logistic postestimation - Postestimation tools for logistic

Postestimation commands	predict	margins
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Postestimation commands

The following postestimation commands are of special interest after logistic:

Command	Description
estat classification	report various summary statistics, including the classification table
estat gof	Pearson or Hosmer-Lemeshow goodness-of-fit test
lroc	compute area under ROC curve and graph the curve
lsens	graph sensitivity and specificity versus probability cutoff

These commands are not appropriate with svy estimation results.

The following standard postestimation commands are also available:

Command	Description	
contrast	contrasts and ANOVA-style joint tests of estimates	
estat ic	Akaike's, consistent Akaike's, corrected Akaike's, and Schwarz's Bayesian information criteria (AIC, CAIC, AICc, and BIC)	
estat summarize	summary statistics for the estimation sample	
estat vce	variance-covariance matrix of the estimators (VCE)	
estat (svy)	postestimation statistics for survey data	
estimates	cataloging estimation results	
etable	table of estimation results	
*forecast	dynamic forecasts and simulations	
*hausman	Hausman's specification test	
lincom	point estimates, standard errors, testing, and inference for linear combi- nations of coefficients	
linktest	link test for model specification	
*lrtest	likelihood-ratio test	
margins	marginal means, predictive margins, marginal effects, and average marginal effects	
marginsplot	graph the results from margins (profile plots, interaction plots, etc.)	
nlcom	point estimates, standard errors, testing, and inference for nonlinear com binations of coefficients	
predict	probabilities, influence statistics, residuals, etc.	
predictnl	point estimates, standard errors, testing, and inference for generalized predictions	

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pwcompare	pairwise comparisons of estimates
suest	seemingly unrelated estimation
test	Wald tests of simple and composite linear hypotheses
testnl	Wald tests of nonlinear hypotheses

*forecast, hausman, and lrtest are not appropriate with svy estimation results. forecast is also not appropriate with mi estimation results.

predict

Description for predict

predict creates a new variable containing predictions such as probabilities, linear predictions, standard errors, influence statistics, deviance residuals, leverages, sequential numbers, Pearson residuals, and the equation-level score.

Menu for predict

Statistics > Postestimation

Syntax for predict

statistic	Description
Main	
pr	probability of a positive outcome; the default
xb	linear prediction
stdp	standard error of the prediction
* <u>db</u> eta	Pregibon (1981) $\Delta \hat{\beta}$ influence statistic
* <u>de</u> viance	deviance residual
* <u>dx</u> 2	Hosmer, Lemeshow, and Sturdivant (2013) $\Delta \chi^2$ influence statistic
* <u>dd</u> eviance	Hosmer, Lemeshow, and Sturdivant (2013) ΔD influence statistic
* <u>h</u> at	Pregibon (1981) leverage
* <u>n</u> umber	sequential number of the covariate pattern
* <u>r</u> esiduals	Pearson residuals; adjusted for number sharing covariate pattern
* <u>rs</u> tandard	standardized Pearson residuals; adjusted for number sharing covariate pattern
<u>sc</u> ore	first derivative of the log likelihood with respect to $\mathbf{x}_i \boldsymbol{\beta}$

predict [type] newvar [if] [in] [, statistic nooffset rules asif]

Unstarred statistics are available both in and out of sample; type predict ... if e(sample) ... if wanted only for the estimation sample. Starred statistics are calculated only for the estimation sample, even when if e(sample) is not specified.

pr, xb, stdp, and score are the only options allowed with svy estimation results.

Options for predict

Main

pr, the default, calculates the probability of a positive outcome.

xb calculates the linear prediction.

stdp calculates the standard error of the linear prediction.

dbeta calculates the Pregibon (1981) $\Delta \hat{\beta}$ influence statistic, a standardized measure of the difference in the coefficient vector that is due to deletion of the observation along with all others that share the same covariate pattern. In Hosmer, Lemeshow, and Sturdivant (2013, 154–155) jargon, this statistic is *M*-asymptotic; that is, it is adjusted for the number of observations that share the same covariate pattern.

deviance calculates the deviance residual.

- dx2 calculates the Hosmer, Lemeshow, and Sturdivant (2013, 191) $\Delta \chi^2$ influence statistic, reflecting the decrease in the Pearson χ^2 that is due to deletion of the observation and all others that share the same covariate pattern.
- ddeviance calculates the Hosmer, Lemeshow, and Sturdivant (2013, 191) ΔD influence statistic, which is the change in the deviance residual that is due to deletion of the observation and all others that share the same covariate pattern.
- hat calculates the Pregibon (1981) leverage or the diagonal elements of the hat matrix adjusted for the number of observations that share the same covariate pattern.
- number numbers the covariate patterns—observations with the same covariate pattern have the same number. Observations not used in estimation have number set to missing. The first covariate pattern is numbered 1, the second 2, and so on.
- residuals calculates the Pearson residual as given by Hosmer, Lemeshow, and Sturdivant (2013, 155) and adjusted for the number of observations that share the same covariate pattern.
- rstandard calculates the standardized Pearson residual as given by Hosmer, Lemeshow, and Sturdivant (2013, 191) and adjusted for the number of observations that share the same covariate pattern.

score calculates the equation-level score, $\partial \ln L / \partial (\mathbf{x}_i \boldsymbol{\beta})$.

Options

- nooffset is relevant only if you specified offset(*varname*) for logistic. It modifies the calculations made by predict so that they ignore the offset variable; the linear prediction is treated as $x_i b$ rather than as $x_j b$ + offset_i.
- rules requests that Stata use any rules that were used to identify the model when making the prediction. By default, Stata calculates missing for excluded observations. See example 1 in [R] logit postestimation.
- asif requests that Stata ignore the rules and the exclusion criteria and calculate predictions for all observations possible by using the estimated parameter from the model. See example 1 in [R] logit postestimation.

margins

Description for margins

margins estimates margins of response for probabilities and linear predictions.

Menu for margins

Statistics > Postestimation

Syntax for margins

margins	[marginlist] [, options]
margins	[marginlist], predict(statistic) [predict(statistic)] [options]
statistic	Description
pr	probability of a positive outcome; the default
xb	linear prediction
stdp	not allowed with margins
<u>db</u> eta	not allowed with margins
<u>de</u> viance	not allowed with margins
<u>dx</u> 2	not allowed with margins
<u>dd</u> eviance	not allowed with margins
hat	not allowed with margins
number	not allowed with margins
<u>r</u> esiduals	not allowed with margins
<u>rs</u> tandard	not allowed with margins
<u>sc</u> ore	not allowed with margins

Statistics not allowed with margins are functions of stochastic quantities other than e(b). For the full syntax, see [R] margins.

Remarks and examples

stata.com

predict is used after logistic to obtain predicted probabilities, residuals, and influence statistics for the estimation sample. The suggested diagnostic graphs below are from Hosmer, Lemeshow, and Sturdivant (2013), where they are more elaborately explained. Also see Collett (2003, 129–168) for a thorough discussion of model checking.

Remarks are presented under the following headings:

predict without options predict with the xb and stdp options predict with the residuals option predict with the number option predict with the deviance option predict with the standard option predict with the hat option predict with the dx2 option predict with the ddeviance option predict with the dbeta option

predict without options

Typing predict *newvar* after estimation calculates the predicted probability of a positive outcome.

In example 1 of [R] logistic, we ran the model logistic low age lwt i.race smoke ptl ht ui. We obtain the predicted probabilities of a positive outcome by typing

```
. use https://www.stata-press.com/data/r18/lbw
(Hosmer & Lemeshow data)
. logistic low age lwt i.race smoke ptl ht ui
 (output omitted)
. predict p
(option pr assumed; Pr(low))
. summarize p low
                                            Std. dev.
                                                                        Max
    Variable
                       Obs
                                   Mean
                                                             Min
                       189
                               .3121693
                                            .1913915
                                                        .0272559
                                                                    .8391283
           р
                       189
                               .3121693
                                            .4646093
                                                               0
                                                                           1
         low
```

predict with the xb and stdp options

predict with the xb option calculates the linear combination $x_j \mathbf{b}$, where x_j are the independent variables in the *j*th observation and **b** is the estimated parameter vector. This is sometimes known as the index function because the cumulative distribution function indexed at this value is the probability of a positive outcome.

With the stdp option, predict calculates the standard error of the prediction, which is *not* adjusted for replicated covariate patterns in the data. The influence statistics described below are adjusted for replicated covariate patterns in the data.

predict with the residuals option

predict can calculate more than predicted probabilities. The Pearson residual is defined as the square root of the contribution of the covariate pattern to the Pearson χ^2 goodness-of-fit statistic, signed according to whether the observed number of positive responses within the covariate pattern is less than or greater than expected. For instance,

- . predict r, residuals
- . summarize r, detail

Pearson residual					
	Percentiles	Smallest			
1%	-1.750923	-2.283885			
5%	-1.129907	-1.750923			
10%	9581174	-1.636279	Obs	189	
25%	6545911	-1.636279	Sum of wgt.	189	
50%	3806923		Mean	0242299	
		Largest	Std. dev.	.9970949	
75%	.8162894	2.23879			
90%	1.510355	2.317558	Variance	.9941981	
95%	1.747948	3.002206	Skewness	.8618271	
99%	3.002206	3.126763	Kurtosis	3.038448	

We notice the prevalence of a few large positive residuals:

```
. sort r
```

```
. list id r low p age race in -5/1
```

	id	r	low	р	age	race
185.	33	2.224501	1	.1681123	19	White
186.	57	2.23879	1	.166329	15	White
187.	16	2.317558	1	.1569594	27	Other
188.	77	3.002206	1	.0998678	26	White
189.	36	3.126763	1	.0927932	24	White

predict with the number option

Covariate patterns play an important role in logistic regression. Two observations are said to share the same covariate pattern if the independent variables for the two observations are identical. Although we might think of having individual observations, the statistical information in the sample can be summarized by the covariate patterns, the number of observations with that covariate pattern, and the number of positive outcomes within the pattern. Depending on the model, the number of covariate patterns can approach or be equal to the number of observations, or it can be considerably less.

Stata calculates all the residual and diagnostic statistics in terms of covariate patterns, not observations. That is, all observations with the same covariate pattern are given the same residual and diagnostic statistics. Hosmer, Lemeshow, and Sturdivant (2013, 154–155) argue that such "M-asymptotic" statistics are more useful than "N-asymptotic" statistics.

To understand the difference, think of an observed positive outcome with predicted probability of 0.8. Taking the observation in isolation, the residual must be positive—we expected 0.8 positive responses and observed 1. This may indeed be the correct residual, but not necessarily. Under the M-asymptotic definition, we ask how many successes we observed across all observations with this covariate pattern. If that number were, say, six, and there were a total of 10 observations with this covariate pattern, then the residual is negative for the covariate pattern—we expected eight positive outcomes but observed six. predict makes this kind of calculation and then attaches the same residual to all observations in the covariate pattern.

Occasionally, you might want to find all observations sharing a covariate pattern. number allows you to do this:

. predict pattern, number					
. summarize pa	ttern				
Variable	Obs	Mean	Std. dev.	Min	Max
pattern	189	89.2328	53.16573	1	182

We previously fit the model logistic low age lwt i.race smoke ptl ht ui over 189 observations. There are 182 covariate patterns in our data.

predict with the deviance option

The deviance residual is defined as the square root of the contribution to the likelihood-ratio test statistic of a saturated model versus the fitted model. It has slightly different properties from the Pearson residual (see Hosmer, Lemeshow, and Sturdivant [2013, 155–157]):

. predict d, deviance

```
. summarize d, detail
```

	deviance residual					
	Percentiles	Smallest				
1%	-1.843472	-1.911621				
5%	-1.33477	-1.843472				
10%	-1.148316	-1.843472	Obs	189		
25%	8445325	-1.674869	Sum of wgt.	189		
50%	5202702		Mean	1228811		
		Largest	Std. dev.	1.049237		
75%	.9129041	1.894089				
90%	1.541558	1.924457	Variance	1.100898		
95%	1.673338	2.146583	Skewness	.6598857		
99%	2.146583	2.180542	Kurtosis	2.036938		

predict with the rstandard option

Pearson residuals do not have a standard deviation equal to 1. rstandard generates Pearson residuals normalized to have an *expected* standard deviation equal to 1.

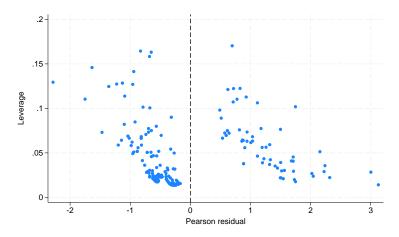
. predict rs, . summarize r					
Variable	Obs	Mean	Std. dev.	Min	Max
r rs	189 189	0242299 0279135	.9970949 1.026406	-2.283885 -2.4478	3.126763 3.149081
. correlate r (obs=189)	rs				
	r	rs			
r rs	1.0000 0.9998	1.0000			

Remember that we previously created r containing the (unstandardized) Pearson residuals. In these data, whether we use standardized or unstandardized residuals does not matter much.

predict with the hat option

hat calculates the leverage of a covariate pattern—a scaled measure of distance in terms of the independent variables. Large values indicate covariate patterns far from the average covariate pattern that can have a large effect on the fitted model even if the corresponding residual is small. Consider the following graph:

- . predict h, hat
- . scatter h r, xline(0) ytitle("Leverage")

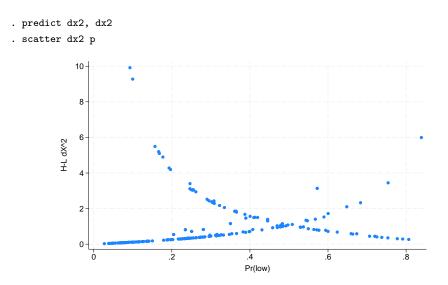


The points to the left of the vertical line are observed negative outcomes; here our data contain almost as many covariate patterns as observations, so most covariate patterns are unique. In such unique patterns, we observe either 0 or 1 success and expect p, thus forcing the sign of the residual. If we had fewer covariate patterns—if we did not have continuous variables in our model—there would be no such interpretation, and we would not have drawn the vertical line at 0.

Points on the left and right edges of the graph represent large residuals—covariate patterns that are not fit well by our model. Points at the top of our graph represent high leverage patterns. When analyzing the influence of observations on the model, we are most interested in patterns with high leverage and small residuals—patterns that might otherwise escape our attention.

predict with the dx2 option

There are many ways to measure influence, and hat is one example. dx2 measures the decrease in the Pearson χ^2 goodness-of-fit statistic that would be caused by deleting an observation (and all others sharing the covariate pattern):



Paraphrasing Hosmer, Lemeshow, and Sturdivant (2013, 195–197), the points going from the top left to the bottom right correspond to covariate patterns with the number of positive outcomes equal to the number in the group; the points on the other curve correspond to 0 positive outcomes. In our data, most of the covariate patterns are unique, so the points tend to lie along one or the other curves; the points that are off the curves correspond to the few repeated covariate patterns in our data in which all the outcomes are not the same.

We examine this graph for large values of dx2—there are two at the top left.

predict with the ddeviance option

Another measure of influence is the change in the deviance residuals due to deletion of a covariate pattern:

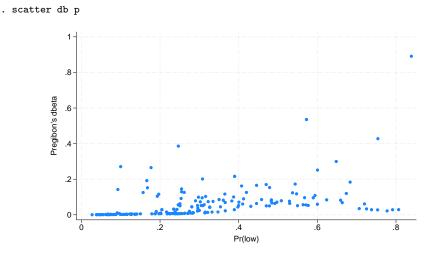
. predict dd, ddeviance

As with dx2, we typically graph ddeviance against the probability of a positive outcome. We direct you to Hosmer, Lemeshow, and Sturdivant (2013, 195) for an example and for the interpretation of this graph.

predict with the dbeta option

. predict db, dbeta

One of the more direct measures of influence of interest to model fitters is the Pregibon (1981) dbeta measure, a measure of the change in the coefficient vector that would be caused by deleting an observation (and all others sharing the covariate pattern):



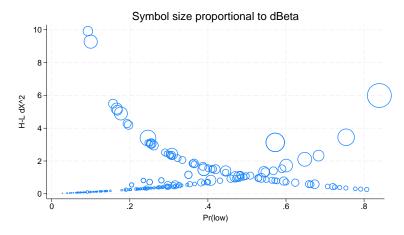
One observation has a large effect on the estimated coefficients. We can easily find this point:

. list in l

189. ptl id low age lwt race smoke htui ftv bwt 188 0 25 95 White Smoker 3 0 1 0 3637 pattern d h r rs р .8391283 -2.283885 -1.911621 .1294439 117 -2.4478dx2 dd db 5.991726 4.197658 .8909163

Hosmer, Lemeshow, and Sturdivant (2013, 196) suggest a graph that combines two of the influence measures:

. scatter dx2 p [aw=db], title("Symbol size proportional to dBeta") mfcolor(none)



We can easily spot the most influential points by the dbeta and dx^2 measures.

Methods and formulas

Let j index observations. Define M_j for each observation as the total number of observations sharing j's covariate pattern. Define Y_j as the total number of positive responses among observations sharing j's covariate pattern.

The Pearson residual for the jth observation is defined as

$$r_j = \frac{Y_j - M_j p_j}{\sqrt{M_j p_j (1 - p_j)}}$$

For $M_j > 1$, the deviance residual d_j is defined as

$$d_j = \pm \left(2 \left[Y_j \ln \left(\frac{Y_j}{M_j p_j} \right) + (M_j - Y_j) \ln \left\{ \frac{M_j - Y_j}{M_j (1 - p_j)} \right\} \right] \right)^{1/2}$$

where the sign is the same as the sign of $(Y_j - M_j p_j)$. In the limiting cases, the deviance residual is given by

$$d_j = \begin{cases} -\sqrt{2M_j |\ln(1-p_j)|} & \text{if } Y_j = 0\\ \sqrt{2M_j |\ln p_j|} & \text{if } Y_j = M_j \end{cases}$$

The unadjusted diagonal elements of the hat matrix h_{Uj} are given by $h_{Uj} = (\mathbf{XVX'})_{jj}$, where V is the estimated covariance matrix of parameters. The adjusted diagonal elements h_j created by hat are then $h_j = M_j p_j (1 - p_j) h_{Uj}$.

The standardized Pearson residual r_{Sj} is $r_j/\sqrt{1-h_j}$.

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The Pregibon (1981) $\Delta \hat{\beta}_j$ influence statistic is

$$\Delta \widehat{\beta}_j = \frac{r_j^2 h_j}{(1 - h_j)^2}$$

The corresponding change in the Pearson χ^2 is r_{Sj}^2 . The corresponding change in the deviance residual is $\Delta D_j = d_j^2/(1 - h_j)$.

References

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Also see

- [R] logistic Logistic regression, reporting odds ratios
- [R] estat classification Classification statistics and table
- [R] estat gof Pearson or Hosmer-Lemeshow goodness-of-fit test
- [R] **lroc** Compute area under ROC curve and graph the curve
- [R] lsens Graph sensitivity and specificity versus probability cutoff
- [U] 20 Estimation and postestimation commands

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