

[Description](#)  
[Option](#)  
[References](#)[Quick start](#)  
[Remarks and examples](#)  
[Also see](#)[Menu](#)  
[Stored results](#)[Syntax](#)  
[Methods and formulas](#)

## Description

`bmastats msize` provides a model-size summary after the `bmaregress` command. `bmastats msize` is useful to assess the overall complexity of the models in Bayesian model averaging (BMA) weighted by their prior and posterior model probabilities. By comparing the overall posterior model sizes with the prior model sizes, we can also assess the impact of the data on the BMA analysis.

## Quick start

Display prior and posterior model-size summary

```
bmastats msize
```

Include a constant term in the model-size computations

```
bmastats msize, constant
```

## Menu

Statistics > Bayesian model averaging > Model-size summary

## Syntax

```
bmastats msize [ , constant ]
```

`collect` is allowed; see [\[U\] 11.1.10 Prefix commands](#).

## Option

Main

`constant` specifies that the constant term be included in model-size computations. By default, the constant term is not included.

## Remarks and examples

Model size is the number of predictors included in a model. The constant term is typically not included in the model size. In BMA, there are multiple models, so we have a distribution of the model sizes. The model prior determines the prior model-size distribution. After you observe the data, the model prior is updated to form the posterior model-size distribution.

You can use the model-size distribution summaries to explore the complexity of the fitted BMA model. For instance, when the posterior median model size is small relative to the total number of regression terms, this means there are only a few strong predictors of the outcome. Conversely, when it is large, there are many weak potential predictors. And by comparing the posterior model size with the prior one, we can assess how the data affect our prior knowledge.

The prior model-size distribution can be computed analytically based on the known formula, with a caveat that in cases when the model space is not explored fully, this analytical distribution is conditional on the visited models.

The posterior model-size distribution is available analytically only with [fixed  \$g\$](#)  and is thus not provided with [random  \$g\$](#) .

Whenever a posterior Markov chain Monte Carlo (MCMC) model sample is available, such as with [random  \$g\$](#)  or when `bmaregress`'s `sampling` option is used, the posterior model-size distribution can be estimated from the sample by using sampling frequencies. See [Methods and formulas](#) for details.

`bmastats msize` reports prior and posterior model-size summaries, including mean and median model sizes. For prior model-size summary, it always provides the analytical estimates. For posterior model-size summary, it provides the analytical estimates with [fixed  \$g\$](#)  and the frequency estimates with [random  \$g\$](#) . With [fixed  \$g\$](#)  and MC3 sampling, the command provides both types of estimates. By default, the constant is not included in the model-size computations, but you can specify the `constant` option to include it.

### ► Example 1: Model-size analysis after BMA regression using enumeration

Consider the performance dataset ([Chatterjee and Hadi 2012](#), sec. 3.3) analyzed in [example 1](#) of [\[BMA\] `bmaregress`](#). The employees' satisfaction with their supervisors, `rating`, is modeled by six potential predictors. The total of 30 observations represent 30 different departments in the surveyed organization.

We fit a linear BMA regression using the `bmaregress` command.

```
. use https://www.stata-press.com/data/r19/performance
(Data on employee satisfaction with supervisor)
. bmaregress rating complaints-advance
Enumerating models ...
Computing model probabilities ...
Bayesian model averaging          No. of obs      =      30
Linear regression                 No. of predictors =      6
Model enumeration                  Groups         =      6
                                   Always            =      0
Priors:                           No. of models   =     64
  Models: Beta-binomial(1, 1)      For CPMP >= .9 =     10
  Cons.: Noninformative           Mean model size =  1.699
  Coef.: Zellner's g
    g: Benchmark, g = 36          Shrinkage, g/(1+g) = 0.9730
  sigma2: Noninformative         Mean sigma2      = 52.302
```

rating	Mean	Std. dev.	Group	PIP
complaints	.7052859	.1224289	1	.99973
learning	.0603014	.1285281	3	.25249
advance	-.0167921	.073883	6	.13148
privileges	-.0074174	.0488635	2	.10998
raises	.0070789	.0670475	4	.10642
critical	.0009713	.0437848	5	.098534
Always				
_cons	14.8472	7.874219	0	1

Note: Coefficient posterior means and std. dev. estimated from 64 models.  
Note: Default priors are used for models and parameter *g*.

From the output, the model space is fully explored through enumeration. There is a total of  $2^6 = 64$  models in the full model space.

Let's use `bmastats msize` to compute the model-size summary.

```
. bmastats msize
Model-size summary
Number of models = 64
Model size:
  Minimum = 0
  Maximum = 6
```

	Mean	Median
Prior		
Analytical	3.0000	3
Posterior		
Analytical	1.6986	1

Note: Frequency summaries not available.

The reported model size does not include the constant, so its range is between 0 and 6. The prior mean and median model sizes are both 3. The posterior mean and median model sizes are, respectively, 1.699 and 1. (The posterior mean model size is the same as the one reported by `bmaregress`.)

The default model prior distribution assumes a uniform prior on the model size. The prior mean model size, 3, is larger than the posterior one, 1.699. The posterior favors smaller models.

For the prior model-size summary, `bmastats msize` always reports analytical estimates. With model enumeration, it reports analytical estimates for the posterior model-size summary too. Frequency-based posterior estimates are not available here because there is no MCMC sample for the models—the models were enumerated.



➤ Example 2: Model-size analysis after BMA regression using MC3 sampling

We fit the same BMA model as in [example 1](#), but this time we use the MC3 sampling algorithm.

```
. bmaregress rating complaints-advance, sampling rseed(18)
Burn-in ...
Simulation ...
Computing model probabilities ...

Bayesian model averaging      No. of obs      =      30
Linear regression            No. of predictors =       6
MC3 sampling                  Groups           =       6
                               Always            =       0
                               No. of models    =      32
                               For CPMP >= .9    =     10
                               Mean model size   =   1.699
                               Burn-in           =   2,500
                               MCMC sample size  = 10,000
                               Acceptance rate    =   0.2417
                               Shrinkage, g/(1+g) =   0.9730
                               Mean sigma2       =  52.292

Priors:
  Models: Beta-binomial(1, 1)
  Cons.: Noninformative
  Coef.: Zellner's g
         g: Benchmark, g = 36
  sigma2: Noninformative
Sampling correlation = 0.9990
```

rating	Mean	Std. dev.	Group	PIP
complaints	.705479	.1218881	1	1
learning	.0601919	.1282869	3	.25234
advance	-.0167514	.0737415	6	.13141
privileges	-.0074265	.048844	2	.10996
raises	.0069949	.0666406	4	.10629
critical	.0009699	.0437742	5	.098526
Always				
_cons	14.84478	7.871046	0	1

Note: Coefficient posterior means and std. dev. estimated from 32 models.  
Note: Default priors are used for models and parameter *g*.

Instead of enumerating models, `bmaregress` generates a sample from the posterior model distribution that includes 32 different models.

```
. bmastats msize
Model-size summary
Number of models = 32
Model size:
  Minimum = 1
  Maximum = 6
```

	Mean	Median
Prior		
Analytical	4.3333	5
Posterior		
Analytical	1.6985	1
Frequency	1.7791	1

Here the minimum model size is 1, compared with 0 in [example 1](#). This means that the null model, having a low posterior probability, was not visited by the MC3 sampler.

Although we used the same model prior as in [example 1](#), the prior model-size estimates are different. This is because our explored model space now contains 32 models instead of all 64, and the prior model-size estimates are now conditional on the visited models.

With fixed  $g$  and when we fit a BMA model using MC3 sampling, in addition to analytical model-size estimates, the frequency estimates are also available. Provided that the model-space sampling converges, the analytical and frequency estimates should be close. In our example, the analytical and frequency model-size estimates, 1.7 and 1.8, are close.

We can also explore the effect of the  $g$  parameter on the complexity of our BMA model. Let us, for example, fix  $g$  to 1, which is much lower than the default value of 36 used above.

```
. bmaregress rating complaints-advance, gprior(fixed 1) sampling rseed(18)
Burn-in ...
Simulation ...
Computing model probabilities ...
Bayesian model averaging          No. of obs      =      30
Linear regression                No. of predictors =       6
MC3 sampling                     Groups          =       6
                                Always            =       0
                                No. of models   =      63
                                For CPMP >= .9 =      29
Priors:
  Models: Beta-binomial(1, 1)    Mean model size =    3.731
  Cons.: Noninformative         Burn-in         =    2,500
  Coef.: Zellner's g            MCMC sample size = 10,000
    g: g = 1                    Acceptance rate  =    0.5678
    sigma2: Noninformative      Shrinkage, g/(1+g) = 0.5000
                                Mean sigma2        = 103.952
Sampling correlation = 0.9957
```

rating	Mean	Std. dev.	Group	PIP
complaints	.3188165	.158556	1	.94416
learning	.0944454	.1508832	3	.61347
advance	-.0520093	.137935	6	.55788
raises	.030129	.1654381	4	.5473
privileges	-.0163312	.1027766	2	.53808
critical	.0062495	.1066877	5	.52978
Always				
_cons	38.76265	10.36275	0	1

Note: Coefficient posterior means and std. dev. estimated from 63 models.  
Note: Default prior is used for models.

```
. bmastats msize
Model-size summary
Number of models = 63
Model size:
  Minimum = 0
  Maximum = 6
```

	Mean	Median
Prior		
Analytical	3.0488	3
Posterior		
Analytical	3.7307	4
Frequency	3.6529	4

The posterior mean model size has increased to 3.73, and the posterior median model size has increased to 4. With  $g = 1$ , BMA appears to favor larger models.

➤ Example 3: Model-size analysis after BMA regression with random  $g$

Both [example 1](#) and [example 2](#) used a fixed  $g$ . Let’s explore the case of a random  $g$ . (An in-depth coverage of the effects of the  $g$ -prior on model complexity can be found in, for example, [Ley and Steel \[2012\]](#).)

To demonstrate, we will use a robust prior for  $g$ .

```
. bmaregress rating complaints-advance, gprior(robust) rseed(18)
Burn-in ...
Simulation ...
Computing model probabilities ...

Bayesian model averaging          No. of obs      =      30
Linear regression                No. of predictors =       6
MC3 and adaptive MH sampling      Groups         =       6
                                   Always            =       0
                                   No. of models    =      34
                                   For CPMP >= .9    =      12
                                   Mean model size  =   1.734
                                   Burn-in          =   2,500
                                   MCMC sample size = 10,000
                                   Acceptance rate   = 0.4232

Priors:
  Models: Beta-binomial(1, 1)      Mean sigma2     = 53.095
  Cons.: Noninformative
  Coef.: Zellner's g
        g: Robust
  sigma2: Noninformative
Sampling correlation = 0.9994
```

rating	Mean	Std. dev.	Group	PIP
complaints	.7000463	.1273543	1	.9998
learning	.0594904	.1286095	3	.25
advance	-.0192712	.0797935	6	.1503
raises	.0079416	.0727859	4	.1201
privileges	-.0072591	.0487009	2	.1069
critical	.0014397	.0466476	5	.1067
Always				
_cons	15.24911	7.988166	0	1

Note: Coefficient posterior means and std. dev. estimated from 34 models.  
Note: Default prior is used for models.

	Mean	Std. dev.	MCSE	Median	Equal-tailed [95% cred. interval]	
g	152.668	1968.132	43.5265	33.81024	8.205076	610.6026
Shrinkage	.9656427	.0276071	.001234	.9712728	.8913639	.9983649

bmaregress now uses MC3 sampling for the models and an adaptive Metropolis–Hastings sampling for  $g$ .

```
. bmastats msize
Model-size summary
Number of models = 34
Model size:
  Minimum = 1
  Maximum = 6
```

	Mean	Median
Prior Analytical	4.1786	4
Posterior Frequency	1.7338	1

Note: Analytical summaries not available.

Analytical posterior estimates are not available with random  $g$ . The frequency posterior estimates are similar to those in [example 2](#) for fixed  $g = 36$ .

◀

## Stored results

bmastats msize stores the following in `r()`:

Scalars

<code>r(k_models)</code>	number of models
<code>r(msize_mean_prior)</code>	prior mean model size
<code>r(msize_mean_a)</code>	analytical posterior mean model size (not available with random $g$ )
<code>r(msize_mean_f)</code>	frequency posterior mean model size (not available with model enumeration)
<code>r(constant)</code>	1 if constant is specified; 0 otherwise

Matrices

<code>r(modelsize)</code>	model-size summary
---------------------------	--------------------

## Methods and formulas

Consider a BMA regression model for an outcome vector  $\mathbf{y}$  with  $p$  predictors. Let  $\mathcal{M}_F = \{M_1, M_2, \dots, M_{2^p}\}$  denote the full space of models formed by considering all  $2^p$  possible subsets of  $p$  variables, and let  $J_F = \{1, 2, \dots, 2^p\}$  denote the full set of the corresponding indices. Let  $|M|$  denote the model size of a regression model  $M$  from  $\mathcal{M}_F$ ; that is,  $|M|$  equals the number of predictors included in model  $M$ .

The prior distribution of  $|M|$  is a discrete distribution on the set  $\{0, 1, \dots, p\}$  such that

$$\Pr(|M| = s) = \sum_{j=1}^{2^p} I(|M_j| = s) P(M_j)$$

where  $I(\cdot)$  is an indicator function,  $M_j$ 's are all possible enumerated models from  $\mathcal{M}_F$ , and  $P(M_j)$ 's are the prior model probabilities.



Similarly, the posterior distribution of  $|M|$  is defined as

$$\Pr(|M| = s | \mathbf{y}) = \sum_{j=1}^{2^p} I(|M_j| = s) P_a(M_j | \mathbf{y})$$

where  $P_a(M_j | \mathbf{y})$ 's are the analytical posterior model probabilities defined by (7) in *Posterior model probability* in *Methods and formulas* of [BMA] **bmaregress**.

When the model space is fully explored through enumeration, the analytical prior mean model size is

$$E(|M|) = \sum_{j=1}^{2^p} |M_j| P(M_j)$$

and the analytical posterior mean model size is

$$E(|M| | \mathbf{y}) = \sum_{j=1}^{2^p} |M_j| P_a(M_j | \mathbf{y})$$

When model sampling is used instead of model enumeration, the analytical prior mean model size is estimated conditionally on the subspace of the visited models indexed by  $J \subset J_F$ :

$$\widehat{E}(|M|) = \frac{\sum_{j \in J} |M_j| P(M_j)}{\sum_{j \in J} P(M_j)}$$

With fixed  $g$  and when model sampling is used, such as when **bmaregress**'s `sampling` option is specified, the analytical posterior mean model size is estimated as

$$\widehat{E}_a(|M| | \mathbf{y}) = \frac{\sum_{j \in J} |M_j| P_a(M_j | \mathbf{y})}{\sum_{j \in J} P_a(M_j | \mathbf{y})}$$

With random  $g$ , analytical formulas for posterior model probabilities and posterior model-size probabilities are not available.

When a posterior MCMC sample of models,  $\{m_t\}_{t=1}^T$ , is available, such as with random  $g$  or when **bmaregress**'s `sampling` option is used, the frequency estimate of the posterior mean model size is computed as follows:

$$\widehat{E}_f(|M| | \mathbf{y}) = \frac{1}{T} \sum_{t=1}^T |m_t|$$

## References

- Chatterjee, S., and A. S. Hadi. 2012. *Regression Analysis by Example*. 5th ed. New York: Wiley.
- Ley, E., and M. F. J. Steel. 2012. Mixtures of  $g$ -priors for Bayesian model averaging with economic applications. *Journal of Econometrics* 171: 251–266. <https://doi.org/10.1016/j.jeconom.2012.06.009>.

## Also see

[BMA] **bmagraph msize** — Model-size distribution plots after BMA regression

[BMA] **bmastats** — Summary for models and predictors after BMA regression

[BMA] **bmaregress** — Bayesian model averaging for linear regression

[BMA] **BMA postestimation** — Postestimation tools for Bayesian model averaging

[BMA] **Glossary**

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