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Description

`bayesstats ic` calculates and reports model-selection statistics, including the deviance information criterion (DIC), log marginal-likelihood, and Bayes factors (BFs), using current Bayesian estimation results. BFs can be displayed in the original metric or in the log metric. The command also provides two different methods to approximate marginal likelihood.

Quick start

Information criteria for previously saved estimation results A and B with A used as the base model by default

```
bayesstats ic A B
```

Same as above, but use B as the base model instead of A

```
bayesstats ic A B, basemodel(B)
```

Report BFs instead of the default log BFs

```
bayesstats ic A B, bayesfactor
```

Menu

Statistics > Bayesian analysis > Information criteria

Syntax

```
bayesstats ic [ namelist ] [ , options ]
```

namelist is a name, a list of names, `_all`, or `*`. A name may be `.`, meaning the current (active) estimates. `_all` and `*` mean the same thing.

<i>options</i>	Description
Main	
<code>basemodel(<i>name</i>)</code>	specify a base or reference model; default is the first-listed model
<code>bayesfactor</code>	report BFs instead of the default log BFs
<code>diconly</code>	report only DIC
<code>* chains(<i>_all</i> <i>numlist</i>)</code>	specify which chains to use for computation; default is <code>chains(<i>_all</i>)</code>
<code>* sepchains</code>	compute results separately for each chain
Advanced	
<code>marglmethod(<i>method</i>)</code>	specify marginal-likelihood approximation method; default is to use Laplace–Metropolis approximation, <code>lmetropolis</code> ; rarely used
* Options <code>chains()</code> and <code>sepchains</code> are relevant only when option <code>nchains()</code> is used during Bayesian estimation. <code>collect</code> is allowed; see [U] 11.1.10 Prefix commands.	
<i>method</i>	Description
<code>lmetropolis</code>	Laplace–Metropolis approximation; the default
<code>hmean</code>	harmonic-mean approximation

Options

Main

`basemodel(name)` specifies the name of the model to be used as a base or reference model when computing BFs. By default, the first-listed model is used as a base model.

`bayesfactor` specifies that BFs be reported instead of the default log BFs.

`diconly` specifies that only DIC be reported in the table and that the log marginal-likelihood and Bayes factors be omitted from the table. Options `basemodel()`, `basefactor`, and `marglmethod()` have no effect when the `diconly` option is specified.

`chains(_all | numlist)` specifies which chains from the MCMC sample to use for computation. The default is `chains(_all)` or to use all simulated chains. Using multiple chains, provided the chains have converged, generally improves MCMC summary statistics. Option `chains()` is relevant only when option `nchains()` is used during Bayesian estimation.

`sepchains` specifies that the results be computed separately for each chain. The default is to compute results using all chains as determined by option `chains()`. Option `sepchains` is relevant only when option `nchains()` is used during Bayesian estimation.

Advanced

`marglmethod(method)` specifies a method for approximating the marginal likelihood. *method* is either `lmetropolis`, the default, for Laplace–Metropolis approximation or `hmean` for harmonic-mean approximation. This option is rarely used.

Remarks and examples

Remarks are presented under the following headings:

Bayesian information criteria
Bayes factors
Using bayesstats ic

Bayesian information criteria

Bayesian information criteria are used for selecting a model among a set of candidate models that best fits the data. Likelihood-based inference is known to be prone to overfitting the data. Indeed, it is often possible to increase the likelihood by simply including more parameters in a model. Bayesian information criteria address this problem by applying a penalty proportional to the complexity of the models to the likelihood.

Consider a finite set of Bayesian models M_1, \dots, M_r , which we want to compare with a base model M_b . All models M_j s are fit to the same dataset but may differ in their likelihood or prior specification.

Three commonly used information criteria are Akaike information criterion (AIC), Bayesian information criterion (BIC), and DIC. All three criteria are likelihood based and include a goodness-of-fit term proportional to the negative likelihood of the model and a penalty term proportional to the number of parameters in the model. Models with smaller values of these criteria are preferable.

The BIC, originally derived for the exponential family of distributions, is based on the assumption that the model has a flat, noninformative prior. In frequentist statistics, BIC is widely used as a variable-selection criterion, particularly in linear regression. In BIC, the penalty term is a product of the number of parameters in the model and the log of the sample size. The penalty of BIC thus increases not only with the number of parameters but also with the sample size. In the AIC, the penalty term is two times the number of parameters and does not depend on the sample size. As a result, BIC is more conservative than AIC and prefers simpler models. DIC is similar to AIC, but its penalty term is based on a complexity term that measures the difference between the expected log likelihood and the log likelihood at the posterior mean point. DIC is designed specifically for Bayesian estimation that involves MCMC simulations.

The limitation of all three criteria is that they either ignore prior distributions or assume that prior distributions are noninformative. They are thus not well suited for Bayesian sensitivity analysis, when models with the same parameters but different priors are being compared.

The `bayesstats ic` command reports DIC. See [R] [estat ic](#) after the corresponding maximum likelihood estimation command for values of AIC and BIC.

Bayes factors

In Bayesian inference, BFs are preferred to model-selection criteria because, unlike BIC, AIC, and DIC, they incorporate the information about model priors. Taking into account prior information is essential for Bayesian sensitivity analysis, when models with the same parameters but different priors are being compared.

The BF of two models is just the ratio of their marginal likelihoods calculated using the same dataset. Unlike BIC, AIC, and DIC, BFs include all information about the specified Bayesian model. Thus BFs are not applicable to models with improper priors, whereas BIC, AIC, and DIC are still applicable because they ignore prior information. BFs, however, are often difficult to compute reliably because of the difficulty in computing marginal likelihoods.

BFs also require that posterior distributions be completely specified, including the normalizing constants. The latter is especially important in Bayesian estimation using MCMC simulations, when the normalizing constants are often omitted from the specification of a posterior distribution. The Bayesian estimation commands always simulate from a complete posterior distribution when you select one of the supported Bayesian models, but you need to make sure to include all normalizing constants with your posterior distribution when you are programming your own Bayesian model (see [BAYES] bayesmh evaluators) and would like to use BFs during postestimation.

Let BF_{jb} , $j = 1, \dots, r$, be the BF of model M_j with respect to the base model M_b . All models M_j are fit to the same dataset; otherwise, BFs are meaningless. The bayesstats ic command calculates BF_{jb} 's and reports them in log metric or in absolute metric when the bayesfactor option is specified.

Jeffreys (1961) proposes the following interpretation of the values of BF_{jb} based on half-units of the log metric:

$\log_{10}(BF_{jb})$	BF_{jb}	Evidence against M_b
0 to 1/2	1 to 3.2	Bare mention
1/2 to 1	3.2 to 10	Substantial
1 to 2	10 to 100	Strong
>2	>100	Decisive

Kass and Raftery (1995) suggest using twice the natural logarithm of the BF to make it have the same scale as the DIC and likelihood-ratio test statistic. They suggest the following interpretation table:

$2 \log_e(BF_{jb})$	BF_{jb}	Evidence against M_b
0 to 2	1 to 3	Bare mention
2 to 6	3 to 20	Positive
6 to 10	20 to 150	Strong
>10	>150	Very strong

Typically, the worst-fitting model is chosen as a base model. If the base model happens to be better than the comparison model, the corresponding BF will be negative. In this case, you can apply results above to the absolute value of the BF.

BFs compute relative probabilities of how well each model fits the data compared with the base model. Being relative quantities, BFs cannot be used to measure goodness of fit of a particular model unless one assumes that the base model fits the data well. Some researchers view this as a limitation of BFs (Gelman et al. 2014). Kass and Raftery (1995), on the other hand, show that BFs can be viewed as differences between predictive scores and thus can be used to measure success of different models at predicting the data.

BFs have several advantages over the more traditional, frequentist testing methods. For example, they do not have the limitation of the p -value approach to systematically reject the null hypothesis in large samples. BFs are also suitable for comparing both nonnested and nested models. Also see [Comparing Bayesian models](#) in [BAYES] [Intro](#) for more information about Bayesian model comparison.

A key element in computing BFs is calculating the marginal likelihood. Except for some rare cases, marginal likelihood does not have a closed form and needs to be approximated. A detailed review of different approximation methods is given by [Kass and Raftery \(1995\)](#). The default method implemented in `bayesstats ic` (and `bayesmh`) is the Laplace–Metropolis approximation ([Lewis and Raftery 1997](#)). The harmonic-mean approximation of the marginal likelihood is also available via the `marglmethod(hmean)` option, but we recommend that you use the default method. See [Methods and formulas](#) in [BAYES] `bayesmh` for technical details.

Using bayesstats ic

► Example 1

The `bayesstats ic` command provides several model-selection statistics that can be used to compare models. To illustrate the use of `bayesstats ic`, we consider `auto.dta`. We model the fuel-efficiency variable `mpg` using a normal distribution with fixed variance but unknown, random mean. There is only one random parameter in this model—`{mpg: _cons}`. We compare the models with three different prior distributions to find the best one among them. We fit the three models using `bayesmh` and save the corresponding estimation results as `uniform1`, `uniform2`, and `normal`.

First, for comparison purposes, let’s obtain the maximum likelihood estimate (MLE) of the mean of `mpg`, which is simply the sample mean in our example:

```
. use https://www.stata-press.com/data/r19/auto
(1978 automobile data)
. summarize mpg
```

Variable	Obs	Mean	Std. dev.	Min	Max
mpg	74	21.2973	5.785503	12	41

The sample mean of `mpg` is roughly 21.3.

Next, we use `bayesmh` to fit our first model of interest. We fix the variance of the normal distribution to 30, which is close to the estimated variance of `mpg` of $5.79^2 = 33.52$.

```
. set seed 14
. bayesmh mpg, likelihood(normal(30))
> prior({mpg:_cons}, uniform(-10, 10))
> initial({mpg:_cons} 2) saving(uniform1_simdata)
```

Burn-in ...
Simulation ...

Model summary

Likelihood:

`mpg ~ normal({mpg:_cons},30)`

Prior:

`{mpg:_cons} ~ uniform(-10,10)`

Bayesian normal regression	MCMC iterations =	12,500
Random-walk Metropolis-Hastings sampling	Burn-in =	2,500
	MCMC sample size =	10,000
	Number of obs =	74
	Acceptance rate =	.4102
Log marginal-likelihood = -397.42978	Efficiency =	.08018

mpg	Mean	Std. dev.	MCSE	Median	Equal-tailed [95% cred. interval]	
_cons	9.965511	.0342812	.001211	9.975729	9.871825	9.998796

file **uniform1_simdata.dta** saved.

. estimates store uniform1

In the first model, we deliberately chose a prior for `{mpg:_cons}, uniform(-10, 10)`, that does not include the value of the sample mean. We thus expect this model to fit poorly. Because of the restricted domain of the specified uniform prior, we also needed to specify an initial value for `{mpg:_cons}` for MCMC to start from a point of positive posterior probability.

We also specified the `saving()` option to save the MCMC simulation dataset so that we could use `estimates store` to store our estimation results for future use. See [Storing estimation results after Bayesian estimation](#) in [\[BAYES\] Bayesian postestimation](#) for details.

```
. set seed 14
. bayesmh mpg, likelihood(normal(30))
> prior({mpg:_cons}, uniform(10, 30))
> initial({mpg:_cons} 20) saving(uniform2_simdata)
```

Burn-in ...
Simulation ...

Model summary

Likelihood:

mpg ~ normal({mpg:_cons},30)

Prior:

{mpg:_cons} ~ uniform(10,30)

Bayesian normal regression	MCMC iterations =	12,500
Random-walk Metropolis-Hastings sampling	Burn-in =	2,500
	MCMC sample size =	10,000
	Number of obs =	74
	Acceptance rate =	.4272
Log marginal-likelihood = -237.08583	Efficiency =	.2414

mpg	Equal-tailed					
	Mean	Std. dev.	MCSE	Median	[95% cred. interval]	
_cons	21.31085	.6447073	.013123	21.31485	20.06381	22.57936

file **uniform2_simdata.dta** saved.

. estimates store uniform2

In the second model, we used a uniform prior that included the value of the sample mean in its domain.

```
. set seed 14
. bayesmh mpg, likelihood(normal(30))
> prior({mpg:_cons}, normal(30)) saving(normal_simdata)
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
  mpg ~ normal({mpg:_cons},30)
Prior:
  {mpg:_cons} ~ normal(0,30)
```

```
Bayesian normal regression                                MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling                  Burn-in         =     2,500
                                                         MCMC sample size =   10,000
                                                         Number of obs    =     74
                                                         Acceptance rate   =    .4295
Log marginal-likelihood = -244.16624                      Efficiency      =    .2319
```

mpg	Mean	Std. dev.	MCSE	Median	Equal-tailed [95% cred. interval]	
_cons	21.01901	.6461194	.013417	21.01596	19.76637	22.3019

```
file normal_simdata.dta saved.
. estimates store normal
```

In the third model, we used a normal prior with a variance fixed at 30. Note that we did not need to specify an initial value for {mpg:_cons} in this model, because the domain of the normal distribution is the whole real line.

Both the uniform2 and normal models yield estimates close to the MLE of 21.3. According to their credible intervals, the domain of the posterior distribution of {mpg:_cons} is concentrated around MLE. For example, the 95% credible interval for the uniform2 model is [20.06, 22.58].

Now, let's use bayesstats ic to compare the three models. We list all the models following the command name and use the normal model as a reference model.

```
. bayesstats ic uniform1 uniform2 normal, basemodel(normal)
Bayesian information criteria
```

	DIC	log(ML)	log(BF)
uniform1	785.8891	-397.4298	-153.2635
uniform2	471.1909	-237.0858	7.080404
normal	471.3905	-244.1662	.

Note: Marginal likelihood (ML) is computed
using Laplace-Metropolis approximation.

The uniform1 model performs worse than the other two models according to the log marginal-likelihood, log(ML), and DIC—the DIC value is much larger, and the log(ML) value is much smaller for the uniform1 model. The other two models have only slightly different values for DIC and log(ML), according to which the uniform2 model is preferable.

Although the `uniform2` and `normal` models have different prior distributions, they have almost identical posterior domain, that is, the range of values of `{mpg: _cons}` where the posterior is strictly positive. As such, they will have the same values for AIC and BIC, and we will not be able to discriminate between the two models based on these information criteria.

The most decisive factor between the `uniform2` and `normal` models is the BF. The value of `log BF`, `log(BF)`, is 7.08, which provides very strong evidence in favor of the `uniform2` model.

We thus conclude that `uniform2` is the best model among the three considered models. This may be explained by the fact that the specified `uniform(10, 30)` prior is in more agreement with the likelihood of the data than the specified `normal(0, 30)` prior.

After your analysis, remember to erase the saved simulation datasets you no longer need. For example, we erase all of them by typing

```
. erase uniform1_simdata.dta
. erase uniform2_simdata.dta
. erase normal_simdata.dta
```

◀

Stored results

`bayesstats ic` stores the following in `r()`:

Scalars

<code>r(bayesfactor)</code>	1 if <code>bayesfactor</code> is specified, 0 otherwise
<code>r(nchains)</code>	number of chains used in the computation

Macros

<code>r(names)</code>	names of estimation results used
<code>r(basemodel)</code>	name of the base or reference model
<code>r(marglmethod)</code>	method for approximating marginal likelihood: <code>lmetropolis</code> or <code>hmean</code>
<code>r(chains)</code>	chains used in the computation, if <code>chains()</code> is specified

Matrices

<code>r(ic)</code>	matrix reporting DIC, <code>log(ML)</code> , and <code>log(BF)</code> or <code>BF</code> , if <code>bayesfactor</code> is specified
<code>r(ic_chain#)</code>	matrix <code>ic</code> for chain <code>#</code> , if <code>sepchains</code> is specified

Methods and formulas

DIC was introduced by Spiegelhalter et al. (2002) for Bayesian model selection using MCMC simulations. DIC is based on the deviance statistics

$$D(\boldsymbol{\theta}) = -2 \{ \log f(\mathbf{y}; \boldsymbol{\theta}) - \log f^*(\mathbf{y}; \boldsymbol{\theta}^*) \}$$

where $f(\cdot; \cdot)$ is the likelihood function of the model and $f^*(\mathbf{y}; \boldsymbol{\theta}^*)$ is the likelihood of the full model that fits data perfectly. Because $f^*(\mathbf{y}; \boldsymbol{\theta}^*)$ is constant across models fit to the same data, it is ignored in the actual calculation of DIC. Given an MCMC sample $\{\boldsymbol{\theta}_t\}_{t=1}^T$, the expected deviance can be estimated by the sample average $\overline{D}(\boldsymbol{\theta}) = 1/T \sum_{t=1}^T D(\boldsymbol{\theta}_t)$. Similarly to AIC and BIC, DIC is a sum of two components: the goodness-of-fit term $\overline{D}(\boldsymbol{\theta})$ and the model complexity term p_D : $\text{DIC} = \overline{D}(\boldsymbol{\theta}) + p_D$. The complexity is defined as the difference between the expected deviance and the deviance at the sample posterior mean: $p_D = \overline{D}(\boldsymbol{\theta}) - D(\overline{\boldsymbol{\theta}})$. We thus have

$$\text{DIC} = D(\overline{\boldsymbol{\theta}}) + 2p_D$$

Models with smaller values of DIC are preferred to models with larger values of DIC.

With multiple chains, the `bayesstats ic` command reports the average DIC and the average log marginal-likelihood computed over the chains. If the `sepchains` option is specified, these statistics are reported separately for each chain.

BFs were introduced by [Jeffreys \(1961\)](#). The BF of two models, M_1 and M_2 , is given by

$$\text{BF}_{12} = \frac{P(\mathbf{y}|M_1)}{P(\mathbf{y}|M_2)} = \frac{m_1(\mathbf{y})}{m_2(\mathbf{y})}$$

where $m_1(\cdot)$ and $m_2(\cdot)$ are the corresponding marginal likelihoods associated with models M_1 and M_2 . (See [Methods and formulas](#) in [\[BAYES\] bayesmh](#) for details about computing marginal likelihood.) BFs are defined only for proper marginal densities. Comparing models with improper priors is allowed as long as the resulting marginal densities are proper. The methodological importance of BFs comes from the fact that the so-called posterior odds is a product of prior odds and BF:

$$\frac{P(M_1|\mathbf{y})}{P(M_2|\mathbf{y})} = \frac{P(M_1)}{P(M_2)} \times \text{BF}_{12}$$

Therefore, if we assume that M_1 and M_2 are equally probable a priori, the posterior odds will be equal to the BF. We thus prefer model M_1 if $\text{BF}_{12} > 1$ and model M_2 otherwise. In practice, because of the higher numerical stability, we often calculate BFs in the (natural) log metric and compare its value against 0.

$$\log \text{BF}_{12} = \log m_1(\mathbf{y}) - \log m_2(\mathbf{y})$$

With multiple chains, BFs are computed using the average log marginal-likelihoods. If the `sepchains` option is specified, BFs are calculated and reported separately for each chain.

References

- Gelman, A., J. B. Carlin, H. S. Stern, D. B. Dunson, A. Vehtari, and D. B. Rubin. 2014. *Bayesian Data Analysis*. 3rd ed. Boca Raton, FL: Chapman and Hall/CRC.
- Jeffreys, H. 1961. *Theory of Probability*. 3rd ed. Oxford: Oxford University Press.
- Kass, R. E., and A. E. Raftery. 1995. Bayes factors. *Journal of the American Statistical Association* 90: 773–795. <https://doi.org/10.1080/01621459.1995.10476572>.
- Lewis, S. M., and A. E. Raftery. 1997. Estimating Bayes factors via posterior simulation with the Laplace–Metropolis estimator. *Journal of the American Statistical Association* 92: 648–655. <https://doi.org/10.1080/01621459.1997.10474016>.
- Spiegelhalter, D. J., N. G. Best, B. P. Carlin, and A. Van Der Linde. 2002. Bayesian measures of model complexity and fit. *Journal of the Royal Statistical Society, B ser.*, 64: 583–639. <https://doi.org/10.1111/1467-9868.00353>.

Also see

- [\[BAYES\] bayes](#) — Bayesian regression models using the bayes prefix
- [\[BAYES\] bayesmh](#) — Bayesian models using Metropolis–Hastings algorithm
- [\[BAYES\] bayesselect](#) — Bayesian variable selection for linear regression
- [\[BAYES\] Bayesian estimation](#) — Bayesian estimation commands
- [\[BAYES\] Bayesian postestimation](#) — Postestimation tools after Bayesian estimation
- [\[BAYES\] bayestest model](#) — Hypothesis testing using model posterior probabilities
- [\[R\] estimates](#) — Save and manipulate estimation results

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