stata

Difference in differences

Difference-in-differences (DID) estimation is one of the most popular methods for causal inference. Stata's **didregress** and **xtdidregress** commands fit DID and triple difference (DDD) models for repeated cross-sectional and panel data. DID and DDD models control for unobserved group and time fixed effects to consistently estimate the average treatment effect on the treated (ATET).

Key assumptions of the models can be tested and graphically displayed via the **estat trendplot**, **estat ptrends**, and **estat granger** commands.

For estimation of ATETs that vary across time and treatment cohorts, you can use the **hdidregress** and **xthdidregress** commands.

- DID and DDD models for ATET estimation
 Repeated cross-sectional data
 - Panel data
- Donald and Lang's aggregation method
- Wild bootstrap p-values and confidence intervals
- Bell and McCaffrey's degrees-of-freedom adjustment for bias-corrected standard errors

Fit a DID model and estimate ATET

We want to study the effect of a new hospital admissions procedure on patient satisfaction using monthly data on patients before and after the new procedure was implemented by some hospitals.

```
. didregress (satis) (procedure),
     group(hospital) time(month)
```

The ATET of **procedure** on satisfaction was 0.85, accounting for **hospital** and **month** fixed effects. The 95% confidence interval does not include 0.

If our data were panel, we would tell Stata using xtset and type

```
. xtdidregress (satis) (procedure),
            group(hospital) time(month)
```



- Mean-outcome and pretreatment parallel-trends graphical diagnostics
- Granger-type and pretreatment parallel-trends tests
- Heterogeneous DID models
- Bacon decomposition to assess treatment-effect heterogeneity

 Viewer - view di 	d.smcl					-		×
view did.smcl 🗙								
+					Dialog 🕶	Also	see 👻 🛛 Ju	mp to
Difference-in- Data type: Rep	differences re eated cross-se	gression ctional			Number	of ob	s = 7,3	68
		(Std. er	r. adjus	ted for 4	6 cluste	rs in	hospita	al)
satis	Coefficient	(Std. er Robust std. err.	r. adjus t	ted for 4 P> t	6 cluste [95%	rs in conf.	hospit:	al) al]

Graphical diagnostics

Our DID model assumes that the trends of **satis** for the control and treatment groups are parallel prior to the implementation of the new procedure. We can obtain a diagnostic of this assumption using **estat trendplot**.



Test for pretreatment parallel trends

We can complement our graphical diagnostic with a formal statistical test using **estat ptrends**.



Thus, the null hypothesis of pretreatment parallel trends is not rejected.

Granger causality test

Our DID model also assumes that the treatment and control groups do not change their behavior in anticipation of the treatment. To test this hypothesis, we can implement a Granger causality test using **estat granger**.

Viewer - view did.smcl		-		×	
view did.smcl 🛛 🗙					-
+	Dialog 🕶	Also se	• •	Jump to	•
. estat granger					
Granger causality test H0: No effect in anticipation of treatment					
F(2, 45) = 0.33 Prob > F = 0.7239					1
		CAP	NUN	INS	

The null hypothesis of no behavior change in anticipation of treatment is not rejected.

A graphical diagnostic is also available using estat grangerplot.

Compute appropriate standard errors

It is common to have few groups. In these scenarios, cluster–robust standard errors are unreliable. For such cases, we can use alternative methods to compute standard errors.

We can use HC2 bias-adjusted clustered standard errors by adding the **vce(hc2)** option.

```
. didregress (satis) (procedure),
group(hospital) time(month) vce(hc2)
```

We can use Donald and Lang's aggregation method by using the **aggregate(dlang)** option.

```
. didregress (satis) (procedure),
     group(hospital) time(month)
     aggregate(dlang)
```

Wild cluster bootstrap *p*-values and confidence intervals are also available. As with all bootstrap methods, we need to set a seed to make results replicable.

. didregress (satis) (procedure), group(hospital) time(month) wildbootstrap(rseed(123))

DDD models

To fit a DDD model, just add another variable to the **group()** option, and define the new treated observations.

. didregress (satis) (new_treated), group(hospital another_group) time(month)

Testing for treatment heterogeneity when treatment time varies

If units are treated at different times, the ATET might change for each treatment cohort. If so, DID estimates are inconsistent.

We can inspect ATET heterogeneity after **didregress** and **xtdidregress** using Bacon decomposition by typing

. estat bdecomp

And we can display the results in a graph by typing

. estat bdecomp, graph

Heterogeneous DID

Heterogeneous DID estimates ATETs when treatment effects change over time and are different across cohorts. Use the **hdidregress** and **xthdidregress** commands to estimate ATETs for each cohort and time period with repeated cross-sectional data and panel data.

- Estimation of the ATET for each cohort and period
 - Repeated cross-sectional data
 - Panel data
- Aggregation of ATETs over the following
 - Cohort
 - Period
 - Exposure to treatment
- Plots and tests of treatment-effect heterogeneity

- Simultaneous confidence intervals
- Four estimators
 - Regression adjustment (RA)
 - Inverse-probability weighting (IPW)
 - Augmented inverse-probability weighting (AIPW)
 - Two-way fixed-effects regression (TWFE)
- Test of pretreatment parallel trends

Fit a model with heterogeneous treatment effects

We would like to know whether a school district program, Healthy Habits, has an effect on students' body mass index (BMI). Our data are at the school district level and include information on whether a school participates in the program and the BMI of students. We have repeated samples of students from 40 school districts from 2014 to 2020.

We use the **aipw** estimator to model both the outcome and the treatment. We use the number of parks in the district to model treatment and the mother's education to model the outcome.

. hdidregress aipw (bmi medu) (hhabit parksd)
 group(schools) time(year)

The AIPW estimator is doubly robust, meaning that even when the treatment model or the outcome model (but not both) is misspecified, the estimates are still consistent.

Treatment-effect heterogeneity is evident in the results. ATET estimates vary across cohort and time combinations.

1						Also	see - jump
Heteroge	neous	treatment-eff	fects regres	ssion		Number of ob	s = 14,896
stimato	r: + lava	Augmented	IPW				
`ontrol	group.	1: SCHOOIS Never trea	ted				
201111-01	Bioup.	never eret					
			(Std. e	err. adju	sted for	40 clusters i	n schools)
			Robust				
Cohort		ATET	std. err.	z	P> z	[95% conf.	interval]
2015							
	year						
2	014	.4383554	.6317095	0.69	0.488	7997724	1.676483
2	015	-1.148953	.4106347	-2.80	0.005	-1.953783	3441241
2	016	-2.442539	.389955	-6.26	0.000	-3.206837	-1.678242
2	017	-2.47216	.2469231	-10.01	0.000	-2.956121	-1.9882
2	018	-2.61101	.6811369	-3.83	0.000	-3.946014	-1.276006
2	019	-3.853724	.3430176	-11.23	0.000	-4.526026	-3.181422
2	020	4349252	.6658255	-0.65	0.514	-1.739919	.8700687
2017							
	year						
2	014	.5847558	.2734447	2.14	0.032	.048814	1.120698
2	015	-1.327894	.4119237	-3.22	0.001	-2.13525	5205384
2	016	.6134559	.4378406	1.40	0.161	244696	1.471608
2	017	-1.655656	.4547377	-3.64	0.000	-2.546926	7643869
2	018	-3.063113	.5123237	-5.98	0.000	-4.06/249	-2.058977
2	019	-2.95452	.4682755	-6.31	0.000	-3.8/2324	-2.036/1/
2	020	.16/93/9	.6764323	0.25	0.804	-1.15/845	1.493/21
2019							
	year						
2	014	-1.582866	.5090601	-3.11	0.002	-2.580605	5851261
2	015	1.189118	.4966923	2.39	0.017	.2156191	2.162617
2	016	3868035	.4540723	-0.85	0.394	-1.276769	.5031617
2	017	.342599	.4860828	0.70	0.481	6101058	1.295304
2	018	.0661505	.6188046	0.11	0.915	-1.146684	1.278985
2	019	-3.733731	.3690283	-10.12	0.000	-4.457013	-3.010448
2	020	-1.275938	.6071755	-2.10	0.036	-2.46598	0858956



Visualizing ATETs for each cohort

It is difficult to see the trends in ATETs just by looking at all the ATETs estimates. We can use **estat atetplot** to visualize the time profile of ATETs for each cohort. We specify the **sci** option to show the simultaneous confidence bands that cover the true values of ATETs across all the cohorts and times with the predefined probability level.

. estat atetplot, sci



Aggregating ATETs

After fitting the model, we can use **estat aggregation** to aggregate the ATETs within cohort, time, or exposure to treatment. For example, we use **estat aggregation, cohort** to summarize the ATETs within each cohort.





If we want to summarize ATETs within time, we specify the **time** option with **estat aggregation**.

CAP NUM INS

. estat aggregation, time graph

Viewer - view he	etdid.smcl				-		×
view hetdid.smcl	×						
÷					Dialog 👻 Also	see 👻 🛛 Jur	np to
ATET over time					Number of ob	s = 14,89	96
		(Std. e	err. adju	sted for	40 clusters i	n school:	5)
		Robust					_
Time	ATET	Robust std. err.	z	P> z	[95% conf.	interva	1]
Time 2015	ATET	Robust std. err. .4106347	z -2.80	P> z 0.005	[95% conf. -1.953783	interva:	1] 11
Time 2015 2016	ATET -1.148953 -2.442539	Robust std. err. .4106347 .389955	z -2.80 -6.26	P> z 0.005 0.000	[95% conf. -1.953783 -3.206837	interva: 344124 -1.67824	1] 41 42
Time 2015 2016 2017	ATET -1.148953 -2.442539 -1.976693	Robust std. err. .4106347 .389955 .3520842	z -2.80 -6.26 -5.61	P> z 0.005 0.000 0.000	[95% conf. -1.953783 -3.206837 -2.666766	interva: 344124 -1.67824 -1.28663	1] 41 42 21
Time 2015 2016 2017 2018	ATET -1.148953 -2.442539 -1.976693 -2.896058	Robust std. err. .4106347 .389955 .3520842 .4285858	z -2.80 -6.26 -5.61 -6.76	P> z 0.005 0.000 0.000 0.000	[95% conf. -1.953783 -3.206837 -2.666766 -3.736071	interva: 344124 -1.67824 -1.28662 -2.05604	1] 41 42 21
Time 2015 2016 2017 2018 2019	ATET -1.148953 -2.442539 -1.976693 -2.896058 -3.462559	Robust std. err. .4106347 .389955 .3520842 .4285858 .2844555	z -2.80 -6.26 -5.61 -6.76 -12.17	P> z 0.005 0.000 0.000 0.000 0.000	[95% conf. -1.953783 -3.206837 -2.666766 -3.736071 -4.020881	interva 344124 -1.67824 -1.28662 -2.05604 -2.90503	1] 41 42 21 46 36



Finally, if we want to summarize ATETs within different lengths of exposure to treatment, we specify the **dynamic** option.

. estat aggregation, dynamic graph

