

bayes — Bayesian regression models using the bayes prefix

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Description

The `bayes` prefix fits [Bayesian regression models](#). It provides Bayesian support for many likelihood-based estimation commands. The `bayes` prefix uses default or user-supplied priors for model parameters and estimates parameters using MCMC by drawing simulation samples from the corresponding posterior model. Also see [\[BAYES\] bayesmh](#) and [\[BAYES\] bayesmh evaluators](#) for fitting more general Bayesian models.

Quick start

Bayesian linear regression of y on x , using default normal priors for the regression coefficients and an inverse-gamma prior for the variance

```
bayes: regress y x
```

As above, but use a standard deviation of 10 instead of 100 for the default normal priors and shape of 2 and scale of 1 instead of values of 0.01 for the default inverse-gamma prior

```
bayes, normalprior(10) igammaprior(2 1): regress y x
```

Bayesian logistic regression of y on x_1 and x_2 , showing model summary without performing estimation

```
bayes, dryrun: logit y x1 x2
```

As above, but estimate model parameters and use uniform priors for all regression coefficients

```
bayes, prior({y: x1 x2 _cons}, uniform(-10,10)): logit y x1 x2
```

As above, but use a shortcut notation to refer to all regression coefficients

```
bayes, prior({y:}, uniform(-10,10)): logit y x1 x2
```

As above, but report odds ratios and use uniform priors for the slopes and a normal prior for the intercept

```
bayes, prior({y: x1 x2}, uniform(-10,10)) ///
      prior({y:_cons}, normal(0,10)) or: logit y x1 x2
```

Report odds ratios for the logit model on replay

```
bayes, or
```

Bayesian ordered logit regression of y on x_1 and x_2 , saving simulation results to `simdata.dta` and using a random-number seed for reproducibility

```
bayes, saving(simdata) rseed(123): ologit y x1 x2 x3
```

Bayesian multinomial regression of y on x_1 and x_2 , specifying 20,000 MCMC samples, setting length of the burn-in period to 5,000, and requesting that a dot be displayed every 500 simulations

```
bayes, mcmcsample(20000) burnin(5000) dots(500): mlogit y x1 x2
```

Bayesian Poisson regression of y on x_1 and x_2 , putting regression slopes in separate blocks and showing block summary

```
bayes, block({y:x1}) block({y:x2}) blocksummary: poisson y x1 x2
```

Bayesian multivariate regression of y_1 and y_2 on x_1 , x_2 , and x_3 , using Gibbs sampling and requesting 90% HPD credible interval instead of the default 95% equal-tailed credible interval

```
bayes, gibbs clevel(90) hpd: mvreg y1 y2 = x1 x2 x3
```

As above, but use `mvreg`'s option `level()` instead of `bayes`'s option `clevel()`

```
bayes, gibbs hpd: mvreg y1 y2 = x1 x2 x3, level(90)
```

Suppress estimates of the covariance matrix from the output

```
bayes, noshow(Sigma, matrix)
```

Bayesian Weibull regression of `stset` survival-time outcome on x_1 and x_2 , specifying starting values of 1 for $\{y:x_1\}$ and of 2 for $\{y:x_2\}$

```
bayes, initial({y:x1} 1 {y:x2} 2): streg x1 x2, distribution(weibull)
```

Bayesian two-level linear regression of y on x_1 and x_2 with random intercepts by `id`

```
bayes: mixed y x1 x2 || id:
```

Menu

Statistics > Bayesian analysis > Regression models > *estimation_command*

Syntax

`bayes` [*, bayesopts*] : *estimation_command* [*, estopts*]

estimation_command is a likelihood-based estimation command, and *estopts* are command-specific estimation options; see [BAYES] [bayesian estimation](#) for a list of supported commands, and see the command-specific entries for the supported estimation options, *estopts*.

<i>bayesopts</i>	Description
Priors	
* <code>gibbs</code>	specify Gibbs sampling; available only with <code>regress</code> or <code>mvreg</code> for certain prior combinations
* <code>normalprior(#)</code>	specify standard deviation of default normal priors for regression coefficients and other real scalar parameters; default is <code>normalprior(100)</code>
* <code>igammaprior(# #)</code>	specify shape and scale of default inverse-gamma prior for variances; default is <code>igammaprior(0.01 0.01)</code>
* <code>wishartprior(# [...])</code>	specify degrees of freedom and, optionally, scale matrix of default inverse-Wishart prior for unstructured random-effects covariance
<code>prior(priorspec)</code>	prior for model parameters; this option may be repeated
<code>dryrun</code>	show model summary without estimation
Simulation	
<code>mcmcsize(#)</code>	MCMC sample size; default is <code>mcmcsize(10000)</code>
<code>burnin(#)</code>	burn-in period; default is <code>burnin(2500)</code>
<code>thinning(#)</code>	thinning interval; default is <code>thinning(1)</code>
<code>rseed(#)</code>	random-number seed
<code>exclude(paramref)</code>	specify model parameters to be excluded from the simulation results
<code>restubs(restub1 restub2 ...)</code>	specify stubs for random-effects parameters for all levels; allowed only with multilevel models
Blocking	
* <code>blocksize(#)</code>	maximum block size; default is <code>blocksize(50)</code>
<code>block(paramref [, blockopts])</code>	specify a block of model parameters; this option may be repeated
<code>blocksummary</code>	display block summary
* <code>noblocking</code>	do not block parameters by default
Initialization	
<code>initial(initspec)</code>	initial values for model parameters
<code>nomleinitial</code>	suppress the use of maximum likelihood estimates as starting values
<code>initransom</code>	specify random initial values
<code>initsummary</code>	display initial values used for simulation
* <code>noisily</code>	display output from the estimation command during initialization
Adaptation	
<code>adaptation(adaptopts)</code>	control the adaptive MCMC procedure
<code>scale(#)</code>	initial multiplier for scale factor; default is <code>scale(2.38)</code>
<code>covariance(cov)</code>	initial proposal covariance; default is the identity matrix

Reporting

<code>clevel(#)</code>	set credible interval level; default is <code>clevel(95)</code>
<code>hpd</code>	display HPD credible intervals instead of the default equal-tailed credible intervals
<i><code>eform_option</code></i>	display coefficient table in exponentiated form
<code>remargl</code>	compute log marginal likelihood
<code>batch(#)</code>	specify length of block for batch-means calculations; default is <code>batch(0)</code>
<code>saving(filename[, replace])</code>	save simulation results to <i>filename.dta</i>
<code>nomodelsummary</code>	suppress model summary
<code>nomesummary</code>	suppress multilevel-structure summary; allowed only with multilevel models
<code>[no]dots</code>	suppress dots or display dots every 100 iterations and iteration numbers every 1,000 iterations; default is command-specific
<code>dots(#[, every(#)])</code>	display dots as simulation is performed
<code>[no]show(paramref)</code>	specify model parameters to be excluded from or included in the output
<code>showreflects((reref))</code>	specify that all or a subset of random-effects parameters be included in the output; allowed only with multilevel commands
<code>melabel</code>	display estimation table using the same row labels as <i>estimation_command</i> ; allowed only with multilevel commands
<code>nogroup</code>	suppress table summarizing groups; allowed only with multilevel models
<code>notable</code>	suppress estimation table
<code>noheader</code>	suppress output header
<code>title(string)</code>	display <i>string</i> as title above the table of parameter estimates
<i><code>display_options</code></i>	control spacing, line width, and base and empty cells

Advanced

<code>search(search_options)</code>	control the search for feasible initial values
<code>corrlag(#)</code>	specify maximum autocorrelation lag; default varies
<code>corrtol(#)</code>	specify autocorrelation tolerance; default is <code>corrtol(0.01)</code>

*Starred options are specific to the `bayes` prefix; other options are common between `bayes` and `bayesmh`.

The full specification of `iwishartprior()` is `iwishartprior(# [matname] [, relevel(levelvar)])`.

Options `prior()` and `block()` can be repeated.

priorspec and *paramref* are defined in [BAYES] `bayesmh`.

paramref may contain factor variables; see [U] 11.4.3 Factor variables.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

Options

Priors

`gibbs` specifies that Gibbs sampling be used to simulate model parameters instead of the default adaptive Metropolis–Hastings sampling. This option is allowed only with the `regress` and `mvreg` estimation commands. It is available only with certain prior combinations such as normal prior for regression coefficients and an inverse-gamma prior for the variance. Specifying the `gibbs` option is equivalent to specifying `block()`'s `gibbs` suboption for all default blocks of parameters. If you

use the `block()` option to define your own blocks of parameters, the `gibbs` option will have no effect on those blocks, and an MH algorithm will be used to update parameters in those blocks unless you also specify `block()`'s `gibbs` suboption.

`normalprior(#)` specifies the standard deviation of the default normal priors. The default is `normalprior(100)`. The normal priors are used for scalar parameters defined on the whole real line; see [Default priors](#) for details.

`igammaprior(# #)` specifies the shape and scale parameters of the default inverse-gamma priors. The default is `igammaprior(0.01 0.01)`. The inverse-gamma priors are used for positive scalar parameters such as a variance; see [Default priors](#) for details. Instead of a number `#`, you can specify a missing value `.` to refer to the default value of 0.01.

`iwishartprior(# [matname] [, relevel(levelvar)])` specifies the degrees of freedom and, optionally, the scale matrix `matname` of the default inverse-Wishart priors used for unstructured covariances of random effects with multilevel models. The degrees of freedom `#` is a positive real scalar with the default value of $d + 1$, where d is the number of random-effects terms at the level of hierarchy `levelvar`. Instead of a number `#`, you can specify a missing value `.` to refer to the default value. Matrix name `matname` is the name of a positive-definite Stata matrix with the default of $I(d)$, the identity matrix of dimension d . If `relevel(levelvar)` is omitted, the specified parameters are used for inverse-Wishart priors for all levels with unstructured random-effects covariances. Otherwise, they are used only for the prior for the specified level `levelvar`. See [Default priors](#) for details.

`prior(priorspec)` specifies a prior distribution for model parameters. This option may be repeated. A prior may be specified for any of the model parameters, except the random-effects parameters in multilevel models. Model parameters with the same prior specifications are placed in a separate block. Model parameters that are not included in prior specifications are assigned default priors; see [Default priors](#) for details. Model parameters may be scalars or matrices, but both types may not be combined in one prior statement. If multiple scalar parameters are assigned a single univariate prior, they are considered independent, and the specified prior is used for each parameter. You may assign a multivariate prior of dimension d to d scalar parameters. Also see [Referring to model parameters](#) in [BAYES] [bayesmh](#).

All `prior()` distributions are allowed, but they are not guaranteed to correspond to proper posterior distributions for all likelihood models. You need to think carefully about the model you are building and evaluate its convergence thoroughly.

`dryrun` specifies to show the summary of the model that would be fit without actually fitting the model. This option is recommended for checking specifications of the model before fitting the model. The model summary reports the information about the likelihood model and about priors for all model parameters.

Simulation

`mcmcsize(#)` specifies the target MCMC sample size. The default MCMC sample size is `mcmcsize(10000)`. The total number of iterations for the MH algorithm equals the sum of the burn-in iterations and the MCMC sample size in the absence of thinning. If thinning is present, the total number of MCMC iterations is computed as `burnin() + (mcmcsize() - 1) * thinning() + 1`. Computation time of the MH algorithm is proportional to the total number of iterations. The MCMC sample size determines the precision of posterior summaries, which may be different for different model parameters and will depend on the efficiency of the Markov chain. Also see [Burn-in period and MCMC sample size](#) in [BAYES] [bayesmh](#).

`burnin(#)` specifies the number of iterations for the burn-in period of MCMC. The values of parameters simulated during burn-in are used for adaptation purposes only and are not used for estimation.

The default is `burnin(2500)`. Typically, burn-in is chosen to be as long as or longer than the adaptation period. The burn-in period may need to be larger for multilevel models because these models introduce high-dimensional random-effects parameters and thus require longer adaptation period. Also see *Burn-in period and MCMC sample size* in [BAYES] `bayesmh` and *Convergence of MCMC* in [BAYES] `bayesmh`.

`thinning(#)` specifies the thinning interval. Only simulated values from every $(1 + k \times \#)$ th iteration for $k = 0, 1, 2, \dots$ are saved in the final MCMC sample; all other simulated values are discarded. The default is `thinning(1)`; that is, all simulation values are saved. Thinning greater than one is typically used for decreasing the autocorrelation of the simulated MCMC sample.

`rseed(#)` sets the random-number seed. This option can be used to reproduce results. `rseed(#)` is equivalent to typing `set seed #` prior to calling the bayes prefix; see [R] `set seed` and *Reproducing results* in [BAYES] `bayesmh`.

`exclude(paramref)` specifies which model parameters should be excluded from the final MCMC sample. These model parameters will not appear in the estimation table, and postestimation features for these parameters and log marginal likelihood will not be available. This option is useful for suppressing nuisance model parameters. For example, if you have a factor predictor variable with many levels but you are only interested in the variability of the coefficients associated with its levels, not their actual values, then you may wish to exclude this factor variable from the simulation results. If you simply want to omit some model parameters from the output, see the `noshow()` option. `paramref` can include individual random-effects parameters.

`restubs(restub1 restub2 ...)` specifies the stubs for the names of random-effects parameters. You must specify stubs for all levels—one stub per level. This option overrides the default random-effects stubs. See *Likelihood model* for details about the default names of random-effects parameters.

Blocking

`blocksize(#)` specifies the maximum block size for the model parameters; default is `blocksize(50)`. This option does not apply to random-effects parameters. Each group of random-effects parameters is placed in one block, regardless of the number of random-effects parameters in that group.

`block(paramref[, blockopts])` specifies a group of model parameters for the blocked MH algorithm. By default, model parameters, except the random-effects parameters, are sampled as independent blocks of 50 parameters or of the size specified in option `blocksize()`. Regression coefficients from different equations are placed in separate blocks. Auxiliary parameters such as variances and correlations are sampled as individual separate blocks, whereas the cutpoint parameters of the ordinal-outcome regressions are sampled as one separate block. With multilevel models, each group of random-effects parameters is placed in a separate block, and the `block()` option is not allowed with random-effects parameters. The `block()` option may be repeated to define multiple blocks. Different types of model parameters, such as scalars and matrices, may not be specified in one `block()`. Parameters within one block are updated simultaneously, and each block of parameters is updated in the order it is specified; the first specified block is updated first, the second is updated second, and so on. See *Improving efficiency of the MH algorithm—blocking of parameters* in [BAYES] `bayesmh`.

`blockopts` include `gibbs`, `split`, `scale()`, `covariance()`, and `adaptation()`.

`gibbs` specifies to use Gibbs sampling to update parameters in the block. This option is allowed only for hyperparameters and only for specific combinations of prior and hyperprior distributions; see *Gibbs sampling for some likelihood-prior and prior-hyperprior configurations* in [BAYES] `bayesmh`. For more information, see *Gibbs and hybrid MH sampling* in [BAYES] `bayesmh`. `gibbs` may not be combined with `scale()`, `covariance()`, or `adaptation()`.

`split` specifies that all parameters in a block are treated as separate blocks. This may be useful for levels of factor variables.

`scale(#)` specifies an initial multiplier for the scale factor corresponding to the specified block. The initial scale factor is computed as $\#/\sqrt{n_p}$ for continuous parameters and as $\#/n_p$ for discrete parameters, where n_p is the number of parameters in the block. The default is `scale(2.38)`. If specified, this option overrides the respective setting from the `scale()` option specified with the command. `scale()` may not be combined with `gibbs`.

`covariance(matname)` specifies a scale matrix *matname* to be used to compute an initial proposal covariance matrix corresponding to the specified block. The initial proposal covariance is computed as $\rho \times \text{Sigma}$, where ρ is a scale factor and $\text{Sigma} = \text{matname}$. By default, *Sigma* is the identity matrix. If specified, this option overrides the respective setting from the `covariance()` option specified with the command. `covariance()` may not be combined with `gibbs`.

`adaptation(tarate())` and `adaptation(tolerance())` specify block-specific TAR and acceptance tolerance. If specified, they override the respective settings from the `adaptation()` option specified with the command. `adaptation()` may not be combined with `gibbs`.

`blocksummary` displays the summary of the specified blocks. This option is useful when `block()` is specified.

`noblocking` requests that no default blocking is applied to model parameters. By default, model parameters are sampled as independent blocks of 50 parameters or of the size specified in option `blocksize()`. For multilevel models, this option has no effect on random-effects parameters; blocking is always applied to them.

Initialization

`initial(initspec)` specifies initial values for the model parameters to be used in the simulation. You can specify a parameter name, its initial value, another parameter name, its initial value, and so on. For example, to initialize a scalar parameter `alpha` to 0.5 and a 2x2 matrix `Sigma` to the identity matrix `I(2)`, you can type

```
bayes, initial({alpha} 0.5 {Sigma,m} I(2)) : ...
```

You can also specify a list of parameters using any of the specifications described in [Referring to model parameters](#) in [BAYES] `bayesmh`. For example, to initialize all regression coefficients from equations `y1` and `y2` to zero, you can type

```
bayes, initial({y1:} {y2:} 0) : ...
```

The general specification of *initspec* is

```
paramref # [paramref # [...]]
```

Curly braces may be omitted for scalar parameters but must be specified for matrix parameters. Initial values declared using this option override the default initial values or any initial values declared during parameter specification in the `likelihood()` option. See [Specifying initial values](#) in [BAYES] `bayesmh` for details.

`nomleinitial` suppresses using maximum likelihood estimates (MLEs) starting values for model parameters. By default, when no initial values are specified, MLE values from *estimation_command* are used as initial values. For multilevel commands, MLE estimates are used only for regression coefficients. Random effects are assigned zero values, and random-effects variances and covariances are initialized with ones and zeros, respectively. If `nomleinitial` is specified and no initial values are provided, the command uses ones for positive scalar parameters, zeros for other

scalar parameters, and identity matrices for matrix parameters. `nomleinitial` may be useful for providing an alternative starting state when checking convergence of MCMC. This option cannot be combined with `initrandom`.

`initrandom` specifies that the model parameters be initialized randomly. Random initial values are generated from the prior distributions of the model parameters. If you want to use fixed initial values for some of the parameters, you can specify them in the `initial()` option or during parameter declarations in the `likelihood()` option. Random initial values are not available for parameters with `flat`, `density()`, `logdensity()`, and `jeffreys()` priors; you must provide fixed initial values for such parameters. This option cannot be combined with `nomleinitial`.

`initsummary` specifies that the initial values used for simulation be displayed.

`noisily` specifies that the output from the estimation command be shown during initialization. The estimation command is executed once to set up the model and calculate initial values for model parameters.

Adaptation

`adaptation(adaptopts)` controls adaptation of the MCMC procedure. Adaptation takes place every prespecified number of MCMC iterations and consists of tuning the proposal scale factor and proposal covariance for each block of model parameters. Adaptation is used to improve sampling efficiency. Provided defaults are based on theoretical results and may not be sufficient for all applications. See *Adaptation of the MH algorithm* in [BAYES] `bayesmh` for details about adaptation and its parameters.

adaptopts are any of the following options:

`every(#)` specifies that adaptation be attempted every #th iteration. The default is `every(100)`.

To determine the adaptation interval, you need to consider the maximum block size specified in your model. The update of a block with k model parameters requires the estimation of a $k \times k$ covariance matrix. If the adaptation interval is not sufficient for estimating the $k(k+1)/2$ elements of this matrix, the adaptation may be insufficient.

`maxiter(#)` specifies the maximum number of adaptive iterations. Adaptation includes tuning of the proposal covariance and of the scale factor for each block of model parameters. Once the TAR is achieved within the specified tolerance, the adaptation stops. However, no more than # adaptation steps will be performed. The default is variable and is computed as `max{25, floor(burnin()/adaptation(every()))}`.

`maxiter()` is usually chosen to be no greater than `(mcmcsz() + burnin())/adaptation(every())`.

`miniter(#)` specifies the minimum number of adaptive iterations to be performed regardless of whether the TAR has been achieved. The default is `miniter(5)`. If the specified `miniter()` is greater than `maxiter()`, then `miniter()` is reset to `maxiter()`. Thus, if you specify `maxiter(0)`, then no adaptation will be performed.

`alpha(#)` specifies a parameter controlling the adaptation of the AR. `alpha()` should be in `[0, 1]`. The default is `alpha(0.75)`.

`beta(#)` specifies a parameter controlling the adaptation of the proposal covariance matrix. `beta()` must be in `[0, 1]`. The closer `beta()` is to zero, the less adaptive the proposal covariance. When `beta()` is zero, the same proposal covariance will be used in all MCMC iterations. The default is `beta(0.8)`.

`gamma(#)` specifies a parameter controlling the adaptation rate of the proposal covariance matrix. `gamma()` must be in $[0,1]$. The larger the value of `gamma()`, the less adaptive the proposal covariance. The default is `gamma(0)`.

`tarate(#)` specifies the TAR for all blocks of model parameters; this is rarely used. `tarate()` must be in $(0,1)$. The default AR is 0.234 for blocks containing continuous multiple parameters, 0.44 for blocks with one continuous parameter, and $1/n_maxlev$ for blocks with discrete parameters, where `n_maxlev` is the maximum number of levels for a discrete parameter in the block.

`tolerance(#)` specifies the tolerance criterion for adaptation based on the TAR. `tolerance()` should be in $(0,1)$. Adaptation stops whenever the absolute difference between the current AR and TAR is less than `tolerance()`. The default is `tolerance(0.01)`.

`scale(#)` specifies an initial multiplier for the scale factor for all blocks. The initial scale factor is computed as $\#/\sqrt{n_p}$ for continuous parameters and $\#/n_p$ for discrete parameters, where n_p is the number of parameters in the block. The default is `scale(2.38)`.

`covariance(cov)` specifies a scale matrix `cov` to be used to compute an initial proposal covariance matrix. The initial proposal covariance is computed as $\rho \times \Sigma$, where ρ is a scale factor and $\Sigma = matname$. By default, Σ is the identity matrix. Partial specification of Σ is also allowed. The rows and columns of `cov` should be named after some or all model parameters. According to some theoretical results, the optimal proposal covariance is the posterior covariance matrix of model parameters, which is usually unknown. This option does not apply to the blocks containing random-effects parameters.

Reporting

`clevel(#)` specifies the credible level, as a percentage, for equal-tailed and HPD credible intervals. The default is `clevel(95)` or as set by [\[BAYES\] set clevel](#).

`hpd` specifies the display of HPD credible intervals instead of the default equal-tailed credible intervals.

`eform_option` causes the coefficient table to be displayed in exponentiated form; see [\[R\] eform_option](#). The estimation command determines which `eform_option` is allowed (`eform(string)` and `eform` are always allowed).

`remargl` specifies to compute the log marginal likelihood for multilevel models. It is not reported by default for multilevel models. Bayesian multilevel models contain many parameters because, in addition to regression coefficients and variance components, they also estimate individual random effects. The computation of the log marginal likelihood involves the inverse of the determinant of the sample covariance matrix of all parameters and loses its accuracy as the number of parameters grows. For high-dimensional models such as multilevel models, the computation of the log marginal likelihood can be time consuming, and its accuracy may become unacceptably low. Because it is difficult to access the levels of accuracy of the computation for all multilevel models, the log marginal likelihood is not reported by default. For multilevel models containing a small number of random effects, you can use the `remargl` option to compute and display the log marginal likelihood.

`batch(#)` specifies the length of the block for calculating batch means, batch standard deviation, and MCSE using batch means. The default is `batch(0)`, which means no batch calculations. When `batch()` is not specified, MCSE is computed using effective sample sizes instead of batch means. Option `batch()` may not be combined with `corrlag()` or `corrtol()`.

`saving(filename[, replace])` saves simulation results in `filename.dta`. The `replace` option specifies to overwrite `filename.dta` if it exists. If the `saving()` option is not specified, the `bayes` prefix saves simulation results in a temporary file for later access by postestimation commands.

This temporary file will be overridden every time the `bayes` prefix is run and will also be erased if the current estimation results are cleared. `saving()` may be specified during estimation or on replay.

The saved dataset has the following structure. Variance `_index` records iteration numbers. The `bayes` prefix saves only states (sets of parameter values) that are different from one iteration to another and the frequency of each state in variable `_frequency`. (Some states may be repeated for discrete parameters.) As such, `_index` may not necessarily contain consecutive integers. Remember to use `_frequency` as a frequency weight if you need to obtain any summaries of this dataset. Values for each parameter are saved in a separate variable in the dataset. Variables containing values of parameters without equation names are named as `eq0_p#`, following the order in which parameters are declared in the `bayes` prefix. Variables containing values of parameters with equation names are named as `eq#_p#`, again following the order in which parameters are defined. Parameters with the same equation names will have the same variable prefix `eq#`. For example,

```
. bayes, saving(mcmc): ...
```

will create a dataset, `mcmc.dta`, with variable names `eq1_p1` for `{y:x1}`, `eq1_p2` for `{y:_cons}`, and `eq0_p1` for `{var}`. Also see macros `e(parnames)` and `e(varnames)` for the correspondence between parameter names and variable names.

In addition, the `bayes` prefix saves variable `_loglikelihood` to contain values of the log likelihood from each iteration and variable `_logposterior` to contain values of the log posterior from each iteration.

`nomodelsummary` suppresses the detailed summary of the specified model. The model summary is reported by default.

`nomesummary` suppresses the summary about the multilevel structure of the model. This summary is reported by default for multilevel commands.

`nodots`, `dots`, and `dots(#)` specify to suppress or display dots during simulation. `dots(#)` displays a dot every `#` iterations. During the adaptation period, a symbol `a` is displayed instead of a dot. If `dots(..., every(#))` is specified, then an iteration number is displayed every `#`th iteration instead of a dot or `a`. `dots(, every(#))` is equivalent to `dots(1, every(#))`. `dots` displays dots every 100 iterations and iteration numbers every 1,000 iterations; it is a synonym for `dots(100)`, `every(1000)`. `dots` is the default with multilevel commands, and `nodots` is the default with other commands.

`show(paramref)` or `noshow(paramref)` specifies a list of model parameters to be included in the output or excluded from the output, respectively. By default, all model parameters (except random-effects parameters with multilevel models) are displayed. Do not confuse `noshow()` with `exclude()`, which excludes the specified parameters from the MCMC sample. When the `noshow()` option is specified, for computational efficiency, MCMC summaries of the specified parameters are not computed or stored in `e()`. `paramref` can include individual random-effects parameters.

`showeffects` and `showeffects(reref)` are used with multilevel commands and specify that all or a list `reref` of random-effects parameters be included in the output in addition to other model parameters. By default, all random-effects parameters are excluded from the output as if you have specified the `noshow()` option. This option computes, displays, and stores in `e()` MCMC summaries for the first $\#_{\text{matsize}} - \#_{\text{npar}}$ random-effects parameters, where $\#_{\text{matsize}}$ is the maximum number of variables as determined by `matsize` (see [R] `matsize`) and $\#_{\text{npar}}$ is the number of other model parameters displayed. If you want to obtain MCMC summaries and display other random-effects parameters, you can use the `show()` option or use `bayesstats summary` (see [BAYES] `bayesstats summary`).

`melabel` specifies that the `bayes` prefix use the same row labels as `estimation_command` in the estimation table. This option is allowed only with multilevel commands. It is useful to match the estimation table output of `bayes: mecnd` with that of `mecnd`. This option implies `nomesummary` and `nomodelsummary`.

`nogroup` suppresses the display of group summary information (number of groups, average group size, minimum, and maximum) from the output header. This option is for use with multilevel commands.

`notable` suppresses the estimation table from the output. By default, a summary table is displayed containing all model parameters except those listed in the `exclude()` and `noshow()` options. Regression model parameters are grouped by equation names. The table includes six columns and reports the following statistics using the MCMC simulation results: posterior mean, posterior standard deviation, MCMC standard error or MCSE, posterior median, and credible intervals.

`noheader` suppresses the output header either at estimation or upon replay.

`title(string)` specifies an optional title for the command that is displayed above the table of the parameter estimates. The default title is specific to the specified likelihood model.

`display_options: vsquish, noemptycells, baselevels, allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), and nolstretch`; see [\[R\] estimation options](#).

Advanced

`search(search_options)` searches for feasible initial values. `search_options` are `on`, `repeat(#)`, and `off`.

`search(on)` is equivalent to `search(repeat(500))`. This is the default.

`search(repeat(k))`, $k > 0$, specifies the number of random attempts to be made to find a feasible initial-value vector, or initial state. The default is `repeat(500)`. An initial-value vector is feasible if it corresponds to a state with positive posterior probability. If feasible initial values are not found after k attempts, an error will be issued. `repeat(0)` (rarely used) specifies that no random attempts be made to find a feasible starting point. In this case, if the specified initial vector does not correspond to a feasible state, an error will be issued.

`search(off)` prevents the command from searching for feasible initial values. We do not recommend specifying this option.

`corrlag(#)` specifies the maximum autocorrelation lag used for calculating effective sample sizes. The default is $\min\{500, \text{mcmcsize}()/2\}$. The total autocorrelation is computed as the sum of all lag- k autocorrelation values for k from 0 to either `corrlag()` or the index at which the autocorrelation becomes less than `corrto1()` if the latter is less than `corrlag()`. Options `corrlag()` and `batch()` may not be combined.

`corrto1(#)` specifies the autocorrelation tolerance used for calculating effective sample sizes. The default is `corrto1(0.01)`. For a given model parameter, if the absolute value of the lag- k autocorrelation is less than `corrto1()`, then all autocorrelation lags beyond the k th lag are discarded. Options `corrto1()` and `batch()` may not be combined.

Remarks and examples

Remarks and examples are presented under the following headings:

- Using the bayes prefix*
 - Likelihood model*
 - Default priors*
 - Initial values*
 - Command-specific options*
- Introductory example*
- Linear regression: A case of informative default priors*
- Logistic regression with perfect predictors*
- Multinomial logistic regression*
- Generalized linear model*
- Truncated Poisson regression*
- Zero-inflated negative binomial model*
- Parametric survival model*
- Heckman selection model*
- Multilevel models*
 - Two-level models*
 - Crossed-effects model*
- Video examples*

For a general introduction to Bayesian analysis, see [\[BAYES\] intro](#). For a general introduction to Bayesian estimation using adaptive MH and Gibbs algorithms, see [\[BAYES\] bayesmh](#). See [\[BAYES\] bayesian estimation](#) for a list of supported estimation commands. For a quick overview example of all Bayesian commands, see *Overview example* in [\[BAYES\] bayesian commands](#).

Using the bayes prefix

The `bayes` prefix provides Bayesian estimation for many likelihood-based regression models. Simply prefix your estimation command with `bayes` to get Bayesian estimates—`bayes: estimation_command`; see [\[BAYES\] bayesian estimation](#) for a list of supported commands. Also see [\[BAYES\] bayesmh](#) for other Bayesian models.

Similarly to the `bayesmh` command, the `bayes` prefix sets up a Bayesian posterior model, uses MCMC to simulate parameters of this model, and summarizes and reports results. The process of specifying a Bayesian model is similar to that described in *Setting up a posterior model* in [\[BAYES\] bayesmh](#), except the likelihood model is now determined by the specified `estimation_command` and default priors are used for model parameters. The `bayes` prefix and the `bayesmh` command share the same methodology of MCMC simulation and the same summarization and reporting of simulation results; see [\[BAYES\] bayesmh](#) for details. In the following sections, we provide information specific to the `bayes` prefix.

Likelihood model

With the `bayes` prefix, the likelihood component of the Bayesian model is determined by the prefixed estimation command, and all posterior model parameters are defined by the likelihood model. For example, the parameters of the model

```
. bayes: streg age smoking, distribution(lognormal)
```

are the regression coefficients and auxiliary parameters you see when you fit

```
. streg age smoking, distribution(lognormal)
```

All estimation commands have regression coefficients as their model parameters. Some commands have additional parameters such as variances and correlation coefficients.

The `bayes` prefix typically uses the likelihood parameterization and the naming convention of the estimation command to define model parameters, but there are exceptions. For example, the `truncreg` command uses the standard deviation parameter `{sigma}` to parameterize the likelihood, whereas `bayes: truncreg` uses the variance parameter `{sigma2}`.

Most model parameters are scalar parameters supported on the whole real line such as regression coefficients, log-transformed positive parameters, and atanh-transformed correlation coefficients. For example, positive scalar parameters are the variance parameters in `bayes: regress`, `bayes: tobit`, and `bayes: truncreg`, and matrix parameters are the covariance matrix `{Sigma, matrix}` in `bayes: mvreg` and covariances of random effects in multilevel commands such as `bayes: meglm`.

The names of model parameters are provided in the model summary displayed by the `bayes` prefix. Knowing these names is useful when specifying the prior distributions, although the `bayes` prefix does provide default priors; see [Default priors](#). You can use the `dryrun` option with the `bayes` prefix to see the names of model parameters prior to the estimation. In general, the names of regression coefficients are formed as `{depvar: indepvar}`, where `depvar` is the name of the specified dependent variable and `indepvar` is the name of an independent variable. There are exceptions such as `bayes: streg`, for which `depvar` is replaced with `_t`. Variance parameters are named `{sigma2}`, log-variance parameters are named `{lnsigma2}`, atanh-transformed correlation parameters are named `{athrho}`, and the covariance matrix of `bayes: mvreg` is named `{Sigma, matrix}` (or `{Sigma, m}` for short).

For multilevel models such as `bayes: meglm`, in addition to regression coefficients and variance components, the `bayes` prefix also estimates [random-effects parameters](#). This is different from the corresponding frequentist commands, such as `meglm`, in which random effects are integrated out and thus are not among the final model parameters. (They can be predicted after estimation.) As such, the `bayes` prefix has its own naming convention for model parameters of multilevel commands. Before moving on, you should be familiar with the syntax of the multilevel commands; see, for example, [Syntax in \[ME\] meglm](#).

The regression coefficients are labeled as usual, `{depvar: indepvar}`. Random-effects parameters are labeled as outlined in tables 1 and 2. You can change the default names by specifying the `restubs()` option. The common syntax of `{rename}` is `{restub#}`, where `restub` is a capital letter, `U` for the level specified first, or a sequence of capital letters that is unique to each random-effects level, and `#` refers to the group of random effects at that level: 0 for random intercepts, 1 for random coefficients associated with the variable specified first in the random-effects equation, 2 for random coefficients associated with the variable specified second, and so on. The full syntax of `{rename}`, `{fullrename}`, is `{restub#[levelvar]}`, where `levelvar` is the variable identifying the level of hierarchy and is often omitted from the specification for brevity. Random effects at the observation level or crossed effects, specified as `_a11: R.varname` with multilevel commands, are labeled as `{U0}`, `{V0}`, `{W0}`, and so on. Random effects at nesting levels, or nested effects, are labeled using a sequence of capital letters starting with the letter corresponding to the top level. For example, the multilevel model

```
. bayes: melogit y x1 x2 || id1: x1 x2 || id2: x1 || id3:
```

will have random-effects parameters `{U0}`, `{U1}`, and `{U2}` to represent, respectively, random intercepts, random coefficients for `x1`, and random coefficients for `x2` at the `id1` level; parameters `{UU0}` and `{UU1}` for random intercepts and random coefficients for `x1` at the `id2` level; and random intercepts `{UUU0}` at the `id3` level. See [Multilevel models](#) for more examples. Also see [Different ways of specifying model parameters](#) for how to refer to individual random effects during postestimation.

Table 1. Random effects at nesting levels of hierarchy (nested effects)

Hierarchy	Random effects	{ <i>rename</i> }
<i>lev1</i>	Random intercepts	{U0}
	Random coefficients	{U1}, {U2}, etc.
<i>lev1>lev2</i>	Random intercepts	{UU0}
	Random coefficients	{UU1}, {UU2}, etc.
<i>lev1>lev2>lev3</i>	Random intercepts	{UUU0}
	Random coefficients	{UUU1}, {UUU2}, etc.
...		

Table 2. Random effects at the observation level, `_all` (crossed effects)

Hierarchy	Random effects	{ <i>rename</i> }
<i>lev1</i>	Random intercepts	{U0}
<i>lev2</i>	Random intercepts	{V0}
<i>lev3</i>	Random intercepts	{W0}
...		

Variance components for independent random effects are labeled as {*rename*:sigma2}. In the above example, there are six variance components: {U0:sigma2}, {U1:sigma2}, {U2:sigma2}, {UU0:sigma2}, {UU1:sigma2}, and {UUU0:sigma2}.

Covariance matrices of correlated random effects are labeled as {*restub*:Sigma,matrix} (or {*restub*:Sigma,m} for short), where *restub* is the letter stub corresponding to the level at which random effects are defined. For example, if we specify an unstructured covariance for the random effects at the `id1` and `id2` levels (with `cov(un)` short for `covariance(unstructured)`)

```
. bayes: melogit y x1 x2 || id1: x1 x2, cov(un) || id2: x1, cov(un) || id3:
```

we will have two covariance matrix parameters, a 3×3 covariance {U:Sigma,m} at the `id1` level and a 2×2 covariance {UU:Sigma,m} at the `id2` level, and the variance component {UUU0:sigma2} at the `id3` level.

For Gaussian multilevel models such as `bayes: mixed`, the error variance component is labeled as {*e.devar*:sigma2}.

Also see command-specific entries for the naming convention of additional parameters such as cutpoints with ordinal models or overdispersion parameters with negative binomial models.

Default priors

For convenience, the `bayes` prefix provides default priors for model parameters. The priors are chosen to be general across models and are fairly uninformative for a typical combination of a likelihood model and dataset. However, the default priors may not always be appropriate. You should always inspect their soundness and, if needed, override the prior specification for some or all model parameters using the `prior()` option.

All scalar parameters supported on the whole real line, such as regression coefficients and log-transformed positive parameters, are assigned a normal distribution with zero mean and variance σ_{prior}^2 , $N(0, \sigma_{\text{prior}}^2)$, where σ_{prior} is given by the `normalprior()` option. The default value for

σ_{prior} is 100, and thus the default priors for these parameters are $N(0, 10000)$. These priors are fairly uninformative for parameters of moderate size but may become informative for large-scale parameters. See the [Linear regression: A case of informative default priors](#) example below.

All positive scalar parameters, such as the variance parameters in `bayes: regress` and `bayes: tobit`, are assigned an inverse-gamma prior with shape parameter α and scale parameter β , $\text{InvGamma}(\alpha, \beta)$. The default values for α and β are 0.01, and thus the default prior for these parameters is $\text{InvGamma}(0.01, 0.01)$.

All cutpoint parameters of ordinal-outcome models, such as `bayes: ologit` and `bayes: oprobit` are assigned flat priors, improper uniform priors with a constant density of 1, equivalent to specifying the `flat` prior option. The reason for this choice is that the cutpoint parameters are sensitive to the range of the outcome variables, which is usually unknown a priori.

For multilevel models with `independent` and `identity` random-effects covariance structures, variances of random effects are assigned inverse-gamma priors, $\text{InvGamma}(0.01, 0.01)$. For `unstructured` random-effects covariances, covariance matrix parameters are assigned fairly uninformative inverse-Wishart priors, $\text{InvWishart}(d + 1, I(d))$, where d is the dimension of the random-effects covariance matrix and $I(d)$ is the identity matrix of dimension d . Setting the degrees-of-freedom parameter of the inverse-Wishart prior to $d + 1$ is equivalent to specifying uniform on $(-1, 1)$ distributions for the individual correlation parameters.

The model summary displayed by the `bayes` prefix describes the chosen default priors, which you can see prior to estimation if you specify `bayes's dryrun` option. You can use the `prior()` option repeatedly to override the default prior specifications for some or all model parameters.

Initial values

By default, the `bayes` prefix uses the ML estimates from the prefixed estimation command as initial values for all scalar model parameters.

For example, the specification

```
. bayes: logit y x
```

will use the ML estimates from

```
. logit y x
```

as default initial values for the regression coefficients.

You can override the default initial values by using the `initial()` option; see [Specifying initial values](#) in [\[BAYES\] bayesmh](#).

If the `nomleinitial` option is specified, instead of using the estimates from the prefixed command, all scalar model parameters are initialized with zeros, except for the variance parameters, which are initialized with ones.

The covariance matrix parameter `{Sigma, matrix}` of `bayes: mvreg` is always initialized with the identity matrix.

For multilevel models, regression coefficients are initialized using the ML estimates from the corresponding model without random effects, variances of random effects are initialized with ones, covariances of random effects are initialized with zeros, and random effects themselves are initialized with zeros.

Command-specific options

Not all command-specific options, that is, options specified with the estimation command, are applicable within the Bayesian framework. One example is the group of maximum-likelihood optimization options such as `technique()` and `gradient`. For a list of supported options, refer to the entry specific to each command; see [BAYES] **bayesian estimation** for a list of commands.

Some of the command-specific reporting options, such as *eform_option* and display options, can be specified either with *estimation_command* or with the `bayes` prefix. For example, to obtain estimates of odds ratios instead of coefficients after the logit model, you can specify the `or` option with the command

```
. bayes: logit y x, or
```

or with the `bayes` prefix

```
. bayes, or: logit y x
```

You can also specify this option on `replay` with the `bayes` prefix

```
. bayes: logit y x
. bayes, or
```

Introductory example

We start with a simple linear regression model applied to `womenwage.dta`, which contains income data for a sample of working women.

```
. use http://www.stata-press.com/data/r15/womenwage
(Wages of women)
```

Suppose we want to regress women's yearly income, represented by the `wage` variable, on their age, represented by the `age` variable. We can fit this model using the `regress` command.

```
. regress wage age
```

Source	SS	df	MS	Number of obs	=	488
Model	3939.49247	1	3939.49247	F(1, 486)	=	43.53
Residual	43984.4891	486	90.503064	Prob > F	=	0.0000
				R-squared	=	0.0822
				Adj R-squared	=	0.0803
Total	47923.9816	487	98.406533	Root MSE	=	9.5133
wage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
age	.399348	.0605289	6.60	0.000	.2804173	.5182787
_cons	6.033077	1.791497	3.37	0.001	2.513041	9.553112

► Example 1: Bayesian simple linear regression

We can fit a corresponding Bayesian regression model by simply adding `bayes:` in front of the `regress` command. Because the `bayes` prefix is simulation based, we set a random-number seed to get reproducible results.


```
. set seed 15
. bayes: regress wage age
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
  wage ~ regress(xb_wage,{sigma2})

Priors:
  {wage:age _cons} ~ normal(0,10000)
  {sigma2} ~ igamma(.01,.01)                                     (1)
```

(1) Parameters are elements of the linear form `xb_wage`.

Bayesian linear regression	MCMC iterations =	12,500
Random-walk Metropolis-Hastings sampling	Burn-in =	2,500
	MCMC sample size =	10,000
	Number of obs =	488
	Acceptance rate =	.3739
	Efficiency: min =	.1411
	avg =	.1766
	max =	.2271

Log marginal likelihood = -1810.1432

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
wage						
age	.4008591	.0595579	.001586	.4005088	.2798807	.5183574
_cons	5.969069	1.737247	.043218	5.997571	2.60753	9.396475
sigma2	90.76252	5.891887	.123626	90.43802	79.71145	102.8558

Note: Default priors are used for model parameters.

The Bayesian model has two regression coefficient parameters, `{wage:age}` and `{wage:_cons}`, and a positive scalar parameter, `{sigma2}`, representing the variance of the error term. The model summary shows the default priors used for the model parameters: `normal(0, 10000)` for the regression coefficients and `igamma(0.01, 0.01)` for the variance parameter. The default priors are provided for convenience and should be used with caution. These priors are fairly uninformative in this example, but this may not always be the case; see the example in [Linear regression: A case of informative default priors](#).

The first two columns of the `bayes` prefix's estimation table report the posterior means and standard deviations of the model parameters. We observe that for the regression coefficients `{wage:age}` and `{wage:_cons}`, the posterior means and standard deviations are very similar to the least-square estimates and their standard errors as reported by the `regress` command. The posterior mean estimate for `{sigma2}`, 90.76, is close to the residual mean squared estimate, 90.50, listed in the ANOVA table of the `regress` command. The estimation table of the `bayes` prefix also reports Monte Carlo standard errors (MCSEs), medians, and equal-tailed credible intervals.

The Bayesian estimates are stochastic in nature and, by default, are based on an MCMC sample of size 10,000. It is important to verify that the MCMC simulation has converged; otherwise, the Bayesian estimates cannot be trusted. The simulation efficiencies reported in the header of the estimation table can serve as useful initial indicators of convergence problems. The minimum efficiency in our example is about 0.14, and the average efficiency is about 0.17. These numbers are typical for the MH sampling algorithm used by `bayes` and do not indicate convergence problems; see [Convergence of MCMC in \[BAYES\] bayesmh](#) for more rigorous convergence diagnostics.

▷ Example 2: Predictions

There are several postestimation commands available after the `bayes` prefix; see [\[BAYES\] bayesian postestimation](#). Among them is the `bayesstats summary` command, which we can use to compute simple predictions. Suppose that we want to predict the expected wage of a 40-year-old woman conditional on the above fitted posterior model. Based on our model, this expected wage corresponds to the linear combination $\{\text{wage} : _cons\} + \{\text{wage} : \text{age}\} \times 40$. We name this expression `wage40` and supply it to the `bayesstats summary` command.

```
. bayesstats summary (wage40: {wage:_cons} + {wage:age}*40)
Posterior summary statistics                MCMC sample size =    10,000
      wage40 : {wage:_cons} + {wage:age}*40
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
wage40	22.00343	.81679	.024045	21.99231	20.39435	23.6718

The posterior mean estimate for the expected wage is about 22 with a 95% credible interval between 20.39 and 23.67.

◀

▷ Example 3: Gibbs sampling

The `bayes` prefix uses adaptive MH as its default sampling algorithm. However, in the special case of linear regression, a more efficient Gibbs sampling is available. We can request Gibbs sampling by specifying the `gibbs` option.

```
. set seed 15
. bayes, gibbs: regress wage age
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
wage ~ normal(xb_wage,{sigma2})
Priors:
{wage:age _cons} ~ normal(0,10000)
{sigma2} ~ igamma(.01,.01) (1)
```

(1) Parameters are elements of the linear form `xb_wage`.

```
Bayesian linear regression      MCMC iterations = 12,500
Gibbs sampling                  Burn-in          = 2,500
                                MCMC sample size = 10,000
                                Number of obs    = 488
                                Acceptance rate    = 1
                                Efficiency: min    = 1
                                avg                  = 1
                                max                  = 1
```

Log marginal likelihood = -1810.087

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
wage						
age	.3999669	.0611328	.000611	.4005838	.2787908	.518693
_cons	6.012074	1.804246	.018042	6.000808	2.488816	9.549921
sigma2	90.84221	5.939535	.059395	90.54834	79.8132	103.0164

Note: Default priors are used for model parameters.

The posterior summary results obtained by Gibbs sampling and MH sampling are very close except for the MCSEs. The Gibbs sampler reports substantially lower MCSEs than the default sampler because of its higher efficiency. In fact, in this example, the Gibbs sampler achieves the highest possible efficiency of 1.



Linear regression: A case of informative default priors

Our example in *Introductory example* used the default priors, which were fairly uninformative for those data and that model. This may not always be true. Consider a linear regression model using the familiar `auto.dta`. Let us regress the response variable `price` on the covariate `length` and factor variable `foreign`.

```
. use http://www.stata-press.com/data/r15/auto, clear
(1978 Automobile Data)
```

```
. regress price length i.foreign
```

Source	SS	df	MS	Number of obs	=	74
Model	200288930	2	100144465	F(2, 71)	=	16.35
Residual	434776467	71	6123612.21	Prob > F	=	0.0000
				R-squared	=	0.3154
				Adj R-squared	=	0.2961
Total	635065396	73	8699525.97	Root MSE	=	2474.6

price	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
length	90.21239	15.83368	5.70	0.000	58.64092 121.7839
foreign					
Foreign	2801.143	766.117	3.66	0.000	1273.549 4328.737
_cons	-11621.35	3124.436	-3.72	0.000	-17851.3 -5391.401

► Example 4: Default priors

We first fit a Bayesian regression model using the `bayes` prefix with default priors. Because the range of the outcome variable `price` is at least an order of magnitude larger than the range of the predictor variables `length` and `foreign`, we anticipate that some of the model parameters may have large scale, and longer adaptation may be necessary for the MCMC algorithm to reach optimal sampling for these parameters. We allow for longer adaptation by increasing the burn-in period from the default value of 2,500 to 5,000.

```
. set seed 15
. bayes, burnin(5000): regress price length i.foreign
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
price ~ regress(xb_price,{sigma2})
Priors:
{price:length 1.foreign _cons} ~ normal(0,10000)
{sigma2} ~ igamma(.01,.01) (1)
```

(1) Parameters are elements of the linear form `xb_price`.

```

Bayesian linear regression          MCMC iterations = 15,000
Random-walk Metropolis-Hastings sampling  Burn-in = 5,000
                                          MCMC sample size = 10,000
                                          Number of obs = 74
                                          Acceptance rate = .3272
                                          Efficiency: min = .05887
                                          avg = .1093
                                          max = .1958
Log marginal likelihood = -699.23257

```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
price						
length	33.03301	1.80186	.060848	33.07952	29.36325	36.41022
foreign						
Foreign	32.77011	98.97104	4.07922	34.3237	-164.1978	222.0855
_cons	-8.063175	102.9479	3.34161	-9.110308	-205.9497	196.9341
sigma2	7538628	1297955	29334.9	7414320	5379756	1.04e+07

Note: Default priors are used for model parameters.

The posterior mean estimates of the regression coefficients are smaller (in absolute value) than the corresponding estimates from the `regress` command, because the default prior for the coefficients, `normal(0, 10000)`, is informative and has a strong shrinkage effect. For example, the least-square estimate of the constant term from `regress` is about $-11,621$, and its scale is much larger than the default prior standard deviation of 100. As a result, the default prior shrinks the estimate of the constant toward 0 and, specifically, to -8.06 .

You should be aware that the default priors are provided for convenience and are not guaranteed to be uninformative in all cases. They are designed to have little effect on model parameters, the maximum likelihood estimates of which are of moderate size, say, less than 100 in absolute value. For large-scale parameters, as in this example, the default priors can become informative.



► Example 5: Flat priors

Continuing with [example 4](#), we can override the default priors using the `prior()` option. We can, for example, apply the completely uninformative flat prior, a prior with the density of 1, for the coefficient parameters.

```

. set seed 15
. bayes, prior({price:}, flat) burnin(5000): regress price length i.foreign
Burn-in ...
Simulation ...
Model summary
-----
Likelihood:
  price ~ regress(xb_price,{sigma2})
Priors:
  {price:length 1.foreign _cons} ~ 1 (flat)
                                {sigma2} ~ igamma(.01,.01)

```

(1) Parameters are elements of the linear form `xb_price`.

Bayesian linear regression	MCMC iterations =	15,000
Random-walk Metropolis-Hastings sampling	Burn-in =	5,000
	MCMC sample size =	10,000
	Number of obs =	74
	Acceptance rate =	.3404
	Efficiency: min =	.07704
	avg =	.1086
	max =	.1898
Log marginal likelihood = -669.62603		

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
price						
length	89.51576	16.27187	.586237	89.60969	57.96996	122.7961
foreign						
Foreign	2795.683	770.6359	26.0589	2787.139	1305.773	4298.785
_cons	-11478.83	3202.027	113.271	-11504.65	-17845.87	-5244.189
sigma2	6270294	1089331	25002.1	6147758	4504695	8803268

Note: Default priors are used for some model parameters.

The posterior mean estimates for the coefficient parameters are now close to the least-square estimates from `regress`. For example, the posterior mean estimate for `{price:_cons}` is about $-11,479$, whereas the least-square estimate is $-11,621$.

However, the flat priors should be used with caution. Flat priors are improper and may result in improper posterior distributions for which Bayesian inference cannot be carried out. You should thus choose the priors carefully, accounting for the properties of the likelihood model.

◀

▷ Example 6: Zellner's g -prior

A type of prior specific to the normal linear regression model is Zellner's g -prior. We can apply it to our example using the `zellnersg0()` prior. For this prior, we need to specify the dimension of the prior, which is the number of regression coefficients (3), a degree of freedom (50) and the variance parameter of the error term in the regression model, `{sigma2}`; the mean parameter is assumed to be 0 by `zellnersg0()`. See [example 9](#) in [\[BAYES\] bayesmh](#) for more details about Zellner's g -prior.

```
. set seed 15
. bayes, prior({price:}, zellnersg0(3, 50, {sigma2})) burnin(5000):
> regress price length i.foreign
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
  price ~ regress(xb_price,{sigma2})
Priors:
  {price:length 1.foreign _cons} ~ zellnersg(3,50,0,{sigma2})
                                {sigma2} ~ igamma(.01,.01)
```

(1) Parameters are elements of the linear form `xb_price`.

```

Bayesian linear regression          MCMC iterations =    15,000
Random-walk Metropolis-Hastings sampling  Burn-in          =     5,000
                                          MCMC sample size =   10,000
                                          Number of obs    =     74
                                          Acceptance rate  =    .3019
                                          Efficiency: min  =   .06402
                                          avg              =    .105
                                          max              =    .1944
Log marginal likelihood = -697.84862
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
price						
length	87.53039	16.24762	.569888	87.72965	55.5177	119.9915
foreign						
Foreign	2759.267	794.043	31.3829	2793.241	1096.567	4202.283
_cons	-11223.95	3211.553	113.34	-11308.39	-17534.25	-4898.139
sigma2	6845242	1159035	26286.9	6716739	4978729	9521252

Note: Default priors are used for some model parameters.

We see that using this Zellner’s *g*-prior has little effect on the coefficient parameters, and the simulated posterior mean estimates are close to the least-square estimates from `regress`.



Logistic regression with perfect predictors

Let’s revisit the example in *Logistic regression model: A case of nonidentifiable parameters* of [BAYES] `bayesmh`. The example uses `heartswitz.dta` to model the binary outcome disease, the presence of a heart disease, using the predictor variables `restecg`, `isfbs`, `age`, and `male`. The dataset is a sample from Switzerland.

```

. use http://www.stata-press.com/data/r15/heartswitz, clear
  (Subset of Switzerland heart disease data from UCI Machine Learning Repository)
    
```

► Example 7: Perfect prediction

The logistic regression model for these data is

```

. logit disease restecg isfbs age male
  (output omitted)
    
```

To fit a Bayesian logistic regression, we prefix the `logit` command with `bayes`. We also specify the `noisily` option to show the estimation output of the `logit` command, which is run by the `bayes` prefix to set up the model and compute starting values for the parameters.

```

. set seed 15
. bayes, noisily: logit disease restecg isfbs age male
note: restecg != 0 predicts success perfectly
      restecg dropped and 17 obs not used
note: isfbs != 0 predicts success perfectly
      isfbs dropped and 3 obs not used
note: male != 1 predicts success perfectly
      male dropped and 2 obs not used

Iteration 0:  log likelihood = -4.2386144
Iteration 1:  log likelihood = -4.2358116
Iteration 2:  log likelihood = -4.2358076
Iteration 3:  log likelihood = -4.2358076

Logistic regression                               Number of obs   =       26
                                                    LR chi2(1)      =        0.01
                                                    Prob > chi2     =       0.9403
                                                    Pseudo R2      =       0.0007

Log likelihood = -4.2358076

```

disease	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
restecg	0 (omitted)					
isfbs	0 (omitted)					
age	-.0097846	.1313502	-0.07	0.941	-.2672263	.2476572
male	0 (omitted)					
_cons	3.763893	7.423076	0.51	0.612	-10.78507	18.31285

```

Burn-in ...
Simulation ...
Model summary

```

```

Likelihood:
disease ~ logit(xb_disease)

Prior:
{disease:age _cons} ~ normal(0,10000) (1)

```

(1) Parameters are elements of the linear form xb_disease.

```

Bayesian logistic regression           MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling
                                         Burn-in         =     2,500
                                         MCMC sample size =   10,000
                                         Number of obs   =     26
                                         Acceptance rate =    .2337
                                         Efficiency: min =    .1076
                                         avg             =    .1113
                                         max             =    .115

Log marginal likelihood = -14.795726

```

disease	Mean	Std. Dev.	MCSE	Median	Equal-tailed	
					[95% Cred. Interval]	
restecg	(omitted)					
isfbs	(omitted)					
age	-.0405907	.1650514	.004868	-.0328198	-.4005246	.2592641
male	(omitted)					
_cons	6.616447	9.516872	.290075	5.491008	-8.852858	28.99392

Note: Default priors are used for model parameters.

As evident from the output of the logit command, the covariates restecg, isfbs, and male are dropped because of perfect prediction. Although these predictors cannot be identified using the likelihood alone, they can be identified, potentially, in a posterior model with an informative prior. The default prior normal(0, 10000), used by the bayes prefix for the regression coefficients, is not

informative enough to resolve the perfect prediction, and we must override it with a more informative prior.



▷ Example 8: Informative prior

In the example in *Logistic regression model: A case of nonidentifiable parameters* of [BAYES] `bayesmh`, we use information from another similar dataset, `hearthungary.dta`, to come up with informative priors for the regression coefficients. We use the same priors with the `bayes` prefix. We specify the `asis` option with the `logit` command to prevent dropping the perfect predictors from the model. We also specify the `nomleinitial` option to prevent the `bayes` prefix from trying to obtain ML estimates to use as starting values; reliable ML estimates cannot be provided by the `logit` command when the perfect predictors are retained.

```
. set seed 15
. bayes, prior({disease:restecg age}, normal(0,10))
> prior({disease:isfbs male}, normal(1,10))
> prior({disease:_cons}, normal(-4,10)) nomleinitial:
> logit disease restecg isfbs age male, asis
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
disease ~ logit(xb_disease)
Priors:
{disease:restecg age} ~ normal(0,10) (1)
{disease:isfbs male} ~ normal(1,10) (1)
{disease:_cons} ~ normal(-4,10) (1)
```

```
(1) Parameters are elements of the linear form xb_disease.
Bayesian logistic regression MCMC iterations = 12,500
Random-walk Metropolis-Hastings sampling Burn-in = 2,500
MCMC sample size = 10,000
Number of obs = 48
Acceptance rate = .2121
Efficiency: min = .01885
avg = .04328
max = .06184
Log marginal likelihood = -11.006071
```

disease	Mean	Std. Dev.	MCSE	Median	Equal-tailed	
					[95% Cred. Interval]	
restecg	1.965122	2.315475	.115615	1.655961	-2.029873	6.789415
isfbs	1.708631	2.726071	.113734	1.607439	-3.306837	7.334592
age	.1258811	.0707431	.003621	.1245266	-.0016807	.2719748
male	.2671381	2.237349	.162967	.3318061	-4.106425	4.609955
_cons	-2.441911	2.750613	.110611	-2.538183	-7.596747	3.185172

For this posterior model with informative priors, we successfully estimate all regression parameters in the logistic regression model.

The informative prior in this example is based on information from an independent dataset, `hearthungary.dta`, which is a sample of observations on the same heart condition and predictor attributes as `heartswitz.dta` but sampled from Hungary’s population. Borrowing information from independent datasets to construct informative priors is justified only when the datasets are compatible with the currently analyzed data.



Multinomial logistic regression

Consider the health insurance dataset, `sysdsn1.dta`, to model the insurance outcome, `insure`, which takes the values `Indemnity`, `Prepaid`, and `Uninsure`, using the predictor variables `age`, `male`, `nonwhite`, and `site`. This model is considered in more detail in [example 4](#) in [\[R\] mlogit](#).

```
. use http://www.stata-press.com/data/r15/sysdsn1, clear
(Health insurance data)
```

First, we use the `mlogit` command to fit the model

```
. mlogit insure age male nonwhite i.site, nolog
Multinomial logistic regression          Number of obs   =          615
                                          LR chi2(10)     =          42.99
                                          Prob > chi2     =          0.0000
Log likelihood = -534.36165              Pseudo R2      =          0.0387
```

insure	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
Indemnity	(base outcome)					
Prepaid						
age	-.011745	.0061946	-1.90	0.058	-.0238862	.0003962
male	.5616934	.2027465	2.77	0.006	.1643175	.9590693
nonwhite	.9747768	.2363213	4.12	0.000	.5115955	1.437958
site						
2	.1130359	.2101903	0.54	0.591	-.2989296	.5250013
3	-.5879879	.2279351	-2.58	0.010	-1.034733	-.1412433
_cons	.2697127	.3284422	0.82	0.412	-.3740222	.9134476
Uninsure						
age	-.0077961	.0114418	-0.68	0.496	-.0302217	.0146294
male	.4518496	.3674867	1.23	0.219	-.268411	1.17211
nonwhite	.2170589	.4256361	0.51	0.610	-.6171725	1.05129
site						
2	-1.211563	.4705127	-2.57	0.010	-2.133751	-.2893747
3	-.2078123	.3662926	-0.57	0.570	-.9257327	.510108
_cons	-1.286943	.5923219	-2.17	0.030	-2.447872	-.1260134

Next, we use the `bayes` prefix to perform Bayesian estimation of the same multinomial logistic regression model.

```
. set seed 15
. bayes: mlogit insure age male nonwhite i.site
Burn-in ...
Simulation ...
Model summary
```

```
Likelihood:
  Prepaid Uninsure ~ mlogit(xb_Prepaid,xb_Uninsure)
Priors:
  {Prepaid:age male nonwhite i.site _cons} ~ normal(0,10000)      (1)
  {Uninsure:age male nonwhite i.site _cons} ~ normal(0,10000)    (2)
```

(1) Parameters are elements of the linear form `xb_Prepaid`.

(2) Parameters are elements of the linear form `xb_Uninsure`.

```

Bayesian multinomial logistic regression      MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling     Burn-in         =     2,500
                                              MCMC sample size = 10,000
Base outcome: Indemnity                     Number of obs   =     615
                                              Acceptance rate =    .2442
                                              Efficiency: min =    .01992
                                              avg            =    .03086
Log marginal likelihood = -614.49286         max            =    .05659
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
Prepaid						
age	-.0125521	.006247	.000396	-.0125871	-.024602	-.0005809
male	.5462718	.2086422	.012818	.5573004	.1263754	.9271802
nonwhite	.9796293	.2275709	.015746	.9737777	.53642	1.401076
site						
2	.098451	.214039	.012887	.0994476	-.3172914	.5260208
3	-.6043961	.2348319	.011596	-.6072807	-1.045069	-.1323191
_cons	.3183984	.3309283	.021325	.3219128	-.3423583	.956505
Uninsure						
age	-.008377	.0118479	.000581	-.0082922	-.0323571	.0140366
male	.4687524	.3537416	.02376	.4748359	-.2495656	1.147333
nonwhite	.1755361	.42708	.022566	.198253	-.7214481	.938098
site						
2	-1.298562	.4746333	.033628	-1.27997	-2.258622	-.4149035
3	-.2057122	.3533365	.020695	-.2009649	-.904768	.4924401
_cons	-1.305083	.5830491	.02451	-1.296332	-2.463954	-.1758435

Note: Default priors are used for model parameters.

For this model and these data, the default prior specification of the `bayes` prefix is fairly uninformative and, as a result, the posterior mean estimates for the parameters are close to the ML estimates obtained with `mlogit`.

We can report posterior summaries for the relative-risk ratios instead of the regression coefficients. This is equivalent to applying an exponential transformation, $\exp(b)$, to the simulated values of each of the regression coefficients, b , and then summarizing them. We can obtain relative-risk ratio summaries by replaying the `bayes` command with the `rrr` option specified. We use the already available simulation results from the last estimation and do not refit the model. We could have also specified the `rrr` option during the estimation.

```
. bayes, rrr
```

```
Model summary
```

```
Likelihood:
```

```
  Prepaid Uninsure ~ mlogit(xb_Prepaid,xb_Uninsure)
```

```
Priors:
```

```
  {Prepaid:age male nonwhite i.site _cons} ~ normal(0,10000) (1)
```

```
  {Uninsure:age male nonwhite i.site _cons} ~ normal(0,10000) (2)
```

(1) Parameters are elements of the linear form `xb_Prepaid`.

(2) Parameters are elements of the linear form `xb_Uninsure`.

```

Bayesian multinomial logistic regression      MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling     Burn-in         =     2,500
                                              MCMC sample size = 10,000
Base outcome: Indemnity                     Number of obs   =     615
                                              Acceptance rate =    .2442
                                              Efficiency: min =    .02149
                                              avg            =    .03181
Log marginal likelihood = -614.49286         max            =    .06007
    
```

	RRR	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
Prepaid						
age	.9875456	.0061686	.000391	.9874918	.9756982	.9994192
male	1.764212	.3634348	.022268	1.745953	1.134708	2.527372
nonwhite	2.732931	.6240495	.042568	2.647929	1.709875	4.059566
site						
2	1.129077	.2450092	.015242	1.104561	.7281185	1.692189
3	.5617084	.1338774	.00665	.5448304	.3516675	.8760614
_cons	1.451983	.4904589	.029972	1.379764	.7100938	2.60259
Uninsure						
age	.9917276	.0117452	.000575	.991742	.9681608	1.014136
male	1.699605	.6045513	.040763	1.60775	.7791391	3.149782
nonwhite	1.301138	.5448086	.027742	1.219271	.4860479	2.555117
site						
2	.3045686	.1461615	.009698	.2780457	.1044944	.6604046
3	.8663719	.3155926	.01806	.8179411	.4046357	1.636304
_cons	.3203309	.1976203	.008063	.2735332	.0850978	.8387492

Note: _cons estimates baseline relative risk for each outcome.
 Note: Default priors are used for model parameters.

Generalized linear model

Consider the insecticide experiment dataset, `beetle.dta`, to model the number of beetles killed, `r`, on the number of subjected beetles, `n`; the type of beetles, `beetle`; and the log-dose of insecticide, `ldose`. More details can be found in [example 2](#) of [\[R\] glm](#).

```
. use http://www.stata-press.com/data/r15/beetle, clear
```

Consider a generalized linear model with a binomial family and a complementary log-log link function for these data.

```
. glm r i.beetle ldose, family(binomial n) link(cloglog) nolog
Generalized linear models          No. of obs      =          24
Optimization      : ML              Residual df    =          20
                                      Scale parameter =          1
Deviance          = 73.76505595      (1/df) Deviance = 3.688253
Pearson          = 71.8901173        (1/df) Pearson = 3.594506
Variance function: V(u) = u*(1-u/n) [Binomial]
Link function     : g(u) = ln(-ln(1-u/n)) [Complementary log-log]
                                      AIC              = 6.74547
Log likelihood    = -76.94564525     BIC              = 10.20398
```

r	OIM		z	P> z	[95% Conf. Interval]	
	Coef.	Std. Err.				
beetle						
Red flour	-.0910396	.1076132	-0.85	0.398	-.3019576	.1198783
Mealworm	-1.836058	.1307125	-14.05	0.000	-2.09225	-1.579867
ldose	19.41558	.9954265	19.50	0.000	17.46458	21.36658
_cons	-34.84602	1.79333	-19.43	0.000	-38.36089	-31.33116

To fit a Bayesian generalized linear model with default priors, we type

```
. set seed 15
. bayes: glm r i.beetle ldose, family(binomial n) link(cloglog)
Burn-in ...
Simulation ...
Model summary
-----
Likelihood:
  r ~ glm(xb_r)
Prior:
  {r:i.beetle ldose _cons} ~ normal(0,10000) (1)
```

```
(1) Parameters are elements of the linear form xb_r.
Bayesian generalized linear models      MCMC iterations = 12,500
Random-walk Metropolis-Hastings sampling Burn-in          = 2,500
                                      MCMC sample size = 10,000
Family : binomial n                    Number of obs    = 24
Link   : complementary log-log         Scale parameter   = 1
                                      Acceptance rate   = .2003
                                      Efficiency: min   = .03414
                                      avg               = .05094
                                      max               = .08012
Log marginal likelihood = -102.9776
```

r	Mean	Std. Dev.	MCSE	Median	Equal-tailed	
					[95% Cred. Interval]	
beetle						
Red flour	-.0903569	.106067	.004527	-.093614	-.2964984	.112506
Mealworm	-1.843952	.130297	.004603	-1.848374	-2.091816	-1.594582
ldose	19.52814	.9997765	.054106	19.52709	17.6146	21.6217
_cons	-35.04832	1.800461	.096777	-35.0574	-38.81427	-31.61378

Note: Default priors are used for model parameters.

The posterior mean estimates of the regression parameters are not that different from the ML estimates obtained with `glm`.

If desired, we can request highest posterior density intervals be reported instead of default equal-tailed credible intervals by specifying the `hpd` option. We can also change the credible-interval level; for example, to request 90% credible intervals, we specify the `clevel(90)` option. We also could specify these options during estimation.

```
. bayes, clevel(90) hpd
Model summary
```

```
Likelihood:
  r ~ glm(xb_r)
Prior:
  {r:i.beetle ldose _cons} ~ normal(0,10000) (1)
```

```
(1) Parameters are elements of the linear form xb_r.
Bayesian generalized linear models          MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling    Burn-in         =     2,500
                                           MCMC sample size =   10,000
Family : binomial n                        Number of obs   =     24
Link   : complementary log-log             Scale parameter =     1
                                           Acceptance rate =    .2003
                                           Efficiency: min =    .03414
                                           avg           =    .05094
                                           max           =    .08012
Log marginal likelihood = -102.9776
```

r	Mean	Std. Dev.	MCSE	Median	HPD	
					[90% Cred. Interval]	
beetle						
Red flour	-.0903569	.106067	.004527	-.093614	-.2444412	.1020305
Mealworm	-1.843952	.130297	.004603	-1.848374	-2.03979	-1.620806
ldose	19.52814	.9997765	.054106	19.52709	17.86148	21.16389
_cons	-35.04832	1.800461	.096777	-35.0574	-37.96057	-32.00411

Note: Default priors are used for model parameters.

Truncated Poisson regression

The semiconductor manufacturing dataset, `probe.dta`, contains observational data of failure rates, `failure`, of silicon wafers with width, `width`, and depth, `depth`, tested at four different probes, `probe`. A wafer is rejected if more than 10 failures are detected. See [example 2](#) in [R] [tpoisson](#).

```
. use http://www.stata.press.com/data/r15/probe, clear
```

We fit a truncated Poisson regression model with a truncation point of 10. We suppress the constant regression term from the likelihood equation using the `noconstant` option to retain all four probe levels by including `ibn.probe` in the list of covariates, which declares `probe` to be a factor variable with no base level.

```
. tpoisson failures ibn.probe depth width, noconstant ll(10) nolog
Truncated Poisson regression
Limits: lower =      10                Number of obs   =      88
        upper =     +inf                Wald chi2(6)     =    11340.50
Log likelihood = -239.35746              Prob > chi2      =      0.0000
```

failures	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
probe						
1	2.714025	.0752617	36.06	0.000	2.566515	2.861536
2	2.602722	.0692732	37.57	0.000	2.466949	2.738495
3	2.725459	.0721299	37.79	0.000	2.584087	2.866831
4	3.139437	.0377137	83.24	0.000	3.065519	3.213354
depth	-.0005034	.0033375	-0.15	0.880	-.0070447	.006038
width	.0330225	.015573	2.12	0.034	.0025001	.063545

► Example 9: Default priors

We first apply the bayes prefix with default priors to perform Bayesian estimation of the model. The estimation takes a little longer, so we specify the dots option to see the progress.

```
. set seed 15
. bayes, dots: tpoisson failures ibn.probe depth width, noconstant ll(10)
Burn-in 2500 aaaaaaaaaa1000.....2000..... done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Model summary
```

```
Likelihood:
failures ~ tpoisson(xb_failures)

Prior:
{failures:i.probe depth width} ~ normal(0,10000) (1)
```

```
(1) Parameters are elements of the linear form xb_failures.
Bayesian truncated Poisson regression                MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling             Burn-in          =     2,500
                                                       MCMC sample size =   10,000
Limits: lower =      10                Number of obs   =      88
        upper =     +inf                Acceptance rate  =     .1383
                                                       Efficiency: min =   .004447
                                                       avg             =   .01322
Log marginal likelihood = -288.22663                 max             =   .04082
```

failures	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
probe						
1	2.689072	.0696122	.008596	2.688881	2.557394	2.833737
2	2.581567	.0644141	.00966	2.588534	2.436973	2.701187
3	2.712054	.0695932	.006415	2.717959	2.55837	2.844429
4	3.13308	.0397521	.004592	3.133433	3.055979	3.208954
depth	-.000404	.0033313	.000165	-.000504	-.0067928	.0061168
width	.036127	.0165308	.001821	.0360637	.001239	.067552

Note: Default priors are used for model parameters.
Note: There is a high autocorrelation after 500 lags.

With the default prior specification, the posterior mean estimates for the regression parameters are similar to the ML estimates obtained with the `tpoisson` command. However, the `bayes` prefix issues a high autocorrelation warning note and reports a minimum efficiency of only 0.004. The posterior model with default priors seems to be somewhat challenging for the MH sampler. We could allow for longer burn-in and increase the MCMC sample size to improve the MCMC convergence and increase the estimation precision. Instead, we will provide an alternative prior specification that will increase the model flexibility and improve its fit to the data.



► Example 10: Hyperpriors

We now assume that the four probe coefficients, `{failures:ibn.probe}`, have a normal prior distribution with mean parameter `{probe_mean}` and a variance of 10,000. It is reasonable to assume that all four probes have positive failure rates and that `{probe_mean}` is a positive hyperparameter. We decide to assign `{probe_mean}` a `gamma(2, 1)` hyperprior, which is a distribution with a positive domain and a mean of 2. We use this prior for the purpose of illustration; this prior is not informative for this model and these data. We initialize `{probe_mean}` with 1 to give it a starting value compatible with its hyperprior.

```
. set seed 15
. bayes, prior({failures:ibn.probe}, normal({probe_mean}, 10000))
> prior({probe_mean}, gamma(2, 1)) initial({probe_mean} 1) dots:
> tpoisson failures ibn.probe depth width, noconstant ll(10)
Burn-in 2500 aaaaaaaaaa1000aaaaaaaaa2000aaaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done

Model summary
-----
Likelihood:
  failures ~ tpoisson(xb_failures)

Priors:
  {failures:i.probe} ~ normal({probe_mean},10000)          (1)
  {failures:depth width} ~ normal(0,10000)                 (1)

Hyperprior:
  {probe_mean} ~ gamma(2,1)
-----
(1) Parameters are elements of the linear form xb_failures.
```



```

Bayesian truncated Poisson regression      MCMC iterations = 12,500
Random-walk Metropolis-Hastings sampling   Burn-in         = 2,500
                                           MCMC sample size = 10,000
Limits: lower = 10                        Number of obs   = 88
      upper = +inf                       Acceptance rate = .304
                                           Efficiency: min = .04208
                                           avg            = .0775
                                           max           = .127
Log marginal likelihood = -287.91504
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
failures						
probe						
1	2.703599	.0770656	.003757	2.704613	2.551404	2.848774
2	2.592738	.0711972	.002796	2.594628	2.446274	2.728821
3	2.716223	.0755001	.003549	2.719622	2.568376	2.863064
4	3.137069	.0388127	.001317	3.136773	3.062074	3.211616
depth	-.000461	.0033562	.000109	-.0004457	-.0067607	.0062698
width	.0337508	.0152654	.000532	.0337798	.003008	.0622191
probe_mean	2.051072	1.462867	.041051	1.71286	.2211973	5.809428

Note: Default priors are used for some model parameters.

The MCMC simulation achieves an average efficiency of about 8% with no indication of convergence problems. Not only are the posterior mean estimates for the regression parameters similar to the ML estimates, but the MCMC standard errors are much lower than those achieved by the previous model with default priors. By introducing the hyperparameter {probe_mean}, we have improved the goodness of fit of the model.

◀

Zero-inflated negative binomial model

In this example, we consider a Bayesian model using zero-inflated negative binomial likelihood. We revisit [example 1](#) in [R] `zinb`, which models the number of fish caught by visitors to a national park. The probability that a particular visitor fished is assumed to depend on the variables `child` and `camper`, which are supplied as covariates to the `inflate()` option of `zinb`.

```
. use http://www.stata-press.com/data/r15/fish, clear
. zinb count persons livebait, inflate(child camper) nolog
Zero-inflated negative binomial regression      Number of obs   =      250
                                                Nonzero obs     =      108
                                                Zero obs        =      142
Inflation model = logit                       LR chi2(2)      =      82.23
Log likelihood = -401.5478                     Prob > chi2     =      0.0000
```

count	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
count						
persons	.9742984	.1034938	9.41	0.000	.7714543	1.177142
livebait	1.557523	.4124424	3.78	0.000	.7491503	2.365895
_cons	-2.730064	.476953	-5.72	0.000	-3.664874	-1.795253
inflate						
child	3.185999	.7468551	4.27	0.000	1.72219	4.649808
camper	-2.020951	.872054	-2.32	0.020	-3.730146	-.3117567
_cons	-2.695385	.8929071	-3.02	0.003	-4.44545	-.9453189
/lnalpha	.5110429	.1816816	2.81	0.005	.1549535	.8671323
alpha	1.667029	.3028685			1.167604	2.380076

Let's fit a Bayesian model with default normal prior distributions.

```
. set seed 15
. bayes, dots: zinb count persons livebait, inflate(child camper)
Burn-in 2500 aaaaaaaaa1000aaaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Model summary
```

```
Likelihood:
count ~ zinb(xb_count,xb_inflate,{lnalpha})
Priors:
{count:persons livebait _cons} ~ normal(0,10000) (1)
{inflate:child camper _cons} ~ normal(0,10000) (2)
{lnalpha} ~ normal(0,10000)
```

- (1) Parameters are elements of the linear form `xb_count`.
- (2) Parameters are elements of the linear form `xb_inflate`.

```

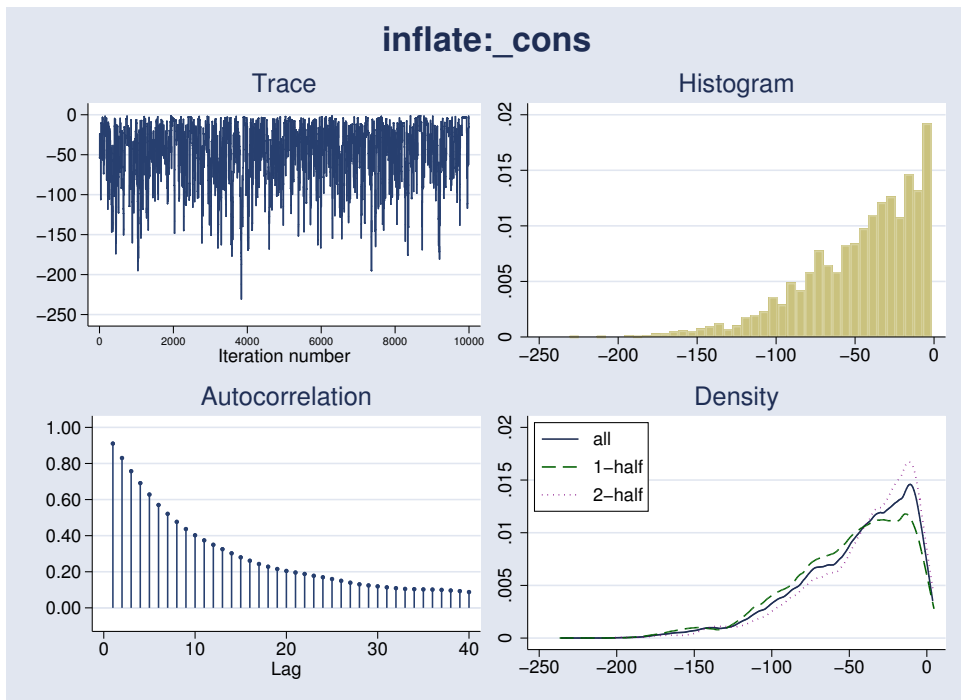
Bayesian zero-inflated negative binomial model  MCMC iterations = 12,500
Random-walk Metropolis-Hastings sampling       Burn-in         = 2,500
                                                MCMC sample size = 10,000
Inflation model: logit                        Number of obs   = 250
                                                Acceptance rate = .3084
                                                Efficiency: min = .03716
                                                avg            = .0791
                                                max            = .1613
Log marginal likelihood = -438.47876
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
count						
persons	.9851217	.1084239	.003601	.985452	.7641609	1.203561
livebait	1.536074	.4083865	.013509	1.515838	.753823	2.3539
_cons	-2.805915	.4700702	.014974	-2.795244	-3.73847	-1.89491
inflate						
child	46.95902	36.33974	1.87977	38.77997	3.612863	138.3652
camper	-46.123	36.34857	1.88567	-37.66796	-137.4568	-2.544566
_cons	-46.62439	36.36232	1.88355	-38.5171	-137.5522	-3.272469
lnalpha	.7055935	.1591234	.003962	.7048862	.3959316	1.025356

Note: Default priors are used for model parameters.

The posterior mean estimates for the main regression coefficients {count:persons}, {count:livebait}, and {count:_cons} are relatively close to the ML estimates from the zinb command, but the inflation coefficients, {inflate:child}, {inflate:camper}, and {inflate:_cons}, are quite different. For example, zinb estimates {inflate:_cons} are about -2.7, whereas the corresponding posterior mean estimate is about -46.6. To explain this large discrepancy, we draw the diagnostic plot of {inflate:_cons}.

```
. bayesgraph diagnostic {inflate:_cons}
```



The marginal posterior distribution of `{inflate:_cons}` is highly skewed to the left, and it is apparent that its posterior mean is much smaller than its posterior mode. In large samples, under proper noninformative priors, the posterior mode estimator and the ML estimator are equivalent. Therefore, it is not surprising that the posterior mean of `{inflate:_cons}` is much smaller than its ML estimate. We can obtain a rough estimate of the posterior mode in this example.

First, we need to save the simulation results in a dataset, say, `sim_zinb.dta`. You can do this during estimation or on replay by specifying the `saving()` option with the `bayes` prefix.

```
. bayes, saving(sim_zinb)
note: file sim_zinb.dta saved
```

Next, we load the dataset and identify the variable that represents the parameter `{inflate:_cons}`.

```
. use sim_zinb, clear
. describe
Contains data from sim_zinb.dta
  obs:      6,874
  vars:      11
  size:     604,912
                        8 Feb 2017 13:27
```

variable name	storage type	display format	value label	variable label
_index	double	%10.0g		
_loglikelihood	double	%10.0g		
_logposterior	double	%10.0g		
eq1_p1	double	%10.0g		
eq1_p2	double	%10.0g		
eq1_p3	double	%10.0g		
eq2_p1	double	%10.0g		
eq2_p2	double	%10.0g		
eq2_p3	double	%10.0g		
eq0_p1	double	%10.0g		
_frequency	double	%10.0g		

Sorted by:

Because `{inflate:_cons}` is the third parameter in the second equation, its corresponding simulation variable is `eq2_p3`.

Finally, we use the `egen`'s `mode()` function to generate a constant variable, `mode`, which contains the mode estimate for `{inflate:_cons}`.

```
. egen mode = mode(eq2_p3)
. display mode[1]
-3.417458
```

The mode estimate for `{inflate:_cons}` is about -3.42 , and it is indeed much closer to the ML estimate of -2.70 than its posterior mean estimate.

The inflation parameter α in the likelihood of the zero-inflated negative binomial model is log-transformed, and it is represented by `{lnalpha}` in our posterior model. To summarize the simulation result for α directly, we can use the `bayesstats summary` command to exponentiate `{lnalpha}`.

```
. bayesstats summary (alpha: exp({lnalpha}))
Posterior summary statistics                MCMC sample size =    10,000
      alpha : exp({lnalpha})
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
alpha	2.050889	.3292052	.008191	2.023616	1.485768	2.788087

Parametric survival model

Consider [example 7](#) in [ST] `streg`, which analyzes the effect of a hip-protection device, age, and sex on the risk of hip fractures in patients. The survival dataset is `hip3.dta` with time to event variable `time1` and failure variable `fracture`. The data are already `stset`.

```

. use http://www.stata-press.com/data/r15/hip3, clear
(hip fracture study)
. stset
-> stset time1, id(id) failure(fracture) time0(time0)
           id: id
           failure event: fracture != 0 & fracture < .
obs. time interval: (time0, time1]
exit on or before: failure

```

```

206 total observations
  0 exclusions

```

```

206 observations remaining, representing
148 subjects
 37 failures in single-failure-per-subject data
1,703 total analysis time at risk and under observation
           at risk from t =           0
           earliest observed entry t =           0
           last observed exit t =           39

```

It is assumed that the hazard curves for men and women have different shapes. We use the `streg` command to fit a model with Weibull survival distribution and the ancillary variable `male` to account for the difference between men and women.

```

. streg protect age, distribution(weibull) ancillary(male) nolog
           failure _d: fracture
           analysis time _t: time1
           id: id

```

Weibull PH regression

```

No. of subjects =           148           Number of obs =           206
No. of failures =           37
Time at risk   =           1703
Log likelihood = -69.323532           LR chi2(2) =           39.80
                                           Prob > chi2 =           0.0000

```

	_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
_t	protect	-2.130058	.3567005	-5.97	0.000	-2.829178	-1.430938
	age	.0939131	.0341107	2.75	0.006	.0270573	.1607689
	_cons	-10.17575	2.551821	-3.99	0.000	-15.17722	-5.174269
ln_p	male	-.4887189	.185608	-2.63	0.008	-.8525039	-.1249339
	_cons	.4540139	.1157915	3.92	0.000	.2270667	.6809611

We then perform Bayesian analysis of the same model using the `bayes` prefix. We apply more conservative normal priors, `normal(0, 100)`, by specifying the `normalprior(10)` option. To allow for longer adaptation of the MCMC sampler, we increase the burn-in period to 5,000, `burnin(5000)`.

```
. set seed 15
. bayes, normalprior(10) burnin(5000) dots:
> streg protect age, distribution(weibull) ancillary(male)
      failure _d: fracture
      analysis time _t: time1
      id: id
Burn-in 5000 aaaaaaaaa1000aaaaaaaa2000aaaaaaaa3000aaaaaaaa4000aaaaaaaa5000
> done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Model summary
```

```
Likelihood:
  _t ~ streg_weibull(xb__t,xb_ln_p)
Priors:
  {_t:protect age _cons} ~ normal(0,100) (1)
  {ln_p:male _cons} ~ normal(0,100) (2)
```

(1) Parameters are elements of the linear form xb__t.
(2) Parameters are elements of the linear form xb_ln_p.

Bayesian Weibull PH regression	MCMC iterations =	15,000	
Random-walk Metropolis-Hastings sampling	Burn-in =	5,000	
	MCMC sample size =	10,000	
No. of subjects =	148	Number of obs =	206
No. of failures =	37		
No. at risk =	1703		
	Acceptance rate =	.3418	
	Efficiency: min =	.01	
	avg =	.03421	
	max =	.05481	

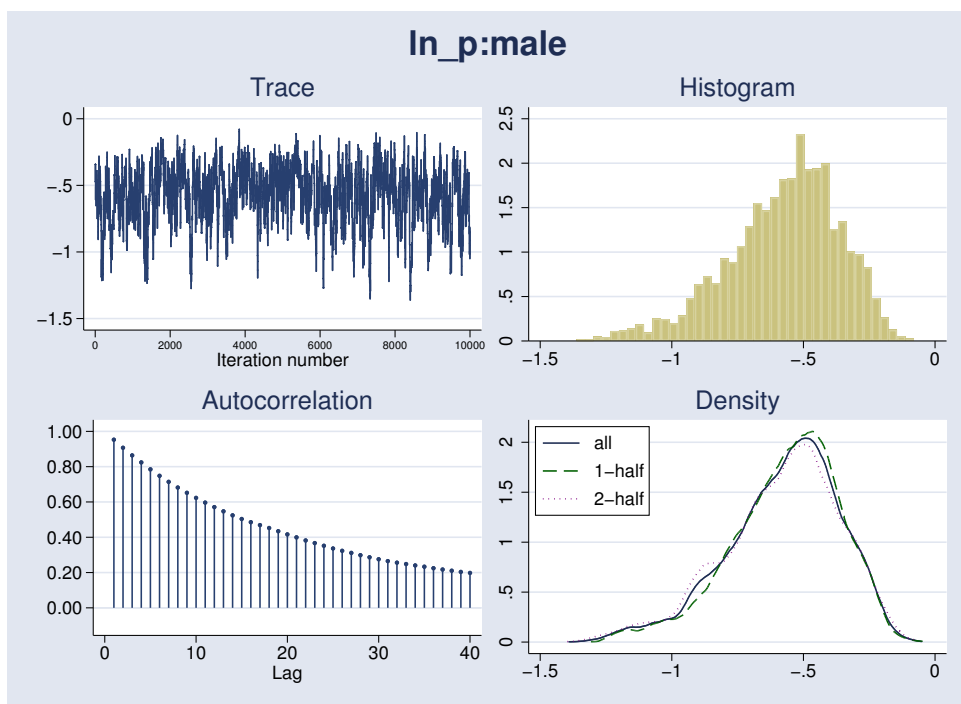
Log marginal likelihood = -91.348814

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
_t						
protect	-2.114715	.3486032	.017409	-2.105721	-2.818483	-1.46224
age	.0859305	.0328396	.001403	.0862394	.0210016	.1518009
_cons	-9.57056	2.457818	.117851	-9.551418	-14.49808	-4.78585
ln_p						
male	-.5753907	.2139477	.014224	-.5468488	-1.07102	-.2317242
_cons	.4290642	.11786	.011786	.4242712	.203933	.6548229

Note: Default priors are used for model parameters.

The posterior mean estimates for the regression parameters `{_t:protect}`, `{_t:age}`, and `{_t:_cons}` are close to the estimates reported by the `streg` command. However, the estimate for `{ln_p:male}` is somewhat different. If we inspect the diagnostic plot for `{ln_p:male}`, we will see that the reason for this is the asymmetrical shape of its marginal posterior distribution.

```
. bayesgraph diagnostic {ln_p:male}
```



As evident from the density plot, the posterior distribution of $\{\ln_p:male\}$ is skewed to the left, so the posterior mean estimate, -0.58 , is expected to be smaller than the ML estimate, -0.49 , given that we used fairly uninformative priors; see [Zero-inflated negative binomial model](#) for the comparison of posterior mean, posterior mode, and ML estimates for highly skewed posterior distributions.

Heckman selection model

► Example 11

A representative example of a Heckman selection model is provided by `wagenwk.dta`, which contains observations on the income of women who choose to work. See [example 1](#) in [\[R\] heckman](#).

```
. use http://www.stata-press.com/data/r15/womenwk, clear
```

The women's income (`wage`) is assumed to depend on their education (`educ`) and their age (`age`). In addition, the selection decision, or the choice of a woman to work, is assumed to depend on their marital status (`married`), number of children (`children`), education, and age. We fit this selection model using the `heckman` command.


```
. heckman wage educ age, select(married children educ age) nolog
Heckman selection model          Number of obs   =    2,000
(regression model with sample selection) Selected       =    1,343
                                     Nonselected    =     657
                                     Wald chi2(2)     =    508.44
Log likelihood = -5178.304        Prob > chi2    =    0.0000
```

	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
wage						
education	.9899537	.0532565	18.59	0.000	.8855729	1.094334
age	.2131294	.0206031	10.34	0.000	.1727481	.2535108
_cons	.4857752	1.077037	0.45	0.652	-1.625179	2.59673
select						
married	.4451721	.0673954	6.61	0.000	.3130794	.5772647
children	.4387068	.0277828	15.79	0.000	.3842534	.4931601
education	.0557318	.0107349	5.19	0.000	.0346917	.0767718
age	.0365098	.0041533	8.79	0.000	.0283694	.0446502
_cons	-2.491015	.1893402	-13.16	0.000	-2.862115	-2.119915
/athrho	.8742086	.1014225	8.62	0.000	.6754241	1.072993
/lnsigma	1.792559	.027598	64.95	0.000	1.738468	1.84665
rho	.7035061	.0512264			.5885365	.7905862
sigma	6.004797	.1657202			5.68862	6.338548
lambda	4.224412	.3992265			3.441942	5.006881

LR test of indep. eqns. (rho = 0): chi2(1) = 61.20 Prob > chi2 = 0.0000

We then apply the bayes prefix to perform Bayesian estimation of the Heckman selection model.

```
. set seed 15
. bayes, dots: heckman wage educ age, select(married children educ age)
Burn-in 2500 aaaaaaaaa1000aaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Model summary
```

```
Likelihood:
wage ~ heckman(xb_wage,xb_select,{athrho} {lnsigma})
Priors:
      {wage:education age _cons} ~ normal(0,10000)      (1)
      {select:married children education age _cons} ~ normal(0,10000)  (2)
      {athrho lnsigma} ~ normal(0,10000)
```

- (1) Parameters are elements of the linear form `xb_wage`.
(2) Parameters are elements of the linear form `xb_select`.

```

Bayesian Heckman selection model          MCMC iterations = 12,500
Random-walk Metropolis-Hastings sampling  Burn-in         = 2,500
                                           MCMC sample size = 10,000
                                           Number of obs   = 2,000
                                           Selected       = 1,343
                                           Nonselected    = 657
                                           Acceptance rate = .3484
                                           Efficiency:    min = .02314
                                           avg           = .03657
                                           max           = .05013
Log marginal likelihood = -5260.2024
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
wage						
education	.9919131	.051865	.002609	.9931531	.8884407	1.090137
age	.2131372	.0209631	.001071	.2132548	.1720535	.2550835
_cons	.4696264	1.089225	.0716	.4406188	-1.612032	2.65116
select						
married	.4461775	.0681721	.003045	.4456493	.3178532	.5785857
children	.4401305	.0255465	.001156	.4402145	.3911135	.4903804
education	.0559983	.0104231	.000484	.0556755	.0360289	.076662
age	.0364752	.0042497	.000248	.0362858	.0280584	.0449843
_cons	-2.494424	.18976	.011327	-2.498414	-2.861266	-2.114334
athrho	.868392	.099374	.005961	.8699977	.6785641	1.062718
lnsigma	1.793428	.0269513	.001457	1.793226	1.740569	1.846779

Note: Default priors are used for model parameters.

The posterior mean estimates for the Bayesian model with default normal priors are similar to the ML estimates obtained with the `heckman` command.

We can calculate posterior summaries for the correlation parameter, ρ , and the standard error, σ , in their natural scale by inverse-transforming the model parameters `{athrho}` and `{lnsigma}` using the `bayesstats summary` command. We also include posterior summaries for the selectivity effect $\lambda = \rho\sigma$.

```

. bayesstats summary (rho:1-2/(exp(2*{athrho})+1))
> (sigma:exp({lnsigma}))
> (lambda:exp({lnsigma})*(1-2/(exp(2*{athrho})+1)))
Posterior summary statistics          MCMC sample size = 10,000
    rho : 1-2/(exp(2*{athrho})+1)
    sigma : exp({lnsigma})
    lambda : exp({lnsigma})*(1-2/(exp(2*{athrho})+1))
    
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
rho	.6970522	.0510145	.003071	.701373	.5905851	.7867018
sigma	6.012205	.1621422	.008761	6.008807	5.700587	6.339366
lambda	4.196646	.3937209	.024351	4.212609	3.411479	4.946325

Again, the posterior mean estimates of ρ , σ , and λ agree with the ML estimates reported by `heckman`.

Multilevel models

The `bayes` prefix supports several [multilevel commands](#) such as `mixed` and `meglm`; see [\[BAYES\] bayesian estimation](#). Multilevel models introduce effects at different levels of hierarchy such as hospital effects and doctor-nested-within-hospital effects, which are often high-dimensional. These effects are commonly referred to as [random effects](#) in frequentist models. Bayesian multilevel models estimate random effects together with other model parameters. In contrast, frequentist multilevel models integrate random effects out, but provide ways to predict them after estimation, conditional on other estimated model parameters. Thus, in addition to regression coefficients and variance components (variances and covariances of random effects), Bayesian multilevel models include random effects themselves as model parameters. With a slight abuse of the terminology, we will sometimes refer to regression coefficients as [fixed effects](#), keeping in mind that they are still random quantities from a Bayesian perspective.

Multilevel models are more difficult to simulate from because of the existence of high-dimensional random-effects parameters. They typically require longer burn-in periods to achieve convergence and larger MCMC sample sizes to obtain precise estimates of random effects and variance components.

Prior specification is particularly important for multilevel models. Using noninformative priors for all model parameters will likely result in nonconvergence or high autocorrelation of the MCMC sample, especially with small datasets. The default priors provided by the `bayes` prefix are chosen to be fairly uninformative, which may often lead to low simulation efficiencies for model parameters and, especially, for variance components; see [Default priors](#). So, do not be surprised to see high autocorrelation with default priors, and be prepared to investigate various prior specifications during your analysis. For example, you may need to use the `iwishartprior()` option to increase the degrees of freedom and to specify a different scale matrix of the inverse-Wishart prior distribution used for the covariance matrices of random effects.

To change the default priors, you will need to know the names of the model parameters. See [Likelihood model](#) to learn how the `bayes` prefix labels the parameters. You can specify your own name stubs for the groups of random-effects parameters using the `restubs()` option. After simulation, see [Different ways of specifying model parameters](#) for how to refer to individual random effects to evaluate MCMC convergence or to obtain their MCMC summaries.

By default, the `bayes` prefix does not compute or display MCMC summaries of individual random effects to conserve computation time and space. You can specify the `showeffects()` or `show()` option to compute and display them for chosen groups of random effects. You cannot compute or display more random effects than the current value of `set matsize` minus other parameters in your model. You can also compute MCMC summaries of random effects after simulation by using [\[BAYES\] bayesstats summary](#).

Also, the `bayes` prefix does not compute the log marginal likelihood by default for multilevel models. The computation involves the inverse of the determinant of the sample covariance matrix of all parameters and loses accuracy as the number of parameters grows. For high-dimensional models such as multilevel models, the computation can be time consuming, and its accuracy may become unacceptably low. Because it is difficult to access the levels of accuracy of the computation for all multilevel models, the log marginal likelihood is not computed by default. For multilevel models containing a small number of random effects, you can use the `remargl` option to compute and display it.

Two-level models

Consider [example 1](#) from [ME] **mixed** that analyzed the weight gain of 48 pigs over 9 successive weeks. Detailed Bayesian analysis of these data using `bayesmh` are presented in [Panel-data and multilevel models](#) in [BAYES] **bayesmh**. Here, we use `bayes: mixed` to fit Bayesian two-level random-intercept and random-coefficient models to these data.

```
. use http://www.stata-press.com/data/r15/pig
(Longitudinal analysis of pig weights)
```

▷ **Example 12: Random-intercept model, using option melabel**

We first consider a simple random-intercept model of dependent variable `weight` on covariate `week` with variable `id` identifying pigs. The random-intercept model assumes that all pigs share a common growth rate but have different initial weight.

For comparison purposes, we first use the `mixed` command to fit this model by maximum likelihood.

```
. mixed weight week || id:
Performing EM optimization:
Performing gradient-based optimization:
Iteration 0:  log likelihood = -1014.9268
Iteration 1:  log likelihood = -1014.9268
Computing standard errors:
Mixed-effects ML regression           Number of obs   =       432
Group variable: id                   Number of groups =        48
Obs per group:
    min =          9
    avg =         9.0
    max =          9
Wald chi2(1)                         =    25337.49
Prob > chi2                          =         0.0000
Log likelihood = -1014.9268
```

weight	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
week	6.209896	.0390124	159.18	0.000	6.133433	6.286359
_cons	19.35561	.5974059	32.40	0.000	18.18472	20.52651

Random-effects Parameters		Estimate	Std. Err.	[95% Conf. Interval]	
id: Identity	var(_cons)	14.81751	3.124226	9.801716	22.40002
	var(Residual)	4.383264	.3163348	3.805112	5.04926

```
LR test vs. linear model: chibar2(01) = 472.65          Prob >= chibar2 = 0.0000
```

To fit a Bayesian analog of this model, we simply prefix the mixed command with bayes. We also specify the melabel option with bayes to label model parameters in the output table as mixed does.

```
. set seed 15
. bayes, melabel: mixed weight week || id:
note: Gibbs sampling is used for regression coefficients and variance
      components
Burn-in 2500 aaaaaaaaa1000aaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Bayesian multilevel regression                MCMC iterations =    12,500
Metropolis-Hastings and Gibbs sampling        Burn-in           =     2,500
                                                MCMC sample size =    10,000
Group variable: id                            Number of groups =     48
                                                Obs per group:
                                                min =             9
                                                avg =             9.0
                                                max =             9
                                                Number of obs    =    432
                                                Acceptance rate  =     .8112
                                                Efficiency: min  =   .007005
                                                avg =            .5064
                                                max =             1
Log marginal likelihood
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
weight						
week	6.209734	.0390718	.000391	6.209354	6.133233	6.285611
_cons	19.46511	.6239712	.07455	19.48275	18.2534	20.67396
id						
var(_cons)	15.7247	3.436893	.049048	15.26104	10.31182	23.60471
var(Residual)	4.411155	.3193582	.004397	4.396044	3.834341	5.080979

Note: Default priors are used for model parameters.

The estimates of posterior means and posterior standard deviations are similar to the ML estimates and standard errors from mixed. The results are also close to those from bayesmh in [example 23](#) in [\[BAYES\] bayesmh](#).

The average efficiency of the simulation is about 51% and there is no indication of any immediate convergence problems, but we should investigate convergence more thoroughly; see, for example, [example 5](#) in [\[BAYES\] bayesian commands](#) and, more generally, [Convergence of MCMC](#) in [\[BAYES\] bayesmh](#).

Because Bayesian multilevel models are generally slower than other commands, the bayes prefix displays dots by default with multilevel commands. You can specify the nodots option to suppress them.

Also, as we described in [Multilevel models](#), the log marginal likelihood is not computed for multilevel models by default because of the high dimensionality of the models. This is also described in the help file that appears when you click on Log marginal likelihood in the output header in the Results window. For models with a small number of random effects, you can specify the remargl option to compute the log marginal likelihood.

An important note about `bayes: mixed` is the default simulation method. Most `bayes` prefix commands use an adaptive MH algorithm to sample model parameters. The high-dimensional nature of multilevel models greatly decreases the simulation efficiency of this algorithm. For Gaussian multilevel models, such as `bayes: mixed`, model parameters can be sampled using a more efficient, albeit slower, Gibbs algorithm under certain prior distributions. The default priors used for regression coefficients and variance components allow the `bayes` prefix to use Gibbs sampling for these parameters with the `mixed` command. If you change the prior distributions or the default blocking structure for some parameters, Gibbs sampling may not be available for those parameters and an adaptive MH sampling will be used instead.



▷ Example 13: Random-intercept model, default output

When we specified the `melabel` option with `bayes` in [example 12](#), we intentionally suppressed some of the essential output from `bayes: mixed`. Here is what we would have seen had we not specified `melabel`.

```
. bayes
Multilevel structure
-----
id
  {U0}: random intercepts
-----
Model summary
-----
Likelihood:
  weight ~ normal(xb_weight,{e.weight:sigma2})
Priors:
  {weight:week _cons} ~ normal(0,10000)                (1)
                    {U0} ~ normal(0,{U0:sigma2})       (1)
  {e.weight:sigma2} ~ igamma(.01,.01)
Hyperprior:
  {U0:sigma2} ~ igamma(.01,.01)
-----
(1) Parameters are elements of the linear form xb_weight.
```

```

Bayesian multilevel regression          MCMC iterations =    12,500
Metropolis-Hastings and Gibbs sampling  Burn-in          =     2,500
                                         MCMC sample size =   10,000
Group variable: id                     Number of groups =     48
                                         Obs per group:
                                         min =            9
                                         avg =           9.0
                                         max =            9
                                         Number of obs    =    432
                                         Acceptance rate  =    .8112
                                         Efficiency: min  =   .007005
                                         avg =           .5064
                                         max =            1
Log marginal likelihood

```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
weight						
week	6.209734	.0390718	.000391	6.209354	6.133233	6.285611
_cons	19.46511	.6239712	.07455	19.48275	18.2534	20.67396
id						
U0:sigma2	15.7247	3.436893	.049048	15.26104	10.31182	23.60471
e.weight						
sigma2	4.411155	.3193582	.004397	4.396044	3.834341	5.080979

Note: Default priors are used for model parameters.

Let's go over the default output in detail, starting with the model summary. For multilevel models, in addition to the model summary, which describes the likelihood model and prior distributions, the bayes prefix displays information about the multilevel structure of the model.

Multilevel structure

```

id
  {U0}: random intercepts

```

Our multilevel model has one set of random effects, labeled as U0, which represent random intercepts at the id level. Recall that in Bayesian models, random effects are not integrated out but estimated together with other model parameters. So, {U0}, or using its full name {U0[id]}, represent [random-effects parameters](#) in our model. See [Likelihood model](#) to learn about the default naming convention for random-effects parameters.

According to the model summary below, the likelihood of the model is a normal linear regression with the linear predictor containing regression parameters `{weight:week}` and `{weight:_cons}` and random-effects parameters `{U0}`, and with the error variance labeled as `{e.weight:sigma2}`. Regression coefficients `{weight:week}` and `{weight:_cons}` have default normal priors with zero means and variances of 10,000. The random intercepts `{U0}` are normally distributed with mean zero and variance `{U0:sigma2}`. The variance components, error variance `{e.weight:sigma2}`, and random-intercept variance `{U0:sigma2}` have default inverse-gamma priors, `InvGamma(0.01, 0.01)`. The random-intercept variance is a hyperparameter in our model.

Model summary

```

Likelihood:
  weight ~ normal(xb_weight, {e.weight:sigma2})

Priors:
  {weight:week _cons} ~ normal(0, 10000)           (1)
    {U0} ~ normal(0, {U0:sigma2})                 (1)
    {e.weight:sigma2} ~ igamma(.01, .01)

Hyperprior:
  {U0:sigma2} ~ igamma(.01, .01)

```

(1) Parameters are elements of the linear form `xb_weight`.

The default output table of `bayes: mixed` uses the names of model parameters as they are defined by the `bayes` prefix.

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
weight						
week	6.209734	.0390718	.000391	6.209354	6.133233	6.285611
_cons	19.46511	.6239712	.07455	19.48275	18.2534	20.67396
id						
U0:sigma2	15.7247	3.436893	.049048	15.26104	10.31182	23.60471
e.weight						
sigma2	4.411155	.3193582	.004397	4.396044	3.834341	5.080979

Note: Default priors are used for model parameters.

Becoming familiar with the native parameter names of the `bayes` prefix is important for prior specification and for later postestimation. The `melabel` option is provided for easier comparison of the results between the `bayes` prefix and the corresponding frequentist multilevel command.

◀

► Example 14: Displaying random effects

By default, the `bayes` prefix does not compute or display MCMC summaries for the random-effects parameters to conserve space and computational time. You can specify the `showeffects` option to display all random effects or the `showeffects()` or `show()` option to display specific random effects. For example, continuing [example 13](#), we can display the random-effects estimates for the first five pigs as follows.


```
. bayes, show({U0[1/5]}) noheader
```

U0[id]	Mean	Std. Dev.	MCSE	Median	Equal-tailed	
					[95% Cred.	Interval]
1	-1.778442	.8873077	.074832	-1.761984	-3.542545	.0062218
2	.7831408	.8775376	.071421	.7961802	-.9547035	2.491798
3	-2.052634	.9038672	.072325	-2.061559	-3.822966	-.3246834
4	-1.891103	.878177	.075611	-1.858056	-3.642227	-.1028766
5	-3.316584	.8894319	.074946	-3.320502	-5.0469	-1.568927

These posterior mean estimates of random-effects parameters should be comparable with those predicted by `predict`, `reffects` after `mixed`. Posterior standard deviations, however, will generally be larger than the corresponding standard errors of random effects predicted after `mixed`, because the latter do not incorporate the uncertainty about the estimated model parameters.

You can also use `[BAYES] bayesstats summary` to obtain MCMC summaries of random-effects parameters after estimation:

```
. bayesstats summary {U0[1/5]}
(output omitted)
```

If you decide to use the `showeffects` option to display all random-effects parameters, beware of the increased computation time for models with many random effects. Then, the `bayes` prefix will compute and display the MCMC summaries for only the first M random-effects parameters, where M is the maximum number of variables as determined by `matsize` minus the other model parameters. You can specify the `show()` option with `bayes` or use `bayesstats summary` to obtain results for other random-effects parameters.



► Example 15: Random-coefficient model

Continuing [example 13](#), let's consider a random-coefficient model that allows the growth rate to vary among pigs.

Following `mixed`'s specification, we include the random slope for `week` at the `id` level by specifying the `week` variable in the random-effects equation.

```

. set seed 15
. bayes: mixed weight week || id: week
note: Gibbs sampling is used for regression coefficients and variance
      components
Burn-in 2500 aaaaaaaaa1000aaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Multilevel structure

```

```

id
  {U0}: random intercepts
  {U1}: random coefficients for week

```

Model summary

Likelihood:

```
weight ~ normal(xb_weight, {e.weight: sigma2})
```

Priors:

```

{weight: week _cons} ~ normal(0, 10000)           (1)
  {U0} ~ normal(0, {U0: sigma2})                 (1)
  {U1} ~ normal(0, {U1: sigma2})                 (1)
  {e.weight: sigma2} ~ igamma(.01, .01)

```

Hyperpriors:

```

{U0: sigma2} ~ igamma(.01, .01)
{U1: sigma2} ~ igamma(.01, .01)

```

(1) Parameters are elements of the linear form `xb_weight`.

Bayesian multilevel regression	MCMC iterations =	12,500
Metropolis-Hastings and Gibbs sampling	Burn-in =	2,500
	MCMC sample size =	10,000
Group variable: id	Number of groups =	48
	Obs per group:	
	min =	9
	avg =	9.0
	max =	9
	Number of obs =	432
	Acceptance rate =	.7473
	Efficiency: min =	.003057
	avg =	.07487
	max =	.1503

Log marginal likelihood

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
weight						
week	6.233977	.0801192	.01449	6.237648	6.05268	6.387741
_cons	19.44135	.3426786	.044377	19.44532	18.76211	20.11843
id						
U0: sigma2	7.055525	1.649394	.050935	6.844225	4.466329	10.91587
U1: sigma2	.3941786	.0901945	.002717	.3825387	.2526756	.6044887
e.weight						
sigma2	1.613775	.1261213	.003254	1.609296	1.386427	1.880891

Note: Default priors are used for model parameters.

Note: There is a high autocorrelation after 500 lags.

In addition to random intercepts $\{U_0\}$, we now have random coefficients for `week`, labeled as $\{U_1\}$, with the corresponding variance parameter $\{U_1:\text{sigma}2\}$. Compared with the random-intercept model, by capturing the variability of slopes on `week`, we reduced the estimates of the error variance and the random-intercept variance.

The average simulation efficiency decreased to only 7%, and we now see a note about a high autocorrelation after 500 lags. We can use, for example, `bayesgraph` diagnostics to verify that the high autocorrelation in this example is not an indication of nonconvergence but rather of a slow mixing of our MCMC sample. If we use `bayesstats` `ess`, we will see that the coefficient on `weight` and the constant term have the lowest efficiency, which suggests that these parameters are likely to be correlated with some of the random-effects estimates. If we want to reduce the autocorrelation and improve precision of the estimates for these parameters, we can increase the MCMC sample size by specifying the `mcmcsize()` option or thin the MCMC chain by specifying the `thinning()` option. ◀

▷ Example 16: Random-coefficient model, unstructured covariance

In [example 15](#), we assumed independence between random intercepts $\{U_0\}$ and random slopes on `week`, $\{U_1\}$. We relax this assumption here by specifying an unstructured covariance matrix.

Before we proceed with estimation, let's review our model summary first by specifying the `dryrun` option.

```
. bayes, dryrun: mixed weight week || id: week, covariance(unstructured)
Multilevel structure
-----
id
  {U0}: random intercepts
  {U1}: random coefficients for week
-----
Model summary
-----
Likelihood:
  weight ~ normal(xb_weight,{e.weight:sigma2})
Priors:
  {weight:week _cons} ~ normal(0,10000) (1)
  {U0}{U1} ~ mvnormal(2,{U:Sigma,m}) (1)
  {e.weight:sigma2} ~ igamma(.01,.01)
Hyperprior:
  {U:Sigma,m} ~ iwishart(2,3,I(2))
-----
(1) Parameters are elements of the linear form xb_weight.
```

The prior distributions for random effects $\{U_0\}$ and $\{U_1\}$ are no longer independent. Instead, they have a joint prior—a bivariate normal distribution with covariance matrix parameter $\{U:\text{Sigma},m\}$, which is short for $\{U:\text{Sigma},\text{matrix}\}$. The random-effects stub `U` is used to label the covariance matrix. The covariance matrix $\{U:\text{Sigma},m\}$ is assigned a fairly uninformative inverse-Wishart prior with three degrees of freedom and an identity scale matrix; see [Default priors](#) for details.

Let's now fit the model but suppress the model summary for brevity.

```
. set seed 15
. bayes, nomodelsummary: mixed weight week || id: week, covariance(unstructured)
note: Gibbs sampling is used for regression coefficients and variance
      components
Burn-in 2500 aaaaaaaaa1000aaaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Multilevel structure
```

```
id
  {U0}: random intercepts
  {U1}: random coefficients for week
```

```
Bayesian multilevel regression          MCMC iterations =    12,500
Metropolis-Hastings and Gibbs sampling  Burn-in           =     2,500
                                          MCMC sample size =   10,000
Group variable: id                      Number of groups =     48
                                          Obs per group:
                                          min =             9
                                          avg =            9.0
                                          max =             9
                                          Number of obs    =    432
                                          Acceptance rate  =    .7009
                                          Efficiency: min  =   .003683
                                          avg              =   .07461
                                          max              =   .1602

Log marginal likelihood                  max =            .1602
```

	Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
weight						
week	6.207086	.0878022	.014469	6.204974	6.041093	6.384891
_cons	19.39551	.4077822	.050353	19.40187	18.53869	20.1993
id						
U:Sigma_1_1	6.872161	1.627769	.061568	6.673481	4.282284	10.62194
U:Sigma_2_1	-.0866373	.2702822	.009861	-.0796118	-.645439	.4341423
U:Sigma_2_2	.399525	.0904532	.002488	.3885861	.2575883	.6104775
e.weight						
sigma2	1.611889	.1263131	.003155	1.605368	1.381651	1.872563

Note: Default priors are used for model parameters.

Note: There is a high autocorrelation after 500 lags.

The 95% credible interval for the covariance between {U0} and {U1}, labeled as {U:Sigma_2_1} in the output, is $[-.65, .43]$, which suggests independence between {U0} and {U1}.

Crossed-effects model

Let's revisit [example 4](#) from [\[ME\] meglm](#), which analyzes salamander cross-breeding data. Two populations of salamanders are considered: whiteside males and females (variables `wsm` and `wsf`) and roughbutt males and females (variables `rbm` and `rbf`). Male and female identifiers are recorded in the male and female variables. The outcome binary variable `y` indicates breeding success or failure.

In example 4 of [ME] `meglm`, we fit a crossed-effects logistic regression for successful mating, in which the effects of `male` and `female` were crossed. For the purpose of illustration, we will fit a crossed-effects probit regression here using `meglm` with the probit link.

```
. use http://www.stata-press.com/data/r15/salamander
. meglm y wsm##wsf || _all: R.male || female:, family(bernoulli) link(probit)
note: crossed random-effects model specified; option intmethod(laplace)
implied
      (iteration log omitted)
Mixed-effects GLM                Number of obs   =       360
Family:                          Bernoulli
Link:                             probit
```

Group Variable	No. of Groups	Observations per Group		
		Minimum	Average	Maximum
_all	1	360	360.0	360
female	60	6	6.0	6

Integration method: laplace

Wald chi2(3) = 41.50
 Prob > chi2 = 0.0000
 Log likelihood = -208.11182

y	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
1.wsm	-.4121977	.2735675	-1.51	0.132	-.9483802	.1239847
1.wsf	-1.720323	.3223052	-5.34	0.000	-2.35203	-1.088617
wsm#wsf						
1 1	2.121115	.3611665	5.87	0.000	1.413242	2.828989
_cons	.5950942	.2350714	2.53	0.011	.1343628	1.055826
_all>male						
var(_cons)	.3867491	.1789793			.156139	.95796
female						
var(_cons)	.4464111	.1976024			.1874794	1.062959

LR test vs. probit model: chi2(2) = 29.35 Prob > chi2 = 0.0000

Note: LR test is conservative and provided only for reference.

To fit the corresponding Bayesian model, we prefix the above command with `bayes:`.

```
. set seed 15
. bayes: meglm y wsm##wsf || _all: R.male || female:, family(bernoulli)
> link(probit)
Burn-in 2500 aaaaaaaaa1000aaaaaaaa2000aaaaa done
Simulation 10000 .....1000.....2000.....3000.....4000.....
> 5000.....6000.....7000.....8000.....9000.....10000 done
Multilevel structure
```

```
male
  {U0}: random intercepts
female
  {V0}: random intercepts
```

Model summary

Likelihood:

y ~ meglm(xb_y)

Priors:

```
{y:1.wsm 1.wsf 1.wsm#1.wsf _cons} ~ normal(0,10000)      (1)
      {U0} ~ normal(0,{U0:sigma2})                      (1)
      {V0} ~ normal(0,{V0:sigma2})                      (1)
```

Hyperpriors:

```
{U0:sigma2} ~ igamma(.01,.01)
{V0:sigma2} ~ igamma(.01,.01)
```

(1) Parameters are elements of the linear form xb_y.

```
Bayesian multilevel GLM          MCMC iterations =    12,500
Random-walk Metropolis-Hastings sampling  Burn-in       =     2,500
                                          MCMC sample size =   10,000
```

Group Variable	No. of Groups	Observations per Group		
		Minimum	Average	Maximum
_all	1	360	360.0	360
female	60	6	6.0	6

```
Family : Bernoulli          Number of obs   =    360
Link   : probit             Acceptance rate =    .3223
                                          Efficiency:  min =   .008356
                                          avg   =   .02043
                                          max   =   .02773
Log marginal likelihood
```

		Mean	Std. Dev.	MCSE	Median	Equal-tailed [95% Cred. Interval]	
y	1.wsm	-.411886	.28122	.016889	-.4158334	-.9645049	.156521
	1.wsf	-1.722195	.3329918	.023312	-1.713574	-2.381169	-1.094443
	wsm#wsf						
	1 1	2.110366	.3671998	.022643	2.09234	1.443113	2.831923
	_cons	.5858733	.2512646	.015407	.5906893	.0812177	1.077352
male	U0:sigma2	.4291858	.2195246	.024015	.3876708	.1347684	.9648611
female	V0:sigma2	.4928416	.2189307	.019043	.4576824	.1648551	1.003193

Note: Default priors are used for model parameters.

The variance components for male and female, {U0:sigma2} and {V0:sigma2}, are slightly higher than the corresponding ML estimates, but the regression coefficients are similar.

Video examples

[Introduction to Bayesian statistics, part 1: The basic concepts](#)

[Introduction to Bayesian statistics, part 2: MCMC and the Metropolis–Hastings algorithm](#)

[A prefix for Bayesian regression in Stata](#)

[Bayesian linear regression using the bayes prefix](#)

[Bayesian linear regression using the bayes prefix: How to specify custom priors](#)

[Bayesian linear regression using the bayes prefix: Checking convergence of the MCMC chain](#)

[Bayesian linear regression using the bayes prefix: How to customize the MCMC chain](#)

Stored results

In addition to the results stored by `bayesmh`, the `bayes` prefix stores the following in `e()`:

Scalars

<code>e(priorsigma)</code>	standard deviation of default normal priors
<code>e(priorshape)</code>	shape of default inverse-gamma priors
<code>e(priorscale)</code>	scale of default inverse-gamma priors
<code>e(blocksize)</code>	maximum size for blocks of model parameters

Macros

<code>e(prefix)</code>	<code>bayes</code>
<code>e(cmdname)</code>	command name from <i>estimation_</i> command
<code>e(cmd)</code>	same as <code>e(cmdname)</code>
<code>e(command)</code>	estimation command line

Methods and formulas

See *Methods and formulas* in [\[BAYES\] bayesmh](#).

Also see

[\[BAYES\] bayesian estimation](#) — Bayesian estimation commands

[\[BAYES\] bayesmh](#) — Bayesian models using Metropolis–Hastings algorithm

[\[BAYES\] bayesian postestimation](#) — Postestimation tools for `bayesmh` and the `bayes` prefix

[\[BAYES\] bayesian commands](#) — Introduction to commands for Bayesian analysis

[\[BAYES\] intro](#) — Introduction to Bayesian analysis

[\[BAYES\] Glossary](#)