male income	5113895 .0071214	.1448843 .0029512	-3.53 2.41	0.000 0.016	7953575 .0013372	2274214 .0129057
European gender Male income	.5841137 .0304543	.2610553 .0075049	2.24 4.06	0.025 0.000	.0724548 .015745	1.095773 .0451637
Korean gender Male income	.0009729 0413177	.4445682 .0156261	0.00 -2.64	0.998 0.008	8703648 0719443	.8723106 0106911
LR test vs. fi	ixed parameter	s: chibar2(01) =	0.00	Prob >= chibar	2 = 0.5000

This model with a random intercept for the European alternative is not significantly different from a fixedcoefficient model. But this illustrates one of the features of cmmixlogit. Making the alternative-specific constants random allows us to fit models that do not satisfy IIA and test them against a fixed-coefficient model that does satisfy IIA.

See [CM] cmmixlogit for examples where the random-coefficients model fits better than the one with fixed coefficients. There we demonstrate how to further interpret results of these models. In addition, you can use margins in the same ways shown in [CM] Intro 1 and as we did after cmclogit above to interpret mixed logit models.

cmmprobit: Multinomial probit choice models

cmmprobit fits a multinomial probit (MNP) choice model. The formulation of the utility for MNP is described in [CM] Intro 8. The model is similar to McFadden's choice model (cmclogit), except that the random-error term is modeled using a multivariate normal distribution, and you can explicitly model the covariance.

The covariance parameters are set using the correlation() and stddev() options of cmmprobit. In general, there are J(J+1)/2 possible covariance parameters, where J is the number of possible alternatives. One of the alternatives is set as the base category, and only the relative differences among the utilities matter. This reduces the possible number of covariance parameters by J.

The scale of the utilities does not matter. Multiply the utilities for all alternatives by the same constant, and the relative differences are unchanged. This further reduces the number of covariance parameters by one. So there are a total of J(J-1)/2-1 covariance parameters you can fit. But you do not have to fit all of them. You can set some of them to fixed values, either zero or nonzero. Or you can constrain some of them to be equal.

When *J* is large, it is a good idea to initially fit just a few parameters and then gradually increase the number. If you try to fit a lot of parameters, your model may have a hard time converging because some of the parameters may not be identified. For example, the true variance for one of the alternatives may be zero, and if you try to estimate the standard deviation for the alternative, the model may not converge because zero is not part of the estimable parameter space.

See Covariance structures in [CM] cmmprobit for full details on all the choices for specifying the covariance parameters.

cmmprobit has some options for reducing the number of covariance parameters. In particular, correlation(exchangeable) fits a model in which correlations between the alternatives are all the same. Another way to reduce the number of parameters estimated is the factor(#) option. cmmprobit with factor(#) fits a covariance matrix of the form $I + \mathbf{C}'\mathbf{C}$, where the row dimension of the matrix \mathbf{C} is #.

Let's fit a model using factor(1) with the data from the previous examples.

```
. cmmprobit purchase dealers, casevars(i.gender income) factor(1)
Iteration 0: Log simulated-likelihood = -949.38598
Iteration 1: Log simulated-likelihood = -949.08161
                                                     (backed up)
Iteration 2: Log simulated-likelihood = -948.87143
                                                     (backed up)
                                                     (backed up)
Iteration 3: Log simulated-likelihood = -948.84362
Iteration 4:
             Log simulated-likelihood = -948.83433
                                                     (backed up)
Iteration 5: Log simulated-likelihood = -948.53624
                                                     (backed up)
Iteration 6: Log simulated-likelihood = -948.52521
Iteration 7: Log simulated-likelihood = -948.42813
Iteration 8: Log simulated-likelihood = -948.14286
Iteration 9:
             Log simulated-likelihood = -948.03466
Iteration 10: Log simulated-likelihood = -948.01302
Iteration 11: Log simulated-likelihood = -947.83629
Iteration 12: Log simulated-likelihood = -947.78297
Iteration 13: Log simulated-likelihood = -947.6765
Iteration 14: Log simulated-likelihood = -947.60503
Iteration 15: Log simulated-likelihood = -947.5831
Iteration 16: Log simulated-likelihood = -947.55131
Iteration 17: Log simulated-likelihood = -947.50624
Iteration 18: Log simulated-likelihood = -947.46284
Iteration 19: Log simulated-likelihood = -947.44467
Iteration 20: Log simulated-likelihood = -947.40163
Iteration 21: Log simulated-likelihood = -947.32181
Iteration 22: Log simulated-likelihood = -947.29791
Iteration 23: Log simulated-likelihood = -947.23404
Iteration 24: Log simulated-likelihood = -947.17847
```

```
Iteration 25: Log simulated-likelihood = -947.13231
Iteration 26: Log simulated-likelihood = -947.08427
Iteration 27: Log simulated-likelihood = -946.83137
Iteration 28: Log simulated-likelihood = -946.73195
Iteration 29: Log simulated-likelihood = -946.44451
Iteration 30: Log simulated-likelihood = -946.37077
Iteration 31: Log simulated-likelihood = -946.34252
Iteration 32: Log simulated-likelihood = -946.32218
Iteration 33: Log simulated-likelihood = -946.31672
Iteration 34: Log simulated-likelihood = -946.31499
Iteration 35: Log simulated-likelihood = -946.31489
Iteration 36: Log simulated-likelihood = -946.31487
Iteration 37: Log simulated-likelihood = -946.31486
Iteration 38: Log simulated-likelihood = -946.3148
Iteration 39: Log simulated-likelihood = -946.3141
Iteration 40: Log simulated-likelihood = -946.31203
Iteration 41: Log simulated-likelihood = -946.3114
Iteration 42: Log simulated-likelihood = -946.31114
Iteration 43: Log simulated-likelihood = -946.31109
Iteration 44: Log simulated-likelihood = -946.31109
Multinomial probit choice model
                                               Number of obs
                                                                          3,075
Case ID variable: consumerid
                                               Number of cases
                                                                            862
Alternatives variable: car
                                               Alts per case: min =
                                                                              3
                                                               avg =
                                                                            3.6
                                                              max =
                                                                              4
Integration sequence:
                           Hammersley
Integration points:
                                  704
                                                  Wald chi2(7)
                                                                          33.07
Log simulated-likelihood = -946.31109
                                                  Prob > chi2
                                                                         0.0000
   purchase
               Coefficient Std. err.
                                                P>|z|
                                                           [95% conf. interval]
car
                  .043345
                                         1.58
                                                0.114
                                                         -.0103521
                                                                       .0970421
    dealers
                             .027397
American
                (base alternative)
Japanese
      gender
                            .1454853
                                        -3.13 0.002
                                                         -.7400741
                                                                      -.1697821
       Male
                -.4549281
      income
                 .0092406
                                        1.70
                                                0.090
                            .0054458
                                                          -.0014331
                                                                       .0199142
       _cons
                 -.419605
                            .2779042
                                        -1.51
                                                0.131
                                                          -.9642872
                                                                       .1250771
European
      gender
      Male
                 .5630868
                            .4209091
                                         1.34
                                                0.181
                                                           -.26188
                                                                       1.388054
                                         1.97
                                                0.049
      income
                            .0102355
                                                           .0000626
                                                                       .0401849
                 .0201237
                            1.499657
                                        -1.52
                                                0.129
                                                         -5.213051
                                                                       .6654965
       _cons
                -2.273777
Korean
     gender
      Male
                            .4970796
                                         0.62
                                                0.535
                                                                       1.282448
                 .3081901
                                                          -.6660681
      income
                 -.035191
                            .0346554
                                        -1.02
                                                0.310
                                                          -.1031143
                                                                       .0327323
       _cons
                -.9509443
                            1.056018
                                        -0.90 0.368
                                                         -3.020701
                                                                       1.118812
       /c1 2
                -.8477292
                            1.362816
                                        -0.62
                                                0.534
                                                         -3.518799
                                                                       1.823341
      /c1 3
                -1.675403
                            1.433511
                                        -1.17
                                                0.243
                                                         -4.485033
                                                                       1.134226
```

(car=American is the alternative normalizing location) (car=Japanese is the alternative normalizing scale)

matrix b704 = e(b)

The estimated covariance parameters are shown in the output, but more useful is to see the estimated covariance matrix or correlation matrix. The postestimation command estat will display them. estat covariance shows the covariance matrix, and estat correlation shows the correlations.

. estat covariance

	Japanese	European	Korean
Japanese European	2 8477292	1.718645	
Korean	-1.675403	1.420288	3.806977

Note: Covariances are for alternatives differenced with American.

. estat correlation

	Japanese	European	Korean
Japanese European Korean	1.0000 -0.4572 -0.6072	1.0000 0.5553	1.0000

Note: Correlations are for alternatives differenced with American.

There are four alternatives in these data. But the matrices shown here are only 3×3 . This is because the parameterization for the covariance matrix is, by default, differed by the base category, which in this case is the alternative American.

To see an undifferenced parameterization, we specify the structural option:

```
. cmmprobit purchase dealers, casevars(i.gender income) factor(1) structural
Iteration 0: Log simulated-likelihood = -949.81324
             Log simulated-likelihood = -948.95649
Iteration 1:
                                                     (backed up)
Iteration 2: Log simulated-likelihood = -948.71164
                                                     (backed up)
Iteration 3: Log simulated-likelihood = -948.70869
                                                     (backed up)
Iteration 4: Log simulated-likelihood = -948.65719
                                                     (backed up)
Iteration 5: Log simulated-likelihood = -948.52707
Iteration 6: Log simulated-likelihood = -948.52682
Iteration 7: Log simulated-likelihood = -948.44886
Iteration 8: Log simulated-likelihood = -948.29451
Iteration 9: Log simulated-likelihood = -948.22865
Iteration 10: Log simulated-likelihood = -948.14213
Iteration 11: Log simulated-likelihood = -947.96801
Iteration 12: Log simulated-likelihood = -947.95862
Iteration 13: Log simulated-likelihood = -947.85813
Iteration 14: Log simulated-likelihood = -947.84956
Iteration 15: Log simulated-likelihood = -947.7153
Iteration 16: Log simulated-likelihood = -947.67296
Iteration 17: Log simulated-likelihood = -947.57769
Iteration 18: Log simulated-likelihood = -947.42721
Iteration 19: Log simulated-likelihood = -947.19551
Iteration 20: Log simulated-likelihood = -947.11421
Iteration 21: Log simulated-likelihood = -946.90873
Iteration 22: Log simulated-likelihood = -946.75482
Iteration 23: Log simulated-likelihood = -946.64695
Iteration 24: Log simulated-likelihood = -946.56345
Iteration 25: Log simulated-likelihood = -946.44076
Iteration 26: Log simulated-likelihood = -946.3817
Iteration 27: Log simulated-likelihood = -946.35537
Iteration 28: Log simulated-likelihood = -946.34227
Iteration 29: Log simulated-likelihood = -946.33841
```

```
Iteration 30: Log simulated-likelihood = -946.33808
Iteration 31: Log simulated-likelihood = -946.33792
Iteration 32: Log simulated-likelihood = -946.33659
Iteration 33: Log simulated-likelihood = -946.33345
Iteration 34: Log simulated-likelihood = -946.32049
Iteration 35: Log simulated-likelihood = -946.30741
Iteration 36: Log simulated-likelihood = -946.29907
Iteration 37: Log simulated-likelihood = -946.29486
Iteration 38: Log simulated-likelihood = -946.29353
Iteration 39: Log simulated-likelihood = -946.29243
Iteration 40: Log simulated-likelihood = -946.29179
Iteration 41: Log simulated-likelihood = -946.29159
Iteration 42: Log simulated-likelihood = -946.29158
Multinomial probit choice model
                                                                           3.075
                                                Number of obs
Case ID variable: consumerid
                                                Number of cases
                                                                             862
Alternatives variable: car
                                                Alts per case: min =
                                                                               3
                                                                             3.6
                                                                avg =
                                                               max =
                                                                               4
Integration sequence:
                           Hammersley
Integration points:
                                   704
                                                   Wald chi2(7)
                                                                           29.28
Log simulated-likelihood = -946.29158
                                                   Prob > chi2
                                                                          0.0001
                                                 P>|z|
   purchase
               Coefficient
                            Std. err.
                                                            [95% conf. interval]
                                            z
car
     dealers
                 .0702705
                             .0443614
                                          1.58
                                                 0.113
                                                          -.0166764
                                                                        .1572173
American
                (base alternative)
Japanese
      gender
      Male
                -.5091748
                             .1855698
                                         -2.74
                                                 0.006
                                                          -.8728849
                                                                       -.1454647
                  .013291
                                         1.98
                                                 0.048
                                                           .0001354
      income
                             .0067122
                                                                        .0264467
       _cons
                -.4826255
                             .3426393
                                         -1.41
                                                 0.159
                                                          -1.154186
                                                                        .1889353
European
      gender
                             .7110091
                                          1.10
                                                 0.270
                                                           -.609389
       Male
                 .7841632
                                                                        2.177715
                             .0163379
                                          1.81
                                                 0.070
      income
                 .0295921
                                                          -.0024296
                                                                        .0616137
                                         -1.25
                                                 0.210
                 -3.12152
                            2.487819
                                                          -7.997555
                                                                        1.754515
       cons
Korean
      gender
       Male
                 .5169588
                             .6933737
                                          0.75
                                                 0.456
                                                          -.8420287
                                                                        1.875946
      income
                -.0271951
                             .0210431
                                         -1.29
                                                 0.196
                                                          -.0684388
                                                                        .0140485
                                         -0.74
                                                 0.461
                 -1.15051
                             1.559623
                                                          -4.207315
                                                                        1.906296
       _cons
       /c1 3
                -1.407567
                             2.06088
                                         -0.68
                                                 0.495
                                                          -5.446817
                                                                        2.631683
       /c1_4
                 -1.70907
                             1.381238
                                         -1.24
                                                 0.216
                                                          -4.416247
                                                                        .9981077
```

(car=American is the alternative normalizing location) (car=Japanese is the alternative normalizing scale)

	American	Japanese	European	Korean
American Japanese European Korean	1 0 0 0	2 -1.407567 -1.70907	2.981244 2.40563	3.920919

. estat correlation

	American	Japanese	European	Korean
American	1.0000			
Japanese	0.0000	1.0000		
European	0.0000	-0.5764	1.0000	
Korean	0.0000	-0.6103	0.7036	1.0000

When using the structural option, you must carefully specify the covariance parameterization because, as we described earlier, not all of J(J+1)/2 elements of the covariance matrix are identifiable. There are at most J(J-1)/2-1 estimable parameters, so either elements have to be set to fixed values or constraints need to be imposed. Specifying any desired parameterization is straightforward. It merely requires learning how to use the correlation() and stddev() options. See *Covariance structures* in [CM] cmmprobit.

nlogit: Nested logit choice models

nlogit fits nested logit choice models. Alternatives can be nested within alternatives. For example, the data could represent first-level choices of what restaurant to dine at and second-level choices of what is ordered at the restaurant. Clearly, the menu choices will depend upon the type of restaurant. The second-level alternatives are conditional on the first-level alternatives.

Although nlogit fits choice models, it is not a cm command, and you do not have to cmset your data. Because of the nested alternatives, nlogit has its own unique data requirements.

See [CM] **nlogit** for full details on nested logit choice models.

Relationships with other estimation commands

If you are familiar with conditional logistic regression or with multinomial logistic regression, you may find it helpful to see how the cm commands, and in particular cmclogit, compare with Stata's clogit and mlogit commands.

Duplicating cmclogit using clogit

Both cmclogit and clogit fit conditional logistic regression models. cmclogit has special handling of errors, alternative-specific and case-specific variables, and special postestimation commands that are appropriate for choice data. However, you can fit the same model with cmclogit and clogit.

Before we try to duplicate our cmclogit results with clogit, we will drop the cases with missing values using the flag variable that we created with our earlier cmsample command. We do this because clogit does not handle missing values the same way cmclogit does. By default, cmclogit drops the entire case when any observation in the case has a missing value. clogit drops only the observations that contain missing values.

```
. drop if flag != 0
(85 observations deleted)
```

To duplicate our cmclogit results with clogit, we merely have to create interactions of the casespecific variables (gender and income) with the alternatives variable car. To do this, we include the factor-variable terms car##gender and car##c.income in our clogit specification. (We use c.income because income is continuous; see [U] 11.4.3 Factor variables for more on factor variables.) The alternative-specific variable dealers is included in the estimation as is.

. clogit purchase dealers car##gender car##c.income, group(consumerid)

note: 1.gender omitted because of no within-group variance.

```
note: income omitted because of no within-group variance.
Iteration 0: Log likelihood = -959.21405
Iteration 1: Log likelihood = -948.48587
Iteration 2: Log likelihood = -948.1217
Iteration 3:
              Log likelihood = -948.12096
Iteration 4:
              Log likelihood = -948.12096
Conditional (fixed-effects) logistic regression
                                                         Number of obs = 3.075
                                                         LR chi2(10)
                                                                       = 279.12
                                                         Prob > chi2
                                                                       = 0.0000
Log likelihood = -948.12096
                                                         Pseudo R2
                                                                       = 0.1283
               Coefficient Std. err.
                                                 P>|z|
                                                           [95% conf. interval]
   purchase
                 .0448082
                             .0262818
                                          1.70
                                                 0.088
                                                          -.0067032
                                                                        .0963196
     dealers
         car
                                        -1.44
                                                          -1.128215
  Japanese
                -.4787261
                             .331378
                                                 0.149
                                                                        .1707628
                                         -6.15
  European
                -2.839606
                             .461613
                                                 0.000
                                                          -3.744351
                                                                      -1.934861
     Korean
                 .0511728
                             .8033048
                                          0.06
                                                 0.949
                                                          -1.523276
                                                                       1.625621
      gender
       Male
                        0 (omitted)
  car#gender
   Japanese #
      Male
                 -.379326
                             .1712399
                                         -2.22
                                                 0.027
                                                            -.71495
                                                                      -.0437021
  European #
      Male
                  .653345
                             .2647694
                                         2.47
                                                 0.014
                                                           .1344065
                                                                       1.172283
Korean#Male
                 .0679233
                             .4464535
                                          0.15
                                                 0.879
                                                          -.8071094
                                                                        .942956
                           (omitted)
      income
car#c.income
                 .0154978
                             .0065145
                                          2.38
                                                 0.017
                                                           .0027296
                                                                        .0282659
  Japanese
                                                                       .0501006
                 .0343647
                             .0080286
                                         4.28
                                                 0.000
                                                           .0186289
  European
                                                           -.068824
                                                                      -.0067191
     Korean
                -.0377716
                             .0158434
                                        -2.38
                                                 0.017
```

The output is in a different order, but all the coefficient estimates and their standard errors are exactly the same as the earlier results from cmclogit.

And they should be—because cmclogit calls clogit to do the estimation.

Multinomial logistic regression and McFadden's choice model

Multinomial logistic regression (mlogit) is a special case of McFadden's choice model (cmclogit). When there are only case-specific variables in the model and when the choice sets are balanced (that is, every case has the same alternatives), then mlogit gives the same results as cmclogit.

We can illustrate this, but the choice data we are working with are not balanced. So let's just use a subset of the dataset that is balanced. We can see the distinct choice sets using cmchoiceset.

. cmchoiceset, generate(choiceset)

Tabulation of choice-set possibilities

Choice set	Freq.	Percent	Cum.
1 2 3 1 2 3 4	373 489	43.27 56.73	43.27 100.00
Total	862	100.00	

Note: Total is number of cases.

We included the generate() option to create an indicator variable choiceset with categories of the choice sets. We use this variable to keep only those cases that have the alternatives $\{1, 2, 3, 4\}$.

```
. keep if choiceset == "1 2 3 4":choiceset
(1,119 observations deleted)
```

(If you are not familiar with the "1 2 3 4":choiceset syntax, see [U] 13.11 Label values.)

Now we run cmclogit on this balanced sample:

```
. cmclogit purchase, casevars(i.gender income)
Iteration 0: Log likelihood = -580.83991
              Log likelihood = -575.60247
Iteration 1:
Iteration 2: Log likelihood = -575.21416
Iteration 3:
              Log likelihood = -575.21287
Iteration 4: Log likelihood = -575.21287
Conditional logit choice model
                                                Number of obs
                                                                           1.956
Case ID variable: consumerid
                                                Number of cases
                                                                             489
Alternatives variable: car
                                                                               4
                                                Alts per case: min =
                                                                             4.0
                                                                avg =
                                                                max =
                                                                               4
                                                   Wald chi2(6)
                                                                           41.24
Log likelihood = -575.21287
                                                   Prob > chi2
                                                                          0.0000
   purchase
               Coefficient
                            Std. err.
                                                 P>|z|
                                                            [95% conf. interval]
                                            z
American
                (base alternative)
Japanese
      gender
      Male
                -.7164669
                             .2351233
                                         -3.05
                                                 0.002
                                                                       -.2556338
                                                             -1.1773
                             .0087817
                                         1.99
                                                 0.047
                                                                        .0346493
      income
                 .0174375
                                                            .0002257
       _cons
                -.2370371
                             .4413551
                                         -0.54
                                                 0.591
                                                           -1.102077
                                                                        .6280029
European
      gender
                             .3494225
                                                           -.4719679
                                                                        .8977433
      Male
                 .2128877
                                          0.61
                                                 0.542
                             .0110817
                                          3.70
                                                 0.000
                                                            .0192494
      income
                 .0409691
                                                                        .0626888
       _cons
                -2.940079
                             .5956109
                                         -4.94
                                                 0.000
                                                           -4.107455
                                                                       -1.772703
Korean
      gender
      Male
                -.1892108
                             .4595242
                                         -0.41
                                                 0.681
                                                           -1.089862
                                                                          .71144
      income
                -.0361748
                             .016143
                                         -2.24
                                                 0.025
                                                           -.0678145
                                                                        -.004535
       _cons
                -.0367581
                             .8051745
                                         -0.05
                                                 0.964
                                                           -1.614871
                                                                        1.541355
```

To run mlogit, we must create a categorical dependent variable containing the chosen alternative, American, Japanese, European, or Korean. The values of the alternatives variable car at the observations representing the chosen alternative (purchase equal to one) yield a dependent variable appropriate for mlogit.

```
. keep if purchase == 1
(1,467 observations deleted)
. mlogit car i.gender income
Iteration 0: Log likelihood = -596.47415
Iteration 1: Log likelihood = -575.81328
Iteration 2: Log likelihood = -575.21417
Iteration 3: Log likelihood = -575.21287
Iteration 4: Log likelihood = -575.21287
                                                         Number of obs =
                                                                            489
Multinomial logistic regression
                                                         LR chi2(6)
                                                                       = 42.52
                                                         Prob > chi2
                                                                       = 0.0000
Log likelihood = -575.21287
                                                         Pseudo R2
                                                                       = 0.0356
         car
               Coefficient Std. err.
                                            z
                                                 P>|z|
                                                           [95% conf. interval]
American
                (base outcome)
Japanese
      gender
       Male
                -.7164669
                             .2351233
                                        -3.05
                                                 0.002
                                                            -1.1773
                                                                      -.2556338
      income
                 .0174375
                            .0087817
                                        1.99
                                                 0.047
                                                           .0002257
                                                                        .0346493
       _cons
                -.2370371
                             .4413551
                                        -0.54
                                                 0.591
                                                          -1.102077
                                                                        .6280029
European
      gender
                 .2128877
                             .3494225
                                         0.61
                                                 0.542
                                                          -.4719679
                                                                        .8977433
      Male
      income
                 .0409691
                            .0110817
                                         3.70
                                                 0.000
                                                           .0192494
                                                                        .0626888
                            .5956109
                                        -4.94
                                                 0.000
                                                          -4.107455
                                                                      -1.772703
       cons
                -2.940079
Korean
      gender
       Male
                -.1892108
                             .4595242
                                         -0.41
                                                 0.681
                                                          -1.089862
                                                                          .71144
                                        -2.24
                                                                       -.004535
      income
                -.0361748
                             .016143
                                                 0.025
                                                          -.0678145
                -.0367581
                             .8051745
                                        -0.05
                                                                       1.541355
                                                 0.964
                                                          -1.614871
       cons
```

The estimates are identical.

Estimation considerations

When fitting choice models, you may need to address issues such as setting the number of integration points, lack of convergence, or data with multiple outcomes selected. Below, we provide advice on these topics.

Setting the number of integration points

In Maximum simulated likelihood of [CM] Intro 8, we describe how the estimators for cmmixlogit, cmxtmixlogit, cmmprobit, and cmroprobit all approximate integrals using Monte-Carlo simulation to compute their likelihoods. Monte-Carlo simulation creates additional variance in the estimated results, and the variance is dependent on the number of points used in the integration. More points give smaller Monte-Carlo variance. Hence, when fitting final models, it is a good idea to use the option intpoints (#) to increase the number of integration points and check that the coefficient and parameter estimates and their standard estimates are stable. That is, check that they do not change appreciably as the number of integration points is increased.

In the first cmmprobit example in this introduction, the default number of integration points was 704. We stored the coefficient vector from that estimation in the vector b704. Let's open a fresh copy of our data and refit the same model, specifying intpoints (2000).

```
. use https://www.stata-press.com/data/r19/carchoice, clear
(Car choice data)
. cmset consumerid car
note: alternatives are unbalanced across choice sets; choice sets of
      different sizes found.
     Case ID variable: consumerid
Alternatives variable: car
. cmmprobit purchase dealers, casevars(i.gender income) factor(1)
> intpoints(2000)
 (iteration log omitted)
Multinomial probit choice model
                                                 Number of obs
                                                                             3,075
Case ID variable: consumerid
                                                 Number of cases
                                                                               862
Alternatives variable: car
                                                 Alts per case: min =
                                                                                 3
                                                                 avg =
                                                                               3.6
                                                                 max =
                                                                                 4
Integration sequence:
                            Hammersley
Integration points:
                                   2000
                                                     Wald chi2(7)
                                                                             32.62
                                                                            0.0000
Log simulated-likelihood = -946.31243
                                                     Prob > chi2
    purchase
               Coefficient
                             Std. err.
                                             7.
                                                  P>|z|
                                                             [95% conf. interval]
car
     dealers
                  .0440584
                              .0279595
                                           1.58
                                                  0.115
                                                            -.0107413
                                                                          .0988581
American
                 (base alternative)
Japanese
      gender
       Male
                -.4558936
                              .1451544
                                          -3.14
                                                  0.002
                                                            -.7403911
                                                                         -.1713961
      income
                  .0091975
                              .0054259
                                           1.70
                                                  0.090
                                                            -.0014371
                                                                           .019832
                                          -1.50
                -.4174474
                              .2776516
                                                  0.133
                                                            -.9616346
                                                                          .1267397
       _cons
European
      gender
       Male
                  .5769601
                               .440494
                                           1.31
                                                  0.190
                                                            -.2863923
                                                                          1.440312
      income
                  .0204216
                              .0108952
                                           1.87
                                                  0.061
                                                            -.0009325
                                                                          .0417757
       _cons
                -2.326064
                             1.586287
                                          -1.47
                                                  0.143
                                                             -5.43513
                                                                          .7830022
Korean
      gender
       Male
                  .3182167
                              .5023253
                                           0.63
                                                  0.526
                                                            -.6663228
                                                                          1.302756
      income
                -.0345119
                              .033025
                                          -1.05
                                                  0.296
                                                            -.0992398
                                                                           .030216
       _cons
                -.9586927
                             1.055673
                                          -0.91
                                                  0.364
                                                            -3.027774
                                                                          1.110389
       /c1_2
                 -.8967061
                             1.400022
                                          -0.64
                                                   0.522
                                                            -3.640699
                                                                          1.847287
                  -1.66729
                             1.366339
                                          -1.22
                                                  0.222
                                                            -4.345265
                                                                          1.010685
       /c1 3
```

(car=American is the alternative normalizing location)
(car=Japanese is the alternative normalizing scale)

[.] matrix b2000 = e(b)

[.] display mreldif(b704, b2000)

^{.02582208}

We now double the number of integration points to 4000 and store the coefficient vector in b4000. We omit showing the cmmprobit results and show only the comparison of the coefficient vectors:

```
. display mreldif(b2000, b4000)
.00176597
```

The relative difference declined as intpoints () is increased. The maximum relative difference between the estimation with 2000 points and the one with 4000 points is only 0.2%.

When we look at the differences between coefficients from different runs, it is important to note the values of the coefficients relative to their standard errors. For example, we may have a variance parameter that is near zero with a big standard error (relative to the parameter estimate). The relative difference of the parameter estimate between runs with different intpoints() may not decline rapidly with increasing numbers of points because we are essentially just fitting random noise.

Convergence

Sometimes, you will try to fit a model with one of the CM commands, and the model will not converge. You might see an iteration log that goes on and on with (backed up) or (not concave) at the end of each line.

In the previous section, we showed you how increasing the number of integration points using the option intpoints (#) improves precision of the estimates by reducing the random variance of the Monte-Carlo integration. The randomness of the Monte-Carlo integration can affect convergence in a random way. It is possible that rerunning the command with a different random-number seed (using set seed # or the option intseed(#)) may cause a model to converge that previously did not. Increasing the number of integration points might cause a model to converge that did not when fewer points were used. It is also possible that a model may converge using the default number of integration points, but no longer converge when more integration points are used.

Our advice is when your model is not converging, first try increasing the number of integration points. If this does not help, try thinking about your model. Perhaps, this should have been the first thing to try. But this might be more painful than setting intpoints() to a big number.

Lack of convergence may be trying to tell you something about your model. Perhaps, the model is misspecified. That is, your model is not close to the true data-generating process. Or, perhaps, you simply need to collect more data.

You may want to try simplifying your model. It is best to start with a covariance parameterization with just a few parameters and then gradually increase them. For cmmprobit, using correlation(independent) and stddev(heteroskedastic) is a good model to start with. Look at the variances before trying to parameterize any correlations. Using correlation(fixed matname) lets you specify which elements are fixed and which are estimated. You can also fit models with just one free correlation parameter. cmroprobit, which we describe in [CM] Intro 6, has the same options and the same advice can be followed.

For the mixed logit models fit by cmmixlogit and cmxtmixlogit, the covariance parameterization is specified by different options, but the same general advice applies. If you are having convergence problems, start with a simple model and gradually increase the number of covariance parameters estimated.

What if we have data in which more than one alternative is chosen for some of or all the cases?

Well, first, we need to assess whether the data are in fact rank-ordered alternatives. If so, see [CM] **Intro** 6. There are two CM estimators for rank-ordered alternatives: cmrologit and cmroprobit.

Second, we need to assess whether the data are perhaps actually panel data and whether the choices were made at different times. For example, we might have data on how people commuted to work on a given week. Some people may have driven a car every day, but some may have driven a car some days and taken the bus on other days. Data such as these are panel data. If we have data by day of the week, we can analyze them as panel data. See [CM] Intro 7 and example 4 in [CM] cmclogit.

But what if the data arose from a design in which multiple choices were allowed and not ranked? For example, suppose consumers were given four breakfast cereals and asked to pick their two favorites, without picking a single most favorite. These data are not rank-ordered data, nor are they panel data.

We note that the random utility model (see [CM] Intro 8) for discrete choices yields only one chosen alternative per case: that with the greatest utility. In rank-ordered models, it yields a set of ranked alternatives without any ties. Because the utility function is continuous, ties are theoretically impossible.

Train (2009, sec. 2.2) notes that the set of alternatives can always be made mutually exclusive by considering the choice of two alternatives as a separate alternative. For example, with one or two choices allowed from alternatives A, B, and C, the set of alternatives is A only, B only, C only, A and B, A and B, and B and B

References

McFadden, D. L., and K. E. Train. 2000. Mixed MNL models for discrete response. *Journal of Applied Econometrics* 15: 447–470. https://doi.org/10.1002/1099-1255(200009/10)15:5<447::AID-JAE570>3.0.CO;2-1.

Train, K. E. 2009. Discrete Choice Methods with Simulation. 2nd ed. New York: Cambridge University Press. https://doi.org/10.1017/CBO9780511805271.

Also see

[CM] Intro 1 — Interpretation of choice models

[CM] Intro 2 — Data layout

[CM] Intro 3 — Descriptive statistics

[CM] Intro $\mathbf{4}$ — Estimation commands

[CM] cmclogit — Conditional logit (McFadden's) choice model

[CM] cmmixlogit — Mixed logit choice model

[CM] **cmmprobit** — Multinomial probit choice model

[CM] **nlogit** — Nested logit regression

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