

xtgee — Fit population-averaged panel-data models by using GEE

Description	Quick start	Menu	Syntax
Options	Remarks and examples	Stored results	Methods and formulas
References	Also see		

Description

`xtgee` fits population-averaged panel-data models. In particular, `xtgee` fits generalized linear models and allows you to specify the within-group correlation structure for the panels.

See [\[R\] logistic](#) and [\[R\] regress](#) for lists of related estimation commands.

Quick start

Population-averaged linear regression of `y` on `x1` and `x2`

```
xtgee y x1 x2
```

As above, but estimate time-varying intragroup correlations

```
xtgee y x1 x2, corr(unstructured)
```

As above, but estimate a common second-order autoregression structure for the within-panel correlation

```
xtgee y x1 x2, corr(ar 2)
```

Population-averaged negative binomial regression of `y2` on `x3` and `x4` equivalent to `xtnbreg, pa`

```
xtgee y2 x3 x4, family(nbinomial 1)
```

Population-averaged logistic regression of `y3` on `x5` and `x6` when `y3` is the number of events out of 10 trials

```
xtgee y3 x5 x6, family(binomial 10)
```

Menu

Statistics > Longitudinal/panel data > Generalized estimating equations (GEE) > Generalized estimating equations (GEE)

Syntax

```
xtgee depvar [indepvars] [if] [in] [weight] [, options]
```

<i>options</i>	Description
Model	
<u>f</u> amily(<i>family</i>)	distribution of <i>depvar</i>
<u>l</u> ink(<i>link</i>)	link function
Model 2	
<u>e</u> xposure(<i>varname</i>)	include $\ln(\text{varname})$ in model with coefficient constrained to 1
<u>o</u> ffset(<i>varname</i>)	include <i>varname</i> in model with coefficient constrained to 1
<u>n</u> oconstant	suppress constant term
<u>a</u> sis	retain perfect predictor variables
<u>f</u> orce	estimate even if observations unequally spaced in time
Correlation	
<u>c</u> orr(<i>correlation</i>)	within-group correlation structure
SE/Robust	
<u>v</u> ce(<i>vcetype</i>)	<i>vcetype</i> may be <u>conventional</u> , <u>robust</u> , <u>bootstrap</u> , or <u>jackknife</u>
<u>n</u> mp	use divisor $N - P$ instead of the default N
<u>r</u> gf	multiply the robust variance estimate by $(N - 1)/(N - P)$
<u>s</u> cale(<i>parm</i>)	overrides the default scale parameter; <i>parm</i> may be <i>x2</i> , <i>dev</i> , <i>phi</i> , or <i>#</i>
Reporting	
<u>l</u> evel(<i>#</i>)	set confidence level; default is level(95)
<u>e</u> form	report exponentiated coefficients
<u>d</u> isplay_ <i>options</i>	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Optimization	
<u>o</u> ptimize_ <i>options</i>	control the optimization process; seldom used
<u>n</u> odisplay	suppress display of header and coefficients
<u>c</u> oefflegend	display legend instead of statistics

A panel variable must be specified. Correlation structures other than `exchangeable` and `independent` require that a time variable also be specified. Use `xtset`; see [XT] `xtset`.

indepvars may contain factor variables; see [U] 11.4.3 **Factor variables**.

depvar and *indepvars* may contain time-series operators; see [U] 11.4 **varlists**.

`by`, `mfp`, `mi estimate`, and `statsby` are allowed; see [U] 11.1.10 **Prefix commands**.

`vce(bootstrap)` and `vce(jackknife)` are not allowed with the `mi estimate` prefix; see [MI] **mi estimate**.

`lweights`, `fweights`, and `pweights` are allowed; see [U] 11.1.6 **weight**. Weights must be constant within panel.

`nodisplay` and `coefflegend` do not appear in the dialog box.

See [U] 20 **Estimation and postestimation commands** for more capabilities of estimation commands.

<i>family</i>	Description
<u>gaussian</u>	Gaussian (normal); <code>family(normal)</code> is a synonym
<u>igaussian</u>	inverse Gaussian
<u>binomial</u> [<i>#</i> <i>varname</i>]	Bernoulli/binomial
<u>poisson</u>	Poisson
<u>nbinomial</u> [<i>#</i>]	negative binomial
<u>gamma</u>	gamma
<hr/>	
<i>link</i>	Link function/definition
<u>identity</u>	identity; $y = y$
<u>log</u>	log; $\ln(y)$
<u>logit</u>	logit; $\ln\{y/(1 - y)\}$, natural log of the odds
<u>probit</u>	probit; $\Phi^{-1}(y)$, where $\Phi()$ is the normal cumulative distribution
<u>cloglog</u>	cloglog; $\ln\{-\ln(1 - y)\}$
<u>power</u> [<i>#</i>]	power; y^k with $k = \#$; $\# = 1$ if not specified
<u>opower</u> [<i>#</i>]	odds power; $[\{y/(1 - y)\}^k - 1]/k$ with $k = \#$; $\# = 1$ if not specified
<u>nbinomial</u>	negative binomial; $\ln\{y/(y + \alpha)\}$
<u>reciprocal</u>	reciprocal; $1/y$
<hr/>	
<i>correlation</i>	Description
<u>exchangeable</u>	exchangeable
<u>independent</u>	independent
<u>unstructured</u>	unstructured
<u>fixed matname</u>	user-specified
<u>ar #</u>	autoregressive of order #
<u>stationary #</u>	stationary of order #
<u>nonstationary #</u>	nonstationary of order #

Options

Model

`family(family)` specifies the distribution of *depvar*; `family(gaussian)` is the default.

`link(link)` specifies the link function; the default is the canonical link for the `family()` specified (except for `family(nbinomial)`).

Model 2

`exposure(varname)` and `offset(varname)` are different ways of specifying the same thing. `exposure()` specifies a variable that reflects the amount of exposure over which the *depvar* events were observed for each observation; `ln(varname)` with coefficient constrained to be 1 is entered into the regression equation. `offset()` specifies a variable that is to be entered directly into the log-link function with its coefficient constrained to be 1; thus, exposure is assumed to be e^{varname} . If you were fitting a Poisson regression model, `family(poisson) link(log)`, for instance, you would account for exposure time by specifying `offset()` containing the log of exposure time.

`noconstant` specifies that the linear predictor has no intercept term, thus forcing it through the origin on the scale defined by the link function.

`asis` forces retention of perfect predictor variables and their associated, perfectly predicted observations and may produce instabilities in maximization; see [R] [probit](#). This option is only allowed with option `family(binomial)` with a denominator of 1.

`force` specifies that estimation be forced even though the time variable is not equally spaced. This is relevant only for correlation structures that require knowledge of the time variable. These correlation structures require that observations be equally spaced so that calculations based on lags correspond to a constant time change. If you specify a time variable indicating that observations are not equally spaced, the (time dependent) model will not be fit. If you also specify `force`, the model will be fit, and it will be assumed that the lags based on the data ordered by the time variable are appropriate.

Correlation

`corr(correlation)` specifies the within-group correlation structure; the default corresponds to the equal-correlation model, `corr(exchangeable)`.

When you specify a correlation structure that requires a lag, you indicate the lag after the structure's name with or without a blank; for example, `corr(ar 1)` or `corr(ar1)`.

If you specify the fixed correlation structure, you specify the name of the matrix containing the assumed correlations following the word `fixed`, for example, `corr(fixed myr)`.

SE/Robust

`vce(vctype)` specifies the type of standard error reported, which includes types that are derived from asymptotic theory (`conventional`), that are robust to some kinds of misspecification (`robust`), and that use bootstrap or jackknife methods (`bootstrap`, `jackknife`); see [XT] [vce_options](#).

`vce(conventional)`, the default, uses the conventionally derived variance estimator for generalized least-squares regression.

`vce(robust)` specifies that the Huber/White/sandwich estimator of variance is to be used in place of the default conventional variance estimator (see [Methods and formulas](#) below). Use of this option causes `xtgee` to produce valid standard errors even if the correlations within group are not as hypothesized by the specified correlation structure. Under a noncanonical link, it does, however, require that the model correctly specifies the mean. The resulting standard errors are thus labeled “semirobust” instead of “robust” in this case. Although there is no `vce(cluster clustvar)` option, results are as if this option were included and you specified clustering on the panel variable.

`nmp`; see [XT] [vce_options](#).

`rgf` specifies that the robust variance estimate is multiplied by $(N - 1)/(N - P)$, where N is the total number of observations and P is the number of coefficients estimated. This option can be used only with `family(gaussian)` when `vce(robust)` is either specified or implied by the use of `pweights`. Using this option implies that the robust variance estimate is not invariant to the scale of any weights used.

`scale(x2 | dev | phi | #)`; see [XT] [vce_options](#).

Reporting

`level(#)`; see [R] [estimation options](#).

`eform` displays the exponentiated coefficients and corresponding standard errors and confidence intervals as described in [R] [maximize](#). For `family(binomial) link(logit)` (that is, logistic regression), exponentiation results in odds ratios; for `family(poisson) link(log)` (that is, Poisson regression), exponentiated coefficients are incidence-rate ratios.

`display_options`: `noci`, `nopvalues`, `noomitted`, `vsquish`, `noemptycells`, `baselevels`, `allbaselevels`, `nofvlabel`, `fvwrap(#)`, `fvwrapon(style)`, `cformat(%fmt)`, `pformat(%fmt)`, `sformat(%fmt)`, and `nolstretch`; see [R] [estimation options](#).

Optimization

`optimize_options` control the iterative optimization process. These options are seldom used.

`iterate(#)` specifies the maximum number of iterations. When the number of iterations equals `#`, the optimization stops and presents the current results, even if convergence has not been reached. The default is `iterate(100)`.

`tolerance(#)` specifies the tolerance for the coefficient vector. When the relative change in the coefficient vector from one iteration to the next is less than or equal to `#`, the optimization process is stopped. `tolerance(1e-6)` is the default.

`nolog` suppresses display of the iteration log.

`trace` specifies that the current estimates be printed at each iteration.

The following options are available with `xtgee` but are not shown in the dialog box:

`nodisplay` is for programmers. It suppresses display of the header and coefficients.

`coeflegend`; see [R] [estimation options](#).

Remarks and examples

[stata.com](http://www.stata.com)

For a thorough introduction to GEE in the estimation of GLM, see [Hardin and Hilbe \(2013\)](#). More information on linear models is presented in [Nelder and Wedderburn \(1972\)](#). Finally, there have been several illuminating articles on various applications of GEE in [Zeger, Liang, and Albert \(1988\)](#); [Zeger and Liang \(1986\)](#), and [Liang \(1987\)](#). [Pendergast et al. \(1996\)](#) surveys the current methods for analyzing clustered data in regard to binary response data. Our implementation follows that of [Liang and Zeger \(1986\)](#).

`xtgee` fits generalized linear models of y_{it} with covariates \mathbf{x}_{it}

$$g\{E(y_{it})\} = \mathbf{x}_{it}\boldsymbol{\beta}, \quad y \sim F \text{ with parameters } \theta_{it}$$

for $i = 1, \dots, m$ and $t = 1, \dots, n_i$, where there are n_i observations for each group identifier i . $g(\cdot)$ is called the link function, and F is the distributional family. Substituting various definitions for $g(\cdot)$ and F results in a wide array of models. For instance, if y_{it} is distributed Gaussian (normal) and $g(\cdot)$ is the identity function, we have

$$E(y_{it}) = \mathbf{x}_{it}\boldsymbol{\beta}, \quad y \sim N(\cdot)$$

yielding linear regression, random-effects regression, or other regression-related models, depending on what we assume for the correlation structure.

If $g(\cdot)$ is the logit function and y_{it} is distributed Bernoulli (binomial), we have

$$\text{logit}\{E(y_{it})\} = \mathbf{x}_{it}\boldsymbol{\beta}, \quad y \sim \text{Bernoulli}$$

or logistic regression. If $g(\cdot)$ is the natural log function and y_{it} is distributed Poisson, we have

$$\ln\{E(y_{it})\} = \mathbf{x}_{it}\boldsymbol{\beta}, \quad y \sim \text{Poisson}$$

or Poisson regression, also known as the log-linear model. Other combinations are possible.

You specify the link function with the `link()` option, the distributional family with `family()`, and the assumed within-group correlation structure with `corr()`.

The binomial distribution can be specified as case 1 `family(binomial)`, case 2 `family(binomial #)`, or case 3 `family(binomial varname)`. In case 2, `#` is the value of the binomial denominator N , the number of trials. Specifying `family(binomial 1)` is the same as specifying `family(binomial)`; both mean that y has the Bernoulli distribution with values 0 and 1 only. In case 3, `varname` is the variable containing the binomial denominator, thus allowing the number of trials to vary across observations.

The negative binomial distribution must be specified as `family(nbinomial #)`, where `#` denotes the value of the parameter α in the negative binomial distribution. The results will be conditional on this value.

You do not have to specify both `family()` and `link()`; the default `link()` is the canonical link for the specified `family()` (excluding `family(nbinomial)`):

Family	Default link
<code>family(binomial)</code>	<code>link(logit)</code>
<code>family(gamma)</code>	<code>link(reciprocal)</code>
<code>family(gaussian)</code>	<code>link(identity)</code>
<code>family(igaussian)</code>	<code>link(power -2)</code>
<code>family(nbinomial)</code>	<code>link(log)</code>
<code>family(poisson)</code>	<code>link(log)</code>

The canonical link for the negative binomial family is obtained by specifying `link(nbinomial)`. If you specify both `family()` and `link()`, not all combinations make sense. You may choose among the following combinations:

	Gaussian	Inverse Gaussian	Binomial	Poisson	Negative Binomial	Gamma
Identity	x	x	x	x	x	x
Log	x	x	x	x	x	x
Logit			x			
Probit			x			
C. log-log			x			
Power	x	x	x	x	x	x
Odds Power			x			
Neg. binom.					x	
Reciprocal	x		x	x		x

You specify the assumed within-group correlation structure with the `corr()` option.

For example, call \mathbf{R} the working correlation matrix for modeling the within-group correlation, a square $\max\{n_i\} \times \max\{n_i\}$ matrix. `corr()` specifies the structure of \mathbf{R} . Let $\mathbf{R}_{t,s}$ denote the t, s element.

The independent structure is defined as

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ 0 & \text{otherwise} \end{cases}$$

The `corr(exchangeable)` structure (corresponding to equal-correlation models) is defined as

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ \rho & \text{otherwise} \end{cases}$$

The `corr(ar g)` structure is defined as the usual correlation matrix for an AR(*g*) model. This is sometimes called multiplicative correlation. For example, an AR(1) model is given by

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ \rho^{|t-s|} & \text{otherwise} \end{cases}$$

The `corr(stationary g)` structure is a stationary(*g*) model. For example, a stationary(1) model is given by

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ \rho & \text{if } |t - s| = 1 \\ 0 & \text{otherwise} \end{cases}$$

The `corr(nonstationary g)` structure is a nonstationary(*g*) model that imposes only the constraints that the elements of the working correlation matrix along the diagonal be 1 and the elements outside the *g*th band be zero,

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ \rho_{ts} & \text{if } 0 < |t - s| \leq g, \rho_{ts} = \rho_{st} \\ 0 & \text{otherwise} \end{cases}$$

`corr(unstructured)` imposes only the constraint that the diagonal elements of the working correlation matrix be 1.

$$\mathbf{R}_{t,s} = \begin{cases} 1 & \text{if } t = s \\ \rho_{ts} & \text{otherwise, } \rho_{ts} = \rho_{st} \end{cases}$$

The `corr(fixed matname)` specification is taken from the user-supplied matrix, such that

$$\mathbf{R} = \textit{matname}$$

Here the correlations are not estimated from the data. The user-supplied matrix must be a valid correlation matrix with 1s on the diagonal.

Full formulas for all the correlation structures are provided in the [Methods and formulas](#) below.

□ Technical note

Some `family()`, `link()`, and `corr()` combinations result in models already fit by Stata:

family()	link()	corr()	Other Stata estimation command
gaussian	identity	independent	regress
gaussian	identity	exchangeable	xtreg, re
gaussian	identity	exchangeable	xtreg, pa
binomial	cloglog	independent	cloglog (see note 1)
binomial	cloglog	exchangeable	xtcloglog, pa
binomial	logit	independent	logit or logistic
binomial	logit	exchangeable	xtlogit, pa
binomial	probit	independent	probit (see note 2)
binomial	probit	exchangeable	xtprobit, pa
nbinomial	log	independent	nbreg (see note 3)
poisson	log	independent	poisson
poisson	log	exchangeable	xtpoisson, pa
gamma	log	independent	streg, dist(exp) nohr (see note 4)
family	link	independent	glm, irls (see note 5)

Notes:

1. For cloglog estimation, `xtgee` with `corr(independent)` and `cloglog` (see [R] [cloglog](#)) will produce the same coefficients, but the standard errors will be only asymptotically equivalent because `cloglog` is not the canonical link for the binomial family.
2. For probit estimation, `xtgee` with `corr(independent)` and `probit` will produce the same coefficients, but the standard errors will be only asymptotically equivalent because `probit` is not the canonical link for the binomial family. If the binomial denominator is not 1, the equivalent maximum-likelihood command is `glm` with options `family(binomial #)` or `family(binomial varname)` and `link(probit)`; see [R] [probit](#) and [R] [glm](#).
3. Fitting a negative binomial model by using `xtgee` (or using `glm`) will yield results conditional on the specified value of α . The `nbreg` command, however, estimates that parameter and provides unconditional estimates; see [R] [nbreg](#).
4. `xtgee` with `corr(independent)` can be used to fit exponential regressions, but this requires specifying `scale(1)`. As with `probit`, the `xtgee`-reported standard errors will be only asymptotically equivalent to those produced by `streg`, `dist(exp) nohr` (see [ST] [streg](#)) because `log` is not the canonical link for the gamma family. `xtgee` cannot be used to fit exponential regressions on censored data.

Using the `independent` correlation structure, the `xtgee` command will fit the same model fit with the `glm`, `irls` command if the family–link combination is the same.

5. If the `xtgee` command is equivalent to another command, using `corr(independent)` and the `vce(robust)` option with `xtgee` corresponds to using the `vce(cluster clustvar)` option in the equivalent command, where *clustvar* corresponds to the panel variable. □

`xtgee` is a generalization of the `glm`, `irls` command and gives the same output when the same family and link are specified together with an independent correlation structure. What makes `xtgee` useful is

- the number of statistical models that it generalizes for use with panel data, many of which are not otherwise available in Stata;
- the richer correlation structure `xtgee` allows, even when models are available through other xt commands; and
- the availability of robust standard errors (see [U] [20.21 Obtaining robust variance estimates](#)), even when the model and correlation structure are available through other xt commands.

In the following examples, we illustrate the relationships of `xtgee` with other Stata estimation commands. Remember that, although `xtgee` generalizes many other commands, the computational algorithm is different; therefore, the answers you obtain will not be identical. The dataset we are using is a subset of the `nlswork` data (see [XT] [xt](#)); we are looking at observations before 1980.

▷ Example 1

We can use xtgee to perform ordinary least squares by regress:

```
. use http://www.stata-press.com/data/r14/nlswork2
(National Longitudinal Survey. Young Women 14-26 years of age in 1968)
. regress ln_w grade age c.age#c.age
```

Source	SS	df	MS	Number of obs	=	16,085
Model	597.54468	3	199.18156	F(3, 16081)	=	1413.68
Residual	2265.74584	16,081	.14089583	Prob > F	=	0.0000
Total	2863.29052	16,084	.178021047	R-squared	=	0.2087
				Adj R-squared	=	0.2085
				Root MSE	=	.37536

ln_wage	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
grade	.0724483	.0014229	50.91	0.000	.0696592	.0752374
age	.1064874	.0083644	12.73	0.000	.0900922	.1228825
c.age#c.age	-.0016931	.0001655	-10.23	0.000	-.0020174	-.0013688
_cons	-.8681487	.1024896	-8.47	0.000	-1.06904	-.6672577

```
. xtgee ln_w grade age c.age#c.age, corr(indep) nmp
```

Iteration 1: tolerance = 8.406e-13

GEE population-averaged model			Number of obs	=	16,085
Group variable:	idcode		Number of groups	=	3,913
Link:	identity		Obs per group:		
Family:	Gaussian		min =		1
Correlation:	independent		avg =		4.1
			max =		9
			Wald chi2(3)	=	4241.04
Scale parameter:	.1408958		Prob > chi2	=	0.0000
Pearson chi2(16081):	2265.75		Deviance	=	2265.75
Dispersion (Pearson):	.1408958		Dispersion	=	.1408958

ln_wage	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
grade	.0724483	.0014229	50.91	0.000	.0696594	.0752372
age	.1064874	.0083644	12.73	0.000	.0900935	.1228812
c.age#c.age	-.0016931	.0001655	-10.23	0.000	-.0020174	-.0013688
_cons	-.8681487	.1024896	-8.47	0.000	-1.069025	-.6672728

When nmp is specified, the coefficients and the standard errors produced by the estimators are the same. Moreover, the scale parameter estimate from the xtgee command equals the MSE calculation from regress; both are estimates of the variance of the residuals.

▷ Example 2

The identity link and Gaussian family produce regression-type models. With the independent correlation structure, we reproduce ordinary least squares. With the exchangeable correlation structure, we produce an equal-correlation linear regression estimator.

`xtgee, fam(gauss) link(ident) corr(exch)` is asymptotically equivalent to the weighted-GLS estimator provided by `xtreg, re` and to the full maximum-likelihood estimator provided by `xtreg, mle`. In balanced data, `xtgee, fam(gauss) link(ident) corr(exch)` and `xtreg, mle` produce the same results. With unbalanced data, the results are close but differ because the two estimators handle unbalanced data differently. For both balanced and unbalanced data, the results produced by `xtgee, fam(gauss) link(ident) corr(exch)` and `xtreg, mle` differ from those produced by `xtreg, re`. Below we demonstrate the use of the three estimators with unbalanced data. We begin with `xtgee`; show the maximum likelihood estimator `xtreg, mle`; show the GLS estimator `xtreg, re`; and finally show `xtgee` with the `vce(robust)` option.

```
. xtgee ln_w grade age c.age#c.age, nolog
GEE population-averaged model
Group variable:          idcode      Number of obs   =   16,085
Link:                   identity     Number of groups =    3,913
Family:                 Gaussian
Correlation:           exchangeable  Obs per group:
                                     min =         1
                                     avg =         4.1
                                     max =         9
Wald chi2(3)           =   2918.26
Prob > chi2            =    0.0000
Scale parameter:      .1416586
```

ln_wage	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
grade	.0717731	.00211	34.02	0.000	.0676377	.0759086
age	.1077645	.006885	15.65	0.000	.0942701	.1212589
c.age#c.age	-.0016381	.0001362	-12.03	0.000	-.001905	-.0013712
_cons	-.9480449	.0869277	-10.91	0.000	-1.11842	-.7776698

```

. xtreg ln_w grade age c.age#c.age, mle
Fitting constant-only model:
Iteration 0:   log likelihood = -5868.3483
Iteration 1:   log likelihood = -5858.8833
Iteration 2:   log likelihood = -5858.8244
Fitting full model:
Iteration 0:   log likelihood = -4591.9241
Iteration 1:   log likelihood = -4562.4406
Iteration 2:   log likelihood = -4562.3526
Iteration 3:   log likelihood = -4562.3525
Random-effects ML regression           Number of obs   =   16,085
Group variable: idcode                 Number of groups =    3,913
Random effects u_i ~ Gaussian          Obs per group:
                                         min =           1
                                         avg =           4.1
                                         max =           9
LR chi2(3)                             =   2592.94
Prob > chi2                             =    0.0000
Log likelihood = -4562.3525

```

ln_wage	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
grade	.0717747	.002142	33.51	0.000	.0675765	.075973
age	.1077899	.0068266	15.79	0.000	.0944101	.1211697
c.age#c.age	-.0016364	.000135	-12.12	0.000	-.0019011	-.0013718
_cons	-.9500833	.086384	-11.00	0.000	-1.119393	-.7807737
/sigma_u	.2689639	.0040854			.2610748	.2770915
/sigma_e	.2669944	.0017113			.2636613	.2703696
rho	.5036748	.0086449			.4867329	.52061

LR test of sigma_u=0: chibar2(01) = 4996.22 Prob >= chibar2 = 0.000

```
. xtreg ln_w grade age c.age#c.age, re
Random-effects GLS regression           Number of obs   =   16,085
Group variable: idcode                  Number of groups =    3,913
R-sq:                                   Obs per group:
    within = 0.0983                      min =           1
    between = 0.2946                     avg =           4.1
    overall = 0.2076                      max =           9
Wald chi2(3) = 2875.02
corr(u_i, X) = 0 (assumed)              Prob > chi2     =    0.0000
```

ln_wage	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
grade	.0717757	.0021666	33.13	0.000	.0675294	.0760221
age	.1078042	.0068125	15.82	0.000	.0944519	.1211566
c.age#c.age	-.0016355	.0001347	-12.14	0.000	-.0018996	-.0013714
_cons	-.9512118	.0863139	-11.02	0.000	-1.120384	-.7820397
sigma_u	.27383747					
sigma_e	.26624266					
rho	.51405959	(fraction of variance due to u_i)				

```
. xtgee ln_w grade age c.age#c.age, vce(robust) nolog
GEE population-averaged model           Number of obs   =   16,085
Group variable:                         idcode          Number of groups =    3,913
Link:                                    identity         Obs per group:
Family:                                  Gaussian          min =           1
Correlation:                             exchangeable      avg =           4.1
Wald chi2(3) = 2031.28
Scale parameter:                         .1416586         Prob > chi2     =    0.0000
(Std. Err. adjusted for clustering on idcode)
```

ln_wage	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
grade	.0717731	.0023341	30.75	0.000	.0671983	.0763479
age	.1077645	.0098097	10.99	0.000	.0885379	.1269911
c.age#c.age	-.0016381	.0001964	-8.34	0.000	-.002023	-.0012532
_cons	-.9480449	.1195009	-7.93	0.000	-1.182262	-.7138274

In [R] **regress**, `regress, vce(cluster clustvar)` may produce inefficient coefficient estimates with valid standard errors for random-effects models. These standard errors are robust to model misspecification. The `vce(robust)` option of `xtgee`, on the other hand, requires that the model correctly specify the mean and the link function when the noncanonical link is used.

Stored results

xtgee stores the following in `e()`:

Scalars

<code>e(N)</code>	number of observations
<code>e(N_g)</code>	number of groups
<code>e(df_m)</code>	model degrees of freedom
<code>e(chi2)</code>	χ^2
<code>e(p)</code>	significance
<code>e(df_pear)</code>	degrees of freedom for Pearson χ^2
<code>e(chi2_dev)</code>	χ^2 test of deviance
<code>e(chi2_dis)</code>	χ^2 test of deviance dispersion
<code>e(deviance)</code>	deviance
<code>e(dispers)</code>	deviance dispersion
<code>e(phi)</code>	scale parameter
<code>e(g_min)</code>	smallest group size
<code>e(g_avg)</code>	average group size
<code>e(g_max)</code>	largest group size
<code>e(tol)</code>	target tolerance
<code>e(dif)</code>	achieved tolerance
<code>e(rank)</code>	rank of <code>e(V)</code>
<code>e(rc)</code>	return code

Macros

<code>e(cmd)</code>	xtgee
<code>e(cmdline)</code>	command as typed
<code>e(depvar)</code>	name of dependent variable
<code>e(ivar)</code>	variable denoting groups
<code>e(tvar)</code>	variable denoting time within groups
<code>e(model)</code>	pa
<code>e(family)</code>	distribution family
<code>e(link)</code>	link function
<code>e(corr)</code>	correlation structure
<code>e(scale)</code>	x2, dev, phi, or #, scale parameter
<code>e(wtype)</code>	weight type
<code>e(wexp)</code>	weight expression
<code>e(offset)</code>	linear offset variable
<code>e(chi2type)</code>	Wald; type of model χ^2 test
<code>e(vce)</code>	vcetype specified in <code>vce()</code>
<code>e(vcetype)</code>	title used to label Std. Err.
<code>e(nmp)</code>	nmp, if specified
<code>e(properties)</code>	b V
<code>e(estat_cmd)</code>	program used to implement <code>estat</code>
<code>e(predict)</code>	program used to implement <code>predict</code>
<code>e(marginsnotok)</code>	predictions disallowed by <code>margins</code>
<code>e(asbalanced)</code>	factor variables <code>fvset</code> as <code>asbalanced</code>
<code>e(asobserved)</code>	factor variables <code>fvset</code> as <code>asobserved</code>

Matrices

<code>e(b)</code>	coefficient vector
<code>e(R)</code>	estimated working correlation matrix
<code>e(V)</code>	variance-covariance matrix of the estimators
<code>e(V_modelbased)</code>	model-based variance

Functions

<code>e(sample)</code>	marks estimation sample
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Methods and formulas

Methods and formulas are presented under the following headings:

[Introduction](#)
[Calculating GEE for GLM](#)
[Correlation structures](#)
[Nonstationary and unstructured](#)

Introduction

`xtgee` fits generalized linear models for panel data with the GEE approach described in [Liang and Zeger \(1986\)](#). A related method, referred to as GEE2, is described in [Zhao and Prentice \(1990\)](#) and [Prentice and Zhao \(1991\)](#). The GEE2 method attempts to gain efficiency in the estimation of β by specifying a parametric model for α and then assumes that the models for both the mean and dependency parameters are correct. Thus there is a tradeoff in robustness for efficiency. The preliminary work of [Liang, Zeger, and Qaqish \(1992\)](#), however, indicates that there is little efficiency gained with this alternative approach.

In the GLM approach (see [McCullagh and Nelder \[1989\]](#)), we assume that

$$\begin{aligned} h(\boldsymbol{\mu}_{i,j}) &= x_{i,j}^T \boldsymbol{\beta} \\ \text{Var}(y_{i,j}) &= g(\mu_{i,j}) \phi \\ \boldsymbol{\mu}_i &= E(\mathbf{y}_i) = \{h^{-1}(x_{i,1}^T \boldsymbol{\beta}), \dots, h^{-1}(x_{i,n_i}^T \boldsymbol{\beta})\}^T \\ \mathbf{A}_i &= \text{diag}\{g(\mu_{i,1}), \dots, g(\mu_{i,n_i})\} \\ \text{Cov}(\mathbf{y}_i) &= \phi \mathbf{A}_i \quad \text{for independent observations.} \end{aligned}$$

In the absence of a convenient likelihood function with which to work, we can rely on a multivariate analog of the quasiscore function introduced by [Wedderburn \(1974\)](#):

$$\mathbf{S}_{\boldsymbol{\beta}}(\boldsymbol{\beta}, \boldsymbol{\alpha}) = \sum_{i=1}^m \left(\frac{\partial \boldsymbol{\mu}_i}{\partial \boldsymbol{\beta}} \right)^T \text{Var}(\mathbf{y}_i)^{-1} (\mathbf{y}_i - \boldsymbol{\mu}_i) = 0$$

We can solve for correlation parameters α by simultaneously solving

$$\mathbf{S}_{\boldsymbol{\alpha}}(\boldsymbol{\beta}, \boldsymbol{\alpha}) = \sum_{i=1}^m \left(\frac{\partial \boldsymbol{\eta}_i}{\partial \boldsymbol{\alpha}} \right)^T \mathbf{H}_i^{-1} (\mathbf{W}_i - \boldsymbol{\eta}_i) = 0$$

In the GEE approach to GLM, we let $\mathbf{R}_i(\boldsymbol{\alpha})$ be a “working” correlation matrix depending on the parameters in α (see the [Correlation structures](#) section for the number of parameters), and we estimate β by solving the GEE,

$$\mathbf{U}(\boldsymbol{\beta}) = \sum_{i=1}^m \left(\frac{\partial \boldsymbol{\mu}_i}{\partial \boldsymbol{\beta}} \right)^T \mathbf{V}_i^{-1}(\boldsymbol{\alpha}) (\mathbf{y}_i - \boldsymbol{\mu}_i) = 0$$

where $\mathbf{V}_i(\boldsymbol{\alpha}) = \mathbf{A}_i^{1/2} \mathbf{R}_i(\boldsymbol{\alpha}) \mathbf{A}_i^{1/2}$

To solve this equation, we need only a crude approximation of the variance matrix, which we can obtain from a Taylor series expansion, where

$$\begin{aligned} \text{Cov}(\mathbf{y}_i) &= \mathbf{L}_i \mathbf{Z}_i \mathbf{D}_i \mathbf{Z}_i^T \mathbf{L}_i + \phi \mathbf{A}_i = \tilde{\mathbf{V}}_i \\ \mathbf{L}_i &= \text{diag}\{\partial h^{-1}(u)/\partial u, u = x_{i,j}^T \beta, j = 1, \dots, n_i\} \end{aligned}$$

which allows that

$$\begin{aligned} \hat{\mathbf{D}}_i &\approx (\mathbf{Z}_i^T \mathbf{Z}_i)^{-1} \mathbf{Z}_i \hat{\mathbf{L}}_i^{-1} \left\{ (\mathbf{y}_i - \hat{\boldsymbol{\mu}}_i)(\mathbf{y}_i - \hat{\boldsymbol{\mu}}_i)^T - \hat{\phi} \hat{\mathbf{A}}_i \right\} \hat{\mathbf{L}}_i^{-1} \mathbf{Z}_i^T (\mathbf{Z}_i^T \mathbf{Z}_i)^{-1} \\ \hat{\phi} &= \sum_{i=1}^m \sum_{j=1}^{n_i} \frac{(y_{i,j} - \hat{\mu}_{i,j})^2 - (\hat{\mathbf{L}}_{i,j})^2 \mathbf{Z}_{i,j}^T \hat{\mathbf{D}}_i \mathbf{Z}_{i,j}}{g(\hat{\mu}_{i,j})} \end{aligned}$$

Calculating GEE for GLM

Using the notation from [Liang and Zeger \(1986\)](#), let $\mathbf{y}_i = (y_{i,1}, \dots, y_{i,n_i})^T$ be the $n_i \times 1$ vector of outcome values, and let $\mathbf{X}_i = (x_{i,1}, \dots, x_{i,n_i})^T$ be the $n_i \times p$ matrix of covariate values for the i th subject $i = 1, \dots, m$. We assume that the marginal density for $y_{i,j}$ may be written in exponential family notation as

$$f(y_{i,j}) = \exp \{ \{y_{i,j} \theta_{i,j} - a(\theta_{i,j}) + b(y_{i,j})\} \phi \}$$

where $\theta_{i,j} = h(\eta_{i,j})$, $\eta_{i,j} = x_{i,j} \beta$. Under this formulation, the first two moments are given by

$$E(y_{i,j}) = a'(\theta_{i,j}), \quad \text{Var}(y_{i,j}) = a''(\theta_{i,j})/\phi$$

In what follows, we let $n_i = n$ without loss of generality. We define the quantities, assuming that we have an $n \times n$ working correlation matrix $\mathbf{R}(\boldsymbol{\alpha})$,

$$\begin{aligned} \boldsymbol{\Delta}_i &= \text{diag}(d\theta_{i,j}/d\eta_{i,j}) && n \times n \text{ matrix} \\ \mathbf{A}_i &= \text{diag}\{a''(\theta_{i,j})\} && n \times n \text{ matrix} \\ \mathbf{S}_i &= \mathbf{y}_i - a'(\boldsymbol{\theta}_i) && n \times 1 \text{ matrix} \\ \mathbf{D}_i &= \mathbf{A}_i \boldsymbol{\Delta}_i \mathbf{X}_i && n \times p \text{ matrix} \\ \mathbf{V}_i &= \mathbf{A}_i^{1/2} \mathbf{R}(\boldsymbol{\alpha}) \mathbf{A}_i^{1/2} && n \times n \text{ matrix} \end{aligned}$$

such that the GEE becomes

$$\sum_{i=1}^m \mathbf{D}_i^T \mathbf{V}_i^{-1} \mathbf{S}_i = 0$$

We then have that

$$\hat{\boldsymbol{\beta}}_{j+1} = \hat{\boldsymbol{\beta}}_j - \left\{ \sum_{i=1}^m \mathbf{D}_i^T(\hat{\boldsymbol{\beta}}_j) \tilde{\mathbf{V}}_i^{-1}(\hat{\boldsymbol{\beta}}_j) \mathbf{D}_i(\hat{\boldsymbol{\beta}}_j) \right\}^{-1} \left\{ \sum_{i=1}^m \mathbf{D}_i^T(\hat{\boldsymbol{\beta}}_j) \tilde{\mathbf{V}}_i^{-1}(\hat{\boldsymbol{\beta}}_j) \mathbf{S}_i(\hat{\boldsymbol{\beta}}_j) \right\}$$

where the term

$$\left\{ \sum_{i=1}^m \mathbf{D}_i^T(\hat{\boldsymbol{\beta}}_j) \tilde{\mathbf{V}}_i^{-1}(\hat{\boldsymbol{\beta}}_j) \mathbf{D}_i(\hat{\boldsymbol{\beta}}_j) \right\}^{-1}$$

is what we call the conventional variance estimate. It is used to calculate the standard errors if the `vce(robust)` option is not specified. This command supports the clustered version of the Huber/White/sandwich estimator of the variance with panels treated as clusters when `vce(robust)` is specified. See [P] `_robust`, particularly *Maximum likelihood estimators* and *Methods and formulas*. Liang and Zeger (1986) also discuss the calculation of the robust variance estimator.

Define the following:

$$\begin{aligned}\mathbf{D} &= (\mathbf{D}_1^T, \dots, \mathbf{D}_m^T) \\ \mathbf{S} &= (\mathbf{S}_1^T, \dots, \mathbf{S}_m^T)^T \\ \tilde{\mathbf{V}} &= nm \times nm \text{ block diagonal matrix with } \tilde{\mathbf{V}}_i \\ \mathbf{Z} &= \mathbf{D}\boldsymbol{\beta} - \mathbf{S}\end{aligned}$$

At a given iteration, the correlation parameters $\boldsymbol{\alpha}$ and scale parameter ϕ can be estimated from the current Pearson residuals, defined by

$$\hat{r}_{i,j} = \{y_{i,j} - a'(\hat{\theta}_{i,j})\} / \{a''(\hat{\theta}_{i,j})\}^{1/2}$$

where $\hat{\theta}_{i,j}$ depends on the current value for $\hat{\boldsymbol{\beta}}$. We can then estimate ϕ by

$$\hat{\phi}^{-1} = \sum_{i=1}^m \sum_{j=1}^{n_i} \hat{r}_{i,j}^2 / (N - p)$$

As this general derivation is complicated, let's follow the derivation of the Gaussian family with the identity link (regression) to illustrate the generalization. After making appropriate substitutions, we will see a familiar updating equation. First, we rewrite the updating equation for $\boldsymbol{\beta}$ as

$$\hat{\boldsymbol{\beta}}_{j+1} = \hat{\boldsymbol{\beta}}_j - \mathbf{Z}_1^{-1} \mathbf{Z}_2$$

and then derive \mathbf{Z}_1 and \mathbf{Z}_2 .

$$\begin{aligned}\mathbf{Z}_1 &= \sum_{i=1}^m \mathbf{D}_i^T(\hat{\boldsymbol{\beta}}_j) \tilde{\mathbf{V}}_i^{-1}(\hat{\boldsymbol{\beta}}_j) \mathbf{D}_i(\hat{\boldsymbol{\beta}}_j) = \sum_{i=1}^m \mathbf{X}_i^T \boldsymbol{\Delta}_i^T \mathbf{A}_i^T \{ \mathbf{A}_i^{1/2} \mathbf{R}(\boldsymbol{\alpha}) \mathbf{A}_i^{1/2} \}^{-1} \mathbf{A}_i \boldsymbol{\Delta}_i \mathbf{X}_i \\ &= \sum_{i=1}^m \mathbf{X}_i^T \text{diag} \left\{ \frac{\partial \theta_{i,j}}{\partial (\mathbf{X}\boldsymbol{\beta})} \right\} \text{diag} \{ a''(\theta_{i,j}) \} \left[\text{diag} \{ a''(\theta_{i,j}) \}^{1/2} \mathbf{R}(\boldsymbol{\alpha}) \text{diag} \{ a''(\theta_{i,j}) \}^{1/2} \right]^{-1} \\ &\quad \text{diag} \{ a''(\theta_{i,j}) \} \text{diag} \left\{ \frac{\partial \theta_{i,j}}{\partial (\mathbf{X}\boldsymbol{\beta})} \right\} \mathbf{X}_i \\ &= \sum_{i=1}^m \mathbf{X}_i^T \boldsymbol{\Pi}(\boldsymbol{\Pi})^{-1} \boldsymbol{\Pi} \mathbf{X}_i = \sum_{i=1}^m \mathbf{X}_i^T \mathbf{X}_i = \mathbf{X}^T \mathbf{X}\end{aligned}$$

$$\begin{aligned}
 \mathbf{Z}_2 &= \sum_{i=1}^m \mathbf{D}_i^T(\hat{\boldsymbol{\beta}}_j) \tilde{\mathbf{V}}_i^{-1}(\hat{\boldsymbol{\beta}}_j) \mathbf{S}_i(\hat{\boldsymbol{\beta}}_j) = \sum_{i=1}^m \mathbf{X}_i^T \boldsymbol{\Delta}_i^T \mathbf{A}_i^T \{ \mathbf{A}_i^{1/2} \mathbf{R}(\boldsymbol{\alpha}) \mathbf{A}_i^{1/2} \}^{-1} (\mathbf{y}_i - \mathbf{X}_i \hat{\boldsymbol{\beta}}_j) \\
 &= \sum_{i=1}^m \mathbf{X}_i^T \text{diag} \left\{ \frac{\partial \theta_{i,j}}{\partial (\mathbf{X}_i \boldsymbol{\beta})} \right\} \text{diag} \{ a''(\theta_{i,j}) \} \left[\text{diag} \{ a''(\theta_{i,j}) \}^{1/2} \mathbf{R}(\boldsymbol{\alpha}) \text{diag} \{ a''(\theta_{i,j}) \}^{1/2} \right]^{-1} \\
 &\quad \left(\mathbf{y}_i - \mathbf{X}_i \hat{\boldsymbol{\beta}}_j \right) \\
 &= \sum_{i=1}^m \mathbf{X}_i^T \mathbf{\Pi}(\mathbf{III})^{-1} (\mathbf{y}_i - \mathbf{X}_i \hat{\boldsymbol{\beta}}_j) = \sum_{i=1}^m \mathbf{X}_i^T (\mathbf{y}_i - \mathbf{X}_i \hat{\boldsymbol{\beta}}_j) = \mathbf{X}^T \hat{\mathbf{s}}_j
 \end{aligned}$$

So, we may write the update formula as

$$\hat{\boldsymbol{\beta}}_{j+1} = \hat{\boldsymbol{\beta}}_j - (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \hat{\mathbf{s}}_j$$

which is the same formula for GLS in regression.

Correlation structures

The working correlation matrix \mathbf{R} is a function of $\boldsymbol{\alpha}$ and is more accurately written as $\mathbf{R}(\boldsymbol{\alpha})$. Depending on the assumed correlation structure, $\boldsymbol{\alpha}$ might be

Independent	no parameters to estimate
Exchangeable	$\boldsymbol{\alpha}$ is a scalar
Autoregressive	$\boldsymbol{\alpha}$ is a vector
Stationary	$\boldsymbol{\alpha}$ is a vector
Nonstationary	$\boldsymbol{\alpha}$ is a matrix
Unstructured	$\boldsymbol{\alpha}$ is a matrix

Also, throughout the estimation of a general unbalanced panel, it is more proper to discuss \mathbf{R}_i , which is the upper left $n_i \times n_i$ submatrix of the ultimately stored matrix in $\mathbf{e}(\mathbf{R})$, $\max\{n_i\} \times \max\{n_i\}$.

The only panels that enter into the estimation for a lag-dependent correlation structure are those with $n_i > g$ (assuming a lag of g). `xtgee` drops panels with too few observations (and mentions when it does so).

Independent

The working correlation matrix \mathbf{R} is an identity matrix.

Exchangeable

$$\boldsymbol{\alpha} = \frac{\sum_{i=1}^m \left(\sum_{j=1}^{n_i} \sum_{k=1}^{n_i} \hat{r}_{i,j} \hat{r}_{i,k} - \sum_{j=1}^{n_i} \hat{r}_{i,j}^2 \right)}{\sum_{i=1}^m \{n_i(n_i - 1)\}} \bigg/ \frac{\sum_{i=1}^m \left(\sum_{j=1}^{n_i} \hat{r}_{i,j}^2 \right)}{\sum_{i=1}^m n_i}$$

and the working correlation matrix is given by

$$\mathbf{R}_{s,t} = \begin{cases} 1 & s = t \\ \alpha & \text{otherwise} \end{cases}$$

Autoregressive and stationary

These two structures require g parameters to be estimated so that α is a vector of length $g + 1$ (the first element of α is 1).

$$\alpha = \sum_{i=1}^m \left(\frac{\sum_{j=1}^{n_i} \widehat{r}_{i,j}^2}{n_i}, \frac{\sum_{j=1}^{n_i-1} \widehat{r}_{i,j} \widehat{r}_{i,j+1}}{n_i}, \dots, \frac{\sum_{j=1}^{n_i-g} \widehat{r}_{i,j} \widehat{r}_{i,j+g}}{n_i} \right) / \left(\sum_{i=1}^m \frac{\sum_{j=1}^{n_i} \widehat{r}_{i,j}^2}{n_i} \right)$$

The working correlation matrix for the AR model is calculated as a function of Toeplitz matrices formed from the α vector; see [Newton \(1988\)](#). The working correlation matrix for the stationary model is given by

$$\mathbf{R}_{s,t} = \begin{cases} \alpha_{1,|s-t|} & \text{if } |s-t| \leq g \\ 0 & \text{otherwise} \end{cases}$$

Nonstationary and unstructured

These two correlation structures require a matrix of parameters. α is estimated (where we replace $\widehat{r}_{i,j} = 0$ whenever $i > n_i$ or $j > n_i$) as

$$\alpha = \sum_{i=1}^m m \begin{pmatrix} N_{1,1}^{-1} \widehat{r}_{i,1}^2 & N_{1,2}^{-1} \widehat{r}_{i,1} \widehat{r}_{i,2} & \cdots & N_{1,n}^{-1} \widehat{r}_{i,1} \widehat{r}_{i,n} \\ N_{2,1}^{-1} \widehat{r}_{i,2} \widehat{r}_{i,1} & N_{2,2}^{-1} \widehat{r}_{i,2}^2 & \cdots & N_{2,n}^{-1} \widehat{r}_{i,2} \widehat{r}_{i,n} \\ \vdots & \vdots & \ddots & \vdots \\ N_{n,1}^{-1} \widehat{r}_{i,n} \widehat{r}_{i,1} & N_{n,2}^{-1} \widehat{r}_{i,n} \widehat{r}_{i,2} & \cdots & N_{n,n}^{-1} \widehat{r}_{i,n}^2 \end{pmatrix} / \left(\sum_{i=1}^m \frac{\sum_{j=1}^{n_i} \widehat{r}_{i,j}^2}{n_i} \right)$$

where $N_{p,q} = \sum_{i=1}^m I(i,p,q)$ and

$$I(i,p,q) = \begin{cases} 1 & \text{if panel } i \text{ has valid observations at times } p \text{ and } q \\ 0 & \text{otherwise} \end{cases}$$

where $N_{i,j} = \min(N_i, N_j)$, $N_i =$ number of panels observed at time i , and $n = \max(n_1, n_2, \dots, n_m)$.

The working correlation matrix for the nonstationary model is given by

$$\mathbf{R}_{s,t} = \begin{cases} 1 & \text{if } s = t \\ \alpha_{s,t} & \text{if } 0 < |s-t| \leq g \\ 0 & \text{otherwise} \end{cases}$$

The working correlation matrix for the unstructured model is given by

$$\mathbf{R}_{s,t} = \begin{cases} 1 & \text{if } s = t \\ \alpha_{s,t} & \text{otherwise} \end{cases}$$

such that the unstructured model is equal to the nonstationary model at lag $g = n - 1$, where the panels are balanced with $n_i = n$ for all i .

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Also see

[XT] **xtgee postestimation** — Postestimation tools for xtgee

[XT] **xtcloglog** — Random-effects and population-averaged cloglog models

[XT] **xtlogit** — Fixed-effects, random-effects, and population-averaged logit models

[XT] **xtnbreg** — Fixed-effects, random-effects, & population-averaged negative binomial models

[XT] **xtpoisson** — Fixed-effects, random-effects, and population-averaged Poisson models

[XT] **xtprobit** — Random-effects and population-averaged probit models

[XT] **xtreg** — Fixed-, between-, and random-effects and population-averaged linear models

[XT] **xtregar** — Fixed- and random-effects linear models with an AR(1) disturbance

[XT] **xtset** — Declare data to be panel data

[MI] **estimation** — Estimation commands for use with mi estimate

[R] **glm** — Generalized linear models

[R] **logistic** — Logistic regression, reporting odds ratios

[R] **regress** — Linear regression

[U] **20 Estimation and postestimation commands**